

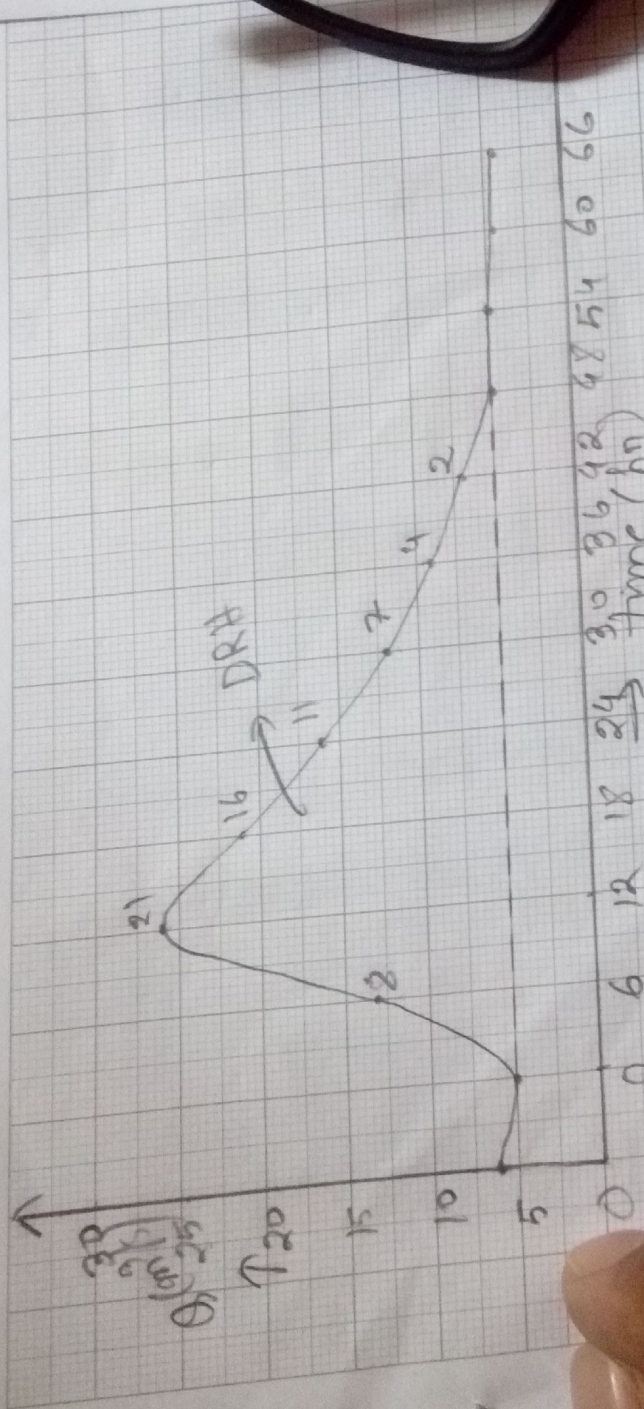
Hydrograph Example-6.2: Rainfall of magnitude 3.8 cm and 2.8 cm occurring on two consecutive 4-h durations on a catchment of area 27 km^2 produced the following hydrograph of flow at the outlet of the catchment. Estimate the rainfall excess and ϕ -index

Time from start of rainfall (hr) -6 0 6 12 18 24 30 36 42 48 54 60 66

Observed flow (m^3/s) 6 5 13 26 21 16 12 9 7 5 5 4 5 4 3

$11/8 = 1 + 1 = \text{ratio of base flow}$

Catchment area
 Let us use simple straight line method for base
 catchment $N = 0.83 \times A^{0.2}$

