

## Consolidation - Muqtadir Sir

NC clay

OC clay

It may emphasize that normally consolidated soil and over consolidated soil are not different types of soil but these are conditions in which the same type of soil can behave as normally consolidated soil in a certain pressure and over consolidated in some other pressure head.

Over consolidation (causes) :-

1) Remove surface load.

If Natural moisture content is significantly less than the Liquid limit, the sample is over consolidated.

For OC clay,  $LI = (0 - 0.6)$

For NC clay =  $LI = (0.6 - 1)$

Red clay → 99% Sure → OC clay.

Settlement কমা ২য় OC clay তে  
 পরিদিল ছুল যাবে।

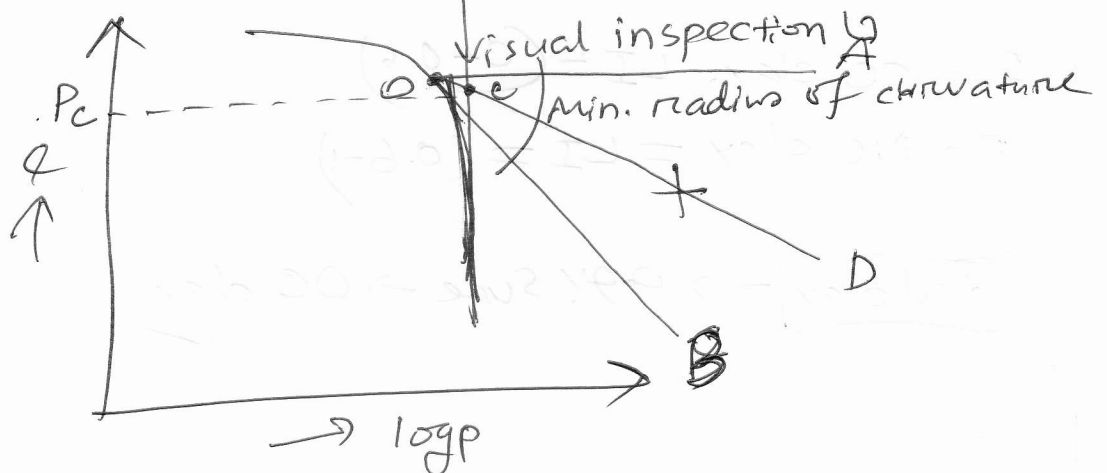
1. Compression Index ( $C_c$ ) : Unwritten
2. Co-efficient of compressibility ( $a_v$ ) : Inverse of Pressure
3. Co-efficient of volume compressibility : Inverse of Pressure

এই ৩টি parameter lab ত measure করে settlement  
 কেবল করা।

Chittagong, ইটপুর → Over consolidated clay  
 ঢাকা clay → NC clay হতে বিস্তারিত।

e      P

বিভিন্ন Pressure → void ratio lab ত করা।



$P_c$ : Past maximum pressure to which soil was subjected

Pressure corresponding to point C is called

Pre-consolidation pressure ( $P_c$ ).

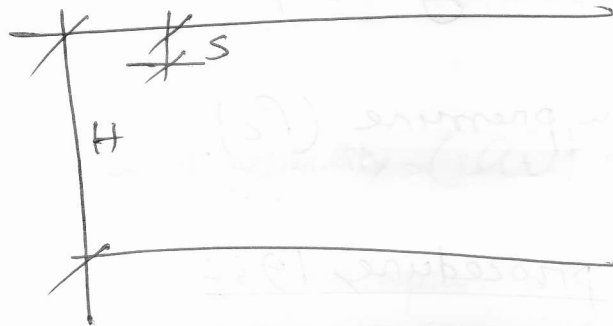
Casagrande's procedure, 1936:

