

Problem 1:

Design horizontal alignment of a mixed highway using following data. Calculate necessary parameters for setting out transition curve and half of circular curve.

- Deflection angle = 45°
- Chainage at PI = 5000 m
- Design speed of vehicle = 70 km/hr

Solution:

$$e_{\max} + f_{\max} = \frac{v^2}{g R_{\min}}$$

$$\begin{aligned} \text{or, } R_{\min} &= \frac{v^2}{(e_{\max} + f_{\max}) \times g} \\ &= \frac{19.44^2}{(0.08 + 0.14) \times 9.8} \\ &= 175 \text{ m} \end{aligned}$$

Given.

Deflection angle, $\Delta = 45^\circ$
Chainage at PI = 5000 m
Design speed of vehicle = 70 km/hr
 $= 19.44 \text{ m/s}$

$$f_{\max} = 0.14$$

$$e_{\max} = 0.08$$

$$\text{If } f = 0$$

$$R = \frac{(19.44)^2}{9.8 \times (0.08 + 0)} = 482 \text{ m}$$

Length of transition curve

Rate of change of radial acceleration (a) is considered 0.3 m/s^3 for high standard road.

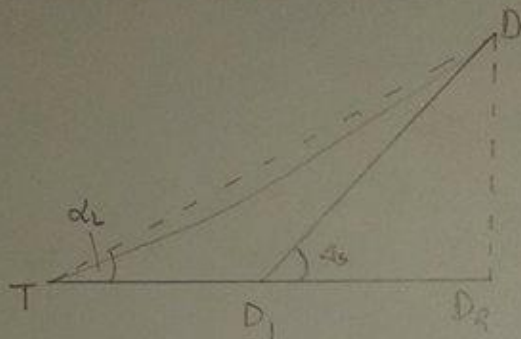
$$\therefore L = \frac{v^3}{RC} = \frac{19.44^3}{482 \times 0.3} \text{ m} = 50.8 \text{ m}$$

$$\begin{aligned} \text{Spiral angle, } \Delta_s &= \frac{L}{2R} = \frac{50.8}{2 \times 482} = 0.05269 \text{ rad} \\ &= 0.05269 \times \frac{180^\circ}{\pi} \\ &= 3.01^\circ \\ &= 3^\circ 1' 10'' \end{aligned}$$

maximum polar-deflection angle, $\alpha_L = \frac{3 \cdot 01}{3} = 1.006^\circ$
 $= 1^\circ 0' 23.39''$

Shift, $s = \frac{L^2}{24R} = \frac{(50.8)^2}{24 \times 482} = 0.2231$

Maximum offset $= 4s = 4 \times 0.2231 = 0.8924 \text{ m}$



$TD_1 = \frac{2 \times 50.8}{3} \text{ m} = 33.86 \text{ m}$

$OD_2 = \frac{1}{3}L = \frac{1}{3} \times 50.8 = 16.93 \text{ m}$

Total tangent length $= \frac{L}{2} + (R+s) \tan \frac{\Delta}{2}$
 $= \frac{50.8}{2} + (482 + 0.223) \tan \frac{45}{2}$
 $= 225.14 \text{ m}$

Apex distance, $E = \frac{R+s}{\cos \frac{\Delta}{2}} - R$
 $= \frac{482 + 0.223}{\cos \frac{45}{2}} - 482$
 $= 39.95 \text{ m}$

length of circular curve $= R(\Delta - 2\Delta_2)$
 $= 482(0.785 - 2 \times 0.05269)$
 $= 327.567 \text{ m}$

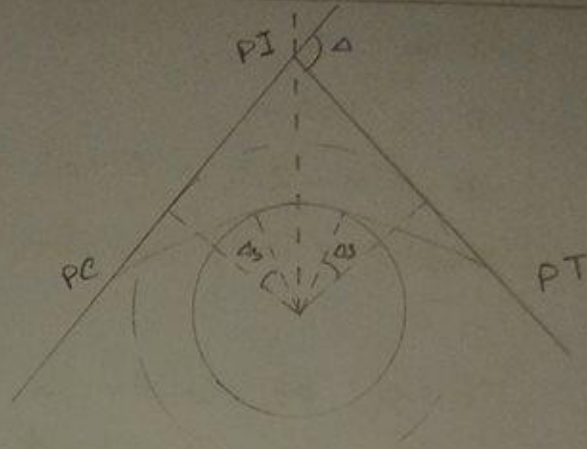
length of combined curve,
 $= (50.8 + 327.567 + 50.8) \text{ m}$
 $= 429.167 \text{ m}$