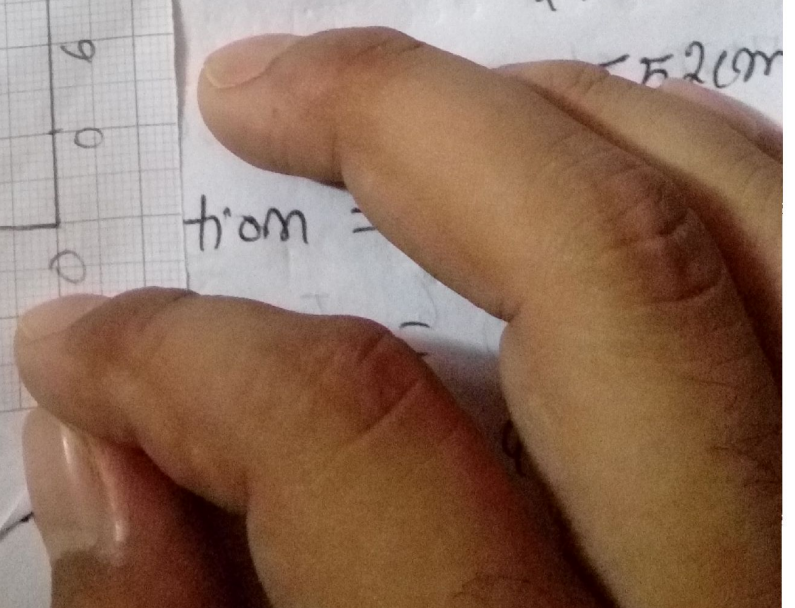


at 5 h
 has the peak at
 let us take $N = 8 - 12 =$

hydrograph (DRH)
 $(8 + 21) + (21 + 16) + (16 +$
 $(7 + 4) + (4 + 2) + 2$

$$\text{excess} = \frac{1.4904 \times 10}{27 \times 10^6}$$

from =



Solve Total rainfall = $3.8 + 2.8 = 6.6 \text{ cm}$

Catchment area = 27 km^2

Let us use simple straight line method for baseflow

separation = $N = 0.83 \times A^{0.2}$

$$= 0.83 \times (27)^{0.2}$$

$$= 1.6 \text{ days}$$

$$= 32.5 \text{ h}$$

from graph, DRH starts at $t=0$ has the peak at $t=12$ and ends at $t=48$ hr. Let us take $N = 48 - 12 = 36 \text{ h}$

Area of direct Runoff Hydrograph (DRH)

$$= 6 \times 3600 \times \frac{1}{2} \left\{ \begin{array}{l} (8 + (8+21)) + (21+16) + (16+11) + (11+7) \\ + (7+4) + (4+2) + 2 \end{array} \right\}$$

$$= 1.4904 \times 10^6 \text{ m}^3$$

$$\text{Runoff depth} = \text{Rainfall excess} = \frac{1.4904 \times 10^6}{27 \times 10^6} \times 100$$

$$= 5.52 \text{ cm}$$

$$\text{Depth of infiltration} = 6.6 - 5.52$$

$$= 1.08 \text{ cm}$$

$$\text{Total rainfall duration} = 4 + 4 = 8 \text{ hr}$$

$$\phi\text{-index} = \frac{1.08}{8}$$

$$= 0.135 \text{ cm/hr}$$

Example 6.3: A storm over a catchment of area 5.0 km^2 had a duration of 14 hours. The mass curve of rainfall of the storm is as follows-

Time from start of storm (hr)	0	2	4	6	8	10	12	14
Accumulated rainfall (cm)	0	0.6	2.8	5.2	6.6	7.5	9.2	9.6

If the ϕ -index of the catchment is 0.4 cm/h , determine the effective rainfall hyetograph and the vol^m of direct runoff from the catchment due to the storm

Solⁿ:

Depth of rainfall (cm)	0	0.6	2.2	2.4	1.4	0.9	1.7	0.4
Intensity of rainfall (cm/hr)	0	0.3	1.1	1.2	0.7	0.45	0.85	0.2

$$\begin{aligned} \text{Total rainfall} &= (0.3 + 1.1 + 1.2 + 0.7 + 0.45 + 0.85 + 0.2) \times 2 \\ &= \cancel{4.8} \text{ cm} \\ &= 9.6 \text{ cm} \end{aligned}$$

Depth of pre-mt time of rainfall excess = $14 - 2 - 2$
 $= 10 \text{ hr}$

Depth of infiltration = 0.4×10
 $= 4 \text{ cm}$

Effective rainfall depth = $10 - 4$

or Depth of Direct Runoff = 5.6 cm

Vol^m of direct runoff = $\frac{5.6}{100} \times 5 \times (10^3)^2$
 $= 28000 \text{ m}^3 \text{ (Ans)}$

(Confusion \rightarrow sin (3) ask 3310 2(1))

