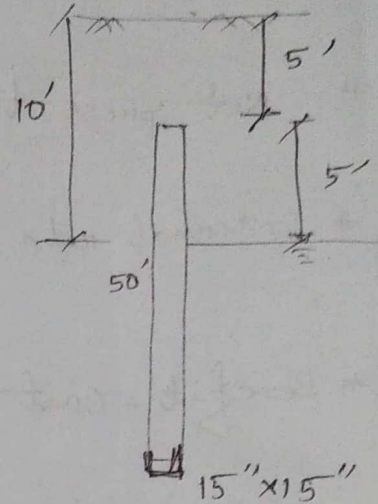


2017-18



2016-17

Settlement

Layer 1

$$\begin{aligned} \sigma'_0 &= 8 \times 120 + 6 \times 120 \\ &= 1680 \text{ psf} \end{aligned}$$

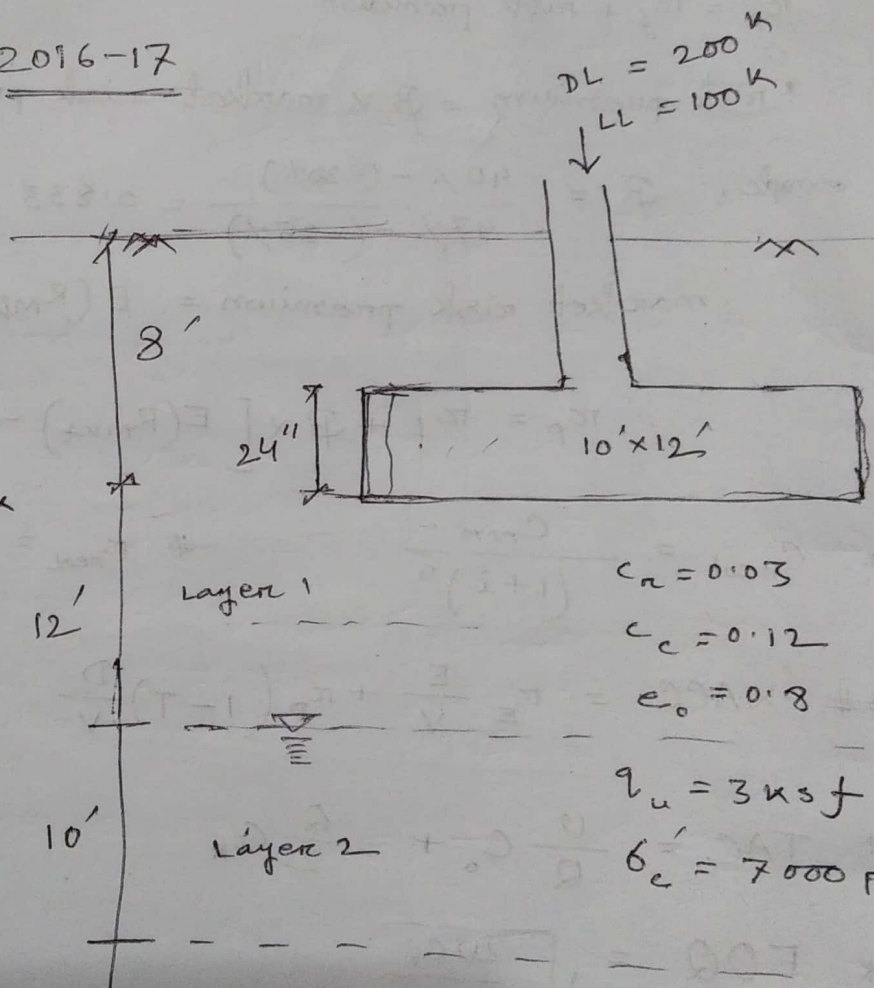
$$\text{load} = 200 + \frac{100}{2} = 250 \text{ k}$$

$$\begin{aligned} \Delta \sigma &= \frac{250 \times 10^3}{16 \times 12} \\ &= 868 \text{ psf} \end{aligned}$$

$$\sigma'_0 + \Delta \sigma = 2548 < \sigma'_c$$

∴ OC clay

$$\begin{aligned} S_1 &= c_r \times \frac{H}{1 + e_0} \log \frac{\sigma'_0 + \Delta \sigma}{\sigma'_0} \\ &= 0.03 \times \frac{12 \times 12}{1 + 0.8} \times \log \frac{2548}{1680} \end{aligned}$$



Layer 2

$$\sigma'_o = 20 \times 120 + 5 \times (120 - 62.5) = 2687.5 \text{ psf}$$

$$\Delta \sigma = \frac{250 \times 10^3}{27 \times 29} = 319.28 \text{ psf}$$

$$\therefore \sigma'_o + \Delta \sigma = 3006.78 \text{ psf} < \sigma_c \quad \therefore \text{OC clay}$$

$$s_z = \frac{0.03 \times 10 \times 12}{1.8} \times \log \frac{3006.78}{2687.5} = 0.1''$$

$$\therefore \text{Total settlement} = 0.434 + 0.1 = \boxed{0.53''}$$

FS calculation

$$\frac{D_f}{B} = 0.8, \text{ from chart } N_c = 6.2$$

$$\text{Actual } N_c = 6.2 \times \left(1 + 0.2 \frac{B}{L}\right) = 7.23$$

$$c = \frac{q_u}{2} = 1.5 \text{ ksf}$$

$$q_u = \frac{300}{10 \times 12} + \left(\frac{150 - 120}{1000}\right) \times 1000 = 2.56$$

$$F.S. = \frac{c \cdot N_c}{q_u}$$

$$= \frac{1.5 \times 7.23}{2.56} = \frac{4.24}{2.56} = \boxed{6.5}$$

$$P_o = 12 \times 120 + 4 \times 120 = 1920 \text{ psf}$$

$$\text{Gross pressure} = \frac{1700 \times 10^3}{100 \times 80}$$

$$= 2125 \text{ psf}$$

$$\therefore \text{net pressure } q = 2125 - 120 \times 12 = 685 \text{ psf}$$

at middle

$$\frac{B}{z} = \frac{40}{4} = 10$$

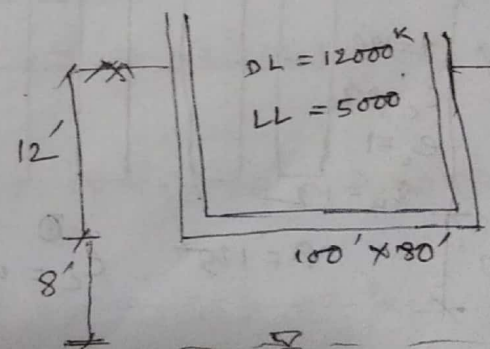
$$\frac{L}{z} = \frac{50}{4} = 12.5$$

$$\Delta P = 4 \times 0.249 \times 685$$

$$= 682.26 \text{ psf}$$

$$P_o + \Delta P = 2602.26 < P_c$$

$$S = \frac{0.04 \times 8 \times 12}{1.9} \log \frac{2602.26}{1920} = \boxed{0.27''}$$



$$\sigma_c = 6000 \text{ psf}$$

$$c_u = 0.04$$

$$e_o = 0.9$$

from chart, $I_g = 0.249$

At corner

$$\frac{B}{z} = \frac{80}{4} = 20$$

$$\frac{L}{z} = \frac{100}{4} = 25$$

$$I_g = 0.25$$

$$\Delta P = 0.25 \times 685 = 171.25 \text{ psf}$$

$$P_o + \Delta P = 2091.25 < P_c$$

$$S = \frac{0.04 \times 8 \times 12}{1.9} \log \frac{2091.25}{1920} = \boxed{0.075''}$$

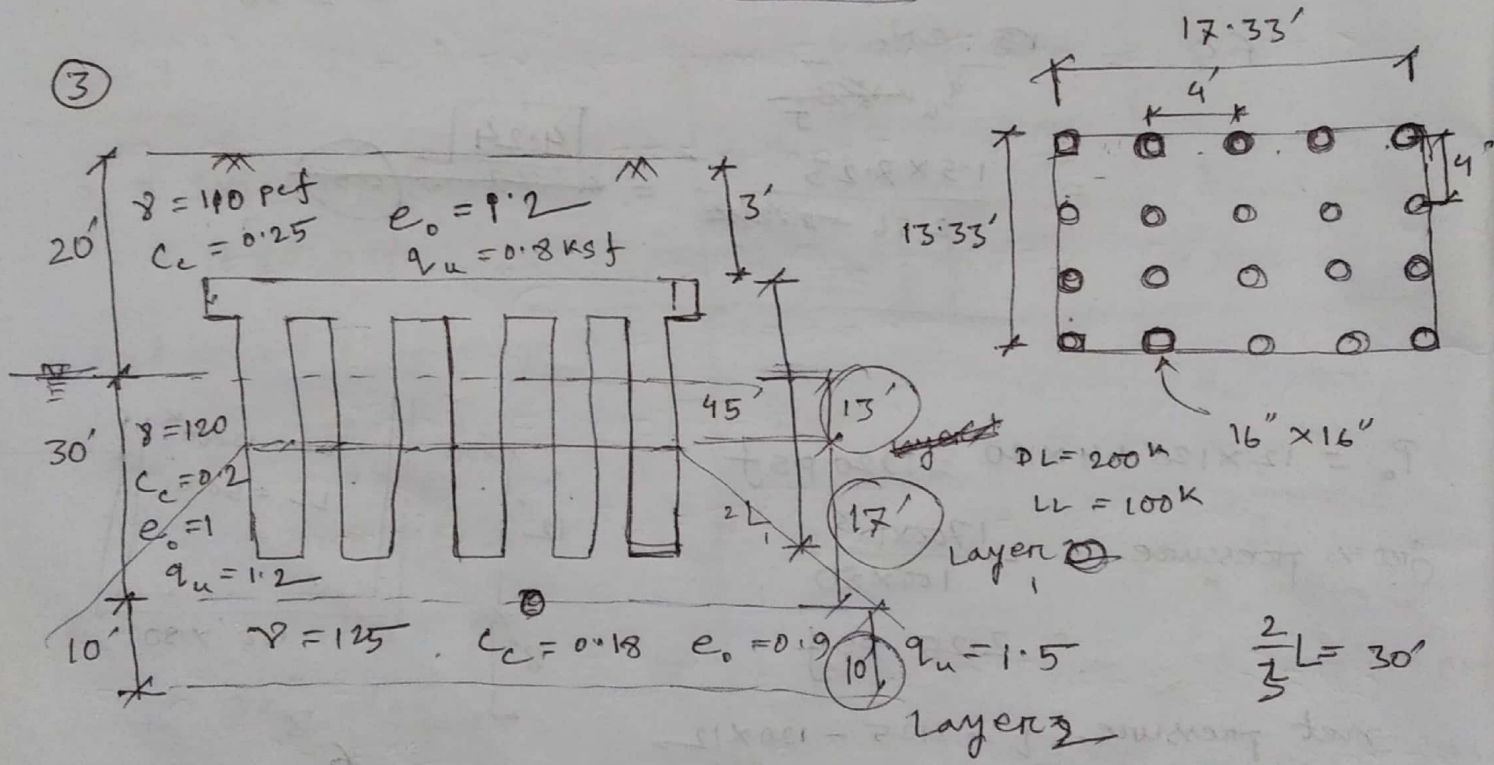
Factor of safety

$$q_b = \frac{Q}{A} = 2125 = 2.125 \text{ ksf}$$

$$\frac{D_f}{B} = \frac{12}{80} = 0.15 \quad \therefore N_c = 5.3 \times \left(1 + 0.2 \times \frac{80}{100}\right) = 6.148$$

$$\therefore \text{F.S.} = \frac{c N_c}{q_b - \gamma D_f} = \frac{9 \times 6.148}{2.125 - 0.12 \times 12} = 8.98 \approx \textcircled{9}$$

③



Layer 1

$$P_o = 20 \times 110 + 13 \times (120 - 62.5) + 8.5 \times (120 - 62.5)$$

$$= 3436.25 \text{ psf}$$

$$\Delta P = \frac{250 \times 10^3}{(17.3 + 8.5) \times (13.3 + 8.5)} = 444.49 \text{ psf}$$

$$S_1 = 0.2 \times \frac{12 \times 12}{2} \log \frac{3436.25 + 444.49}{3436.25} = 1.07''$$

Layer 2

$$P_o = 3436.25 + 8.5 \times (120 - 62.5) + 5 \times (125 - 62.5)$$

$$= 4237.5 \text{ psf}$$

$$\Delta P = \frac{250 \times 10^3}{39.3 \times 35.3} = 180.2 \text{ psf}$$

$$S_2 = \frac{0.18 \times 10 \times 12}{1.9} \log \frac{4237.5 + 180.2}{4237.5} = 0.205''$$

$$\therefore \text{Total settlement} = S_1 + S_2 = \boxed{1.275''}$$

Capacity as a single pile

$$0-20', \text{ friction} = \alpha C A_f = 0.9 \times 0.4 \times 4 \times \frac{16}{12} \times 17 = 32.64^k$$

$$20'-50', \text{ friction} = 0.8 \times 0.6 \times 4 \times \frac{16}{12} \times 28 = 71.68^k$$

$$\text{end bearing} = C N_c A_b = 0.6 \times 9 \times \frac{16 \times 16}{144} = 9.6^k$$

$$\therefore \text{Total capacity of 20 pile, } Q_{u1} = 20 \times (9.6 + 71.68 + 32.64)$$

$$= 2278.4^k$$

Capacity as group action

$$0-20', \text{ friction} = \alpha C A_f = 1 \times 0.4 \times (17.33 + 13.33) \times 2 \times 17$$

$$= 416.976^k$$

$$20-50' \text{ friction} = 1 \times 0.6 \times 2 \times (17.33 + 13.33) \times 28 = 1030.176^k$$

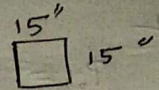
$$\text{end bearing} = 0.6 \times 9 \times 13.33 \times 17.33 = 1247.45^k$$

$$\text{Total capacity } Q_{ug} = 2694.6^k$$

$$\therefore \text{Capacity of the pile group} = 2278.4^k$$

$$F.S = \frac{2278.4}{300} = \boxed{7.60}$$

4. (a)



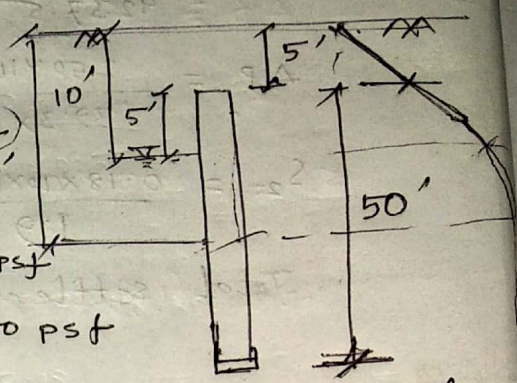
Skin Friction = $k \sigma_v \tan \delta A_{\text{surface}}$

End bearing = $q N_q A_{\text{tip}}$

$k = 1.5$

$\delta = 10^\circ$

$D_c = 20'$



~~Sf = 1.5 x~~

$0-5'$
 $\sigma_v = 120 \times 5 = 600 \text{ psf}$

$5-10'$
 $\sigma_v = 120 \times 10 = 1200 \text{ psf}$

$10-20'$
 $\sigma_v = 1200 + 10 \times (120 - 62.5) = 1775 \text{ psf}$

$0-10'$
 $Sf = 1.5 \times \left(\frac{600 + 1200}{2} \right) \times \tan 25^\circ \times 4 \times \frac{15}{12} \times 5 = 15.738 \text{ k}$

$10-20'$
 $Sf = 1.5 \times \frac{1200 + 1775}{2} \times \tan 25^\circ \times 4 \times \frac{15}{12} \times 10 = 52.039 \text{ k}$

$20-50'$
 $Sf = 1.5 \times 1775 \times \tan 25^\circ \times 4 \times \frac{15}{12} \times 30 = 186.23 \text{ k}$

$50-55'$
 $Sf = 1.5 \times 1775 \times \tan 28^\circ \times 4 \times \frac{15}{12} \times 5 = 35.4 \text{ k}$

End bearing = $\sigma_v N_q A_{\text{tip}} = 1775 \times 140 \times \frac{15 \times 15}{144} = 388.28 \text{ k}$

$\therefore \text{Total} = 677.67 \text{ k}$

capacity, $P_u = \frac{677.67}{2.5} = 271.068 \text{ k}$

5. (c)

$N_q = 41$

$N_\gamma = 42$

$\gamma = 110 \text{ pcf}$

$D_f = 6.5'$

$q_u = c N_c + \gamma D_f N_q + \frac{1}{2} \gamma B N_\gamma$

$= 0 + 110 \times 6.5 \times 41 + \frac{1}{2} \times 110 \times B \times 42$

~~$= 29315 + 2310 B$~~ $= 47.795 \text{ ksf}$

$q_{nu} = 47.795 - 0.110 \times 6.5 = 47.08 \text{ ksf}$

$Q = 1688 \text{ k}$

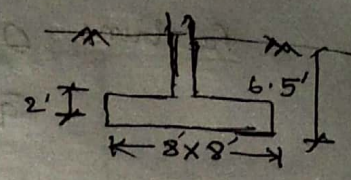
$q_a = \frac{1688}{8 \times 8} = 26.375 \text{ ksf}$

Surcharge = $2 \times \frac{150 - 110}{1000} = 0.08 \text{ ksf}$

Let, $L = B = 8'$
 $t = 2'$

$$\therefore q_a = 26.375 + 0.08 = 26.455 \text{ ksf}$$

$$F.S. = \frac{47.08}{26.455} = 1.78 > 1.5 \quad \underline{\underline{OK}}$$



Use 8x8' Footing, ~~depth~~ $t_f = 2'$

6. (c) $H = 8 \text{ m}$

$\beta = 36^\circ$

DH = large depth $\therefore D = \infty$

$H_{cr} = \frac{c_u}{\gamma_m}$

$\therefore m = 0.181$ (from graph)

$\Rightarrow c_u = \gamma_m H_{cr} = 17.3 \times 0.181 \times 8$

$= 25 \text{ kN/m}^3$

From the figure, we can see

that critical circle is a mid point circle

(Ans)

7. (c) $k = 1.5$ (medium dense)

$\bar{q} = \frac{13 \times 17.5}{2} = 113.75 \text{ kN/m}^2$

$\delta = \frac{3}{4} \times 36 = 27^\circ$

Friction load, $Q_f = \bar{q} k \tan \delta A_{\text{surface}} = 113.75 \times 1.5 \times \tan 27^\circ \times \pi \times 0.5 \times 13$
 $= 1775.3 \text{ kN}$

For pullout, $Q_b = 0$

Pullout capacity, $Q_u = Q_f + W_{\text{pile}} = 1837 \text{ kN}$ (Ans)

Allowable Pullout capacity, $Q_a = \frac{Q_f}{F.S} + W_{\text{pile}}$

$= \frac{1775.3}{3} + \frac{\pi}{4} \times 0.5^2 \times 13 \times (24)$

$= 653 \text{ kN}$ (Ans)

$N_1 = 80$

Now, $q'_0 = 13 \times 17.5 = 227.5 \text{ kN/m}^2$

End bearing, $Q_b = q'_0 N_q A_{\text{tip}} = 227.5 \times 80 \times \frac{\pi}{4} \times (0.8)^2$
 $= 948.32 \text{ kN} \quad 9500.18 \text{ kN}$

friction:

$$Q_f = \cancel{17.75 \times 2} +$$

$$\bar{q} = \frac{13.5 \times 17.5}{2} = 118.125 \text{ KN/m}^2$$

$$Q_f = 1.5 \times 118.125 \times \tan 27^\circ \times \pi \times 0.5 \times 13 + 1.5 \times 118.125 \times \tan 27^\circ \times \pi \times 0.8 \times 0.5$$

$$= \cancel{622.94 \text{ KN}} + 1957 \text{ KN}$$

∴ Total capacity, $Q_u = 11457.18 \text{ KN}$

$$\text{Allowable load} = \frac{11457.18}{3} = \boxed{3819 \text{ KN}} \quad (\text{Ans.})$$

8. (b) $c = \frac{q_u}{2} = 25 \text{ kPa} = 25 \text{ KN/m}^2$

$$\gamma = 16.8 \text{ KN/m}^3$$

$$F_s = \frac{c \sum_{n=1}^{n=p} \Delta l_n + \sum_{n=1}^{n=p} W_n \cos \alpha_n \tan \phi}{\sum_{n=1}^{n=p} W_n \sin \alpha_n}$$

$$\Delta l_n = \frac{b_n}{\cos \alpha_n}$$

slime no.	b_n (m)	h_n (m)	W_n (KN/m)	α_n (deg)	Δl_n (m)	$W_n \cos \alpha_n$	$W_n \sin \alpha_n$
1	2.6	4	174.72	58°	4.91	92.59	148.17
2	3	5.8	292.32	39°	3.86	227.18	183.96
3	3	5.6	282.24	20°	3.19	265.22	96.53
4	3	4.2	211.68	9°	3.04	209.07	33.11
5	3.5	1.9	111.72	-5°	3.51	111.29	-9.74
Σ					18.51	905.35	452.03

$$\therefore F_s = \frac{25 \times 18.51 + 905.35 \times \tan 0^\circ}{452.03}$$

$$F_s = \boxed{1.024}$$

(Ans.)