Chainage of T_1 (PC)
 $= (5000 - 225.14) \text{ m}$
 $= 4774.86 \text{ m}$

Chainage of T_2 (PT)
 $= (4774.86 + 429.167) \text{ m}$
 $= 5204.027 \text{ m}$

maximum offset, $y = 4s$
 $= 4 \times 0.223 \text{ m} = 0.892 \text{ m}$

setting out transition curve,
 $\theta = \frac{l^3}{2RL}, \alpha = \frac{\theta}{3}, y = \frac{l^3}{6RL}$



Peg stn	l = x(m)	alpha (grad)	alpha (degree)	alpha		y (m)	super elevation	
				Deg	min			
01	5	0.00017	0.0097	0	0	35.67	0.00085	0.1260
02	10	0.00068	0.03896	0	2	20.26	0.00068	0.252
03	15	0.00159	0.0877	0	5	15.59	0.00297	0.378
04	20	0.00272	0.156	0	9	21.04	0.0545	0.504
05	25	0.00425	0.2435	0	14	36.63	0.1061	0.630
06	30	0.00613	0.3512	0	21	4.4	0.1837	0.756
07	35	0.00834	0.4778	0	28	40.25	0.2918	0.882
08	40	0.01089	0.6239	0	37	26.22	0.4356	1.001
09	45	0.01378	0.7895	0	47	22.33	0.6203	1.134
10	50	0.01702	0.9752	0	58	20.63	0.8508	1.250
11	50.8	0.01756	1.006	0	0	23.39	0.892	1.28

setting out half circle,

$$R = 482 \text{ m}$$

$$\beta = 4 - 2\Delta_s = 0.785 - 2 \times 0.6527 = 0.679 \text{ rad}$$

$$\begin{aligned} \text{length of half circular curve} &= \frac{327.567 \text{ m}}{2} \\ &= 163.784 \text{ m} \end{aligned}$$

Taking 20 chords in half-circle,

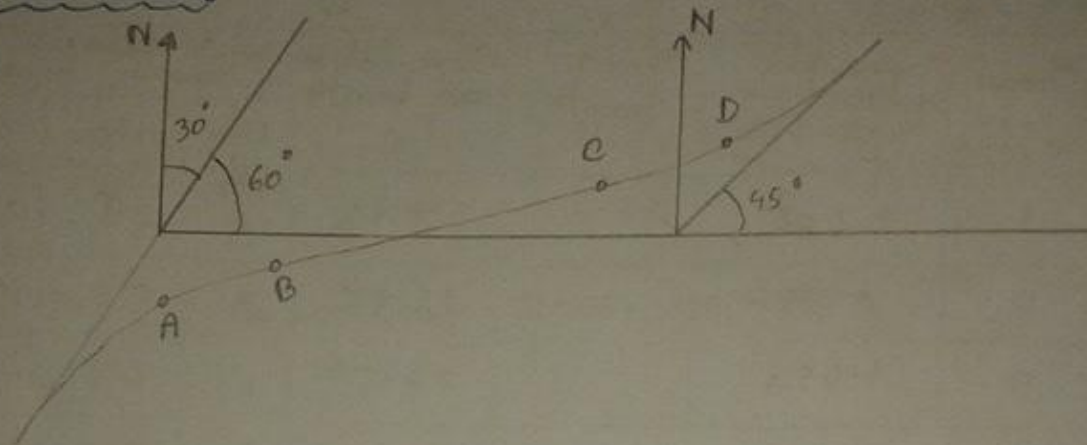
$$\text{length of each chord} = \frac{163.784}{20} = 8.189 \text{ m}$$

$$\begin{aligned} \text{subtended angle by each chord} &= \frac{0.679/20}{20} \text{ rad} \\ &= 0.017 \text{ rad} \\ &= 0.973^\circ \\ &= 58' 21.35'' \end{aligned}$$

tangential deflection angle by each chord

$$\begin{aligned} &= \frac{58' 21.35''}{2} \\ &= 0.486^\circ \\ &= 0^\circ 29' 10.67'' \end{aligned}$$

Problem 2 solve:



Given,

1st deflection angle, $\Delta_1 = 60^\circ$

2nd deflection angle, $\Delta_2 = 45^\circ$

$e_{\max} = 0.08$

$t_{\max} = 0.12$

design speed, $v = 80 \text{ km/h} = 22.22 \text{ ms}^{-1}$

setting out circular curve: Using Rankine's method:

Chord	Tangential deflection angle (deg)	Chord length (m)	Cumulative arc length (m)	Total deflection angle from common tangent			Super elevation
				Deg	min	sec	
1	0.486		8.18	0	29	0.6	
2	0.972		16.36	0	58	19.2	
3	1.458		24.54	1	27	28.8	
4	1.944		32.72	1	56	38.4	
5	2.430		40.90	2	25	48	
6	2.916		49.08	2	54	57.6	
7	3.402		57.26	3	24	7.2	
8	3.888		65.44	3	53	16.8	
9	4.374		73.62	4	22	26.4	
10	4.860	8.18	81.80	4	51	36	1.28
11	5.346		89.98	5	20	45.6	
12	5.832		98.16	5	49	55.2	
13	6.318		106.34	6	19	4.8	
14	6.804		114.52	6	48	14.4	
15	7.290		122.7	7	17	24	
16	7.776		130.88	7	46	33.6	
17	8.262		139.06	8	15	43.2	
18	8.748		147.24	8	44	52.8	
19	9.234		155.42	9	14	2.4	
20	9.72		163.6	9	43	12	

$$R_{\min} = \frac{v^2}{(e_{\max} + f_{\max})g} = \frac{(22.22)^2}{9.8 \times (0.08 + 0.12)} = 251.902 \text{ m}$$

$$\text{for } f=0, R = \frac{v^2}{g(e+0)} = \frac{(22.22)^2}{9.8 \times 0.08} = 629.756 \text{ m}$$

Let length of transition curve between AB and BC is L_1

$$\begin{aligned} \therefore L_1 &= \frac{v^3}{RC} \\ &= \frac{(22.22)^3}{629 \times 0.3} \\ &= 58.138 \text{ m} \end{aligned}$$

Length of transition curve between BC and CD is L_2 . It is same as L_1 as all elements v, R, C are same for both case.

$$\text{Shift}(s_1) = \frac{L_1^2}{24R} = 0.224 \text{ m}$$

Tangent distance for curve 1.

$$\begin{aligned} T_1 &= \frac{L_1}{2} + (R+s) \tan \frac{\Delta_1}{2} \\ &= \frac{58.138}{2} + (629.756 + 0.224) \tan \frac{60}{2} \\ &= 392.79 \text{ m} \end{aligned}$$

Tangent distance for curve - 2

$$\begin{aligned} T_2 &= \frac{L_2}{2} + (R+s) \tan \frac{\Delta_2}{2} \\ &= \frac{58.138}{2} + (629.756 + 0.224) \tan \frac{45}{2} \\ &= 290.02 \text{ m} \end{aligned}$$

$$\begin{aligned} \text{Total tangent distance, } T_1 + T_2 &= (392.79 + 290.02) \text{ m} \\ &= 682.805 \text{ m} \end{aligned}$$

Calculation of elements of circular and transition curves:-

$$\begin{aligned}\text{Spiral angle, } \Delta_s &= \frac{L}{2R} = \frac{58.138}{2 \times 629.756} \\ &= 0.046 \text{ rad} \\ &= 2.63^\circ = 2^\circ 38' 8.18''\end{aligned}$$

Maximum polar deflection angle,

$$\begin{aligned}\alpha_L &= \frac{\Delta_s}{3} = 0.0153 \text{ rad} \\ &= 0.876^\circ \\ &= 0^\circ 52' 42.73''\end{aligned}$$

Apex distance for curve-1,

$$\begin{aligned}E_1 &= \frac{R+S}{\cos \frac{\Delta_1}{2}} - R \\ &= \frac{629.756 + 0.224}{\cos(60/2)} - 629.756 \\ &= 97.213 \text{ m}\end{aligned}$$

Apex distance for curve-2,

$$\begin{aligned}E_2 &= \frac{R+S}{\cos \frac{\Delta_2}{2}} - R \\ &= \frac{629.756 + 0.224}{\cos(45/2)} - 629.756 \\ &= 52.129 \text{ m}\end{aligned}$$

$$\begin{aligned}\text{Length of circular curve-1} &= R(\Delta_1 - 2\Delta_s) \\ &= 629.756(1.0472 - 2 \times 0.046) \\ &= 601.54 \text{ m}\end{aligned}$$

$$\begin{aligned}\text{Length of circular curve-2} &= R(\Delta_2 - 2\Delta_s) \\ &= 629.756 \times (0.7854 - 2 \times 0.046) \\ &= 436.67 \text{ m}\end{aligned}$$

$$\text{Length of combined curve-1} = (2 \times 58.138 + 601.54) \text{ m} \\ = 717.816 \text{ m}$$

$$\text{Length of combined curve-2} = (2 \times 58.138 + 436.67) \text{ m} \\ = 552.946 \text{ m}$$

$$\text{maximum offset, } Y = 4s \\ = 4 \times 0.224 \\ = 0.896 \text{ m}$$

$$\text{setting out transition curve } \theta = \frac{L^2}{2RL}, \alpha \approx \frac{\theta}{3}, y = \frac{l^3}{6RL}$$