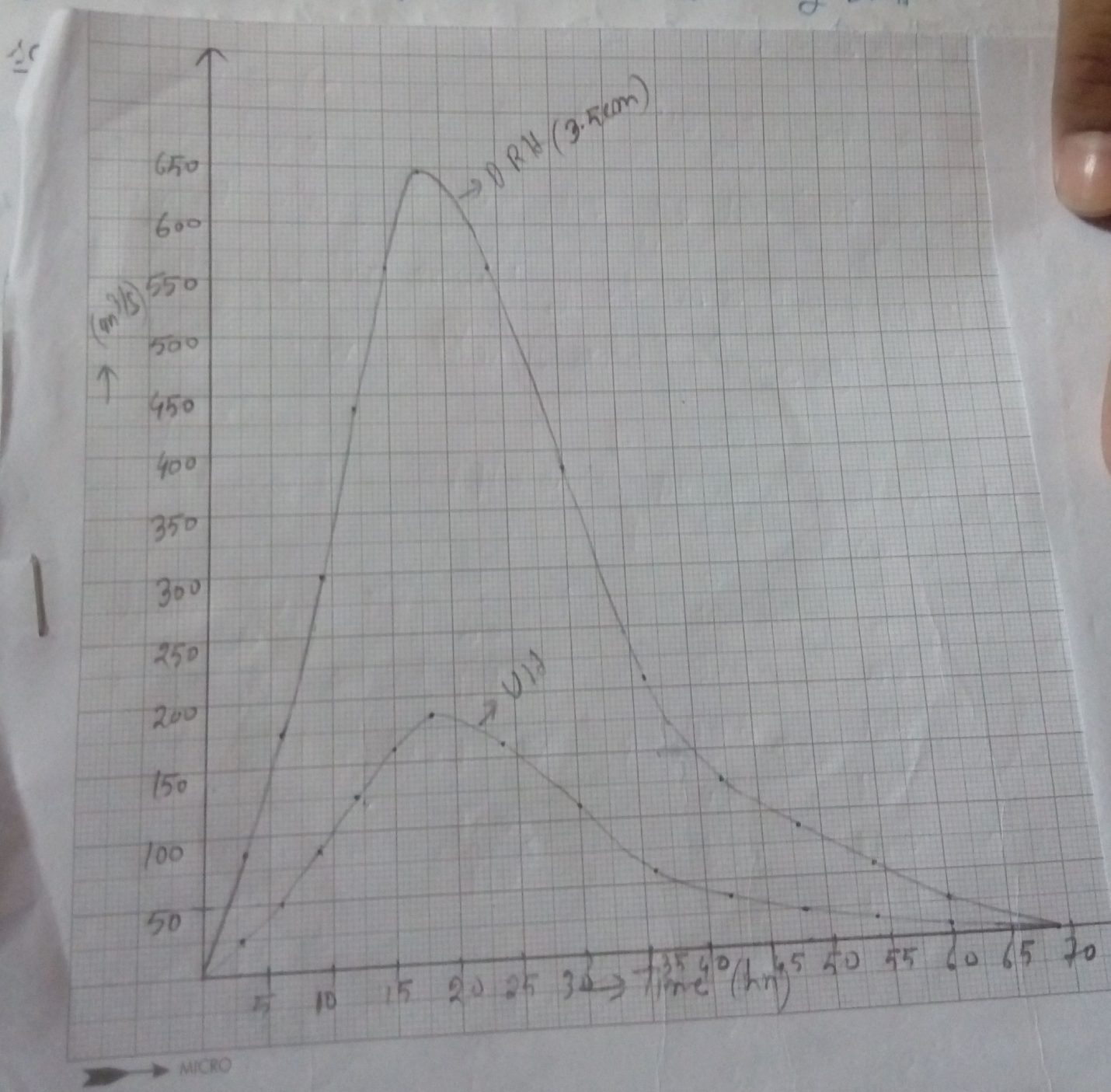
Unit Hydrograph Example 6.4: Given below are the ordinates of a 6-h unit hydrograph for a catchment. Calculate the ordinates of the DRH due to a rainfall excess of 3.5 cm occurring in 6 hr.

Time (h)	0	3	6	9	12	15	18	24	30	36	42	48	54	60
UH Ordinates (m^3/s)	0	25	50	85	125	160	185	160	110	60	36	25	16	8

Solve!

Time (h)	0	3	6	9	12	15	18	24	30	36	42	48	54	60
RH (m^3/s)	0	875	175	2925	4375	560	6475	560	385	210	126	875	56	28

Example-65: Two storms each of 6-h duration and having rainfall excess values of 3.0 and 2.0 cm respectively occur successively. The 2cm ER rain follows the 3cm rain. The 6-h unit hydrograph for the catchment is the same as given in example-64. Calculate the resulting DRH



60 24 (8)(16) 24

Example-65: Two storms each of 6-h duration and having rainfall excess values of 3.0 and 2.0 cm respectively occur successively. The 2cm ER rain follows the 3cm rain. The 6-h unit hydrograph for the catchment is the same as given in example-64. Calculate the resulting DRH

Soln:

Time	DRH ₁ ordinates	DRH ₂ ordinates	Resulting DRH ordinates
0	0	0	0
3	75	0	75
6	150	0	150
9	255	50	305
12	375	100	475
15	480	170	650
18	555	250	805
21	(172.5)	(132)	837.5
24	480	370	850
30	330	320	650
36	180	220	400
42	108	120	228
48	75	72	147
54	42	50	92
60	24	32	56
(66)	(2.7)	(8)	(16)

6.9 -0 10-7 10-7
 2.5 0 0 0

2012-13 1(b) The rainfall values over a catchment in three successive 5-hr intervals are known to be 3, 7 and 7 cm. The ϕ index for the catchment to be 0.2 cm/hr. Given below are the ordinates of a 5hr unit hydrograph.