8. (c)

$c = 0$ (sand) $(D_f = 3m)$

$L' = L = 6m$

$B' = 6 - 2 \times \frac{6}{10} = 4.8m$

$\gamma = 18.5 \text{ kN/m}^3$

$\phi = \sqrt{20N_{cor} + 15^\circ} = 35^\circ$

$\therefore N_q = 33.55, N_\gamma = 37.75$

$N_\phi = \tan^2(45^\circ + \frac{\phi}{2}) = 3.69$

$S_q = 1 + 0.1 N_\phi (\frac{B'}{L'}) = 1.295$

$S_\gamma = S_q = 1.295$

$d_q = 1 + 0.1 \sqrt{N_\phi} (\frac{D_f}{B'})$

$= 1.12$

$d_\gamma = d_q = 1.12$

$q = cN_c s_c d_c + \gamma D_f N_q s_q d_q + \frac{1}{2} \gamma B' N_\gamma s_\gamma d_\gamma$

$= 0 + 18.5 \times 3 \times 33.55 \times 1.295 \times 1.12 + \frac{1}{2} \times 18.5 \times 4.8 \times 37.75$

$\times 1.295 \times 1.12$
 $= 5131.70 \text{ kN/m}^2$

$Q_{ult} = q \times L' \times B' = 147792.96 \text{ kN} = \boxed{148 \text{ MN}}$

(Ans.)

2015-16

1. (a)

skin friction

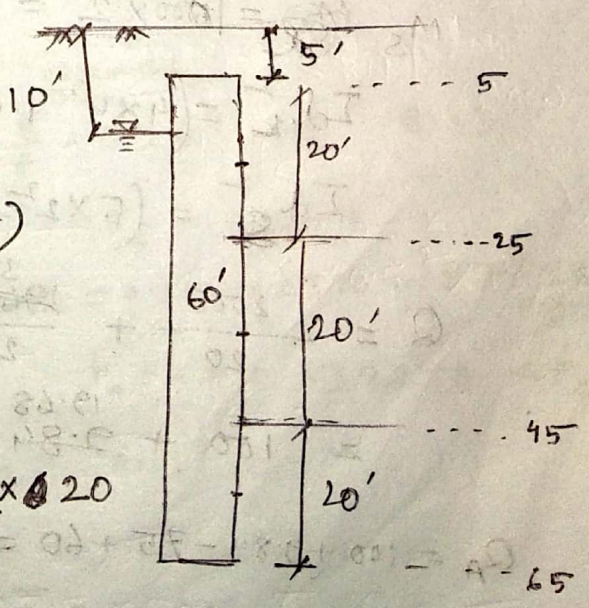
$\frac{5-25}{5-25} \quad 6_v = 120 \times 10 + 5 \times (120 - 62.5)$

$= 1487.5 \text{ psf}$

$\beta = 1.5 - 0.135 \sqrt{15} = 0.98$

skin friction = $1487.5 \times 0.98 \times \pi \times \frac{30}{12} \times 20$

$= 228.98 \text{ kip}$



$$\underline{25' - 45'}$$

$$G_v = 10 \times 120 + 25 \times (120 - 62.5) = 2637.5 \text{ psf}$$

$$\beta = 1.5 - 0.135 \sqrt{35} = 0.701$$

$$\text{skin friction} = 2637.5 \times 0.701 \times \pi \times 2.5 \times 20 = 290.42 \text{ k}$$

$$\underline{45' - 65'}$$

$$G_v = 10 \times 120 + 45 \times (120 - 62.5) = 3787.5 \text{ psf}$$

$$\beta = 1.5 - 0.135 \sqrt{55} = 0.4988$$

$$\text{skin friction} = 296.76 \text{ k}$$

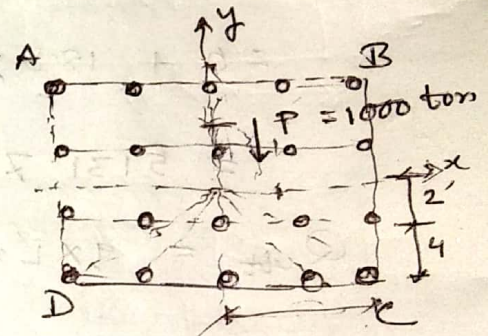
$$\text{End bearing} = 1.2 N_f A_{\text{tip}} = 1.2 \times 35 \times \frac{\pi \times 2.5^2}{4} = 206.17 \text{ k}$$

$$\therefore \text{capacity of the pier} = \boxed{1022 \text{ k}}$$

2. (a)

Additional load

4' soil



$$= 20 \times 16 \times 5 \times 150 + 4 \times 20 \times 16 \times 120$$

(pile cap)

$$= 393.6 \text{ k} = 196.8 \text{ ton}$$

$$M_L = 1000 \times 3 = 3000 \text{ ton-ft} = 6000 \text{ k-ft}$$

$$M_S = 1000 \times 2 = 4000 \text{ k-ft}$$

$$I_{d_x} = (4 \times 4^2 + 4 \times 8^2) \times 2 = 640 \text{ ft}^2$$

$$I_{d_y} = (5 \times 2^2 + 5 \times 6^2) \times 2 = 400 \text{ ft}^2$$

$$Q = \frac{2000}{20} + \frac{196.8}{20} \pm \frac{6000 \times 8}{640} \pm \frac{4000 \times 6}{400}$$

$$= 100 + 9.84 \pm 75 \pm 60$$

$$Q_A = 100 + 9.84 - 75 + 60 = 94.84 \text{ k} \quad 104.68 \text{ k}$$

$$Q_B = 244.84 \text{ k}$$

$$Q_D = -25.16 \text{ k} \text{ (tension)}$$

$$Q_C = 124.84 \text{ k}$$

3. (a) gross pressure = 4000 psf
~~psf~~
 net pressure = (4000 - 14 × 120)
 = 2320 psf

Settlement at Layer 1

$P_0 = 18 \times 120 + 3 \times (120 - 62.5)$
~~= 2320 psf~~ 2040 psf
 2160 psf

at center

$\frac{B}{z} = \frac{40}{4} = 10$
 $\frac{L}{z} = \frac{50}{4} = 12.5$

From chart, $I_6 = 0.24989$

$\Delta P = 4 \times 0.24989 \times 2320$
 = 2319 psf

$P_0 + \Delta P = 4479 \text{ psf} < P_c$

$S_1 = \frac{0.03 \times 8 \times 12}{1.8} \log \frac{4479}{2160}$
 = 0.51"

Layer 2 $P_0 = 20 \times 120 + 6 \times (120 - 62.5) = 2745 \text{ psf}$

at center

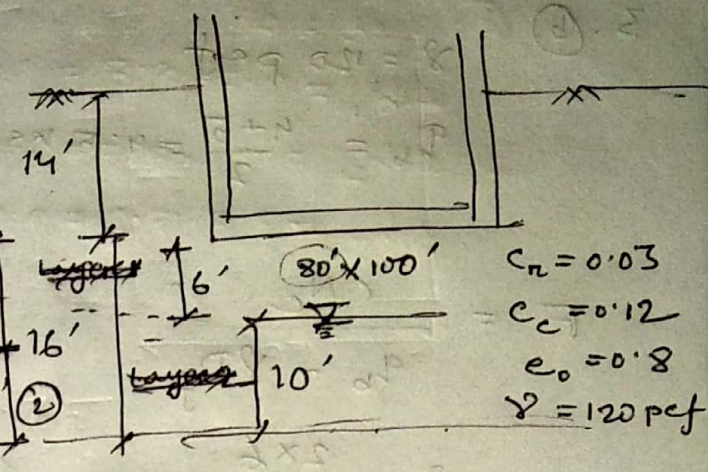
$\frac{B}{z} = \frac{40}{12} = 3.33$
 $\frac{L}{z} = \frac{50}{12} = 4.17$
 $I_6 = 0.246$

$\Delta P = 4 \times 0.246 \times 2320 = 2282.88$

$P_0 + \Delta P = 5027.88 < P_c$

$S_2 = \frac{0.03 \times 8 \times 12}{1.8} \log \frac{5027.88}{2745} = 0.42"$

∴ Total S at center = 0.93"
 corner = 0.30" (Ans.)



at corner

$\frac{B}{z} = 20$ & $\frac{L}{z} = 25$

$I_6 = 0.25$

$\Delta P = 6 \times 0.25 \times 2320 = 580 \text{ psf}$

$P_0 + \Delta P = 2740 < P_c$

$S_1 = \frac{0.03 \times 8 \times 12}{1.8} \log \frac{2740}{2160}$
 = 0.17"

at corner

$\frac{B}{z} = 6.67$, $\frac{L}{z} = 8.33$

$I_6 = 0.249$

$\Delta P = 0.249 \times 2320 = 577.68 \text{ psf}$

$P_0 + \Delta P = 3322.68 < P_c$

$S_2 = 0.13"$

3. (b)

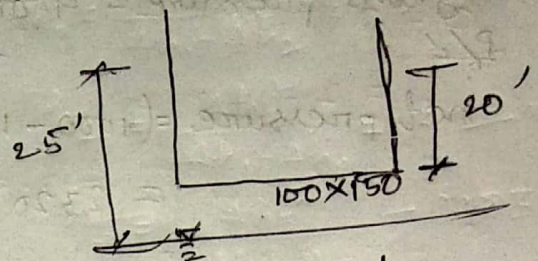
$$\gamma = 120 \text{ pcf}$$

$$q_b = \frac{4+5}{2} = 4.5 \text{ ksf}$$

$$F = \frac{CN_c}{q_b - \gamma D_f}$$

$$= \frac{2 \times 6}{4.5 - 0.12 \times 20} = 5.7$$

(Ans.)



$$c = 2 \text{ ksf}$$

$$\frac{D_f}{B} = 0.2$$

$$N_c = 5.3 \times \left(1 + 0.2 \times \frac{120}{150}\right) = 6$$

4. (a)

We have to take N value

$$\text{at a depth } D_f + B = 15'$$

$$N_{avg} = 20$$

net pressure at the bottom

$$\text{of footing, } q_{net} = \frac{200}{10 \times 10} + 2.5 \times \frac{150 - 120}{1000}$$

$$= 2.075 \text{ ksf} = 1.0375 \text{ tsf}$$

water table correction factor, $C_w = 0.5 + 0.5 \times \frac{DN}{D_f + B}$

$$= 0.5 + 0.5 \times \frac{10}{10+5}$$

$$= 0.833$$

$$\frac{D_f}{B} = 0.5 \text{ and } N = 20$$

$$\therefore \text{Allowable } q_a = 0.11N = 2.20 \text{ tsf}$$

$$\text{Corrected } q_a = 2.20 \times 0.833 = 1.83 \text{ tsf}$$

for 1" settlement

$$\text{settlement of the footing} = \frac{1}{1.83} \times 1.0375$$

$$= 0.567'' \approx 0.57''$$

For $q_a = 1.83 + 2.20 \text{ tsf}$, $B = 3.3'$

for, $B = 10'$, $q_a = \frac{2.20}{3.30} \times 10 = 6.67 \text{ tsf}$

Corrected $q_a = 0.833 \times 6.67 = 5.56 \text{ tsf}$

Factor of safety = $\frac{5.56 \times 2}{1.0375} = 10.7$ (Ans.)

5. (c) $N_{avg.} = 19$

$\gamma = 100 \text{ pcf}$

$D_f + B = 10 + 30 = 40$

$q_a = 0.22 N = 4.18 \text{ tsf}$

$C_w = 0.5 + 0.5 \times \frac{10}{40} = 0.625$

Corrected $q_a = 4.18 \times 0.625 = 2.6125 \text{ tsf}$

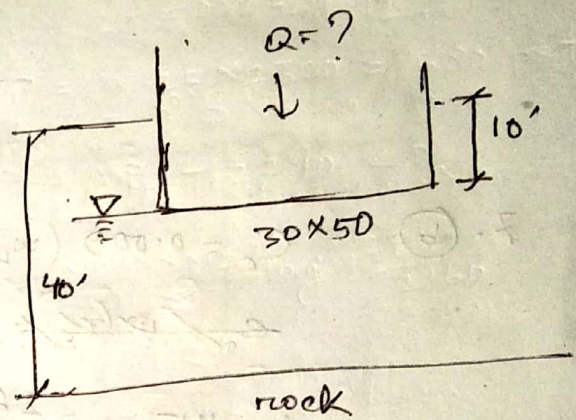
Surcharge = $\gamma D_f = 100 \times 10 = 1000 \text{ psf} = 1 \text{ ksf}$
 $= 0.5 \text{ tsf}$

Contact pressure = $(2.6125 + 0.5) = 3.1125 \text{ tsf}$

$\therefore Q = 3.1125 \times 30 \times 50 = 4668.75 \text{ tons}$

$\approx 4670 \text{ tons}$

(Ans.)



6. (b)

~~Final N₂~~ standard wt. of hammer = 140 lb
 hammer wt. of used " = 120 lb

⊙

$W_1 N_1 = W_2 N_2$

$\Rightarrow 120 \times 10 = 140 \times N_2$

$\Rightarrow N_2 = 8.57 \approx 9$

(Ans.)

2

$$\Delta t = 24$$

$$\Delta h_1 = 9.5 - 8.5 = 1 \text{ m}$$

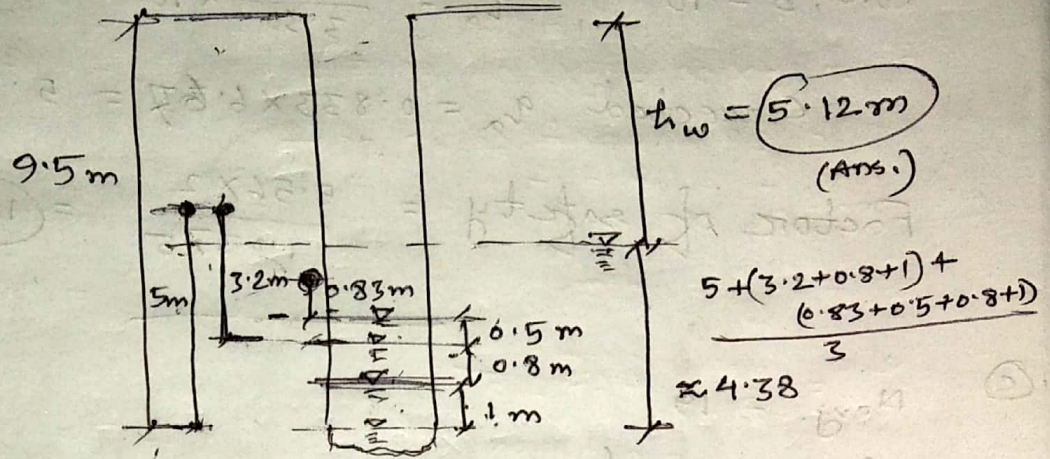
$$\Delta h_2 = 8.5 - 7.7 = 0.8 \text{ m}$$

$$\Delta h_3 = 7.7 - 7.2 = 0.5 \text{ m}$$

$$h_0 = \frac{\Delta h_1^2}{\Delta h_1 - \Delta h_2} = 5 \text{ m}$$

$$h_2 = \frac{\Delta h_2^2}{\Delta h_1 - \Delta h_2} = 3.2 \text{ m}$$

$$h_3 = \frac{\Delta h_3^2}{\Delta h_2 - \Delta h_3} = 0.83 \text{ m}$$



7. (b)

$$C_c = 0.009 (w_L - 10) = 0.27$$

$$\gamma_{sat} = \frac{G_s + e}{1 + e} \gamma_w$$

$$\Rightarrow 115 = \frac{2.65 + e}{1 + e} \times 62.5$$

$$\Rightarrow e_0 = 0.96$$

$$P_0 = 10 \times 125 + 20 \times (125 - 62.5) + 10 \times (115 - 62.5)$$

$$= 3025 \text{ psf}$$

$$\Delta P = \frac{500 \times \frac{\pi}{4} \times 80^2}{\frac{\pi}{4} \times (80 + 40)^2} = 222.22 \text{ psf}$$

$$S = \frac{0.27 \times 20 \times 12}{1.96} \log \frac{3025 + 222.22}{3025}$$

$$= 0.10508'' \approx 0.1'' = 1.02'' \text{ (Ans.)}$$

8. (a) (i)

$$H_{cr} = \frac{c}{\gamma_m} = \frac{25}{18 \times 0.06} = 23.15 \text{ m (Ans.)}$$

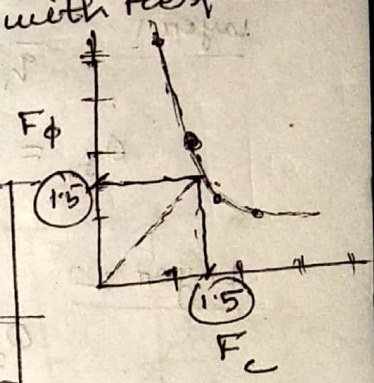
$\beta = 45^\circ$
 $\phi = 20^\circ$
 $m = 0.06$

(ii) Let us assume that the full friction is mobilized
 $\phi_d = \phi = 20^\circ$

$$m = 0.06 = \frac{c_d}{\gamma H} \Rightarrow c_d = 0.06 \times 18 \times 10 = 10.8 \text{ kN/m}^2$$

$$F_\phi = \frac{\tan \phi}{\tan \phi_d} = 1 \quad \text{and} \quad F_c = \frac{c}{c_d} = \frac{25}{10.8} = 2.31$$

$\therefore F_\phi \neq F_c$, so this not the F.S. with respect to strength

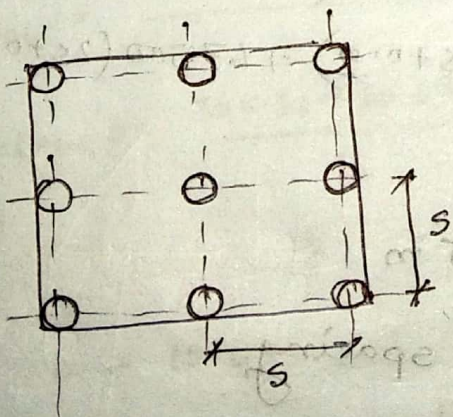


ϕ_d	F_ϕ	m	c_d (kN/m ²)	F_c
20	1	0.06	10.8	2.31
15	1.36	0.085	15.3	1.63
10	2.06	0.11	19.8	1.26
5	4.16	0.136	24.48	1.02

From graph, $F_\phi = F_c = F_s = 1.50$ (Ans.)