$$\frac{e}{1+e} = \frac{\Delta e}{\Delta \sigma}$$

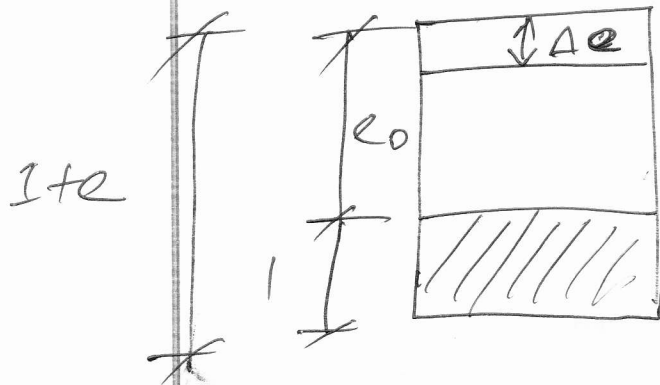


Height of clay ions

## Basic equation of settlement:



Building Pressure



$$\frac{\Delta e}{1+e} = \frac{S}{H}$$

$$\Rightarrow H \cdot \Delta e = (1+e)S$$

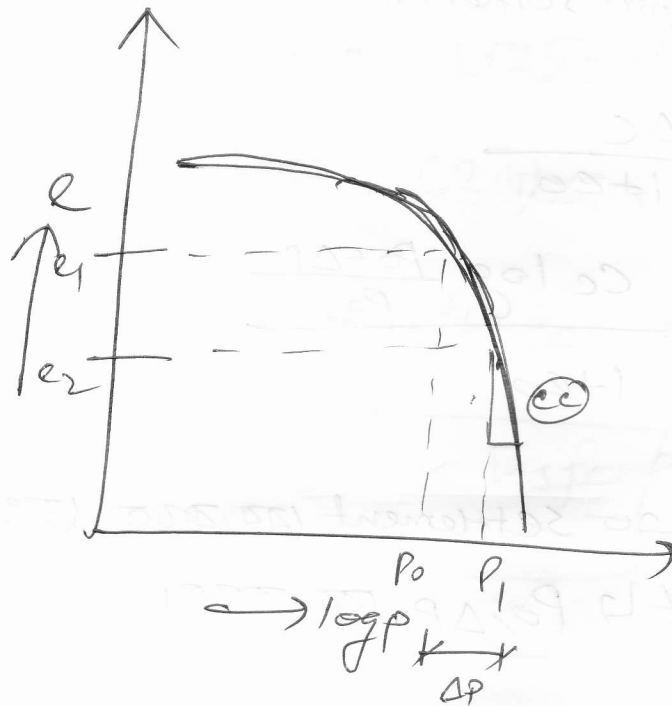
↳ Basic equation of settlement

$H \rightarrow$  Height of clay layer

$\Delta e \rightarrow$

$e \rightarrow$  lab  $\rightarrow$  ovs

$e = w w_g$  At 100% degree of sat.



$$\Delta e = e_1 - e_2$$

$$C_c = \frac{\Delta e}{\log p_1 - \log p_0}$$

$$= \frac{\Delta e}{\log p_1 / p_0}$$

$$= \frac{\Delta e}{\log \frac{(p_0 + \Delta p)}{p_0}}$$

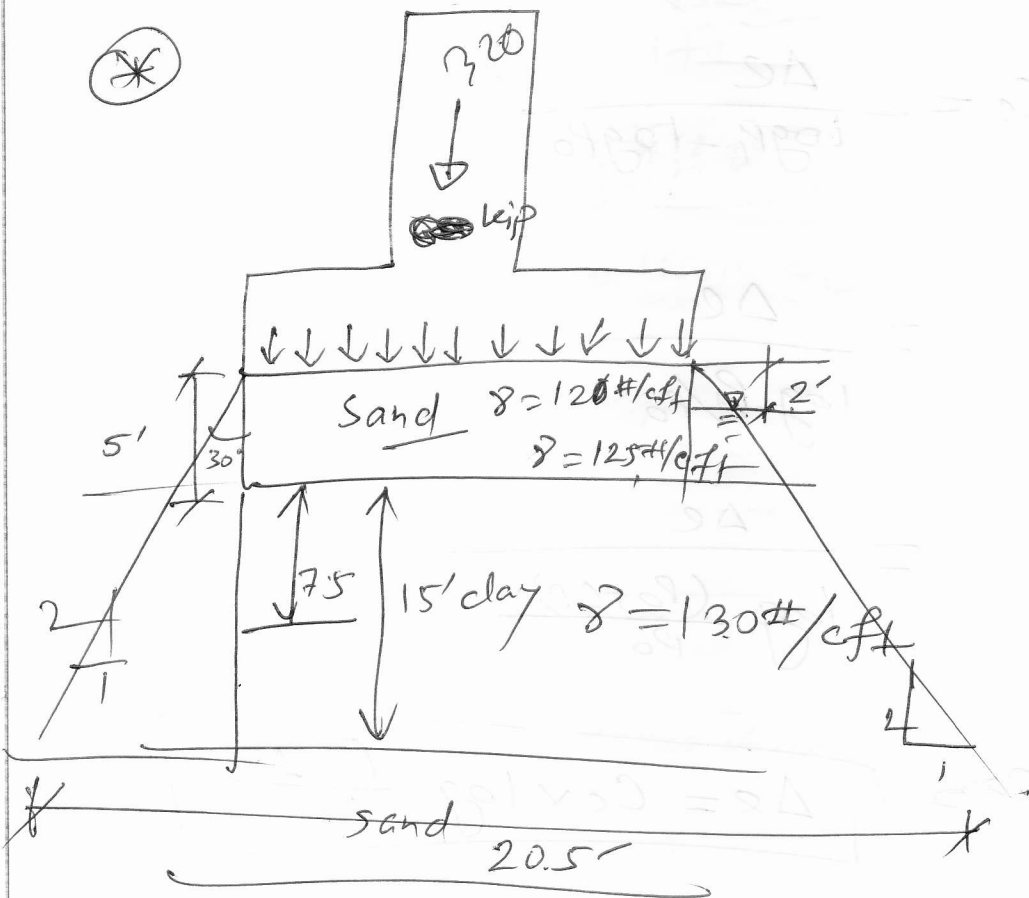
$$\Delta e = C_c \times \log \frac{p_0 + \Delta p}{p_0}$$

Final expression for settlement,

$$S = H \times \frac{\Delta e}{1 + e_0}$$

$$= H \times \frac{C_c \log \frac{P_0 + \Delta P}{P_0}}{1 + e_0}$$

(2) clay layer settlement at 200' from clay layer  
 at middle point  $\rightarrow P_0, \Delta P$  at 200'



$$P_0 = 120 \times 2 + (125 - 62.4) \times 3 +$$

$$(130 - 62.4) \times 7.5$$

$$= 0.935 \text{ ksf}$$

$$\boxed{\frac{320}{20.5 \times 20.5} = 0.75 \text{ ksf}}$$

$$C_c = 1.8 \text{ (1.5)}$$

↓  
very soft  
clay

$$S = \frac{15 \times 12 \times 0.2}{1 + e_0} \log \frac{0.935 + 0.75}{0.935}$$

~~So~~ If  $s > 1$  inch,

Not accepted.