Time (hr)	0	5	10	15	20	25	30	35	40	45	50
Ordinates of 5-hr UH (m^3/s)	0	50	125	185	160	110	60	36	25	12	0

Calculate the resulting storm hydrograph if the initial base flow is $10 m^3/s$ and increase by $2 m^3/s$ every 5 hours.

Solve!

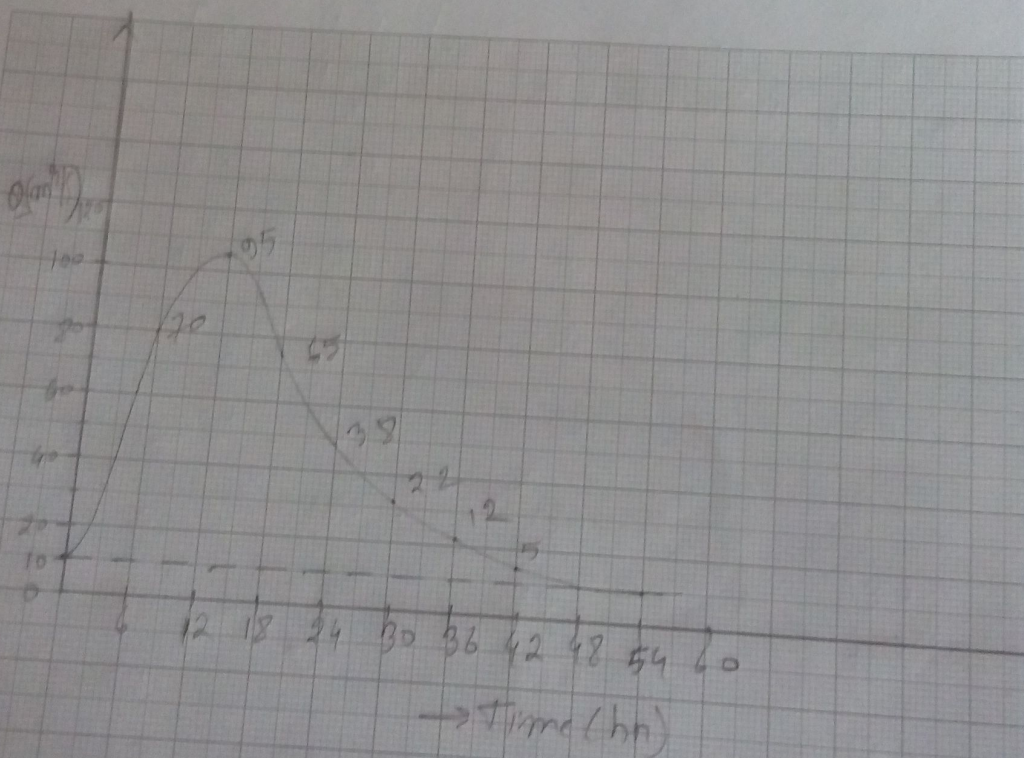
Time (hr)	UH Ordinates (m^3/s)	DRH(1) (m^3/s)	DRH(2) (m^3/s)	DRH(3) (m^3/s)	Base flow (m^3/s)
0	0	0	0	0	10
5	50	150	0	0	12
10	125	325	50	0	14
15	185	555	125	0	16
20	160	480	185	0	18
25	110	330	160	50	20
30	60	180	110	125	22
35	36	108	60	185	24
40	25	75	36	160	26
45	12	36	25	125	28
50	0	0	12	110	30

~~55~~ Effective rainfall depth in 1st 5h = $3 - 5 \times 0.2 = 2 \text{ cm}$
 " " " " 2nd 5h = $1 - 5 \times 0.2 = 0$
 " " " " 3rd 5h = $7 - 5 \times 0.2 = 6 \text{ cm}$

Time	VH ordinates (m^3/h)	DRH(2) (m^3/s)	DRH(6) m^3/s	Base flow (m^3/s)	Storm Hydrograph
0	0	0	0	10	10
5	250	100	0	12	112
10	125 125	250	0	14	264
15	185	370	300	16	686
20	160	320	750	18	1088
25	110	220	1110	20	1950
30	60	120	960	22	1102
35	36	72	660	24	756
40	25	50	360	26	434
45	12	24	216	28	268
50	0	0	150	30	180
53	0	0	60	32	72
55	0	0	0	32	32

2012-13 1(c) Following are the ordinates of a storm hydrograph of a river draining a catchment area of 50 km^2 due to a 6-hr isolated storm. Derive the ordinates of a 6-hr unit hydrograph for the catchment

Time from start of storm (hr) 0 6 12 18 24 30 36 42 48 54



Volume ordinates of direct runoff are, 0, 70, 95, 65, 38, 22, 12, 5, 0

$$\begin{aligned} \text{Volume of direct runoff} &= (6 \times 3600) \times \frac{1}{2} \left\{ 70 + (70 + 95) + (95 + 65) \right. \\ &\quad \left. + (65 + 38) + (38 + 22) + (22 + 12) \right. \\ &\quad \left. + (12 + 5) + 5 \right\} \end{aligned}$$