Peg stn	l=x(m)	alpha (rad)	alpha			y(m)
			Deg	Min	Sec	
01	5	0.0001	0	0	20.63	0.0005
02	10	0.0004	0	1	22.51	0.00455
03	15	0.0010	0	3	26.26	0.0154
04	20	0.0018	0	6	11.28	0.0364
05	25	0.0028	0	9	37.54	0.0711
06	30	0.0041	0	14	5.69	0.1229
07	35	0.0056	0	19	15.08	0.1951
08	40	0.0073	0	25	5.73	0.2913
09	45	0.0092	0	31	37.64	0.4148
10	50	0.0114	0	39	11.42	0.569
11	55	0.0138	0	47	26.45	0.757
12	58.138	0.0153	0	52	42.72	0.896

$$R = 629.756 \text{ m}$$

$$\beta_1 = \Delta_1 - 2\Delta_s = 1.047 - 2 \times 0.046 = 0.955 \text{ rad}$$

$$\beta_2 = \Delta_2 - 2\Delta_s = 0.785 - 2 \times 0.046 = 0.693 \text{ rad}$$

$$\text{Length of circular curve-1} = 601.54 \text{ m}$$

$$\therefore \text{Half length of circular curve-1} = \frac{601.54 \text{ m}}{2} \\ = 300.77 \text{ m}$$

length of each chord for 15 chords in curve-1.

$$\frac{300.77}{15} = 20.05 \text{ m}$$

$$\text{Angle subtended by each chord for curve-1} = \frac{\beta_1/2}{15} \\ = \frac{0.955/2}{0.032}$$

$$\therefore \text{Tangential deflection angle for 1}^{\text{st}} \text{ curve by each} \\ \text{chord} = \frac{1.82}{2} = 0.91$$

$$\text{length of circular curve-2} = 436.67 \text{ m}$$

$$\text{Half length of circular curve-2} = \frac{436.67}{2} = 218.335 \text{ m}$$

$$\text{Length of each chord} = \frac{218.335}{15} = 14.56 \text{ m}$$

$$\text{Angle subtended by each chord for curve-2} \\ = \frac{\beta_2/2}{15} = 0.0231 \\ = 1.32^\circ$$

$$\therefore \text{Tangential deflection angle for 2nd curve} \\ = \frac{1.32^\circ}{2} = 0.655^\circ$$

For 1st circular curve:

Chord	Tangential Deflection (deg)	Chord length	Cumulative chord length	Tangential deflection angle		
				Deg	min	sec
C ₁	0.91		20.05	0	54	36
C ₂	1.82		40.1	1	49	12
C ₃	2.73		60.15	2	43	48
C ₄	3.64		80.2	3	38	24
C ₅	4.55		100.25	4	33	0
C ₆	5.46		120.3	5	27	36
C ₇	6.37	20.05	140.35	6	22	12
C ₈	7.28		160.4	7	16	48
C ₉	8.19		180.45	8	11	24
C ₁₀	9.1		200.5	9	6	0
C ₁₁	10.01		220.55	10	0	36
C ₁₂	10.92		240.6	10	55	12
C ₁₃	11.83		260.65	11	49	48
C ₁₄	12.74		280.7	12	44	24
C ₁₅	13.65		300.75	13	39	0

For 2nd circular curve:

Chord	Tangential deflection angle	Chord length	Cumulative chord length	Tangential deflection angle		
				deg	min	sec
C_1	0.655		14.56	0	39	18
C_2	1.31		29.12	1	18	36
C_3	1.965		43.68	1	54	54
C_4	2.62		58.24	2	37	12
C_5	3.272		72.80	3	16	19.2
C_6	3.930		87.36	3	55	48
C_7	4.585	14.56	101.92	4	35	06
C_8	5.240		116.48	5	14	24
C_9	5.895		131.04	5	53	42
C_{10}	6.55		145.6	6	33	0
C_{11}	7.205		160.16	7	12	18
C_{12}	7.806		174.72	7	51	36
C_{13}	8.515		189.28	8	30	54
C_{14}	9.17		203.84	9	10	12
C_{15}	9.825		218.335	9	49	30

Problem 3 solve

Given,

$$\text{Deflection angle, } \Delta = 18^\circ 36' = 18.60^\circ$$

$$\text{Radius of circular curve, } R = 450 \text{ m}$$

$$\text{Design speed, } v = 70 \text{ km/h} = 19.44 \text{ m s}^{-1}$$

$$\text{chainage at PI} = 2524.20 \text{ m}$$

$$\text{Road width} = 16 \text{ m}$$

$$f_{\text{max}} = 0.10$$

$$e_{\text{max}} = 0.06$$

Length of transition curve

$$L = \frac{v^3}{R \cdot e} = \frac{(19.44)^3}{450 \times 0.06} = 54.42 \text{ m} = 55 \text{ m}$$