2014-15

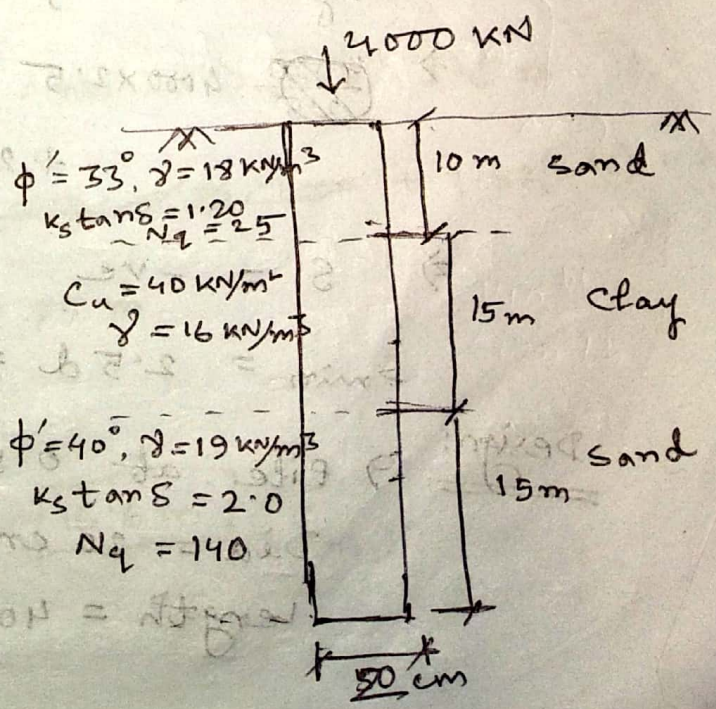
3.



Assume,

Dia of pile, $d = 50 \text{ cm} = 0.5 \text{ m}$
 $= 25 \text{ m} \times 0.2 \text{ m}$

Length = 40m



End bearing, $Q_b = \cancel{cN_c A_b} = q'_0 N_c A_b$

$$q'_0 = 10 \times 18 + 15 \times 16 + 15 \times 19 = 705 \text{ kN/m}^2$$

$$\therefore Q_b = 705 \times 140 \times (2.5 + 0.5)^2 = 98700 (2.5 + 0.5)^2$$

Skin Friction:

$$A_{f1} = 4 \times (2.5 + 0.5) \times 10$$

$$A_{f2} = 4 \times (2.5 + 0.5) \times 15$$

$$A_{f3} = 4 \times (2.5 + 0.5) \times 15$$

Layer 1

$$\bar{q}_1 = \frac{10 \times 18}{2} = 90 \text{ kN/m}^2$$

$$Q_{f1} = \bar{q}_1 k_1 \tan \delta_1 A_{f1} = 90 \times 1.20 \times 4 (2.5 + 0.5) \times 10 = 4320 (2.5 + 0.5)$$

Layer 2

$$Q_{f2} = \alpha C_u A_{f2} = 1 \times 40 \times 4 (2.5 + 0.5) \times 15 = 2400 (2.5 + 0.5)$$

Layer 3

$$\bar{q}_3 = 10 \times 18 + 15 \times 16 + \frac{15}{2} \times 19 = 562.5 \text{ kN/m}^2$$

$$Q_{f3} = 562.5 \times 2 \times 4 (2.5 + 0.5) \times 15 = 67500 (2.5 + 0.5)$$

Now,

$$Q_{ug} = \cancel{Q_b} + Q_f \quad Q_{allow} = \frac{Q_b + Q_f}{F.S.}$$

$$\Rightarrow \frac{4000}{1.25} \times 2.5 = 98700 (2.5 + 0.5)^2 + 4320 (2.5 + 0.5) + 2400 (2.5 + 0.5) + 67500 (2.5 + 0.5)$$

$$\Rightarrow S = -ve$$

$$S_{min} = 2.5 d = 0.5 \text{ m}$$

Design:

9 Pile at 0.5 m spacing

Dia = 20 cm

length = 40 m

Check:

capacity as a single pile

$$Q_b = q' N_c A_b = 705 \times 140 \times \frac{\pi}{4} \times 0.2^2 = 3100.75 \text{ kN}$$

$$Q_f = Q_{f_1} + Q_{f_2} + Q_{f_3}$$

$$= 90 \times 1.20 \times \pi \times 0.2 \times 10 + 1 \times 40 \times \pi \times 0.2 \times 15 + 562.5 \times 2 \times \pi \times 0.2 \times 15$$

$$= 11658.45 \text{ kN}$$

$$Q_{allow} = \frac{(3100.75 + 11658.45) \times 9}{2.5} = 53133 \text{ kN}$$

$$= 5904 \text{ kN} > 4000 \text{ kN}$$

OK

4.

end bearing, $Q_b = 100 \times 9 \times \frac{\pi}{4} \times 0.45^2$

$$= 143.14 \text{ kN}$$

skin friction:

layer 1: $Q_{f_1} = 0.8 \times 45 \times \pi \times 0.45 \times 6$

$$= 305.36 \text{ kN}$$

layer 2: $Q_{f_2} = 0.5 \times 100 \times \pi \times 0.45 \times L = 70.686L \text{ kN}$

$$W_{pile} = \frac{\pi}{4} \times 0.45^2 \times (6+L) \times 24 = 3.82(L+6) \text{ kN}$$

1st condition:

$$143.14 + 305.36 + 70.686L = 400 \Rightarrow L = 10.6 \text{ m}$$

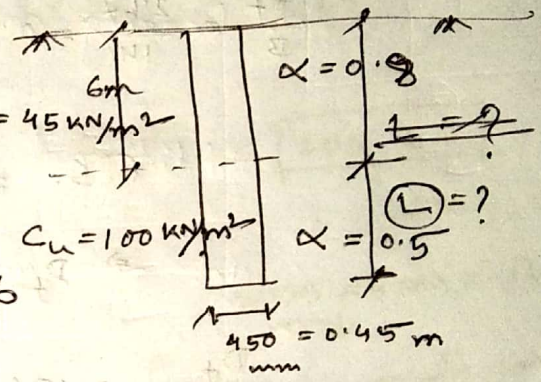
① $Q_{allow} = \frac{3}{3}$

② $Q_{allow} = \frac{305.36 + 70.686L}{3} = \frac{200}{3} + 3.82(L+6) = 200$

$$\Rightarrow L = 2.75 \text{ m}$$

$$L = 10.6 \text{ m}$$

∴ Length of pile = 16.6 m (Ans.)



6. Raft size = 14 m x 21 m

$$q_u = 80 \text{ kN/m}^2 \quad \therefore c = 40 \text{ kN/m}^2$$

$$q_b = 120 \text{ kN/m}^2$$

Let, $\frac{D_f}{B} = 0.1$ From chart, $N_c = 5.3$

$$\text{modified } N_c = 5.3 \times \left(1 + 0.2 \times \frac{14}{21}\right) = 6$$

$$\text{F.S.} = \frac{c N_c}{q_b - \gamma D_f}$$

$$\Rightarrow 120 - 15 \times D_f = \frac{40 \times 6}{3}$$

$$\Rightarrow D_f = 2.67 \text{ m}$$

Now,

$$\frac{D_f}{B} = \frac{2.67}{14} = 0.19 \quad \text{From chart, } N_c = 5.4$$

$$\text{modified } N_c = 6.12$$

$$\text{F.S.} = 3 = \frac{40 \times 6.12}{120 - 15 \times D_f}$$

$$\Rightarrow D_f = 2.56 \text{ m} \approx 2.6 \text{ m}$$

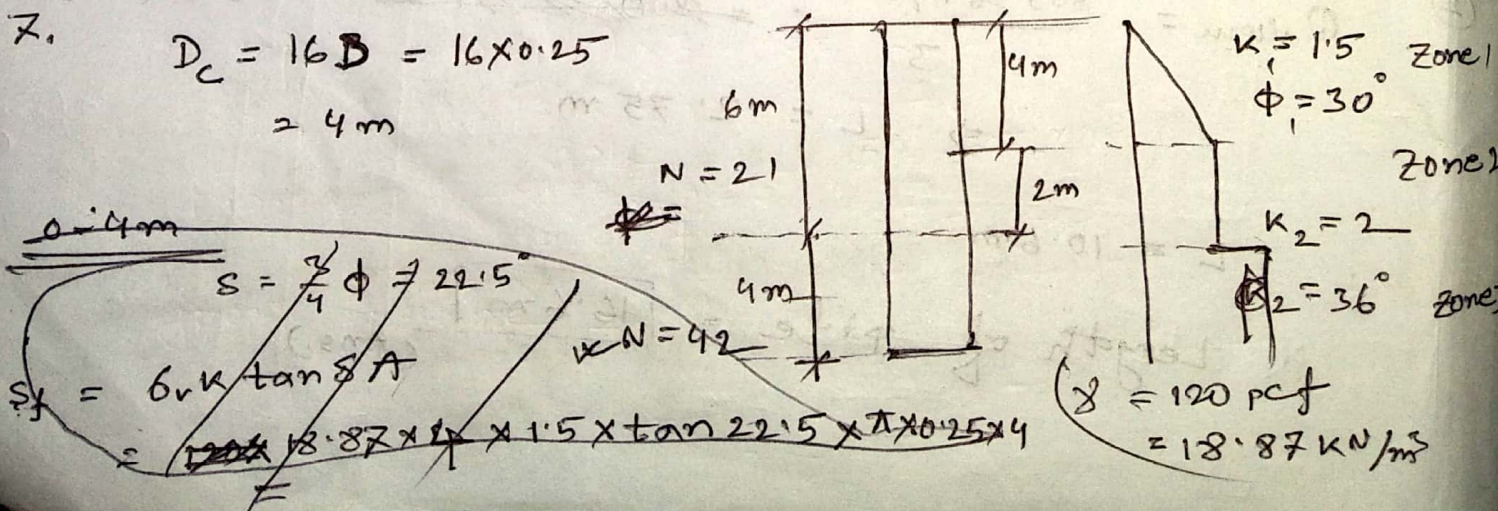
$$\frac{D_f}{B} = 0.186 \text{ which is close to } 0.19$$

So, further trial is not required

∴ Required depth for raft, $D_f = \boxed{2.6 \text{ m}}$

(Ans.)

7. $D_c = 16B = 16 \times 0.25 = 4 \text{ m}$



$$q'_0 = 4 \times 18.87 = 75.48 \text{ kN/m}^2$$

$$\text{at layer 2, } q'_2 = 75.48 + \frac{1}{2} \times 4 \times 18.87 = 113.22 \text{ kN/m}^2$$

0-4m $\delta = \frac{3}{4}\phi = 22.5^\circ$

$$\text{skin friction} = \frac{75.48}{2} \times 1.5 \times \tan 22.5^\circ \times \pi \times 0.25 \times 4$$

$$= 73.67 \text{ kN}$$

4-6m skin friction = $75.48 \times 1.5 \times \tan 22.5^\circ \times \pi \times 0.25 \times 2$

$$= 73.67 \text{ kN}$$

6-10m skin friction = $113.22 \times 2 \times \tan 27^\circ \times \pi \times 0.25 \times 4$

$$= 362.47 \text{ kN}$$

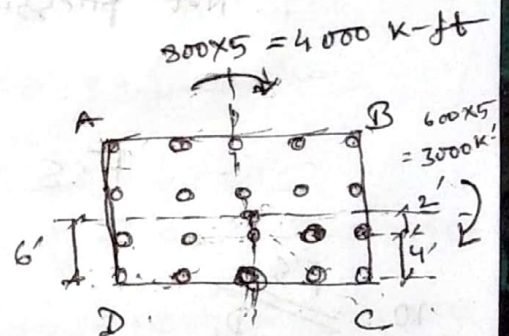
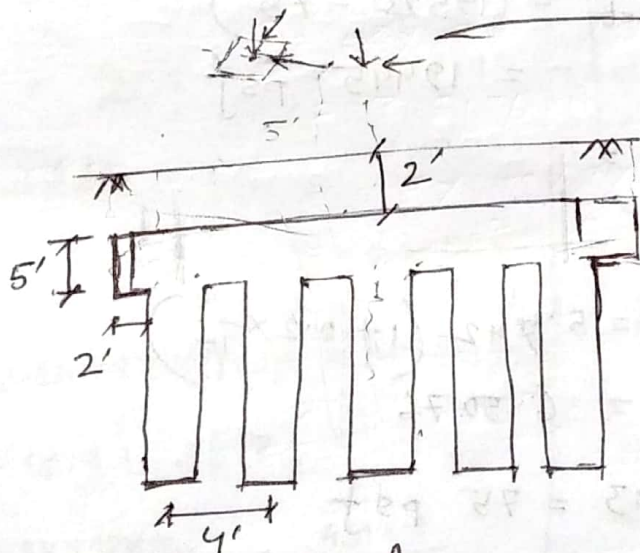
$\delta = \frac{3}{4}\phi = 27^\circ$

End bearing, $Q_b = (75.48 + 4 \times 18.87) \times 42 \times \frac{\pi}{4} \times 0.25^2$

$$= 311.23 \text{ kN}$$

$\therefore P_{\text{total}} = 821.04 \text{ kN}$ $\therefore P_{\text{allow}} = \frac{821.04}{4} = \boxed{205 \text{ kN}}$ (Ans.)

9. (b)



~~Q~~ Additional load

$$= 20 \times 16 \times 5 \times 150 + \frac{1}{2} \times 20 \times 16 \times 120$$

$$= 316.8 \text{ k}$$

$$\Sigma d_L^2 = (4 \times 4^2 + 4 \times 8^2) \times 2$$

$$= 640 \text{ ft}^2$$

$$\Sigma d_s^2 = (5 \times 2^2 + 5 \times 6^2) \times 2$$

$$= 400 \text{ ft}^2$$

$$Q = \frac{2000}{20} + \frac{316.8}{20} \pm \frac{4000 \times 8}{640} \pm \frac{3000 \times 6}{400}$$

$$Q_{\max} = 210.84 \text{ k}$$

$$Q_{\min} = 20.84 \text{ k} \quad \left. \vphantom{Q_{\min}} \right\} \text{(Ans.)}$$

10.

Factor of safety

$$\therefore \frac{D_f}{B} = \frac{7}{10} = 0.7 \rightarrow N_c = 5.742$$

$$\text{corrected } N_c = 5.742 \times \left(1 + 0.2 \times \frac{10}{15}\right) = 6.5076$$

$$\text{net bearing capacity, } q_d = C N_c = 3 \times 6.5076 = 19.52 \text{ ksf}$$

$$\text{additional weight} = (150 - 125) \times 3 = 75 \text{ psf}$$

$$\therefore \text{Net pressure, } q_{\text{net}} = (19520 - 75) = 19445 \text{ psf}$$

$$F.S. = 19.5$$

10. FS

$$\frac{D_f}{B} = 0.7, \quad N_c = 5.742 \left(1 + 0.2 \times \frac{10}{15}\right) = 6.5076$$

$$q_u = (150 - 125) \times 3 = 75 \text{ psf}$$

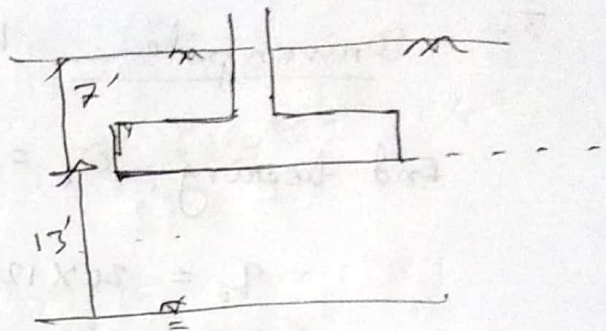
$$F.S. = \frac{C N_c}{q_u} = \frac{3 \times 6.5076 \times 10^3}{75}$$

gross pressure =

$$P_0 = 13.5 \times 125 = 1687.5 \text{ psf}$$

$$P_0 + \Delta P < P_c, \text{ OK clay}$$

$$S = \frac{0.03 \times 13 \times 12}{1.7} \log 1 = 0$$

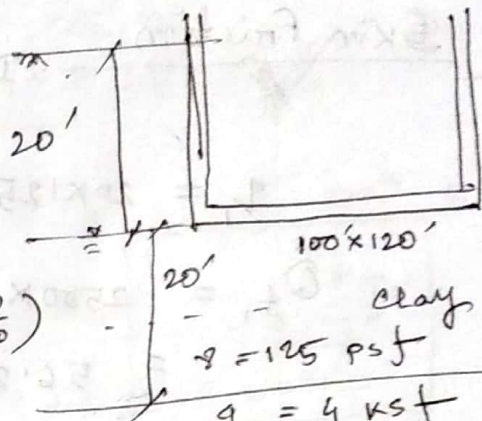


11. Factor of safety

$$q_{net} = 4000 - 125 \times 20 = 1500 \text{ psf}$$

$$\frac{D_f}{B} = \frac{20}{100} = 0.2, \quad N_c = 5.312 \times \left(1 + 0.2 \times \frac{100}{120}\right) = 6.2$$

$$F.S. = \frac{c N_c}{q_{net}} = \frac{2000 \times 6.2}{1500} = 8.27 \approx \textcircled{8} \text{ (Ans.)}$$



$$q_u = 4 \text{ ksf}$$

$$e_0 = 0.8$$

$$c_u = 0.15$$

$$c_n = 0.04$$

$$P_c = 7000 \text{ psf}$$

$$P_0 = 20 \times 125 + 10 \times (125 - 62.5) = 3125 \text{ psf}$$

At middle

$$\frac{B}{Z} = 5, \quad \frac{L}{Z} = 6 \quad \therefore I_6 = 0.24885$$

$$\Delta P = 4 \times 0.24885 \times 1500 = 1493.1 \text{ psf}$$

$$P_0 + \Delta P = 4618.1 < P_c$$

$$\therefore S = \frac{0.04 \times 20 \times 12}{1.8} \log \frac{4618.1}{3125}$$

$$= \textcircled{0.45} = \textcircled{0.91} \text{ (Ans.)}$$

At corner

$$\frac{B}{Z} = 10, \quad \frac{L}{Z} = 12 \quad \therefore I_6 = 0.24989$$

$$\Delta P = 0.24989 \times 1500 = 374.835 \text{ psf}$$

$$P_0 + \Delta P = 3499.835 \text{ psf} < P_c$$

$$S = \frac{0.04 \times 20 \times 12}{1.8} \log \frac{3499.835}{3125}$$

$$= \textcircled{0.13} = \textcircled{0.26} \text{ (Ans.)}$$

3.