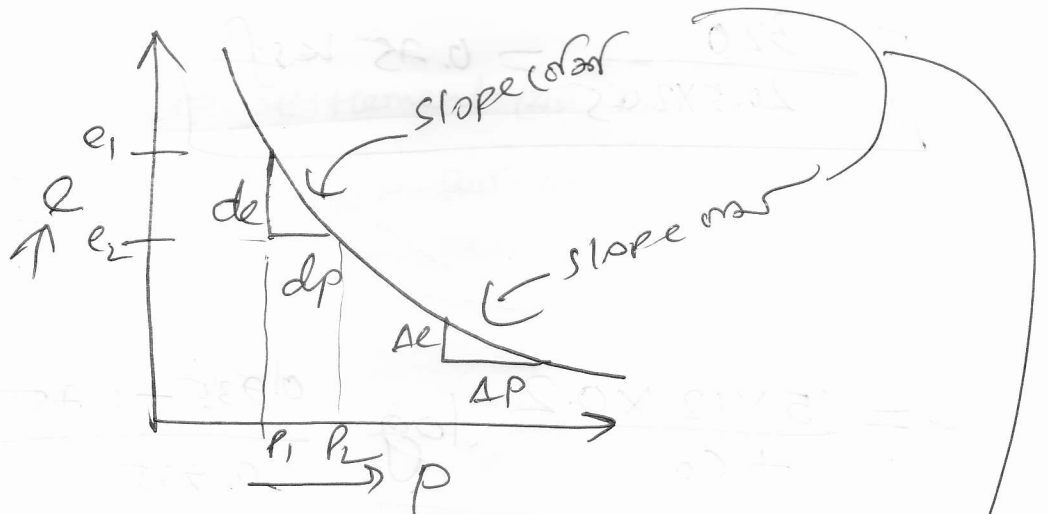
So, it can be improved by increasing foundation  
base area (8x8 to 9x9 or 10x10), so

AP gets decreased

Scampton / Terzaghi

$$C_c = 0.009(LL-10) \quad (\text{Undisturbed}) \quad \text{Completely}$$
$$= 0.007(LL-10) \quad (\text{Disturbed, remolded})$$

Co-efficient of compressibility:



$$a_v = \frac{de}{dp} = \frac{e_1 - e_2}{p_2 - p_1}$$

With the increase in effective stress,  
the value of  $a_v$  decreases.

$$S = H \times \frac{\Delta e}{1 + e_0}$$

$$= \frac{H a_v}{1 + e_0} \Delta p = H \alpha \Delta p$$

coefficient of  
volume  
compressibility

যেহেতু  $a_v$  vary করে, তাই expression settlement কে  
করা হয় এই use করে।

(১০০) প্রতিদিক

$$\frac{1}{\Delta p} \times \frac{\Delta p}{\Delta p}$$

Effective overburden Pressure  $\sigma_v'$  (for 2H OC clay)

A  $\frac{c}{p'} = 0.10 + 0.004 I_p$  → plasticity

$c, \phi$  → Angle of internal friction

Soil strength characteristics

Onconfined compaction test

Shear strength of soil

Shear strength theory

Volume Compressibility ( $m_v$ )