Calculation of elements of circular curve and transition curve.

$$\text{spiral angle, } \Delta_s = \frac{L}{2R} = \frac{55}{2 \times 450} = 0.061 \text{ rad} \\ = 3.50^\circ$$

Maximum polar deflection angle,

$$\alpha_L = \frac{\Delta_s}{3} = \frac{0.061}{3} \text{ rad} \\ = 0.0203 \text{ rad} \\ = 1.167^\circ$$

$$\text{shift, } s = \frac{L^2}{24R} = \frac{55^2}{24 \times 450} = 0.28 \text{ m}$$

total tangent length,

$$T = \frac{L}{2} + (R + s) \tan \frac{\Delta}{2} \\ = \frac{55}{2} + (450 + 0.28) \tan \left(\frac{18.60}{2} \right) \\ = 101.236 \text{ m}$$

Apex distance, $E = \frac{R+S}{\cos \frac{\Delta}{2}} - R$

$$= \frac{450 + 0.28}{\cos\left(\frac{18.60}{2}\right)} - 450$$

$$= 6.277 \text{ m}$$

Length of circular curve = $R(4 - 2\Delta_s)$

$$= 450(0.325 - 2 \times 0.061)$$

$$= 91.35 \text{ m}$$

Length of combined curve = $(2 \times 55 + 91.35)$

$$= 201.35 \text{ m}$$

chainage at T_1 (PC) = $(2524.20 - 101.236) \text{ m}$

$$= 2422.964 \text{ m}$$

chainage at T_2 (PT) = $(2422.964 + 201.35) \text{ m}$

$$= 2624.2 \text{ m}$$

Setting out transition curve:

$$x = \frac{l^2}{2RL}, \quad y = \frac{l^3}{6RL}$$

$$e_{\max} = 0.06$$

$$h_{\max} = 0.96 \text{ m}$$

Peg stn	l=x	alpha (rad)	alpha (deg)	alpha			y(m)	super elevation
				(deg)	min	sec		
1	5	0.00017	0.0096	0	0	35	0.00084	0.0872
2	10	0.00067	0.0386	0	2	19	0.00673	0.1745
3	15	0.00152	0.0868	0	5	13	0.02273	0.2618
4	20	0.00269	0.1543	0	9	16	0.05387	0.3491
5	25	0.00421	0.2411	0	14	28	0.10521	0.4363
6	30	0.00606	0.3472	0	20	50	0.18181	0.5236
7	35	0.00824	0.4726	0	28	22	0.28872	0.6109
8	40	0.01077	0.6173	0	37	02	0.43027	0.6911
9	45	0.01363	0.7813	0	46	33	0.61363	0.7854
10	50	0.01683	0.9645	0	57	52	0.84175	0.8723
11	55	0.02037	1.1671	1	10	02	1.12037	0.9600

Setting out half circle using Rankine's method by tangential deflection angle:

$$R = 450 \text{ m}$$

$$\begin{aligned}\beta &= 4 - 2\Delta_s = (0.325 - 2 \times 0.0611) \\ &= 0.2028 \text{ rad} \\ &= 11.6195^\circ\end{aligned}$$

$$\text{length of circular curve} = 91.35 \text{ m}$$

length of each chord taking 15 chords in a half circle.

$$\text{length of each chord} = \frac{91.35}{2 \times 15} = 3.045 \text{ m}$$

$$\begin{aligned}\text{Subtended angle by each chord} &= \frac{\beta/2}{15} = \frac{11.6195/2}{15} \\ &= 0.387^\circ\end{aligned}$$

Tangential deflection angle by each chord

$$= \frac{0.387}{2} = 0.194$$

Problem 4 solve

Given,

road width, $(b) = 10\text{m}$

Maximum rate of super elevation $= 0.06$

Maximum side friction coefficient $= 0.12$

The rate of change of radial acceleration $= 0.3\text{m/s}^3$

Chainage of PI $= 2000\text{m}$

Deflection angle, $\Delta = 15^\circ$

$$\text{Design speed, } v = 80\text{ km/h} = \frac{80 \times 1000}{3600}\text{ ms}^{-1}$$
$$= \frac{200}{9}\text{ ms}^{-1}$$

Radius of the end of transition curve, $R = 500\text{m}$

We know,

$$e + f = \frac{v^2}{gR}$$

$$\therefore R_{\min} = \frac{v^2}{g(e+f)} = \frac{(200/9)^2}{9.8 \times (0.06 + 0.12)}$$
$$= 279.66\text{m}$$

$$\text{For } f_{\max} = 0, \quad R = \frac{(200/9)^2}{9.81 \times 0.06} = 838.98\text{m}$$

Since the curve is wholly transitional, so there is no angle subtended by circular curve.