2012-13 1(c) Following are the ordinates of a storm hydrograph of a river draining a catchment area of 50 km^2 due to a 6 hr isolated storm. Derive the ordinates of a 6 hr unit hydrograph for the catchment

Time from start of storm (hr)	0	6	12	18	24	30	36	42	48	54
Discharge (cm^3/s)	10	30	105	75	48	32	22	15	10	10

Solve! Catchment area $A = 50 \text{ km}^2$

Let us use simple straight line method for base flow separation.

$$N = 0.83 \times A^{0.2} = 0.83 \times (50)^{0.2}$$

$$= 1.815 \text{ days}$$

$$= 43.6 \text{ hr}$$

from graph DRH straight at $t=0$, has the peak at $t=12 \text{ hr}$ and ends at $t=48 \text{ hr}$

let us take $N = 48 - 12 = 36 \text{ hr}$ instead of 43.6 hr

volume ordinates of direct runoff are, 0, 70, 95, 65, 38, 22, 12, 5, 0

$$\begin{aligned} \text{Volume of direct runoff} &= (6 \times 3600) \times \frac{1}{2} \left\{ 70 + (70 + 95) + (95 + 15) \right. \\ &\quad \left. + (15 + 38) + (38 + 22) + (22 + 12) \right. \\ &\quad \left. + (12 + 5) + 5 \right\} \end{aligned}$$

$$= 6.6312 \times 10^6 \text{ m}^3$$

depth of direct runoff on effective rainfall

$$= \frac{6.6312 \times 10^6}{50 \times 10^6} \times 100$$

$$= 13.2624 \text{ cm}$$

~~sa ordinates~~ DRH ordinates

UH ordinates

sa ordinates	DRH ordinates	UH ordinates
	0	0
	70	5.28
	95	7.16
	65	4.0
	38	2.87
	22	1.66
	12	0.9
	5	0.15
	0	0

Method of Superposition

Example-69: Given the ordinates of a 4-h unit hydrograph as below. Derive the ordinates of a 12-hr unit Hydrograph for the same catchment

Time (h)	0	4	8	12	16	20	24	28	32	36	40	44
Ordinate of UH (4-h)	0	20	80	130	150	130	90	52	27	15	5	0

Solve:

Time	Ordinates of 4-h UH	Ordinates of 4-h UH (Lagged by 4h)	Ordinates of 4-h UH (Lagged by 8h)	DR of 3 con m 12 hr
0	0	0	0	0
4	20	0	0	20
8	80	20	0	100
12	130	80	20	230
16	150	130	80	360
20	130	150	130	410
24	90	130	150	370
28	52	90	130	272
32	27	52	90	169
36	15	27	52	94
40	5	15	27	47
44	0	5	15	20
48	0	0	5	5
52	0	0	0	0