Driven pile

$L = 40'$

End bearing, $Q_b = q_o N_c A_b$

$$q_o = 20 \times 125 + 25 \times (125 - 62.5) = 4062.5$$

$$\therefore Q_b = 4062.5 \times 80 \times \frac{15 \times 15}{144} = 507.8 \text{ k}$$

Skin friction

$D_c = 20'$

$$q_1 = 20 \times 125 = 2500 \text{ psf}$$

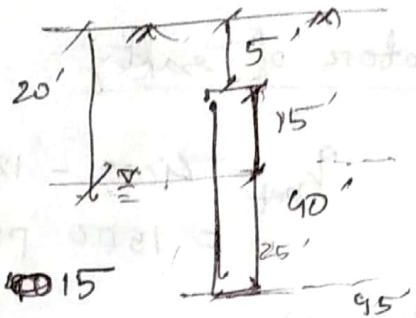
$$Q_{f1} = 2500 \times 1 \times 0.3 \times 4 \times \frac{15}{12} \times 15 = 56.25 \text{ k}$$

$$q_2 = 2500 + \frac{1}{2} \times 25 \times (125 - 62.5) = 3281.25 \text{ psf}$$

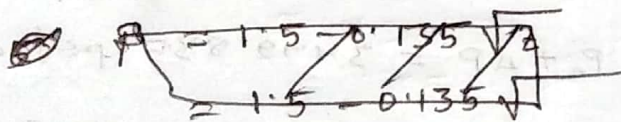
$$Q_{f2} = 3281.25 \times 2 \times 0.5 \times 4 \times \frac{15}{12} \times 25 = 410.156 \text{ k}$$

$$\text{Allowable capacity} = \frac{507.8 + 56.25 + 410.2}{2.5}$$

$$= \boxed{390 \text{ k}} \quad (\text{Ans.})$$

Drilled Pier

$\text{Dia} = 30'' = 2.5'$



$5 - 20'$

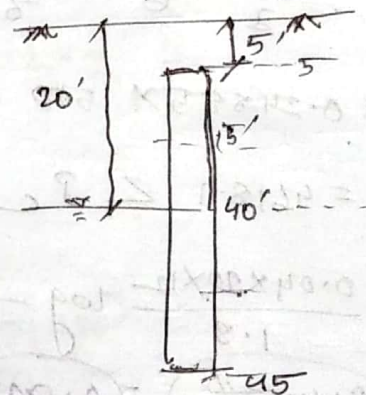
$$q_v = 20 \times 125 = 2500 \text{ psf}$$

$$\beta = 1.5 - 0.135 \sqrt{12.5} = 1.023$$

$$Q_{f1} = 2500 \times 1.023 \times 2.5 \times 15 = 301.3 \text{ k}$$

$$q_v = 20 \times 125 + 25 \times (125 - 62.5) = 4062.5 \text{ psf}$$

$$\beta = 1.5 - 0.135 \sqrt{32.5} = 0.73$$



$$Q_{fz} = 4062.5 \times 0.73 \times \pi \times 2.5 \times 25 = 582.3 \text{ k}$$

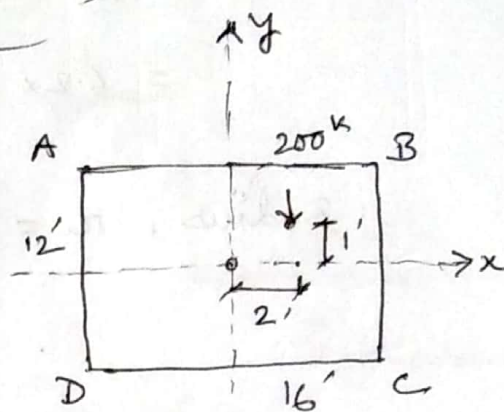
End bearing: $Q_b = 1.2 N_f A_{tip} = 1.2 \times 30 \times \frac{\pi}{4} \times 2.5^2$
 $= 176.7 \text{ k}$

\therefore Allowable capacity = $\frac{301.3 + 582.3 + 176.7}{2.5}$
 $= \boxed{424 \text{ k}}$ (Ans.)

9. (a)

~~Conventional~~ $M_x = 200 \times 1 = 200 \text{ k-ft}$

$M_y = 200 \times 2 = 400 \text{ k-ft}$



Conventional method

$$q = \frac{200}{12 \times 16} \pm \frac{200 \times 6}{\frac{16 \times 12^3}{12}} \pm \frac{400 \times 8}{\frac{12 \times 16^3}{12}}$$

$$= 1.042 \pm 0.521 \pm 0.781$$

$q_A = 0.782 \text{ ksf}$

$q_C = 1.302 \text{ ksf}$

$q_B = 2.344 \text{ ksf}$

$q_D = -0.26 \text{ ksf}$ (tension)

Meyerhof method

$L' = 16 - 2 \times 2 = 12'$

$B' = 12 - 2 \times 1 = 10'$

$\therefore q = \frac{200}{10 \times 12} = \boxed{1.67}$ (Ans.)

6. (a)

(i) $H_{crit} = \frac{c_u}{\gamma m} = \frac{20}{17 \times 0.19}$

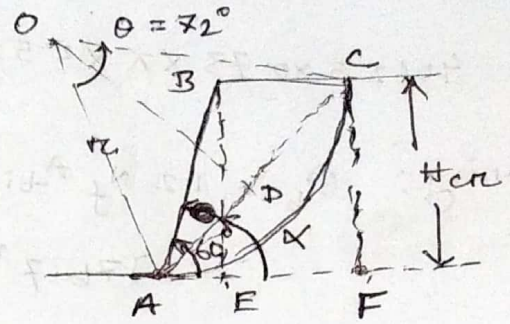
From graph, $m = 0.19$

$= \boxed{6.2 \text{ m}}$ (Ans.)

(ii) As $\beta = 60^\circ > 53^\circ$, the critical circle is a toe circle.

(c)

From graph,
 $\alpha = 36^\circ$
 $\theta = 72^\circ$



$$\overline{AF} = H_{cr} \cot \alpha$$

$$= 6.2 \times \cot 36^\circ = \boxed{8.53 \text{ m}}$$

$$\overline{BE} = \overline{AF} - \overline{AE} = H_{cr} \cot \alpha - H_{cr} \cot \beta$$

$$= 6.2 \times (\cot 36^\circ - \cot 60^\circ) = \boxed{4.95 \text{ m}}$$

$$\text{Radius, } r = \frac{H_{cr}}{2 \sin \alpha \sin \frac{\theta}{2}} = \boxed{8.97 \text{ m}}$$

8.

$$s_d = \frac{q_s s_w}{1 + e_0} \Rightarrow e_0 = 0.325$$

Settlement

$$q_0 = 9 \times 125 = 1125 \text{ psf}$$

$$\Delta q = \frac{250 \times 10^3}{9 \times 11} = 2525.25 \text{ psf}$$

$$\therefore q_0 + \Delta q = 3650.25 < q_{v \max}$$

\therefore OC clay

$$S = \frac{0.4 \times 2 \times 12}{1.325} \log \frac{3650.25}{1125}$$

$$= \boxed{0.37''}$$

(Ans)

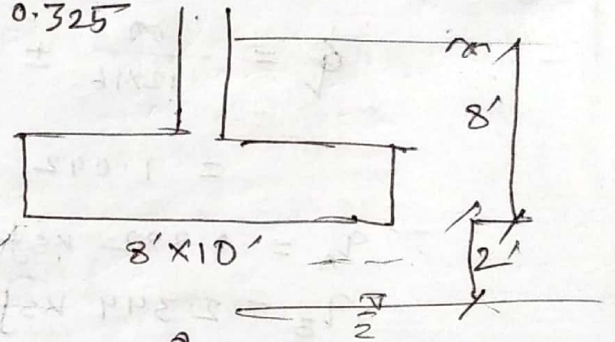
Capacity:

$$\frac{D_f}{B} = \frac{8}{8} = 1$$

From graph, $N_c = 6.2$

$$\text{corrected } N_c = 6.2 \times \left(1 + 0.2 \times \frac{8}{10}\right) = 7.192$$

$$q_d = C N_c = 1 \times 7.192 = 7.192 \text{ ksf}$$



$$q = 125 \text{ pcf}$$

$$c_c = 0.15$$

$$\phi_c = 0.04$$

$$q_{v \max} = 2000 \text{ psf}$$

Additional weight = $(150 - 125) \times 2.5 = 62.5 \text{ psf}$

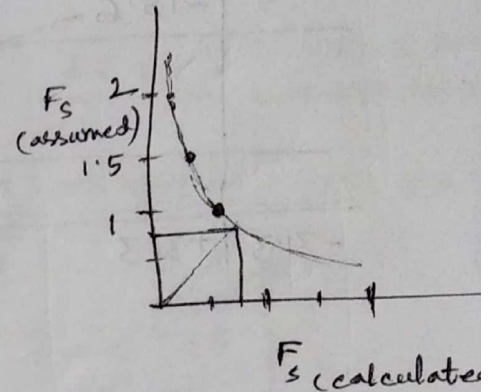
Net pressure under footing = $(7192 - 62.5) = 7129.5 \text{ psf}$

Capacity of the footing = $7129.5 \times 8 \times 10 = 570.36 \text{ k}$

Allowable capacity = $\frac{570.36}{2.5} = \boxed{228 \text{ k}}$ (Ans.)

7. (a)

Assumed	$\frac{C}{F_s \gamma H}$	ϕ_d	$F = \frac{\tan \phi}{\tan \phi_d}$
1	0.0508	16.1°	1.26
1.5	0.0339	21.9°	0.905
2	0.0254	24°	0.82



$\gamma = 105 \text{ pcf}$

$c = 400 \text{ psf}$

$F_s = 0.75$

$\phi = 20^\circ$

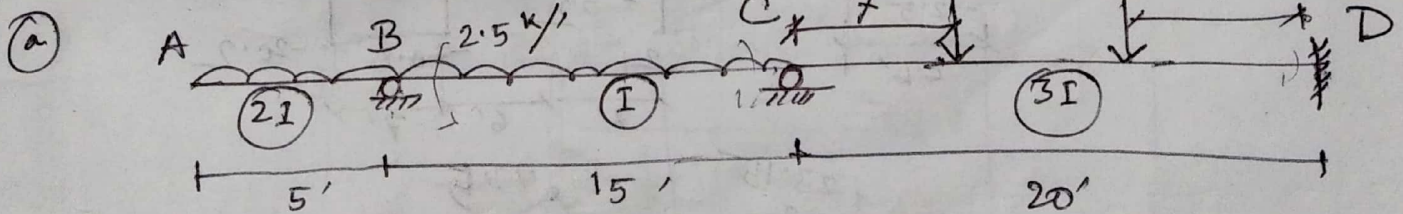
$\alpha_u = 0.4$

$\beta = 20^\circ$

$H = 75'$

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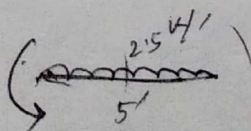
~~DF_{BA}~~

$DF_{BC} = 1$

$DF_{DC} = 0$

$DF_{CD} = \frac{\frac{3I}{20}}{\frac{3I}{20} + \frac{3}{4} \times \frac{I}{15}} = 0.75$

$DF_{CB} = 0.25$



$$FEM_{BA} = \frac{2.5 \times 15^2}{12} = +31.3 \text{ k-ft}$$

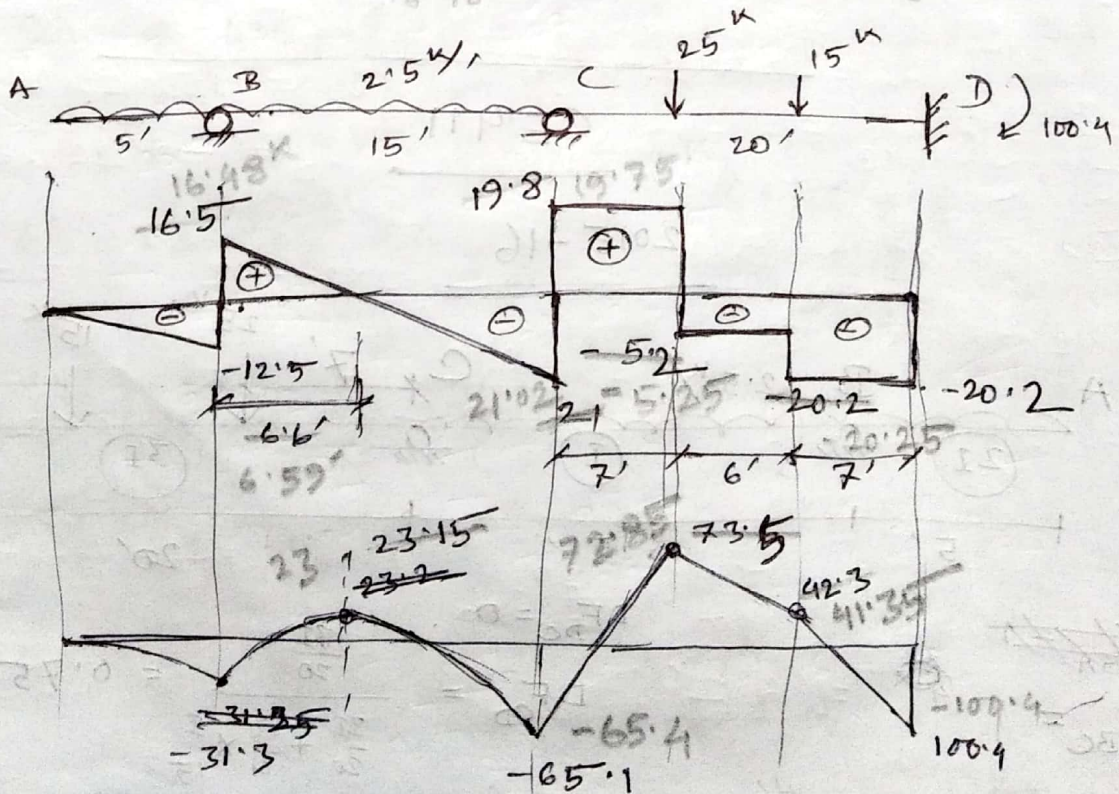
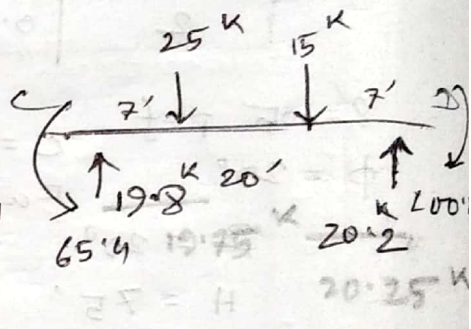
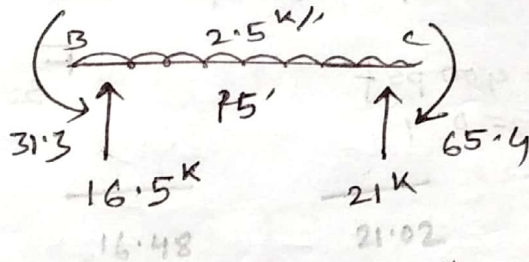
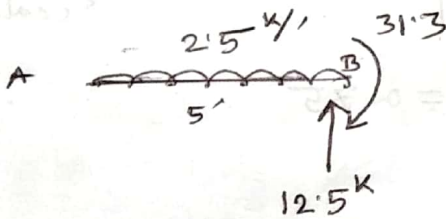
$$FEM_{CD} = +97.8 \text{ k-ft}$$

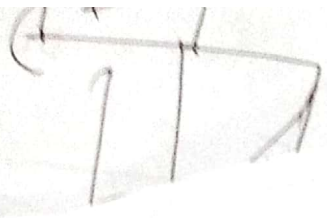
$$FEM_{BC} = +\frac{2.5 \times 15^2}{12} = +46.9 \text{ k-ft}$$

$$FEM_{DC} = -84.2 \text{ k-ft}$$

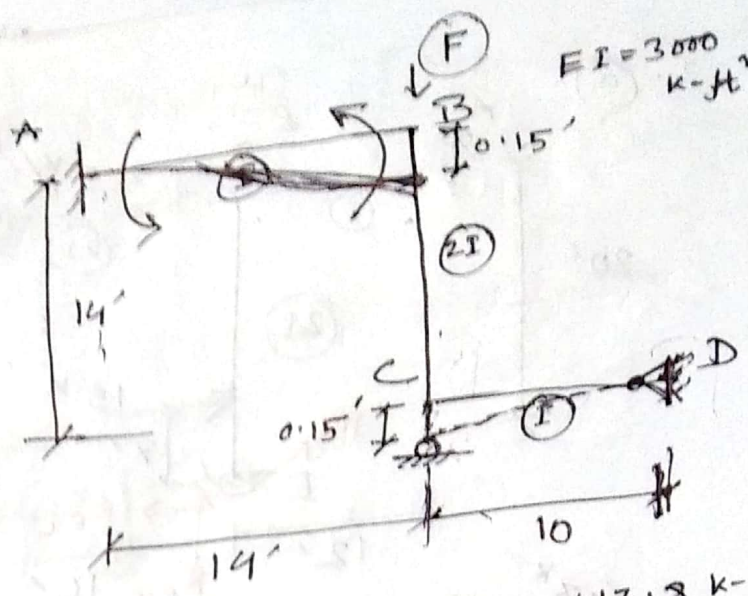
$$FEM_{CB} = -46.9 \text{ k-ft}$$

	1	0.25	0.75	
BA	BC	CB	CD	DC
-31.3	+46.9	-46.9	+97.8	-84.2
	-15.6	-12.7	-38.2	+21.2
		-7.8		-19.1
		+2.0	+5.8	
				+2.9
-31.3	+31.3	-65.4	+65.4	-100.4





$$EI = 3000 \text{ k-ft}^2$$



$$DF_{AB} = 0$$

$$DF_{BA} = \frac{\frac{I}{14}}{\frac{I}{14} + \frac{2I}{14}} = 0.33$$

$$DF_{BC} = 0.67$$

$$DF_{CB} = \frac{\frac{2I}{14}}{\frac{2I}{14} + \frac{3}{4} \times \frac{I}{10}} = 0.66$$

$$DF_{CD} = 0.34$$

$$DF_{DC} = 1$$

$$FEM_{AB} = \frac{6EI\Delta}{L^2} = +13.78 \text{ k-ft}$$

$$FEM_{BA} = +13.78 \text{ k-ft}$$

	0.33 BA	0.67 BC	0.66 CB	0.34 CD	1 DC
AB	+13.8	+13.8			
	-4.6	-9.2	-4.6		
			+3.0	+1.6	
		+1.5			
	-0.5	-1.0	-0.5		
			+0.3	+0.2	
		+0.2			
	-0.1	-0.1			
	+11.2	+8.6	-1.8	+1.8	