$$\therefore \Delta - 2\Delta_s = 0$$

$$\text{or, } \Delta_s = \frac{\Delta}{2} = \frac{15}{2} = 7.5^\circ = \frac{7.5\pi}{180}\text{ rad.}$$

Again, we know spiral angle, $\theta_s = \frac{L}{2R}$

$$\begin{aligned}L &= 2R\theta_s \\ &= 2 \times 500 \times \frac{7.5\pi}{180} \\ &= 130.90\text{ m}\end{aligned}$$

$$L_{\min} = \frac{\sqrt{3}}{R\theta} \quad (\because \text{considering } \theta \text{ maximum})$$

$$= \frac{(200/g)^3}{0.3 \times 500} = 73.16$$

$$\text{So, } L_{\min} = 73.16 < 130.90\text{ m}$$

$$\text{shift, } (s) = \frac{L^2}{24R} = \frac{(130.9)^2}{24 \times 500} = 1.43\text{ m}$$

$$\begin{aligned}\text{Total tangent Length} &= \frac{L}{2} + (R+s)\tan\frac{\theta}{2} \\ &= \frac{130.90}{2} + (500 + 1.43)\tan 7.5^\circ \\ &= 131.463\text{ m}\end{aligned}$$

$$\begin{aligned}\text{Apex distance, } E &= \frac{R+s}{\cos\frac{\theta}{2}} - R \\ &= \frac{500 + 1.43}{\cos 7.5^\circ} - 500 \\ &= 5.757\text{ m}\end{aligned}$$

$$\begin{aligned}\text{total length of curve} &= (130.90 + 130.90)\text{ m} \\ &= 261.8\text{ m}\end{aligned}$$

$$\begin{aligned}\text{chainage of point of curve} &= (3000 - 131.463)\text{ m} \\ &= 2868.537\text{ m}\end{aligned}$$

$$\begin{aligned}\text{chainage of point of tangent} &= (2868.537 + 261.80)\text{ m} \\ &= 3130.337\text{ m}\end{aligned}$$

Problem 5 solve:

Given that,

$$\text{Road width, } (b) = 10 \text{ m}$$

$$\text{Maximum rate of super elevation } (e_{\text{max}}) = 0.04$$

$$\text{Maximum side friction coefficient } (f_{\text{max}}) = 0.12$$

$$\text{Chainage at PI} = 2000 \text{ m}$$

$$\text{Deflection angle, } \Delta = 30^\circ$$

$$\text{Design speed, } v = 1000 \text{ km/h}$$

$$= \frac{1000 \times 1000}{3600} \text{ ms}^{-1} = \frac{250}{9} \text{ ms}^{-1}$$

$$\text{Radius of circular curve, } R = 1000 \text{ m}$$

$$\text{Apex distance, } E = \frac{R+s}{\cos \frac{\Delta}{2}} - R$$

As there is no transition curve, so there is no shift.

$$E = \frac{100}{\cos 15^\circ} - 1000 = 95.276 \text{ m}$$

$$\begin{aligned} \text{total length of tangent length, } T &= \frac{L}{2} + (R+s) \tan \frac{\Delta}{2} \\ &= R \tan \frac{\Delta}{2} \quad [\because L, s = 0] \\ &= 267.95 \text{ m} \end{aligned}$$

$$\text{total length of curve, } L_c = R \Delta_0$$

$$= 1000 \times 30 \frac{\pi}{180}$$

$$= 523.60 \text{ m}$$

$$\text{Here, } \Delta_0 = 30^\circ$$

$$= 30 \times \frac{\pi}{180} \text{ rad}$$

$$\begin{aligned} \text{chainage of point of curve (PC)} &= (2000 - 267.95) \text{ m} \\ &= 1732.05 \text{ m} \end{aligned}$$

$$\text{chaining of point of tangent} = (1732.05 + 523.60) \text{ m} \\ = 2255.65 \text{ m}$$

Now, at zero speed. $e + f_1 = \frac{v^2}{gR}$

$$\Rightarrow 0.04 + f_1 = 0$$

$$\therefore f_1 = -0.04$$

$$f_1 < f_{\max}$$

So, the curve is safe.

at speed, $v = 150 \text{ km/h} = \frac{150 \times 1000}{3600} \text{ ms}^{-1} = 41.67 \text{ ms}^{-1}$

$$e + f_2 = \frac{v^2}{gR}$$

$$\text{or, } 0.04 + f_2 = \frac{(41.67)^2}{9.8 \times 1000}$$

$$\therefore f_2 = 0.137$$

$\therefore f_2 > f_{\max}$, so that the road is not safe.

at $e=0$, $v = \frac{250}{9} \text{ ms}^{-1}$ $f_{\text{req}} = \frac{(250/9)^2}{9.81 \times 1000}$

$$= 0.079$$

Ans, $f_{\text{req}} < f_{\max}$, so that the road is safe for $e=0$.