$m_v$  is the volumetric strain per unit increase in effective stress

Volumetric strain  $= \frac{\Delta V}{V_0}$

$m_v = \frac{\Delta V}{V_0} \times \frac{1}{\Delta p}$

$$\frac{\Delta v}{v} = \frac{\Delta e}{1+e_0}$$

for 1d consolidation,

$$\frac{\Delta H}{H} = \frac{\Delta e}{1+e_0}$$

$$m_v = \frac{\Delta H}{H} \times \frac{1}{\Delta p}$$

~~$$m_v = \frac{\Delta H}{H} \times \frac{1}{\Delta p}$$~~

$$m_v = \frac{\Delta e}{1+e_0} \times \frac{1}{\Delta p}$$

$$m_v = \frac{a_v}{1+e_0}$$

$a_v, m_v$

They are the function of  
the current stage of  
stress

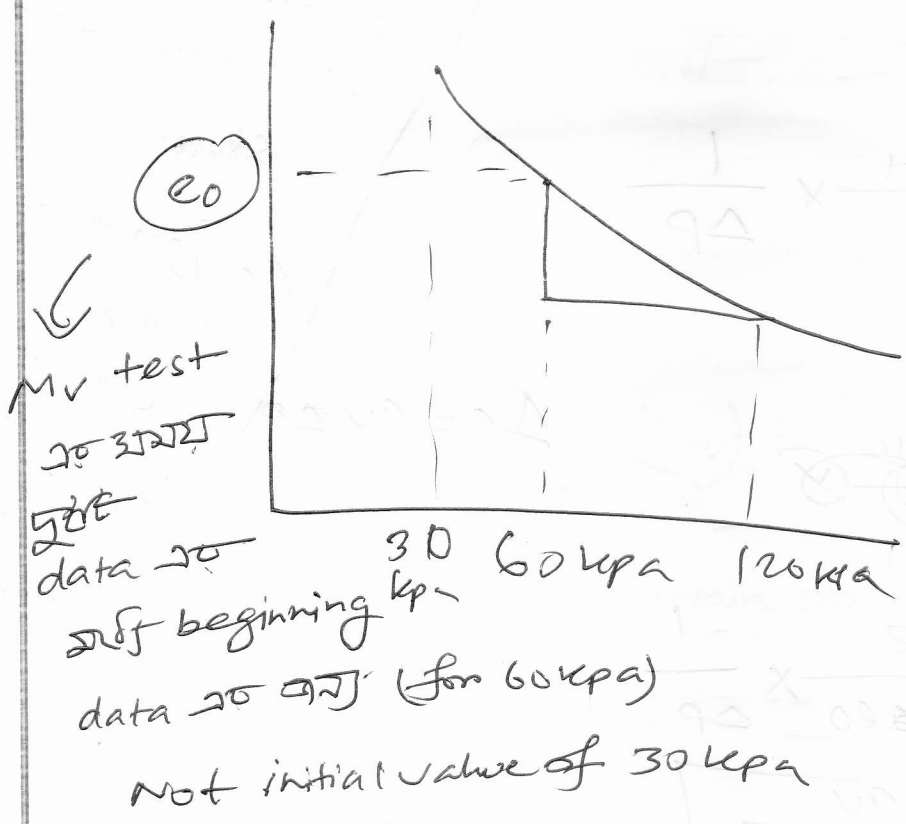
$C_c$  is not,  
independent of  
current stress

Slope of  
virgin portion  
of e-gamma curve

$$\Delta e = a_v \cdot \Delta p$$

In terms of  $m_v$ , consolidation determination always use  $e_0$

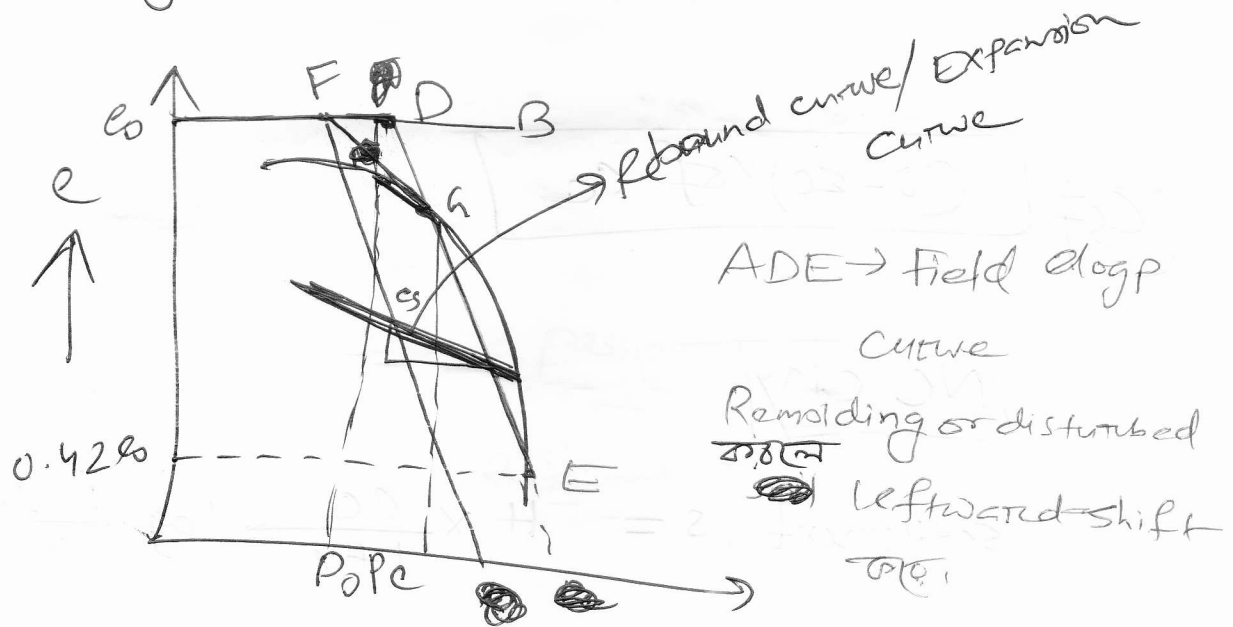
$$\Delta H = H m_v \Delta P$$



Remolded soil sample এর stiffness (কঠোরতা),

Schemmertmann (1955) procedure

for NC Clay,



Disturbed soil sample এর e-log p curve and  
 Undisturbed soil sample এর (field e-log p) e-log p curve  
 pass through a common point  $0.42 e_0$  of initial void ratio.