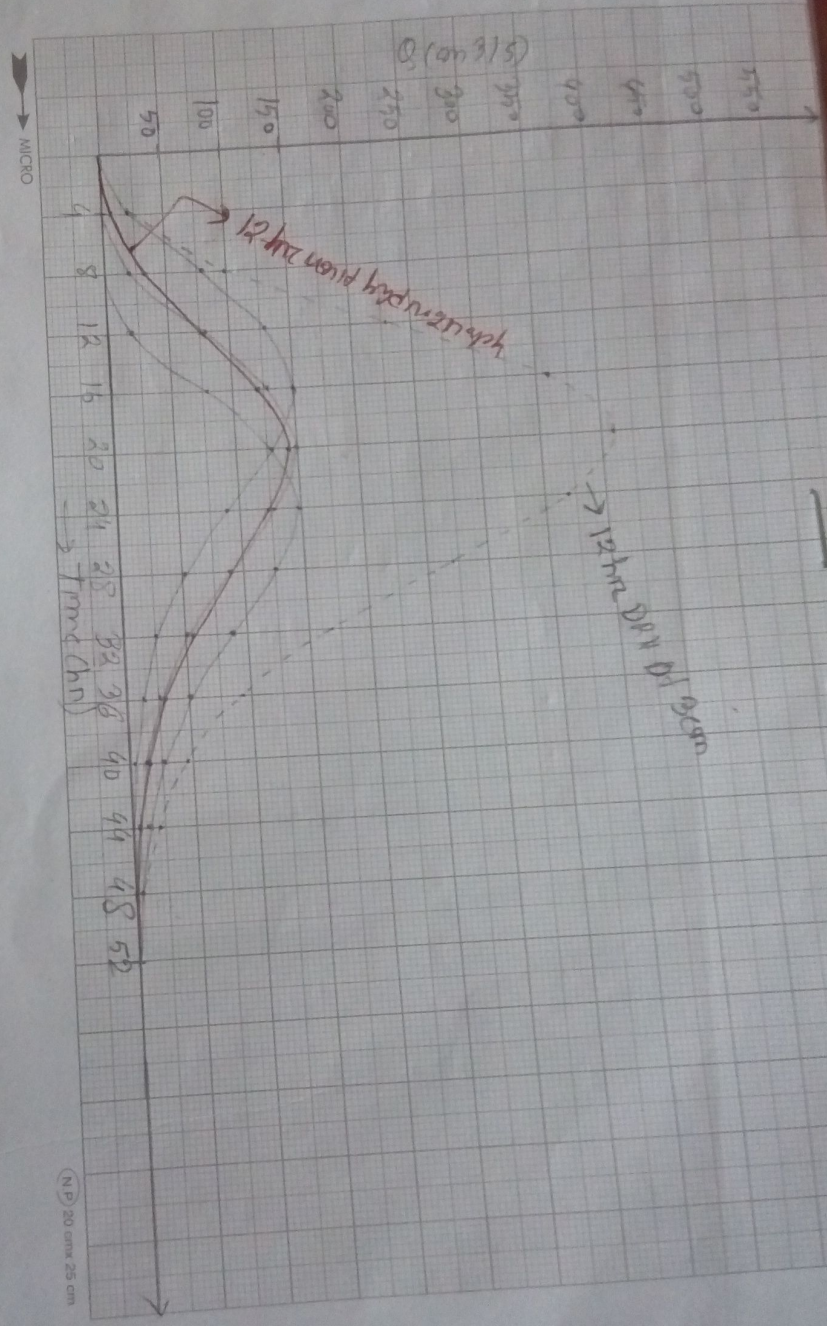
no.
DR
UH

On

now.

DRA of 3 cm / m 12h
 U17 of 12-h

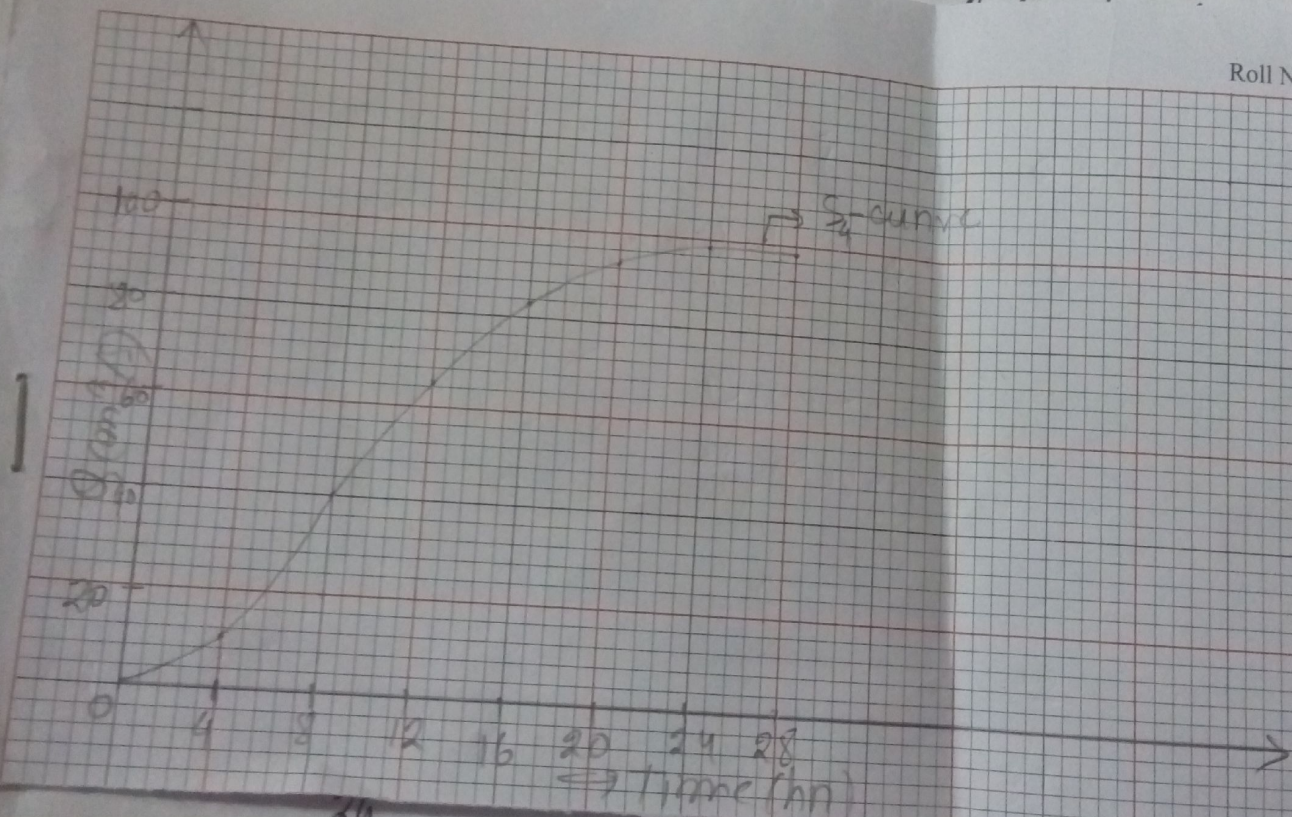
- Oscillator of 12-
- U17
 - 0
 - 6.67
 - 33.33
 - 76.67
 - 120
 - 136.67
 - 123.33
 - 90.67
 - 56.33
 - 31.33
 - 15.67
 - 6.67
 - 6.67
 - 0