[Proved]

Problem 6 solve:

Given that,

Radius of the larger curve, $R_1 = 1000 \text{ m}$

Radius of the smaller curve, $R_2 = 600 \text{ m}$

Design speed, $v = 100 \text{ km/h} = 27.778 \text{ ms}^{-1}$

Rate of change of radial acceleration, $c = 0.33 \text{ ms}^{-3}$

Chainage of the junction point with the

curve of large radius = 1224.00 m

$$\text{Now, } c = \frac{\frac{v^2}{R_2} - \frac{v^2}{R_1}}{L/v}$$

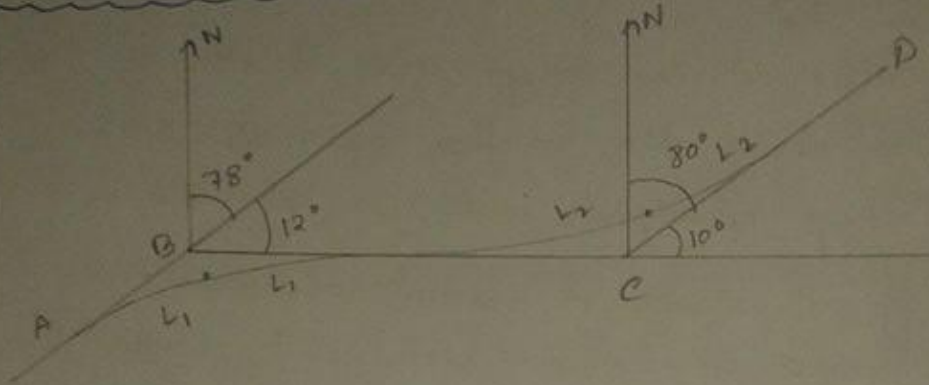
$$\Rightarrow L = \frac{\frac{v^2}{R_2} - \frac{v^2}{R_1}}{c/v} = \frac{\frac{27.778^2}{600} - \frac{27.778^2}{1000}}{\frac{0.33}{27.778}}$$

$$= 43.30 \text{ m}$$

So, chainage of other junction = $(1224.00 + 43.30) \text{ m}$

$$= 1267.30 \text{ m}$$

Problem 7 solve:



Given,

1st deflection angle, $\Delta_1 = 12^\circ$

2nd deflection angle, $\Delta_2 = 10^\circ$

Design speed, $v = 70 \text{ kmh}^{-1} = 19.44 \text{ ms}^{-1}$

rate of change of radial acceleration, $e = 0.3 \text{ ms}^{-3}$

change of PC on AB = 1736.31

step 1:

Determination of the radius of curve 1 2 2.

Here the curve is wholly transitional.

So, the length of circular curve = 0

$$\therefore R_1 (\Delta_1 - 2\Delta_{s1}) = 0 \quad (\text{for curve 1})$$

$$\Rightarrow \Delta_{s1} = \frac{\Delta_1}{2} = \frac{12^\circ}{2} = 6^\circ = 0.1047 \text{ rad}$$

$$\text{Now, } \Delta_{s1} = \frac{L_1}{2R_1}$$

$$\Rightarrow 0.1047 = \frac{L_1}{2R_1}$$

$$\therefore L_1 = 0.2094 R_1$$

Again,

$$L_1 = \frac{v^3}{R_1 e}$$

$$\Rightarrow 0.2094 R_1^2 = \frac{v^3}{e}$$

$$\Rightarrow R_1^2 = \frac{(10.44)^3}{0.2094 \times 0.3}$$

$$\therefore R_1 = 342.09 \text{ m}$$

Again, $R_2(\Delta_2 - \Delta_{s2}) = 0$ (for curve 2)

$$\Rightarrow \Delta_{s2} = \frac{\Delta_2}{2} = \frac{10^\circ}{2} = 5^\circ = 0.0873 \text{ rad}$$

Now, $\Delta_{s2} = \frac{L_2}{2R_2}$

$$\Rightarrow 0.0873 = \frac{L_2}{2R_2}$$

$$\therefore L_2 = 0.1745 R_2$$

And $L_2 = \frac{v^3}{R_2 e}$

$$\Rightarrow 0.1745 R_2^2 = \frac{v^3}{e}$$

$$\Rightarrow 0.1745 R_2^2 = \frac{(10.44)^3}{0.3}$$

$$\therefore R_2 = 375 \text{ m}$$

step 2:

Determination of the length of transition curve

1 & 2

$$L_1 = \frac{v^3}{R_1 e} = \frac{(10.44)^3}{342.09 \times 0.3} = 71.635 \text{ m}$$

$$L_2 = \frac{v^3}{R_2 e} = \frac{(10.44)^3}{375 \times 0.3} = 65.348 \text{ m}$$

Step 3:

Determination of the length of common tangent BC.

$$\text{Shift } s_1 = \frac{L_1^2}{24 R_1} \quad (\text{for curve-1})$$

$$= \frac{(71.635)^2}{24 \times 342.09}$$

$$= 0.6250 \text{ m}$$

$$\text{Shift } s_2 = \frac{L_2^2}{24 R_2}$$

$$= \frac{(65.348)^2}{24 \times 375} = 0.4744 \text{ m}$$

For curve-1, total tangent length,

$$T_1 = \frac{L_1}{2} + (R_1 + s_1) \tan \frac{\theta_1}{2}$$

$$= \frac{71.635}{2} + (342.09 + 0.625) \tan \frac{12}{2}$$

$$= 71.839 \text{ m}$$

For curve-2, total tangent length,

$$T_2 = \frac{L_2}{2} + (R_2 + s_2) \tan \frac{\theta_2}{2}$$

$$= \frac{65.348}{2} + (375 + 0.4744) \tan \frac{10}{2}$$

$$= 65.524 \text{ m}$$

\therefore Length of common tangent, BC = $T_1 + T_2$

$$= (71.839 + 65.524) \text{ m}$$

$$= 137.36 \text{ m}$$

Step 4:

Determination of the chainage of the tangent point on CD.

$$\text{Total length of curve-1} = (71.635 + 71.635) \text{ m}$$

$$= 143.378 \text{ m}$$

$$\text{Total length of curve-2} = (65.348 + 65.348) \text{ m} \\ = 130.696 \text{ m}$$

$$\text{chainage of the tangent point on CD} \\ = (1736.91 + 143.378 + 130.696) \text{ m} \\ = 2010.981 \text{ m}$$

Problem 8 solve:

Given,

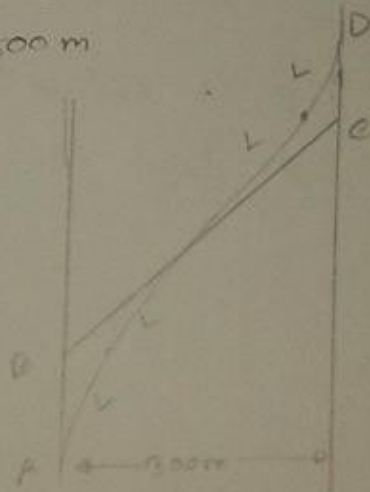
$$\text{Road width, } b = 12 \text{ m}$$

$$\text{Distance between centre lines of roads} = 30 \text{ m}$$

$$\text{Design speed, } v = 100 \text{ km/h}^{-1}$$

$$= 27.78 \text{ ms}^{-1}$$

$$\text{Radius of curvature, } R = 500 \text{ m}$$



$$\text{Rate of change of Radial acceleration, } e = 0.3 \text{ ms}^{-3}$$

$$\text{Length of transition curve, } L = \frac{v^3}{R \cdot e} \\ = \frac{(27.78)^3}{500 \times 0.3} \\ = 142.889 \text{ m}$$

As there is no circular curve.
So, total length of the curve = $(142.889 \times 4) \text{ m}$
 $= 571.559 \text{ m}$

Here, length of circular curve = 0

$$\therefore R(\Delta - 2\Delta_s) = 0$$

$$\text{or, } \Delta = 2\Delta_s$$

$$\text{Now, } \Delta_s = \frac{L}{2R}$$

$$= \frac{142.889}{2 \times 500} = 0.142889 \text{ rad}$$
$$= 8.187^\circ$$

$$\therefore \Delta = 2 \times 8.187^\circ = 16.3738^\circ = 16^\circ 22' 26''$$

Final deflection angle to locate the end
of first transition curve, $\alpha_L = \frac{\Delta_s}{3} = \frac{0.142889}{3}$

$$= 0.0476 \text{ rad}$$

$$= 2.7289^\circ$$

$$= 2^\circ 43' 44''$$



Problem 9 solve:

$$\begin{aligned} R_{\min} &= \frac{v^2}{g(e+f)} \\ &= \frac{(16.67)^2}{9.8 \times 0.12} \\ &= 236.30 \text{ m} \end{aligned}$$

Here,

$$\begin{aligned} v &= 60 \text{ kmh}^{-1} \\ &= \frac{60 \times 1000}{3600} \text{ m s}^{-1} \\ &= 16.77 \text{ m s}^{-1} \end{aligned}$$

$$f_{\max} = 0.12$$

$$e = 0$$