Unloading & reloading ~~path~~ curve same path follow করে

It follows the slope of the rebound curve

AFGE

AFG → OC clay ( $P_c \leq p_0$ )

GE → NC clay ( $P_c > p_0$ )

$$C_s = (10-20)\% \text{ of } C_c$$

NC clay

$$\text{settlement, } s = H \times \frac{C_c}{1+e_0} \log \frac{P_0 + \Delta P}{P_0}$$

$$S_{F \rightarrow G} = H \times \frac{C_s}{1+e_0} \log \frac{P_0 + \Delta P}{P_0} \quad (P_0 + \Delta P \leq P_c)$$

$$S_G = H \times \frac{C_s}{1+e_0} \log \frac{P_c}{P_0}$$

$$S_{G \rightarrow E} = \frac{H C_c}{1+e_0} \log \frac{P_c}{P_0} + \frac{H \times e_0}{1+e_0} \log \frac{P_0 + \Delta P}{P_c}$$

$$(P_0 + \Delta P) > P_c$$

যিহেঁ mention করা না থাকলে normally settlement  
বনতে primary settlement বুঝায়।

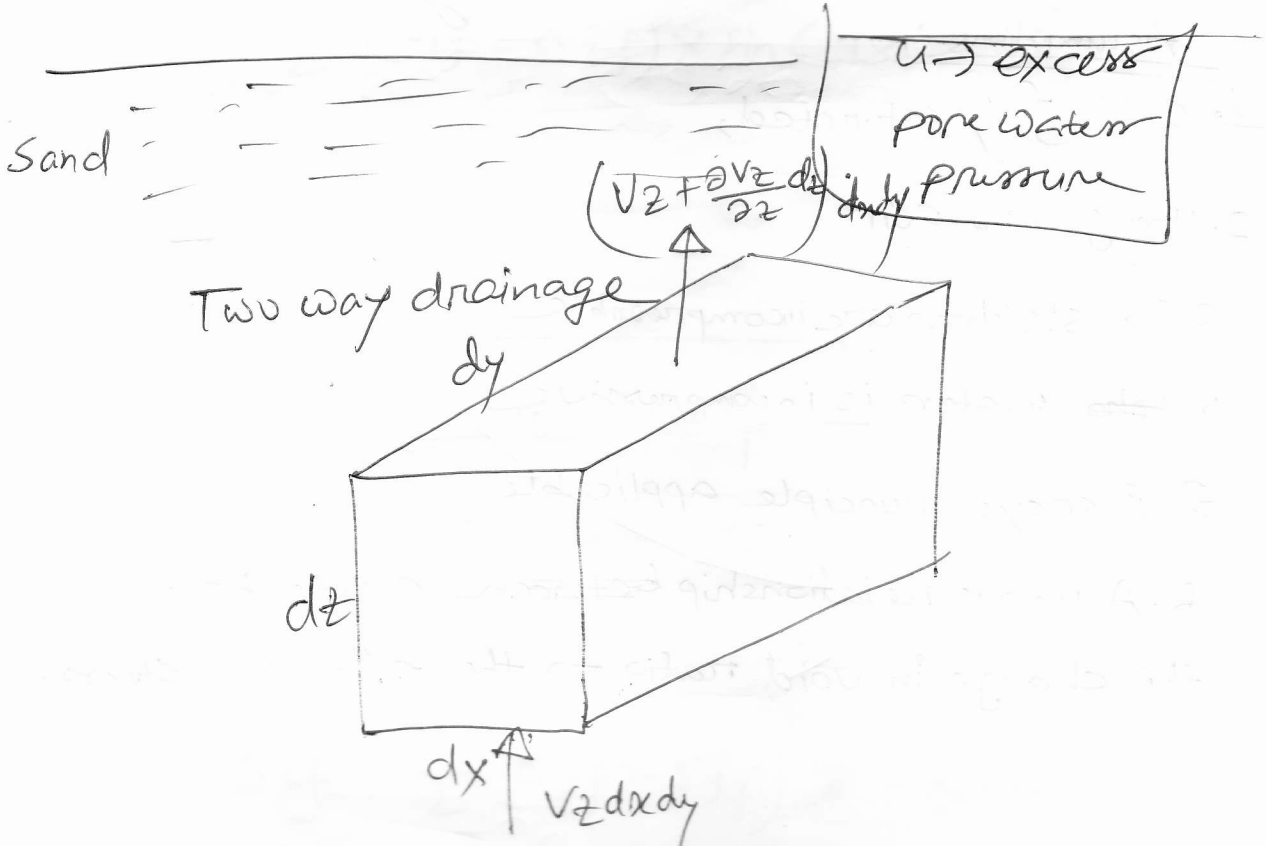
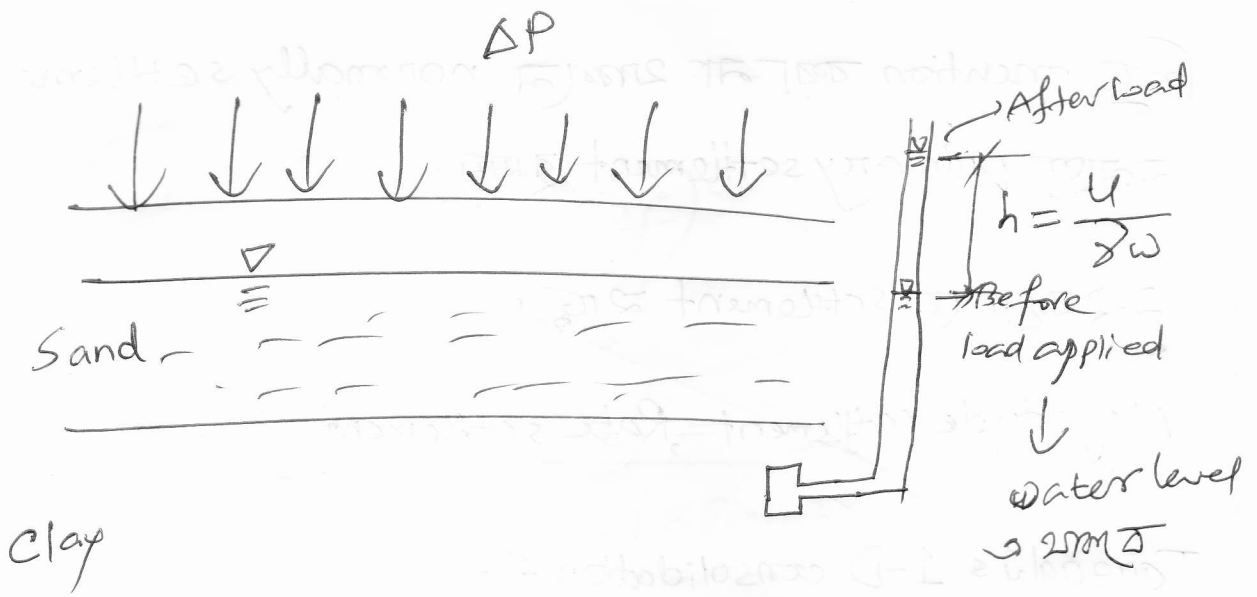
২-২ বছরে যে settlement হচ্ছে।