Example - 6-10! Derive the score for the 4th unit Hydrograph given below:

Time (h)	0	4	8	12	16	20	24	28
Ordinate of 4h UH (m ³ /s)	0	10	30	25	18	10	5	0

Answer:



28

0

98

00.00

00.10

00.20

00.30

00.40

00.50

Example - 6.10! Derive the S-curve for the 4-h unit hydrograph given below:

Time (h)	0	4	8	12	16	20	24	28
Ordinate of 4h UH (m^3/s)	0	10	30	25	18	10	5	0

Solve!

Time (hr)	Ordinates of 4h UH (m^3/s)	Ordinates of S-curve
0	0	0
4	10	10
8	30	40
12	25	65
16	18	83
20	10	93
24	5	98
28	0	98

Problem: Given the ordinates of a 4-h unit hydrograph as below. Derive the ordinates of a 12-h unit hydrograph for the same catchment by S-curve method.

Time (hr)	0	4	8	12	16	20	24	28	32	36	40	44
Ordinate of 4h UH (m^3/s)	0	20	80	130	150	130	90	52	27	15	5	0

Solve!

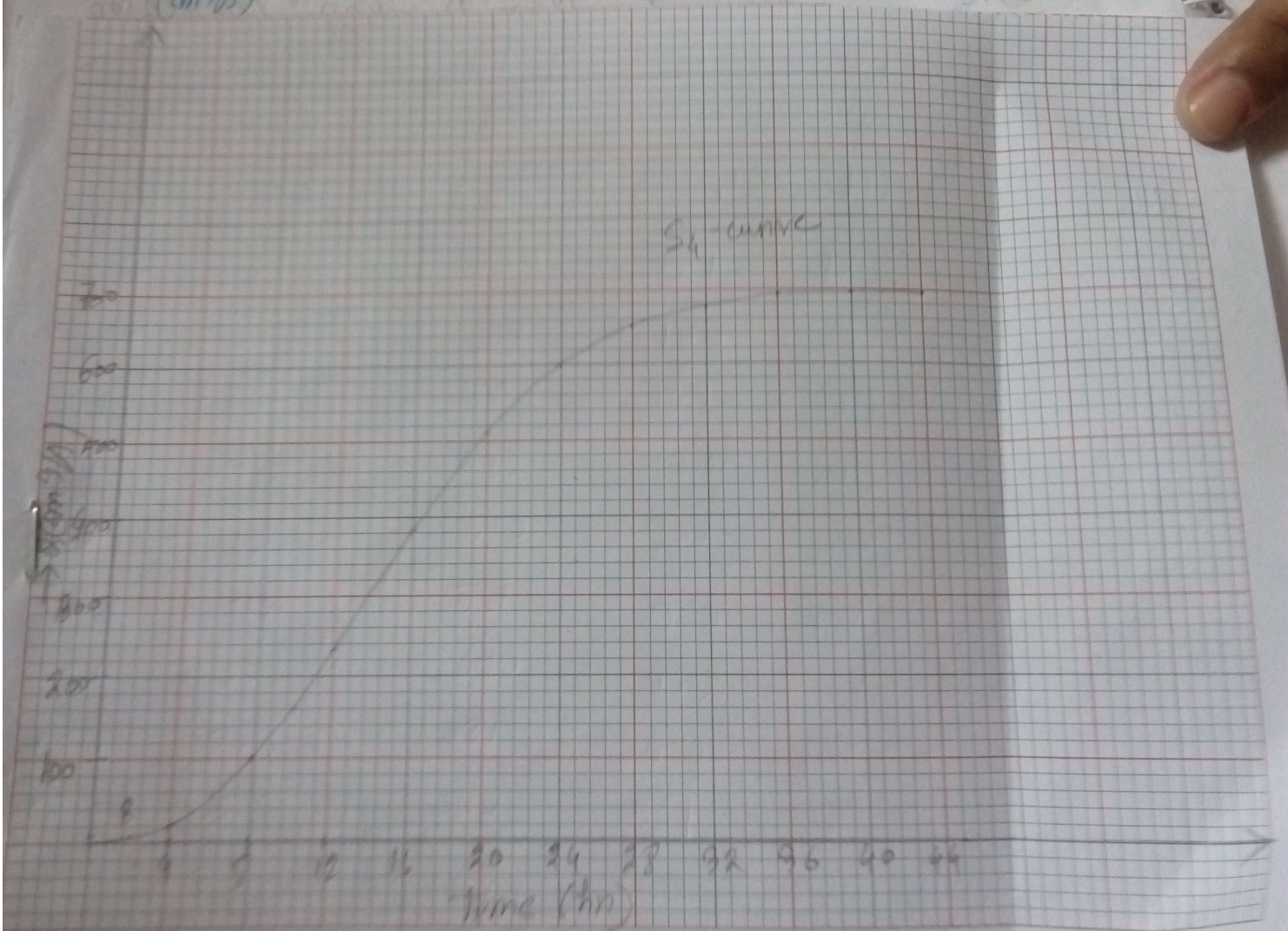
Given, $T = 12 \text{ hr}$, $D = 4 \text{ hr}$, $T/D = 3 \text{ cm}$