Force, $F = \frac{11.2 + 8.6}{14} = 1.41 \text{ k}$ (Ans.)

$$\Rightarrow \begin{bmatrix} 0 \\ 0 \end{bmatrix} = \begin{bmatrix} 77.22 \\ -53.33 \end{bmatrix} + \begin{bmatrix} -2.734 \\ -24.609 \end{bmatrix} + \begin{bmatrix} 4316.67 & 875 \\ 875 & 2450 \end{bmatrix} \begin{bmatrix} u_1 \\ u_2 \end{bmatrix}$$

$$\Rightarrow \begin{bmatrix} u_1 \\ u_2 \end{bmatrix} = \begin{bmatrix} -0.026 \\ +0.041 \end{bmatrix}$$

Now,

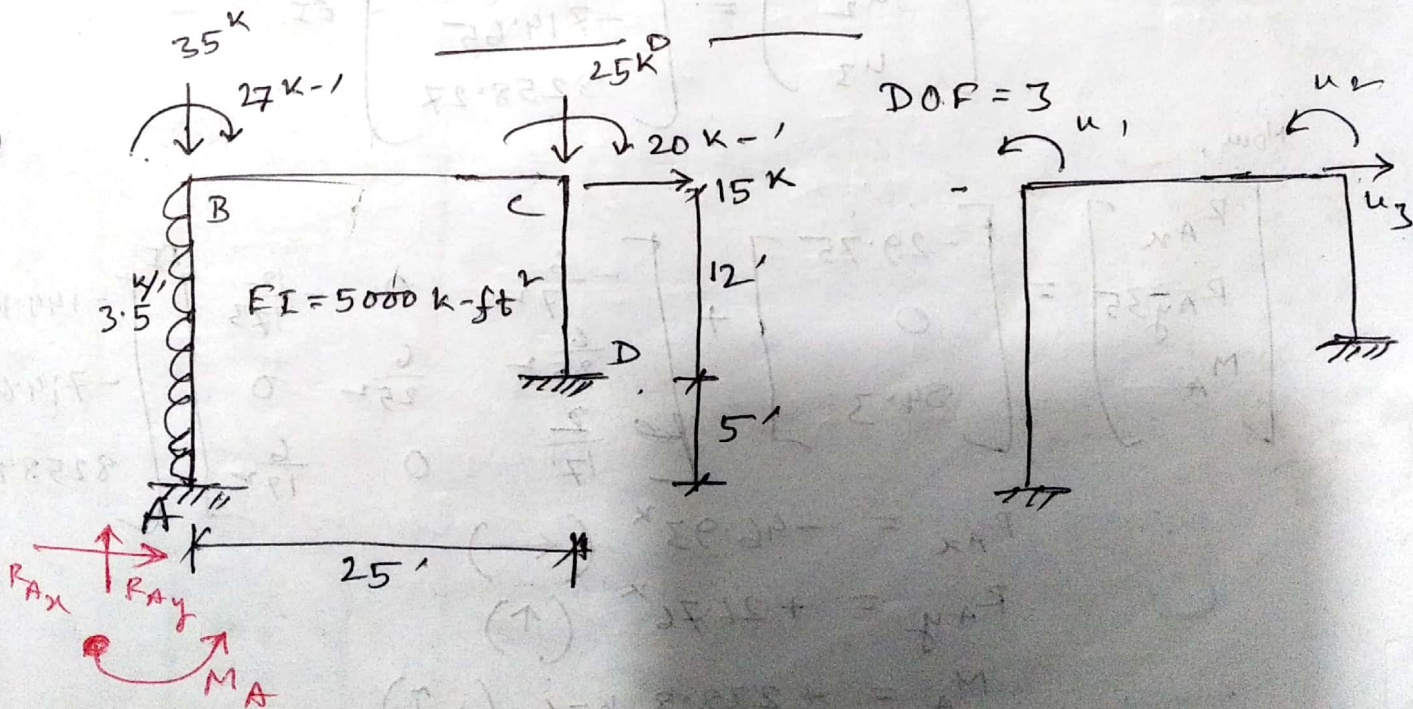
$$\begin{bmatrix} R_{Ex} \\ R_{Ey} \\ M_E \end{bmatrix} = \begin{bmatrix} 10.77 \\ 20 \\ 44.36 \end{bmatrix} + \begin{bmatrix} 0 \\ -\frac{12EI}{12^3} \times 0.15 - \frac{12 \times 2EI}{16^3} \times 0.15 \\ 0 \end{bmatrix} +$$

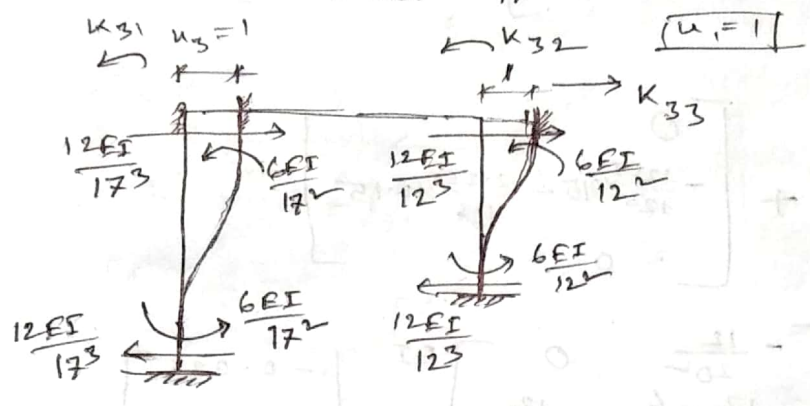
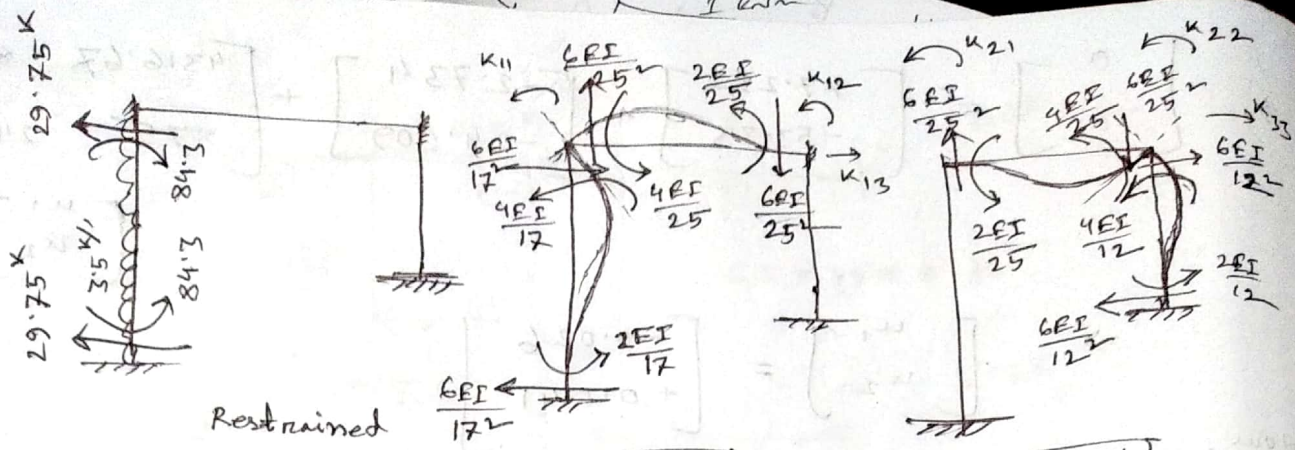
$$\begin{bmatrix} -\frac{12}{20^2} & 0 \\ \frac{12}{16^2} + \frac{6}{12^2} & \frac{12}{16^2} \\ -\frac{4}{20} & 0 \end{bmatrix} EI \begin{bmatrix} -0.026 \\ +0.041 \end{bmatrix}$$

$$\therefore \begin{bmatrix} R_{Ex} \\ R_{Ey} \\ M_E \end{bmatrix} = \begin{bmatrix} 13.5 \text{ k} (\rightarrow) \\ 19.5 \text{ k} (\uparrow) \\ 62.56 (\curvearrowright) \end{bmatrix}$$

(Ans.)

2. (b)





$$\begin{bmatrix} -27 \\ -20 \\ 15 \end{bmatrix} = \begin{bmatrix} -84.3 \\ 0 \\ -29.75 \end{bmatrix} + \begin{bmatrix} \left(\frac{4}{25} + \frac{4}{17}\right) \frac{2}{25} & \frac{6}{172} \\ \frac{2}{25} & \left(\frac{4}{25} + \frac{4}{12}\right) \frac{6}{122} \\ \frac{6}{172} & \left(\frac{12}{173} + \frac{12}{123}\right) \end{bmatrix} EI \begin{bmatrix} u_1 \\ u_2 \\ u_3 \end{bmatrix}$$

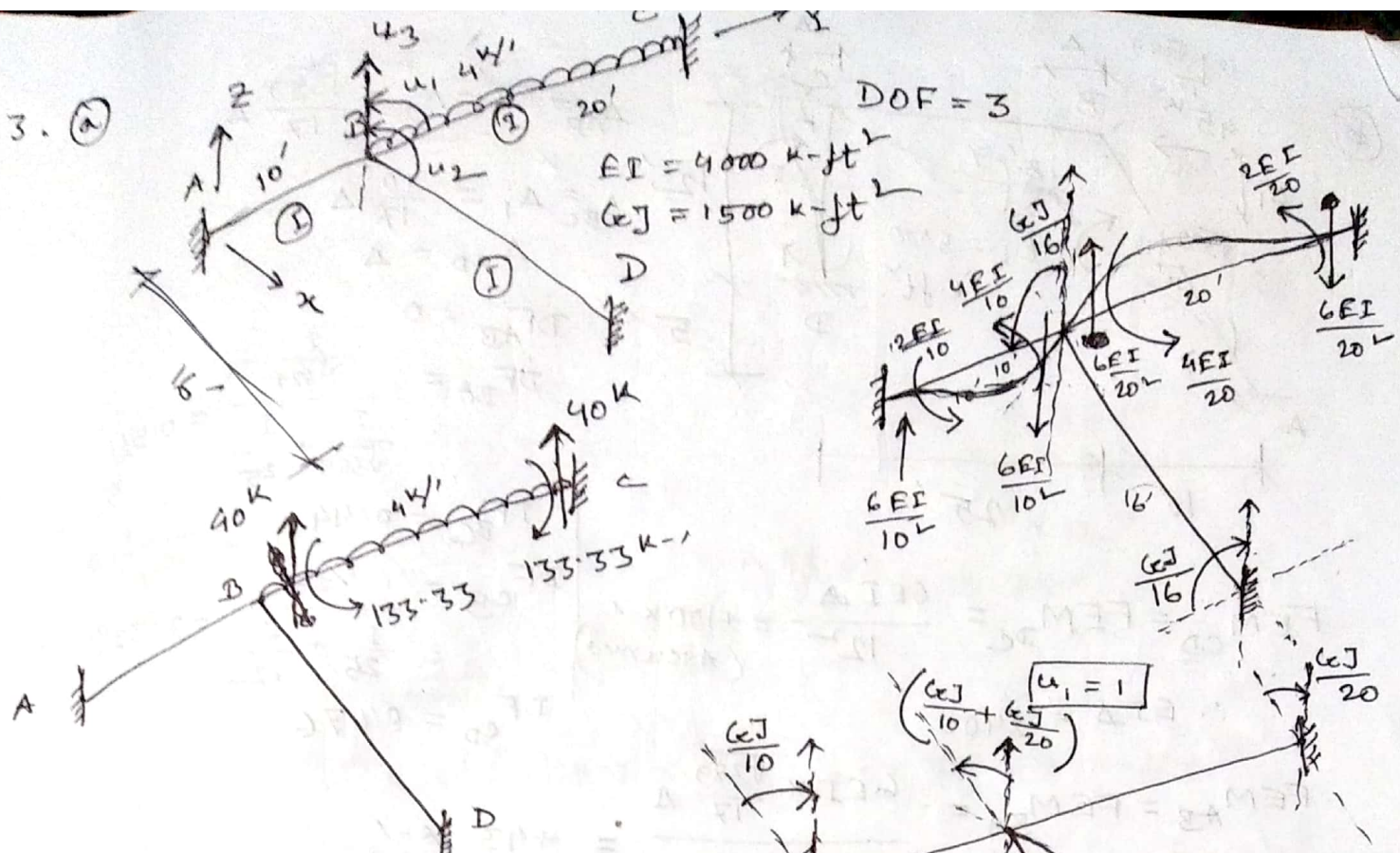
$$\Rightarrow \begin{bmatrix} u_1 \\ u_2 \\ u_3 \end{bmatrix} = \begin{bmatrix} -144.14 \\ -714.65 \\ 8258.27 \end{bmatrix} \frac{1}{EI}$$

Now,

$$\begin{bmatrix} R_{Ax} \\ R_{Ay} \\ M_A \end{bmatrix} = \begin{bmatrix} -29.75 \\ 0 \\ 84.3 \end{bmatrix} + \begin{bmatrix} -\frac{6}{172} & 0 & -\frac{12}{173} \\ \frac{6}{25} & \frac{6}{25} & 0 \\ \frac{2}{17} & 0 & \frac{6}{172} \end{bmatrix} EI \begin{bmatrix} -144.14 \\ -714.65 \\ 8258.27 \end{bmatrix} \frac{1}{EI}$$

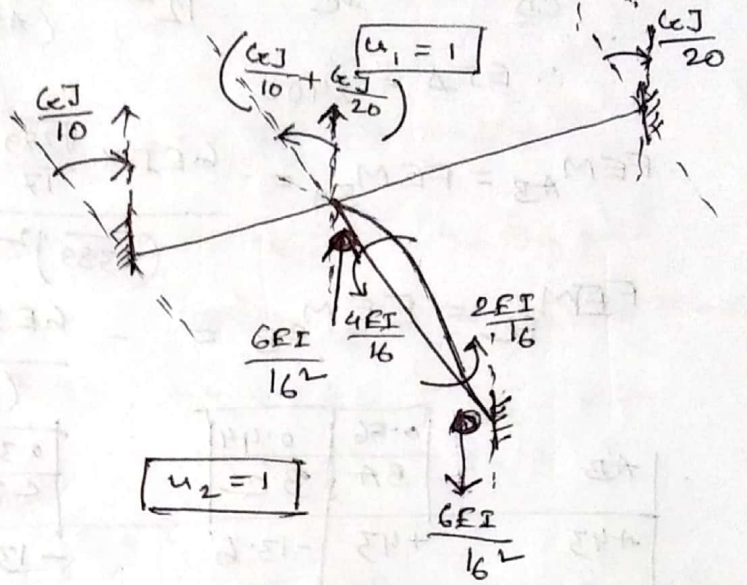
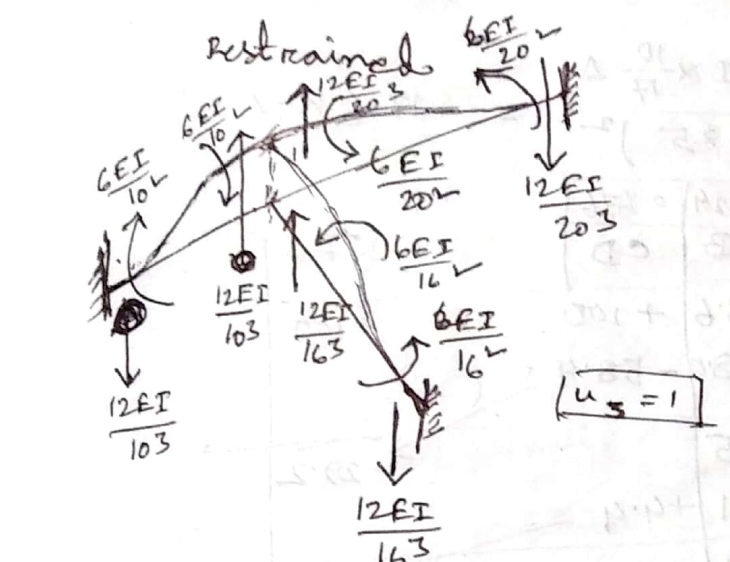
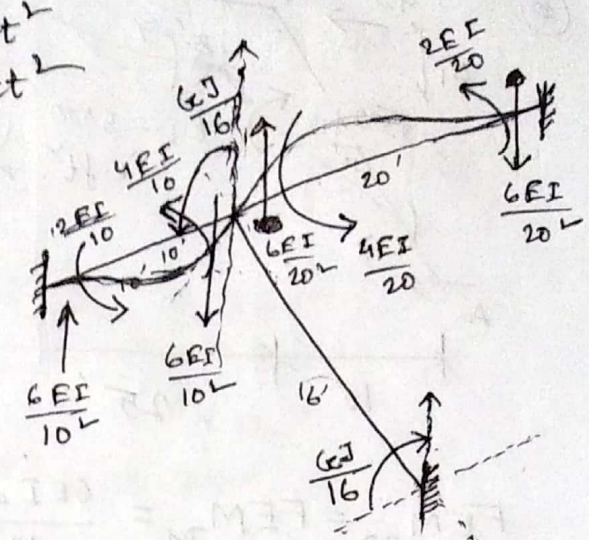
$$\begin{aligned} R_{Ax} &= -46.93 \text{ k} \quad (\leftarrow) \\ R_{Ay} &= +26.76 \text{ k} \quad (\uparrow) \\ M_A &= +238.8 \text{ k-m} \quad (\curvearrowright) \end{aligned}$$

3. (a)



DOF = 3

$EI = 4000 \text{ k-ft}^2$
 $GJ = 1500 \text{ k-ft}^2$

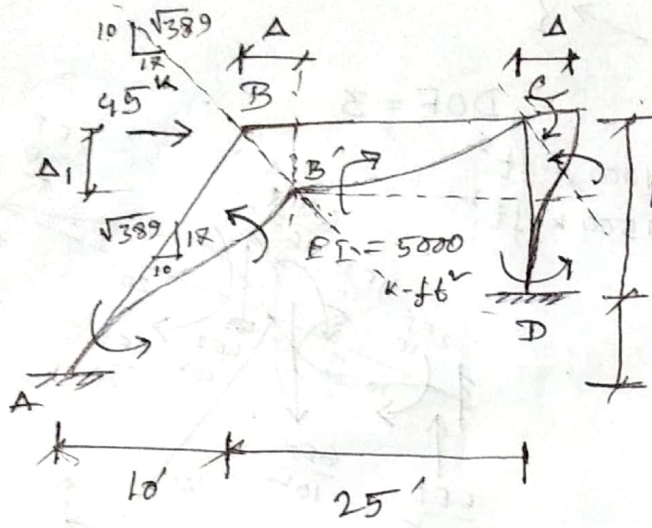


Vertical deflection at B = $1.089' \approx 1.1'$ (Ans)

$$\begin{bmatrix} 0 \\ 0 \\ 0 \end{bmatrix} = \begin{bmatrix} 133.33 \\ 0 \\ 40 \end{bmatrix} + \begin{bmatrix} \left(\frac{4EI}{10} + \frac{4EI}{20} + \frac{GJ}{16}\right) & 0 & \left(\frac{6EI}{20} - \frac{6EI}{10}\right) \\ 0 & 0 & \left(\frac{4EI}{16} + \frac{GJ}{10} + \frac{GJ}{20}\right) \\ \left(-\frac{6EI}{10} + \frac{6EI}{20}\right) & \frac{6EI}{16} & \left(\frac{12EI}{10^3} + \frac{12EI}{20^3} + \frac{12EI}{16^3}\right) \end{bmatrix} \begin{bmatrix} u_1 \\ u_2 \\ u_3 \end{bmatrix}$$

$$\Rightarrow \begin{bmatrix} u_1 \\ u_2 \\ u_3 \end{bmatrix} = \begin{bmatrix} -0.132 \\ 0.083 \\ -1.089 \end{bmatrix}$$