Magnitude settlement, Rate settlement

Terzaghi's 1-D consolidation theory

Assumptions:

1. Soil is fully saturated,
2. Homogeneous soil
3. Soil skeletons are incompressible
4. ~~Water~~ Water is incompressive
5. Darcy's principle applicable.
6. A unique relationship ~~between~~ exists between the change in void ratio to the effective stress.



Outflow rate - Inflow rate = Rate of volume change

$$V = dx \cdot dy \cdot dz$$

$$\left( V_z + \frac{\partial V_z}{\partial z} \cdot dz \right) \cdot dx dy - V_z dx \cdot dy = \frac{\partial V}{\partial t}$$

$$\Rightarrow \frac{\partial V_z}{\partial z} \cdot dx dy dz = \frac{\partial V}{\partial t}$$

$$V_z = -k z i z \quad (\ominus \text{ is used to indicate loss})$$

$$= -k \cdot \frac{\partial h}{\partial z}$$

$$= -\frac{k}{\gamma_w} \times \frac{\partial u}{\partial z}$$

$$-\frac{k}{\gamma_w} \frac{\partial u}{\partial z} dx dy dz = \frac{\partial V}{\partial t}$$

Rate of volume change:

$$V = V_s + V_w = V_s + e V_s$$

$$\frac{\partial V}{\partial t} = V_s \times \frac{\partial e}{\partial t}$$

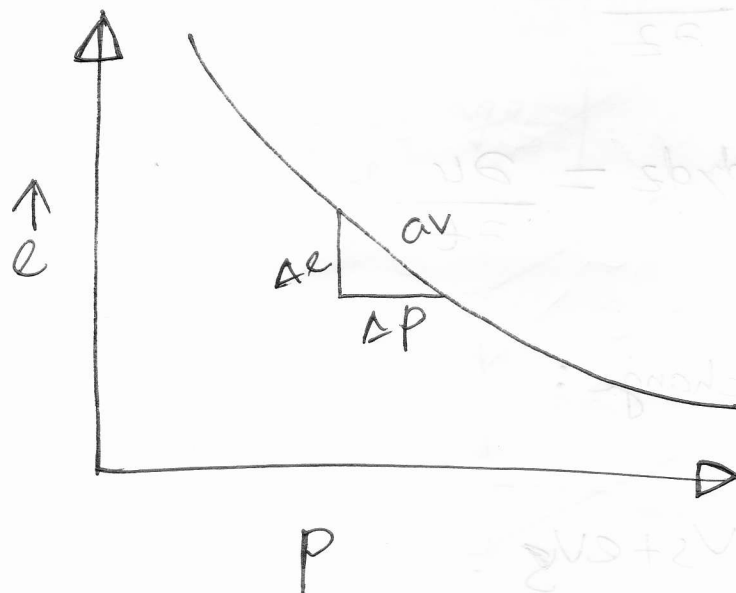
$$V = V_s (1+e)$$

$$\Rightarrow \boxed{V_s = \frac{V}{1+e}} = \frac{dx \cdot dy \cdot dz}{1+e}$$

$$\frac{\partial v}{\partial t} = \frac{dx \cdot dy \cdot dz}{1te} \cdot \frac{\partial e}{\partial t}$$

$$-\frac{k}{\partial w} \frac{\partial u}{\partial z^r} (\cancel{dx dy dz}) = \frac{(\cancel{dx dy dz})}{1te} \cdot \frac{\partial e}{\partial t}$$

$$\Rightarrow -\frac{k}{\partial w} \cdot \frac{\partial u}{\partial z^r} = \frac{\partial e}{(1te) \partial t}$$



$$a_v = \frac{\Delta e}{\Delta P} = \frac{\partial e}{\partial P}$$

$$\partial e = a_v \partial(\Delta P) = -a_v \partial u$$

$$\partial e =$$

Increment দিয়া হলে যেসব fluid ratio থাকে সেগুলো

$$\frac{k}{\gamma_w} \frac{\partial^2 u}{\partial z^2} = \frac{q_v}{1+e_0} \frac{\partial u}{\partial t}$$

$$\Rightarrow \frac{k}{\gamma_w} \frac{\partial^2 u}{\partial z^2} = m_v \cdot \frac{\partial u}{\partial t}$$