(b)



$$\Delta_{AB} = BB' = \Delta_2 = \frac{\sqrt{389}}{17} \Delta$$

$$\Delta_{BC} = \Delta_1 = \frac{10}{17} \Delta$$

$$\Delta_{CD} = \Delta$$

$$DF_{AB} = 0$$

$$DF_{BA} = \frac{\frac{I}{\sqrt{389}}}{\frac{I}{\sqrt{389}} + \frac{I}{25}} = 0.56$$

$$DF_{BC} = 0.44$$

$$DF_{CB} = \frac{\frac{I}{25}}{\frac{I}{25} + \frac{I}{12}} = 0.322$$

$$DF_{CD} = 0.676$$

$$FEM_{CD} = FEM_{DC} = \frac{6EI\Delta}{12^2} = +100 \text{ k-ft}$$

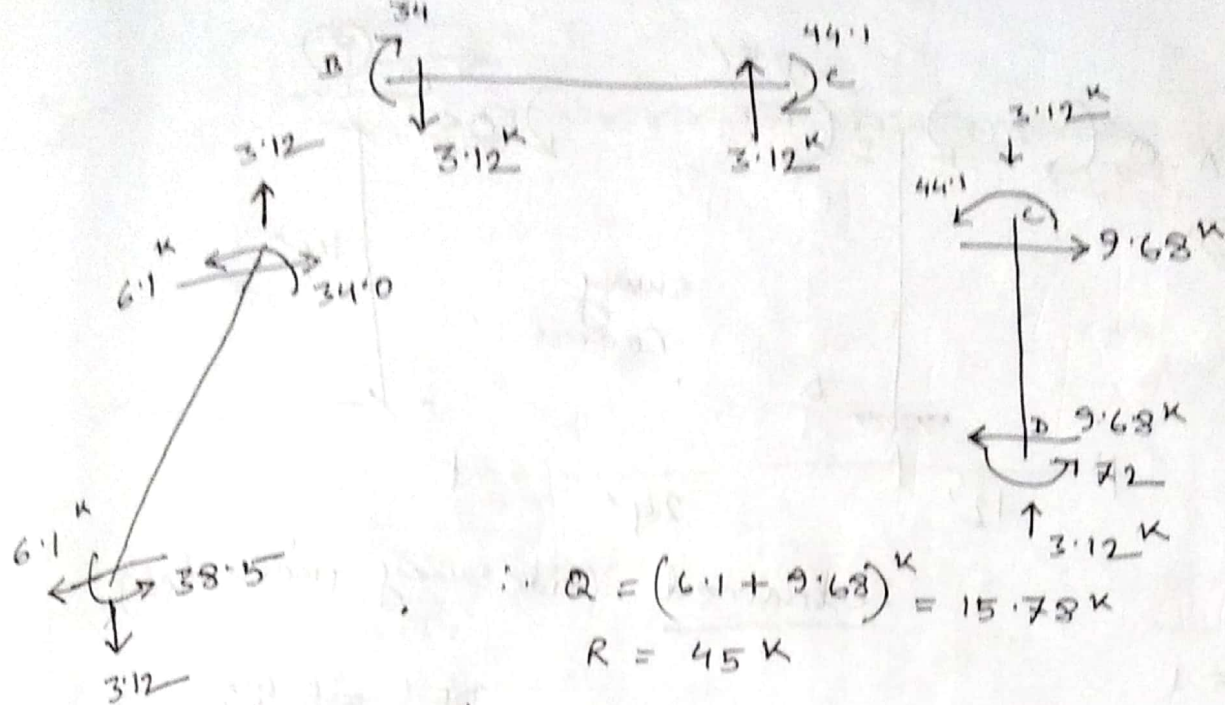
(Assumed)

$$\therefore EID = 2400$$

$$FEM_{AB} = FEM_{BA} = \frac{6EI \times \frac{\sqrt{389}}{17} \Delta}{(\sqrt{389})^2} = +43 \text{ k-ft}$$

$$FEM_{BC} = FEM_{CB} = -\frac{6EI \times \frac{10}{17} \Delta}{(25)^2} = -13.6 \text{ k-ft}$$

AB	0.56	0.44		0.322	0.676		DC
	BA	BC		CB	CD		
+43	+43	-13.6		-13.6	+100		+100
	-16.5	-12.9		-28.0	-58.4		
-8.3		-14.0		-6.5			-29.2
	+7.8	+6.2		+2.1	+4.4		
+3.9		+1.1		+3.1			+2.2
	-0.6	-0.5		-1.0	-2.1		
-0.3		-0.5		-0.3			-1.1
	+0.3	+0.2		+0.1	+0.2		
+0.2							+0.1
+38.5	+34.0	-34.0		-44.1	+44.1		+72.0



$$\therefore Q = (6.1 + 9.68) k = 15.78 k$$

$$R = 45 k$$

\therefore Final moments,

$$FEM_{AB} = +38.5 \times \frac{45}{15.78} = +109.79 k-ft$$

$$FEM_{BA} = +96.96 k-ft \quad FEM_{BC} = -96.96 k-ft$$

$$FEM_{CB} = -125.76 k-ft \quad FEM_{CD} = +125.76 k-ft$$

$$FEM_{DC} = +205.32 k-ft$$

\therefore Horizontal sway at point C,

$$\frac{6EI\Delta}{12^2} = 100 \Rightarrow \Delta = \frac{12}{25} \text{ for } Q = 15.78 k$$

$$\therefore \text{For } R = 45 k, \quad \Delta_c = \frac{12}{25} \times \frac{45}{15.78} = 1.37'$$

$$\approx \boxed{16.44''} \quad (\text{Ans.})$$

By superposition,

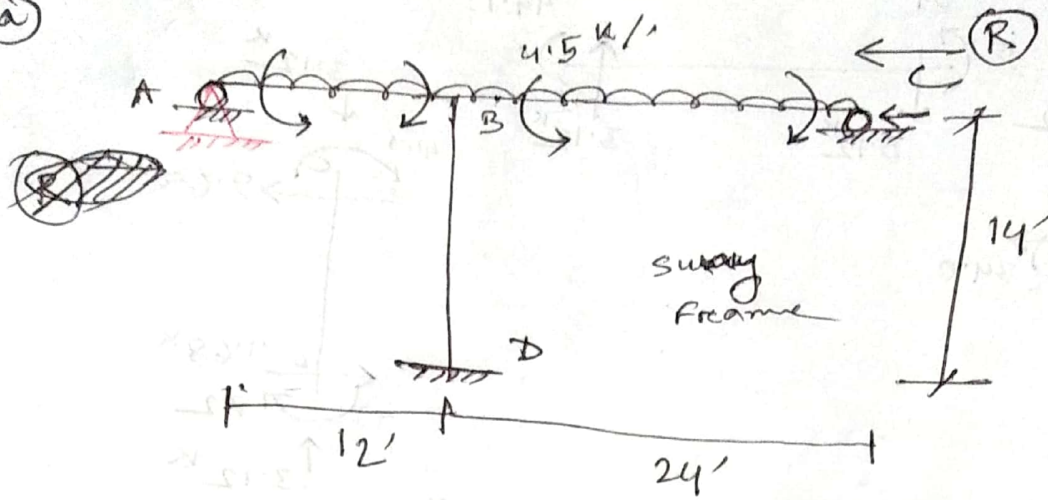
$$M_A = +109.79 k-ft \quad (\curvearrowright)$$

$$R_A = 3.12 \times \frac{45}{15.78} = 8.9 k \quad (\downarrow)$$

$$M_D = +205.32 k-ft \quad (\curvearrowright)$$

$$R_D = 8.9 k \quad (\uparrow)$$

4. (a)



Restrained (sideways prevented)

$$DF_{AB} = 1$$

$$DF_{BA} = \frac{\frac{3}{4} \times \frac{I}{12}}{\frac{3}{4} \times \frac{I}{12} + \frac{3}{4} \times \frac{I}{24} + \frac{I}{14}} = 0.38$$

$$DF_{BD} = 0.43$$

$$DF_{CB} = 1$$

$$DF_{BC} = \frac{\frac{3}{4} \times \frac{I}{24}}{\frac{3}{4} \times \frac{I}{12} + \frac{3}{4} \times \frac{I}{24} + \frac{I}{14}} = 0.19$$

$$DF_{DB} = 0$$

$$FEM_{AB} = +54 \text{ k-ft}$$

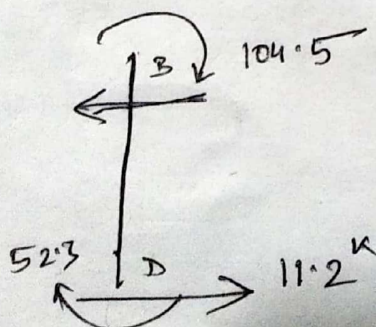
$$FEM_{BC} = +216 \text{ k-ft}$$

$$FEM_{BA} = -54 \text{ k-ft}$$

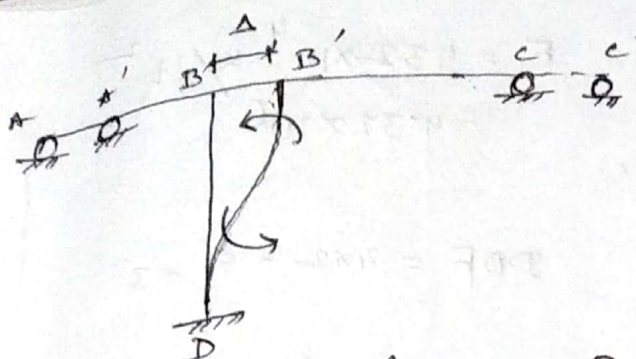
$$FEM_{CB} = -216 \text{ k-ft}$$

carry over

	0.38	0.43	0.19		
	BA	BD	BC		
AB				CB	DB
+54	-54		+216	-216	
-54	-61.6	-69.7	-30.7	+216	
	-27		+108		-34.9
	-30.8	-34.8	-15.4		-17.4
0	-173.4	-104.5	+277.9	0	-52.3



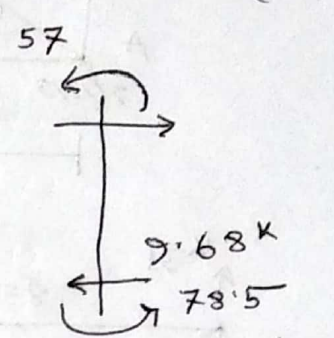
$\therefore R = 11.2 \text{ k}$ to be applied to make it non-sway frame.



~~FEM~~ $FEM_{BD} = FEM_{DB} = \frac{6EIA}{142}$
 $= +100 \text{ k-}$
 (assumed)

sway permitted

carry over



$\therefore Q = -9.68 \text{ k}$

	0.38	0.43	0.19		
1	BA	BD	BC	1	DB
AB		+100		CB	+100
	-38	-43	-079		-21.5
0	-38	+57	-19	0	+78.5

$M = M_0 + \left(\frac{R}{Q}\right) M_Q$ *

Final moments: $FEM_{AB} = 0$

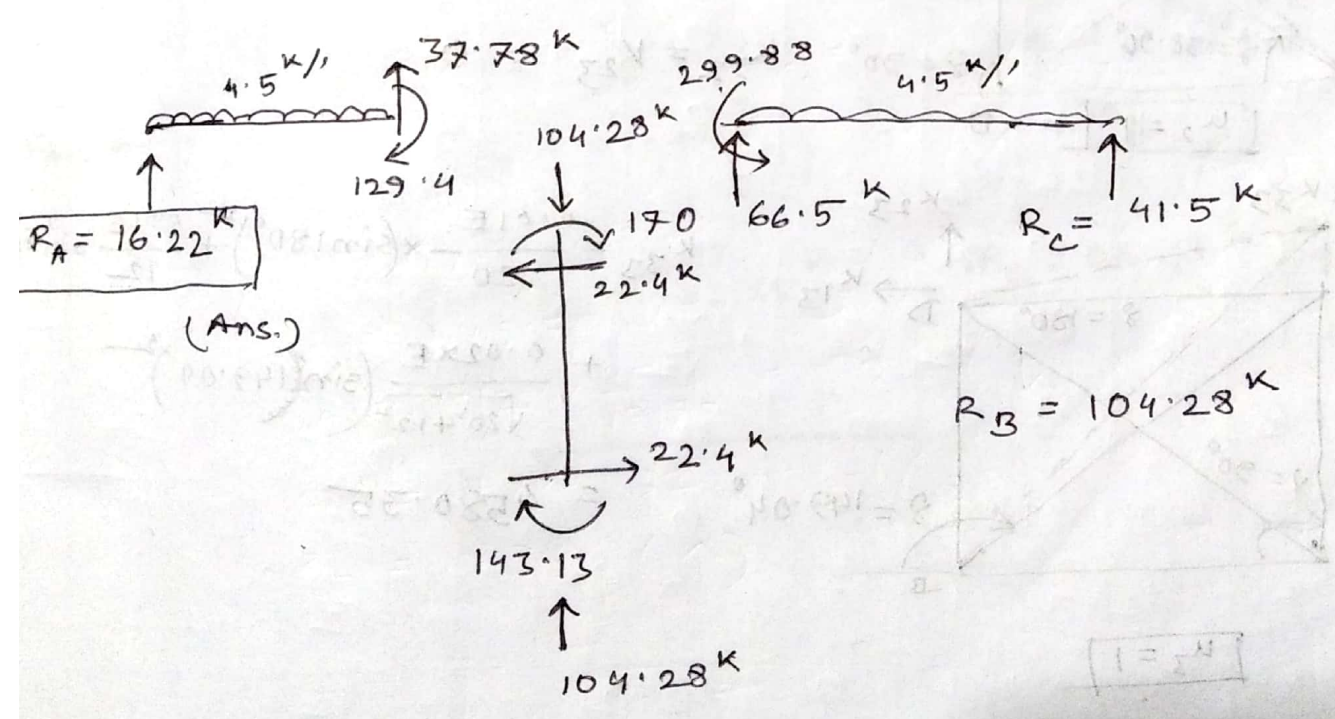
$FEM_{BA} = -173.4 + \left(\frac{11.2}{-9.68}\right) \times -38 = -129.4 \text{ k-}$

$FEM_{BD} = -170.45 \text{ k-}$

$FEM_{CB} = 0$

$FEM_{BC} = 299.88 \text{ k-}$

$FEM_{DB} = -143.13 \text{ k-}$

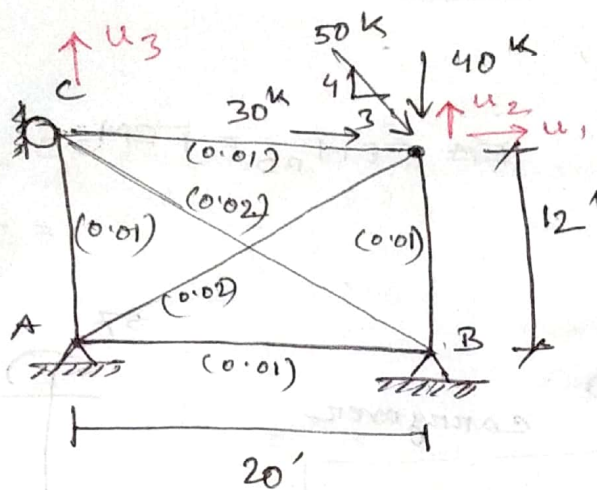


(Ans.)

$R_B = 104.28 \text{ k}$

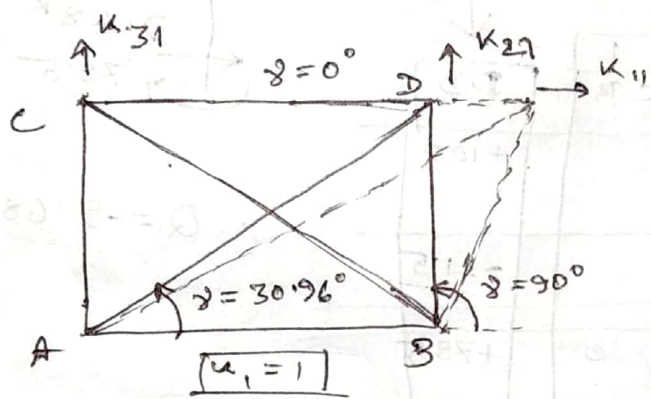
$I = 142$

(b)



$$E = 432 \times 10^4 \text{ k/ft}^2 = 4.32 \times 10^6$$

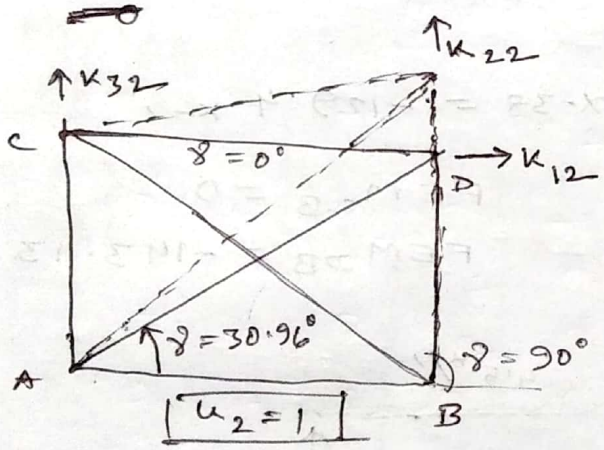
$$DOF = 4 \times 2 - 5 = 3^0$$



$$K_{11} = \frac{0.01 \times E}{20} \cos^2 0^\circ + \frac{0.01 \times E}{12} \cos^2 30.96^\circ + \frac{0.02 \times E}{\sqrt{20^2 + 12^2}} \cos^2 30.96^\circ = 4884.02$$