~~$$\frac{\partial^2 u}{\partial z^2} = \frac{m_v \gamma_w}{k} \times \frac{\partial u}{\partial t}$$~~

~~$$\frac{\partial^2 u}{\partial z^2} = C_v \cdot \frac{\partial^2 u}{\partial z^2}$$~~

~~$$C_v = \frac{m_v \gamma_w}{k}$$~~

$$\Rightarrow \frac{\partial u}{\partial t} = \frac{k}{m_v \gamma_w} \cdot \frac{\partial^2 u}{\partial z^2} \Rightarrow \frac{\partial u}{\partial t} = C_v \cdot \frac{\partial^2 u}{\partial z^2}$$

$$\boxed{\frac{k}{m_v \gamma_w}} = C_v$$

$C_v$  (বহুলাংশে)  $\gamma_w$ ,  
 $m_v$  দ্বারা,  
 পরিণত  $k$  দ্বারা,

# Rate Analysis : Muqtadir Sir

$$\frac{\partial u}{\partial t} = C_v \frac{\partial^2 u}{\partial z^2}$$

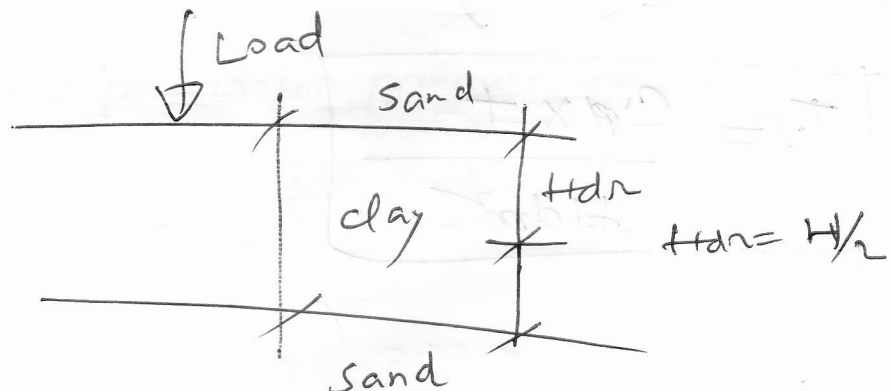
$$C_v = \frac{k}{\gamma_w m_v}$$

$(k/m_v)$  ratio is constant

$\gamma_w$  constant for different forces.

- ⊗ logarithm of time method / Casagrande's procedure
- ⊗ sq. root of time method / Taylor's method.

Boundary condition:



For both way drainage, length of the drainage path will be half of the clay layer thickness ( $H$ ) ( $H_{dr}$ )


For one way drainage, length of the drainage path will be thickness of clay layer

B.C. associated with geometry

$$z=0, u=0$$

$$z=2Hd_{dr}, u=0$$

Initial condition at  $t=0$  →

$$u = \sum_{m=0}^{\infty} \left[ \frac{240}{M} \sin \frac{Mz}{Hd_{dr}} \right] e^{-M^2 \frac{T_v}{T_v}}$$


$T_v$  = Dimensionless time factor

$$m = 0, 1, 2, \dots, \infty$$

$$M = \frac{\pi}{2} (2m+1)$$

$$T_v = \frac{C_v \times t}{Hd_{dr}^2}$$

$$u_z = \frac{u_0 - u_z}{u_0} = 1 - \frac{u_z}{u_0}$$

↓

Degree of consolidation

↓

Depends on the depth (Length of the drainage path)

$$u_{av} = 1 - \frac{\int_0^{2H_{dr}} u_z \cdot dz}{u_0 \cdot 2H_{dr}}$$

$$= 1 - \sum_{m=0}^{\infty} \frac{2}{M^2} e^{-M^2 \frac{T}{T_0}}$$

Previously settlement measure का 2 प्रकार हैं (एक दिन)

Ultimate settlement: ~~सु~~

इसका time and pore water pressure का दोनों depend करे इसका settlement का का।

$T_V$  corresponding to 50%

$T_V$  corresponding to 90%

$$M = \frac{\pi}{2} (2m+1)$$

$$= \pi/2$$

$$U_{av} = 1 - \sum_{m=0}^{\infty} \frac{2}{m^2 \pi^2} e^{-M^2 \pi^2 / 4 T_V}$$

$$\Rightarrow 0.90 = 1 - \sum_{m=0}^{\infty} \frac{2}{m^2 \pi^2} e^{-\frac{\pi^2}{4} \times T_V}$$

$$\Rightarrow T_V = 0.848$$

Curve Fitting Method:

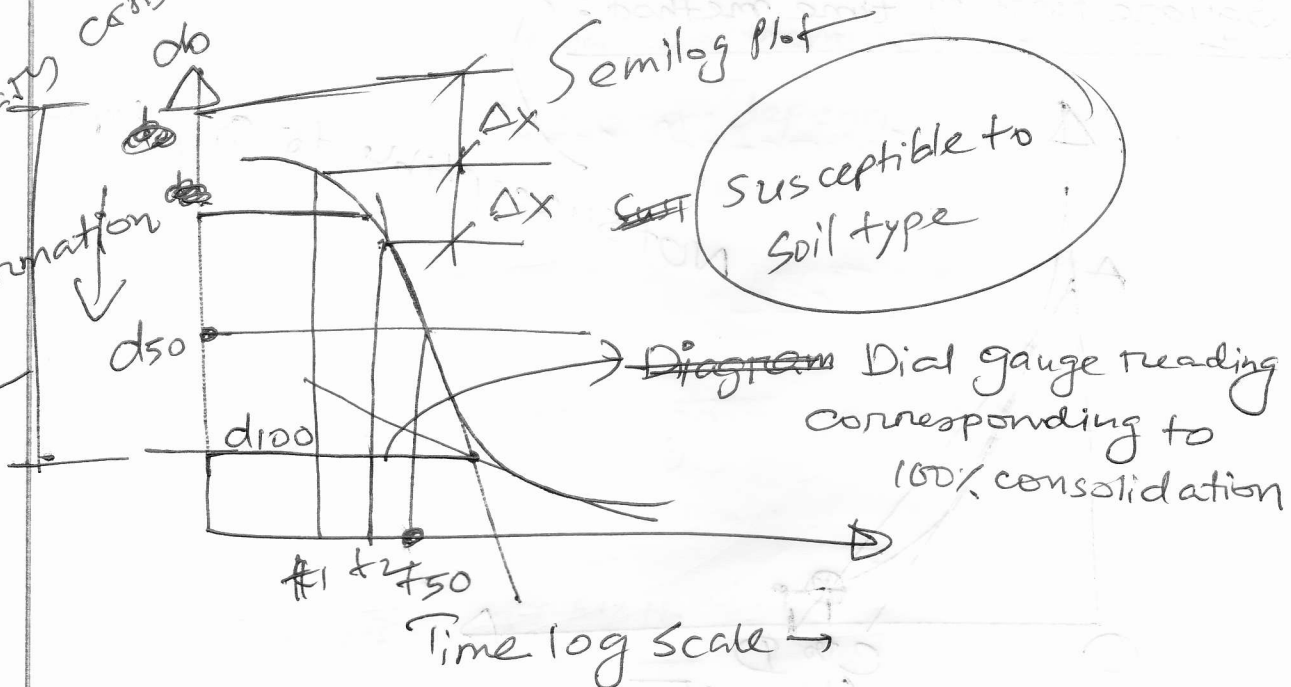
$$T_V = \pi/4 \times (U/100)^2 \quad U \leq 60$$

$$U = 50, T_V = 0.196$$

$$T_V = 1.781 - 0.9331 \log_{10} (100-U) \quad U > 60$$

$$U = 90, T_V = 0.848$$

Primary consolidation  
 Deformation



Deformation associated with 0% consolidation.  
 " " " " 100% "

~~t2 = 4t1~~      t2 = 4t1

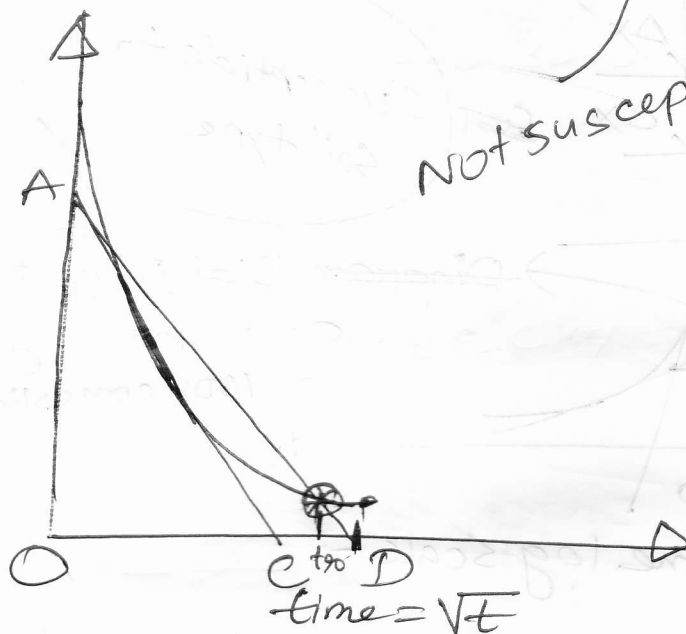
$$d_{50} = \frac{d_0 + d_{100}}{2}$$

$$Tv_{50} = \frac{c_v t_{50}}{H d_{50}}$$

~~QED~~

Taylor's Method

Square root of time method:



A → Dial gauge reading corresponding to 0% consolidation

$$OD = 1.15 OC$$

AD line graph ke (A) point se (D) tak ka slope point 90% consolidation निर्धारण करते,

$$\sqrt{\frac{0.848}{0.636}} = 1.15$$

$$U = \pi/4 \left( \frac{U}{100} \right) = 0.636$$