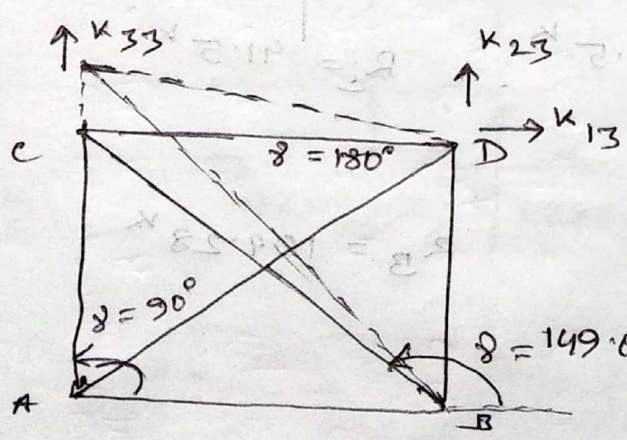
$$K_{12} = K_{21} = \frac{0.01 E}{20} \cos 0^\circ \sin 0^\circ + \frac{0.01 E}{12} \cos 90^\circ \sin 90^\circ + \frac{0.02 \times E}{\sqrt{20^2 + 12^2}} \cos 30.96^\circ \sin 30.96^\circ = 1634.17$$

$$K_{13} = K_{31} = 0$$



$$K_{22} = \frac{0.01 \times E}{12} \times (\sin 90^\circ)^2 + \frac{0.02 \times E}{\sqrt{20^2 + 12^2}} \sin^2(30.96^\circ) = 4580.35$$

$$K_{32} = K_{23} = 0$$



$$K_{33} = \frac{0.01 E}{20} \times (\sin 180^\circ)^2 + \frac{0.01 E}{12} \sin^2 90^\circ + \frac{0.02 \times E}{\sqrt{20^2 + 12^2}} (\sin 149.04^\circ)^2 = 4580.35$$

$$u_3 = 1$$

$$\begin{bmatrix} 30 \\ -40 \\ 0 \end{bmatrix} = \begin{bmatrix} 4884.02 & 1634.17 & 0 \\ 1634.17 & 4580.35 & 0 \\ 0 & 0 & 4580.35 \end{bmatrix} \begin{bmatrix} u_1 \\ u_2 \\ u_3 \end{bmatrix}$$

$$\Rightarrow \begin{bmatrix} u_1 \\ u_2 \\ u_3 \end{bmatrix} = \begin{bmatrix} 0.0103 \\ -0.0124 \\ 0 \end{bmatrix}$$

Bar Forces:

$$F_{CD} = \frac{0.01 \times 4.32 \times 10^6}{20} \times \left[0.0103 \times \cos 0^\circ + (-0.0124) \sin 0^\circ \right]$$

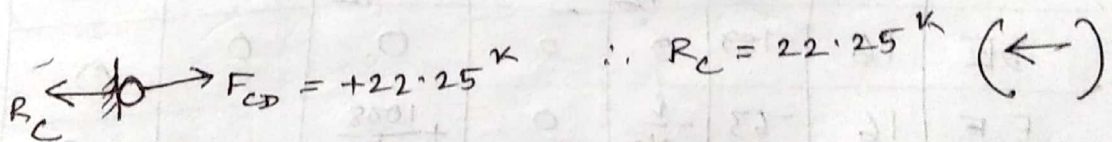
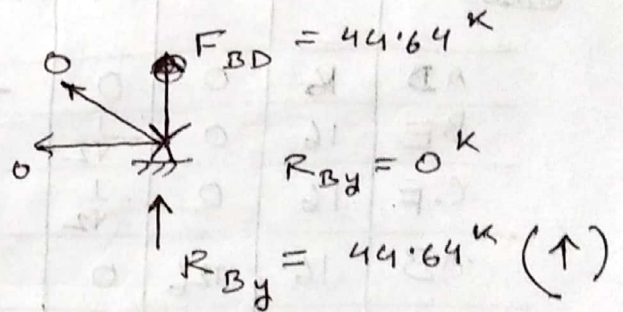
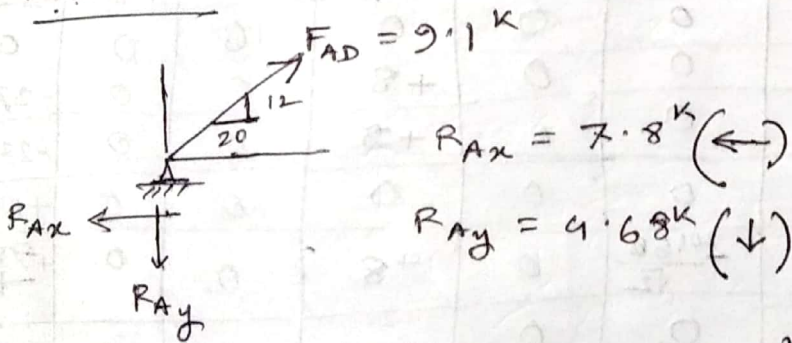
$$= +22.25 \text{ k (Tension)}$$

$$F_{BD} = \frac{0.01 \times 4.32 \times 10^6}{12} \times \left[0.0103 \cos 90^\circ + (-0.0124) \sin 90^\circ \right] = -44.64 \text{ k (compression)}$$

$$F_{AD} = \frac{0.02 \times 4.32 \times 10^6}{\sqrt{20^2 + 12^2}} \times \left[0.0103 \cos 30.96^\circ + (-0.0124) \sin 30.96^\circ \right] = 9.1 \text{ k (Tension)}$$

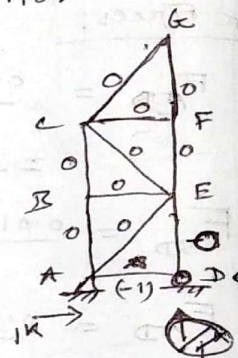
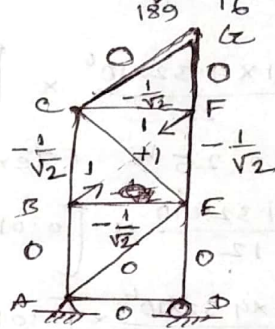
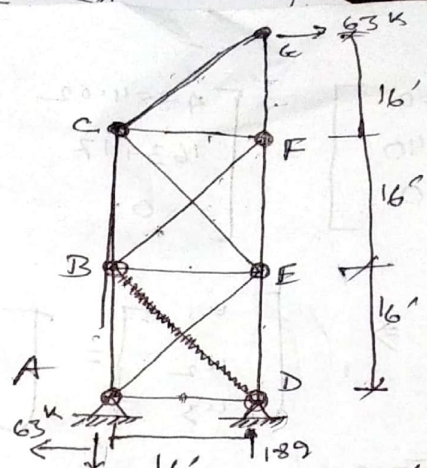
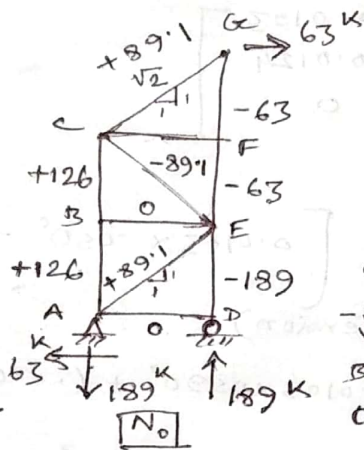
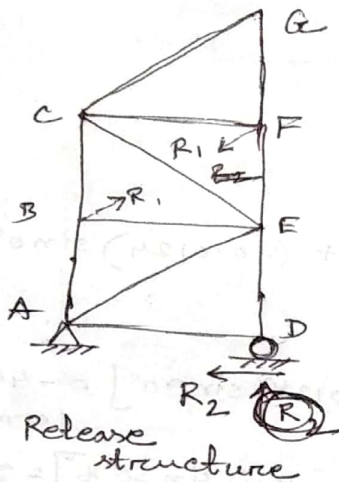
$$F_{AB} = 0, \quad F_{AC} = 0, \quad F_{BC} = 0$$

Reactions:



5. (a)

$$\begin{aligned}
 \text{DoS I} &= 6 + r - 2j \\
 &= 12 + 4 - 2 \times 7 \\
 &= 2
 \end{aligned}$$



$$N = N_0 + N_1 R_1 + N_2 R_2$$

[N₁]

[N₂]

Bar	L	N ₀	N ₁	N ₂	N ₀ N ₁ L	N ₀ N ₂ L	N ₁ N ₁ L	N ₂ N ₂ L	N ₁ N ₂ L	N
AB	16	0	0	-1	0	0	0	16	0	0
BE	16	0	-1/√2	0	0	0	+8	0	0	-27
CF	16	0	-1/√2	0	0	0	+8	0	0	-27
AD	16	126	0	0	0	0	0	0	0	+126
BC	16	126	-1/√2	0	2016/√2	0	+8	0	0	+98
DE	16	-189	0	0	0	0	0	0	0	-189
EF	16	-63	-1/√2	0	1008/√2	0	+8	0	0	-98
FG	16	-63	0	0	0	0	0	0	0	-63
AE	16√2	89.1	0	0	0	0	0	0	0	+89.1
BF	16√2	0	1	0	0	0	+16√2	0	0	39.2
CE	16√2	-89.1	1	0	-1424√2	0	+16√2	0	0	-49
CG	16√2	89.1	0	0	0	0	0	0	0	+89.1
Σ							+69.255	16	0	

$$A_{01} = \int \frac{N_0 N_1 L}{AE} = -\frac{272660}{AE} \quad S_{11} = \int \frac{N_1 N_1 L}{AE} = \frac{69.255}{AE}$$

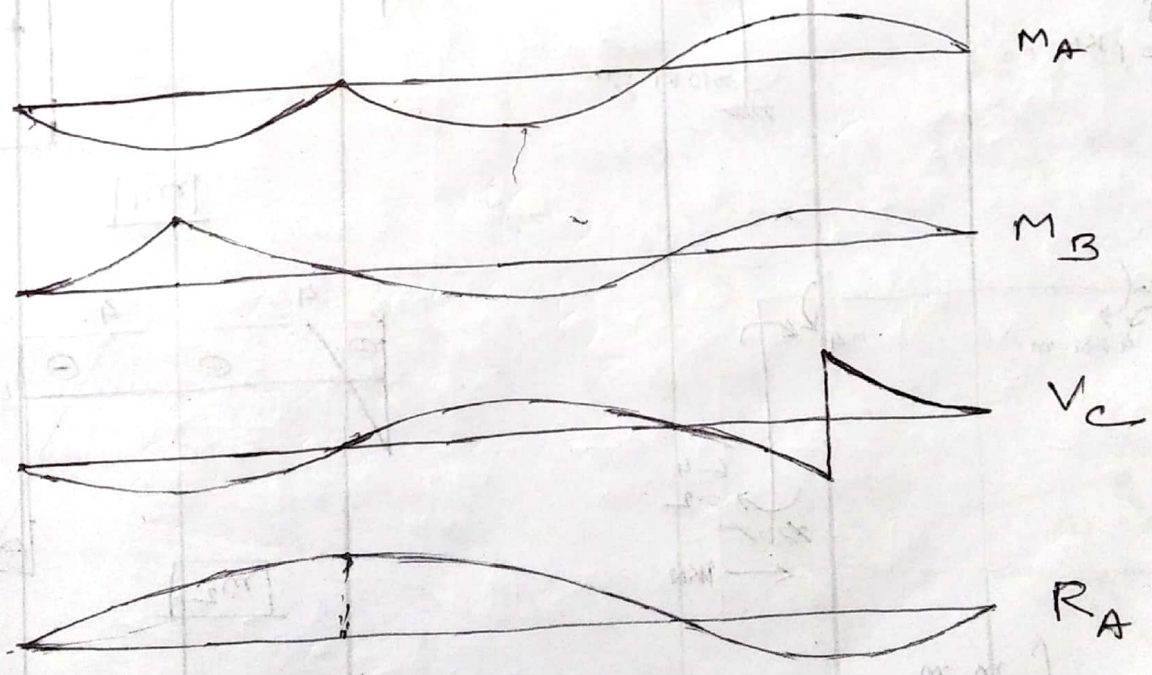
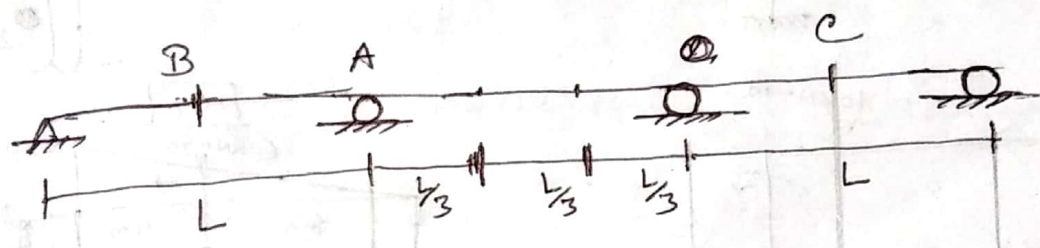
$$A_{02} = \int \frac{N_0 N_2 L}{AE} = 0$$

$$S_{12} = S_{21} = \int \frac{N_1 N_2 L}{AE} = 0$$

$$S_{22} = \int \frac{N_2 N_2 L}{AE} = \frac{16}{AE}$$

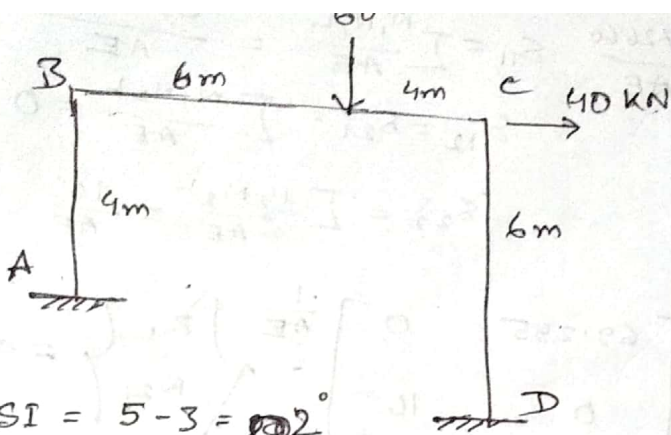
$$\begin{Bmatrix} -272660 \\ 0 \end{Bmatrix} \frac{1}{AE} + \begin{bmatrix} 69.255 & 0 \\ 0 & 16 \end{bmatrix} \frac{1}{AE} \begin{Bmatrix} R_1 \\ R_2 \end{Bmatrix} = \begin{Bmatrix} 0 \\ 0 \end{Bmatrix}$$

$$\Rightarrow \begin{Bmatrix} R_1 \\ R_2 \end{Bmatrix} = \begin{Bmatrix} 39.37 \\ 0 \end{Bmatrix}$$

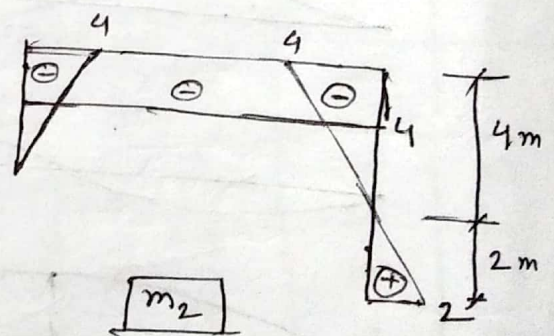
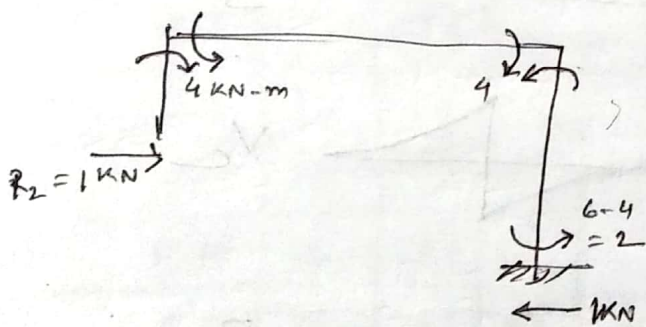
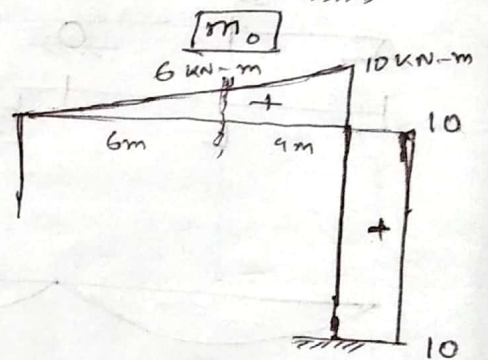
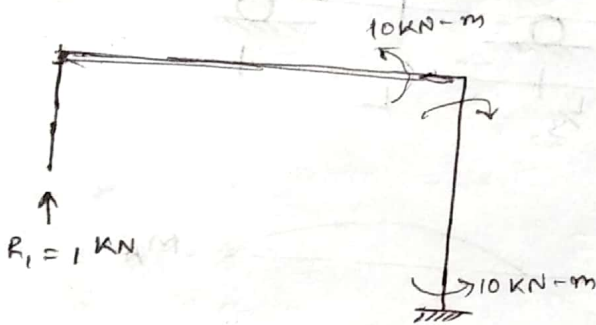
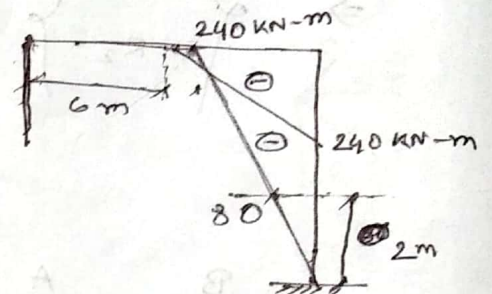
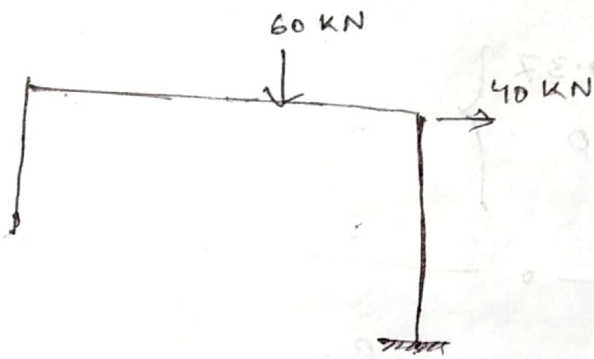
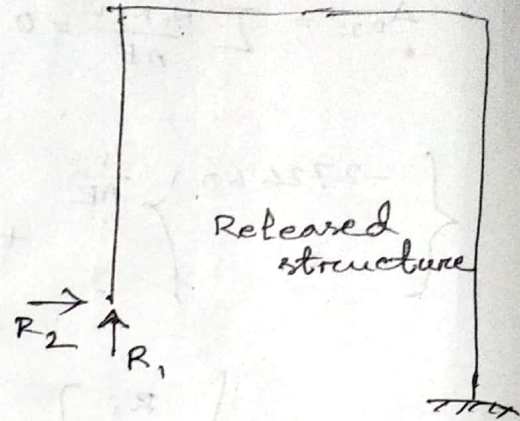


$$1 \times \left[\frac{1}{3} \times \left(\frac{1}{3} \times \frac{1}{3} \right) + \frac{1}{3} \times \left(\frac{1}{3} \times \frac{1}{3} \right) \right] \times \left(\frac{1}{3} \times \frac{1}{3} \right) \times \frac{1}{3} \times \frac{1}{3} = \frac{1}{3} \times \frac{1}{3} \times \frac{1}{3} \times \frac{1}{3} = \frac{1}{81}$$

(b)



$DOF = 5 - 3 = 2$



$$\Delta_{01} = \int \frac{m_0 m_1}{EI} dx = \frac{1}{EI} \times \frac{1}{6} \times (-240) \times [6 + 2 \times 10] \times 4 + \frac{1}{EI} \times \frac{1}{2} \times (-240) \times 10 \times 6$$

$$= - \frac{11360}{EI}$$

$$\Delta_{02} = \int \frac{m_0 m_2}{EI} = \frac{1}{EI} \times \frac{1}{2} \times (-240) \times (-4) \times 4 + \frac{1}{EI} \times \frac{1}{6} \times (-4) \times \left[\begin{matrix} -2 \times 240 \\ -80 \end{matrix} \right] \times 4 + \frac{1}{6EI} \times (-80) \times 2 \times 2$$

$$= \frac{3360}{EI}$$

$$\delta_{11} = \int \frac{m_1 m_1}{EI} = \frac{1}{3EI} \times 10 \times 10 \times 10 + \frac{1}{6EI} \times 10 \times 10 \times 6 = \frac{2800}{3EI}$$

$$\delta_{12} = \delta_{21} = \int \frac{m_1 m_2}{EI} = \frac{1}{2EI} \times (-4) \times 10 \times 10 + \frac{1}{2EI} \times 10 \times (-4) \times 4 + \frac{1}{2EI} \times 2 \times 10 \times 2 = -\frac{260}{EI}$$

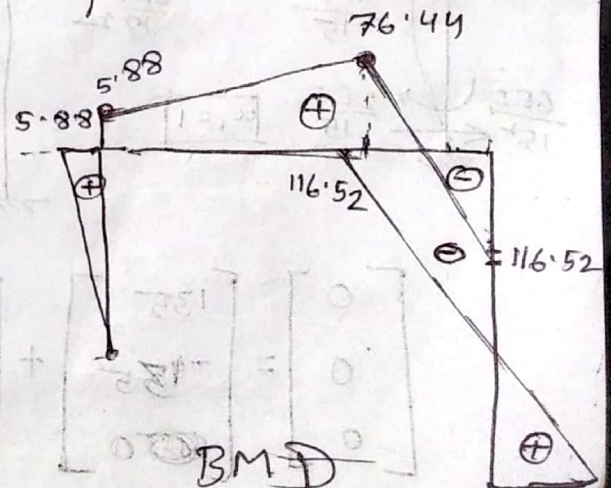
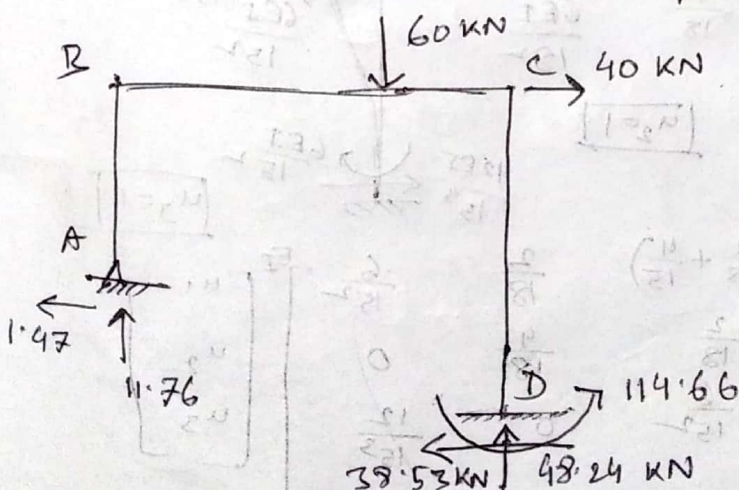
$$\delta_{22} = \int \frac{m_2 m_2}{EI} = \frac{1}{3EI} \times (-4) \times (-4) \times 4 + \frac{1}{EI} \times (-4) \times (-4) \times 10 +$$

$$\frac{1}{3EI} \times (-4) \times (-4) \times 4 + \frac{1}{3EI} \times 2 \times 2 \times 2$$

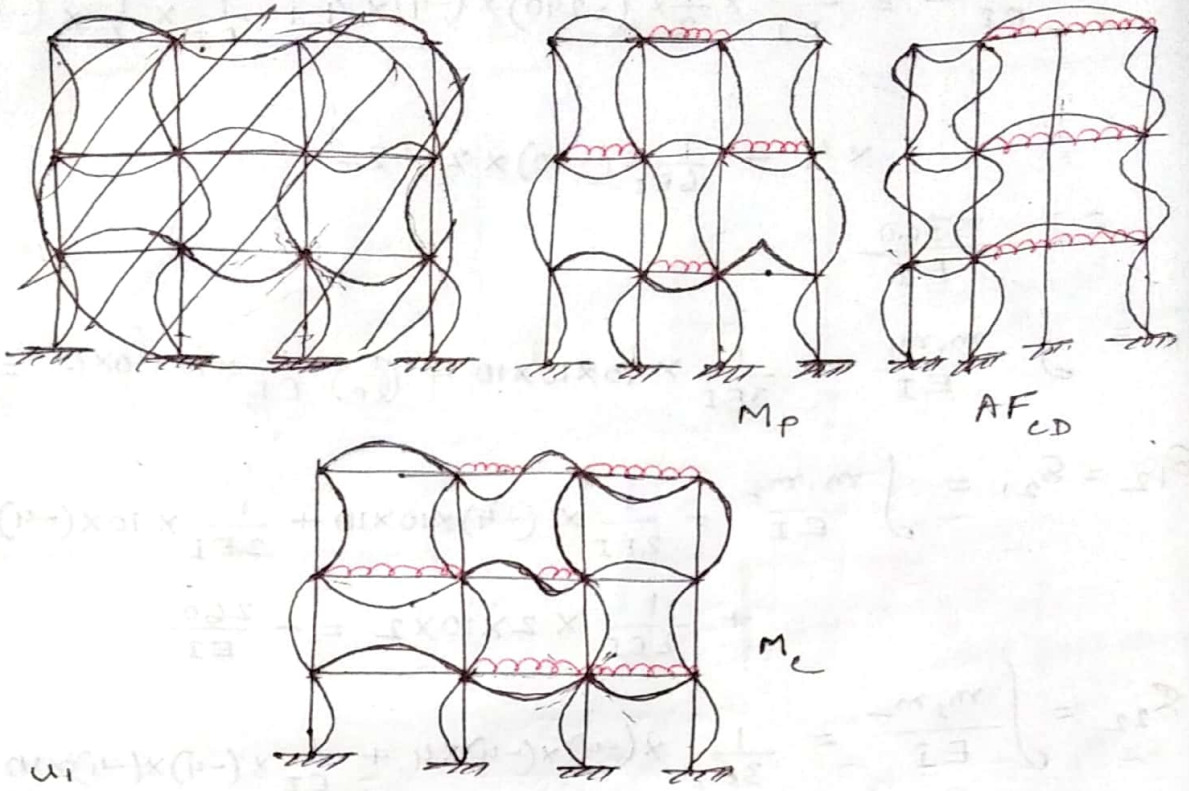
$$= \frac{616}{3EI}$$

$$\begin{Bmatrix} -11360 \\ 3360 \end{Bmatrix} \frac{1}{EI} + \begin{bmatrix} \frac{2800}{3} & -260 \\ -260 & \frac{616}{3} \end{bmatrix} \frac{1}{EI} \begin{Bmatrix} R_1 \\ R_2 \end{Bmatrix} = \begin{Bmatrix} 0 \\ 0 \end{Bmatrix}$$

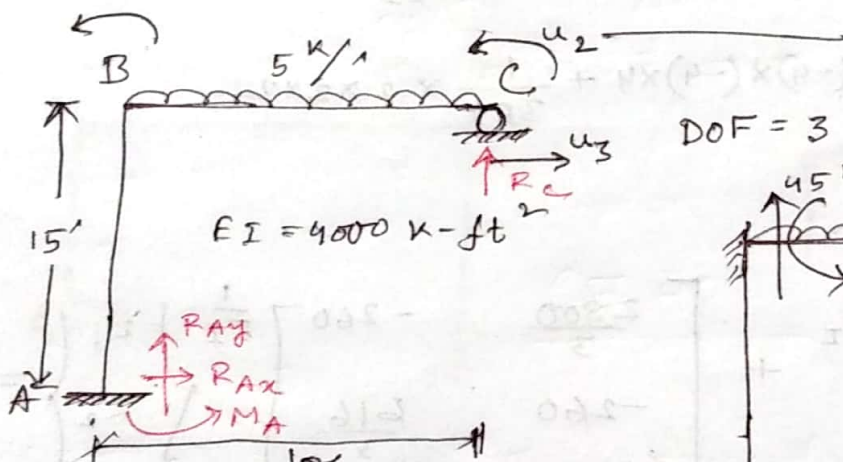
$$\Rightarrow \begin{Bmatrix} R_1 \\ R_2 \end{Bmatrix} = \begin{Bmatrix} 11.76 \\ -1.47 \end{Bmatrix}$$



7. (a)

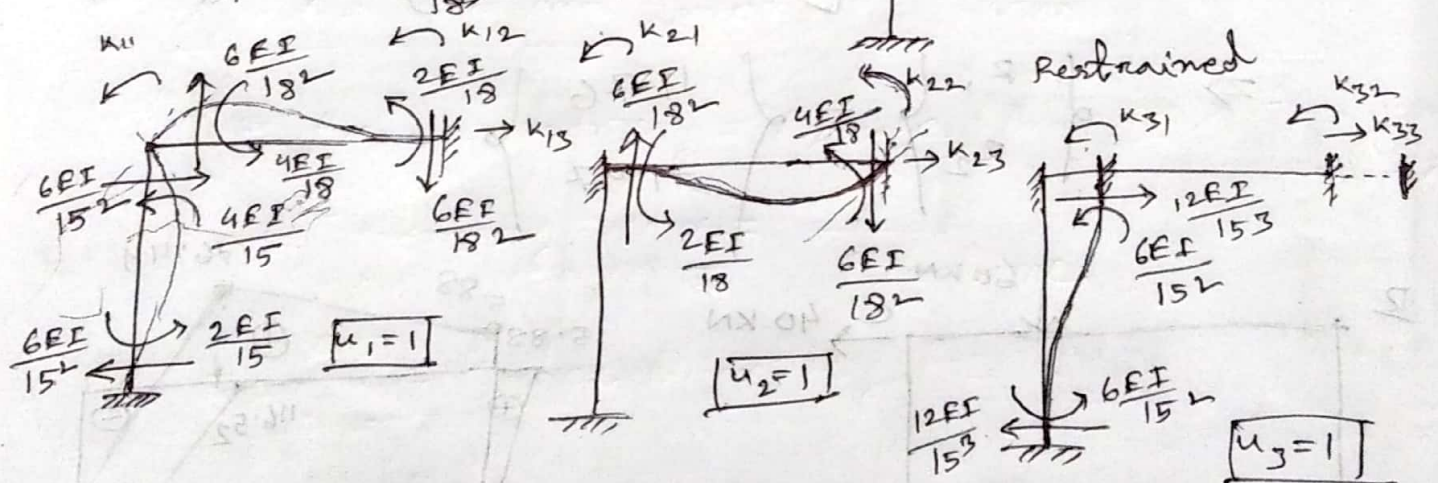
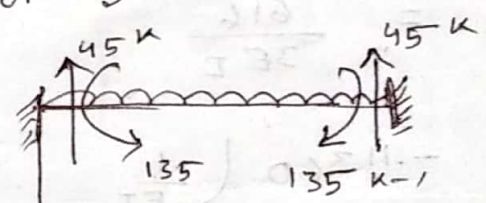


(b)



$EI = 4000 \text{ k-ft}^2$

DOF = 3



$$\begin{bmatrix} 0 \\ 0 \\ 0 \end{bmatrix} = \begin{bmatrix} 135 \\ -135 \\ 0 \end{bmatrix} + \begin{bmatrix} \left(\frac{4}{18} + \frac{4}{15}\right) & \frac{2}{18} & \frac{6}{152} \\ \frac{2}{18} & \frac{4}{18} & 0 \\ \frac{6}{152} & 0 & \frac{12}{153} \end{bmatrix} \begin{bmatrix} u_1 \\ u_2 \\ u_3 \end{bmatrix}$$

$$\Rightarrow \begin{bmatrix} u_1 \\ u_2 \\ u_3 \end{bmatrix} = \frac{1}{EI} \begin{bmatrix} -867.86 \\ 1041.43 \\ 6508.93 \end{bmatrix}$$

\therefore The amount of sway, $u_3 = \frac{6508.93}{4000} = \boxed{1.63'}$ (Ans.)

Now,

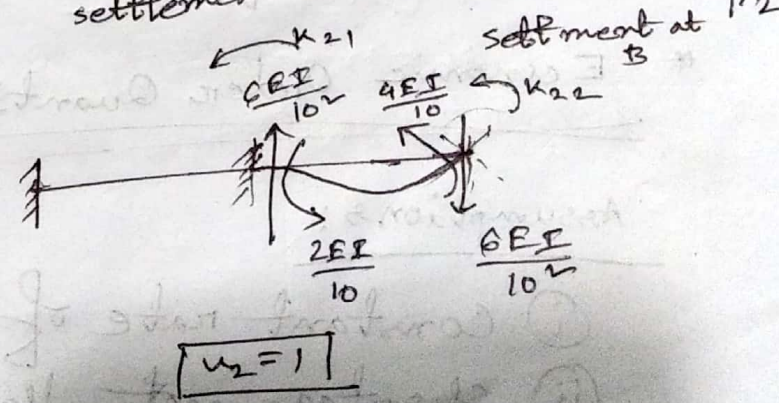
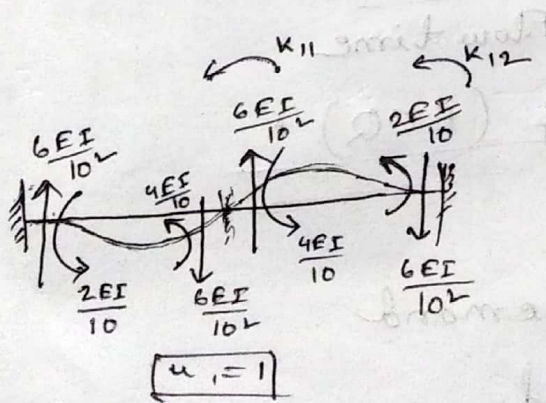
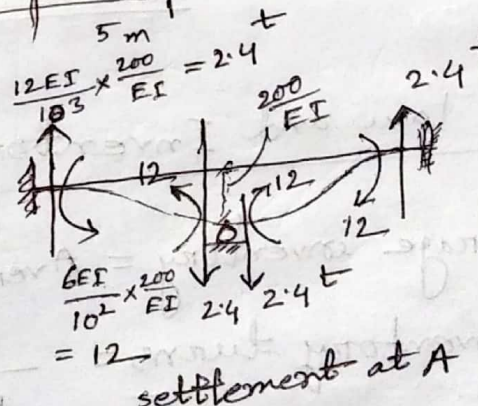
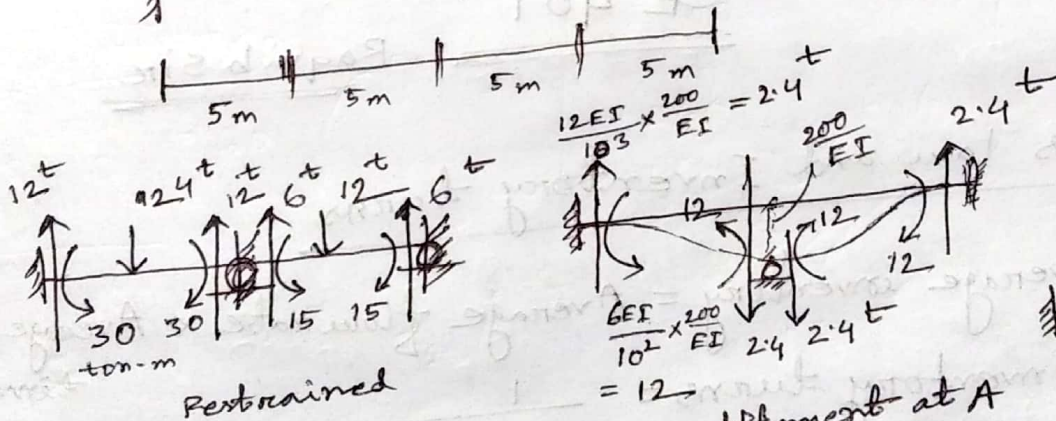
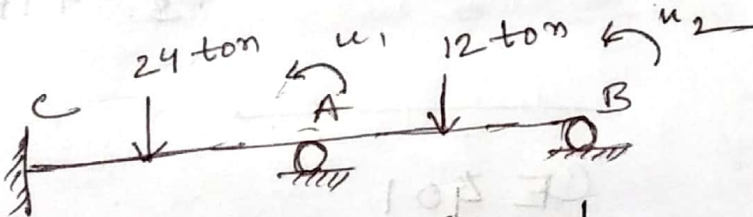
$$\begin{bmatrix} R_{Ax} \\ R_{Ay} \\ M_A \\ R_C \end{bmatrix} = \begin{bmatrix} 0 \\ 45 \\ 0 \\ 45 \end{bmatrix} + \begin{bmatrix} -\frac{6}{152} & 0 & -\frac{12}{153} \\ \frac{6}{182} & \frac{6}{182} & 0 \\ \frac{2}{15} & 0 & \frac{6}{15} \\ -\frac{6}{182} & -\frac{6}{182} & 0 \end{bmatrix} EI \begin{bmatrix} -867.86 \\ 1041.43 \\ 6508.93 \end{bmatrix} \frac{1}{EI}$$

$$R_{Ax} = 0 \quad M_A = 57.86 \text{ k-ft}$$

$$R_{Ay} = 48.21 \text{ k} (\uparrow) \quad R_C = 41.79 \text{ k} (\uparrow)$$

~~M_A~~

8. (a)



$$\boxed{u_1 = 1}$$

$$\boxed{u_2 = 1}$$

$$\begin{bmatrix} 0 \\ 0 \end{bmatrix} = \begin{bmatrix} -15 \\ -15 \end{bmatrix} + \begin{bmatrix} 0 \\ -12 \end{bmatrix} + \begin{bmatrix} 6 \\ 6 \end{bmatrix} + \begin{bmatrix} \frac{.4}{5} \\ \frac{2}{10} \end{bmatrix} EI \begin{bmatrix} u_1 \\ u_2 \end{bmatrix}$$

$$\Rightarrow \begin{bmatrix} u_1 \\ u_2 \end{bmatrix} = \begin{bmatrix} -\frac{15}{7} \\ \frac{375}{7} \end{bmatrix} \frac{1}{EI}$$

Now,

$$\begin{bmatrix} R_{cy} \\ M_c \\ R_A \\ R_B \end{bmatrix} = \begin{bmatrix} 12 \\ 30 \\ 18 \\ 6 \end{bmatrix} + \begin{bmatrix} 2.4 \\ 12 \\ -4.8 \\ 2.4 \end{bmatrix} + \begin{bmatrix} 0 \\ 0 \\ 7.2 \\ -1.2 \end{bmatrix} + \begin{bmatrix} \frac{6}{10} \\ \frac{2}{10} \\ 0 \\ -\frac{6}{10} \end{bmatrix} EI \begin{bmatrix} -\frac{15}{7} \\ \frac{375}{7} \end{bmatrix}$$

$$\therefore R_{cy} = 14.3 \text{ ton} (\uparrow)$$

$$M_c = 41.57 \text{ ton-m}$$

$$R_A = 17.6 \text{ ton} (\uparrow)$$

$$R_B = 4.1 \text{ ton} (\uparrow)$$

CE 401

Raajib Sir

* Little's law and Inventory turns :

$$\square \text{ Average inventory} = \text{Average flow rate} \times \text{Average flow time}$$

$$\square \text{ Inventory turns} = \frac{1}{\text{Flow time}}$$

* Economic Order Quantity (EOQ) *

Assumptions:

- (i) Constant rate of demand
- (ii) Shortage not allowed