Time (hr)	Ordinates of 4h UH (m^3/s)	S-curve Ordinates (m^3/s)	S-curve lagged by 12h (m^3/s)	DRH of 3cm	Ordinates of 12-h UH
0	0	0	0	0	0
4	20	20	0	20	6.7
8	80	100	0	100	33.33
12	130	230	20	230	76.7
16	150	380	100	360	120
20	130	510	230	410	136.7
24	90	600	380	370	123.3
28	52	652	510	272	90.7
32	27	679	600	169	56.3
36	15	694	652	94	31.3
40	5	699	679	47	15.7
44	0	699	699	20	6.7

98 0 699 ~~699~~ 694 5 1.7
 52 0 699 699 0 0

Example - 6121 Determine 2-h Unit Hydrograph from 4-h Unit Hydrograph given below

Time (hr)	0	4	8	12	16	20	24	28	32	36	40	44
UH ordinates (cm ³ /s)	0	20	80	130	150	130	90	52	27	15	5	0



20 150

98 0 699 ~~699~~ 699 5 1-2
 52 0 699 699 0 0

Example - 6.12.1 Determine 2-h Unit Hydrograph from 4-h Unit Hydrograph given below

Time (hr)	0	4	8	12	16	20	24	28	32	36	40	44
UH ordinates (cm ² /s)	0	20	80	130	150	130	90	52	27	15	5	0

Solve: here, $T = 2$, $D = 4$ $T/D = 0.5 \text{ cm}$
 common num bet T and D is 2

Time	4-hn UH ordinates	Scurve Ordinate	Scurve lagged by 2hr	DR of 0.5cm	UH for 2-hr ordinates
0	0	0	0	0	0
2	0	0	0	8	16
4	20	20	0	12	24
6	43	51	0	31	62
8	80	100	20	49	98
10	110	161	51	61	122
12	130	230	100	69	138
14	146	307	161	77	154
16	150	380	230	73	146
18	142	449	307	69	138
20	130	510	449	61	122

22	112	-	561	510	51	102
24	90		600	561	39	78
26	20	-	631	600	31	62
28	52		652	631	21	42
30	38		669	652	17	34
32	27		679	669	10	20
34	20	-	689	679	10	20
36	15		694	689	5	10
38	10	-	699	694	5	(10) 6
40	5		699	699	0	(10) 3
42	2	-	701	699	2	0
44	0		699	701	-2	0
46	0		699	699	0	0
48	0		699	699	0	0

Exam problem: Ordinates of a 4-h unit hydrograph are given. Using this derive the ordinates of a 6-h unit hydrograph for the same catchment.

Time (h)	0	4	8	12	16	20	24	28	32	36	40
Ordinate of 4h UH (cm/s)	0	20	80	130	150	130	90	52	27	15	5

Solve: here, $D = 4$, $T = 6$, $T/D = 6/4 = 1.5$ cm

least common number betⁿ 4 and 6 is 2.

Time (hr)	4-h VA ordinates	S ₄ curve Ordinates	S-curve lagged by 6hr	DRH of 1.5cm	6-h VA ordinates
0	0	0	0	0	0
2	8	8	0	8	5.33
4	20	20	0	20	13.33
6	43	51	0	51	34
8	80	100	8	92	61.33
10	110	161	20	141	94
12	130	230	51	179	119.33
14	146	307	100	207	138
16	150	380	161	219	146
18	142	449	230	219	146
20	130	510	307	203	135.3
22	112	561	380	181	120.67
24	90	600	449	151	100.7
26	70	631	510	121	80.7
28	52	652	561	91	60.7
30	38	669	600	69	39.3
32	27	679	631	48	32
34	20	689	652	37	24.7

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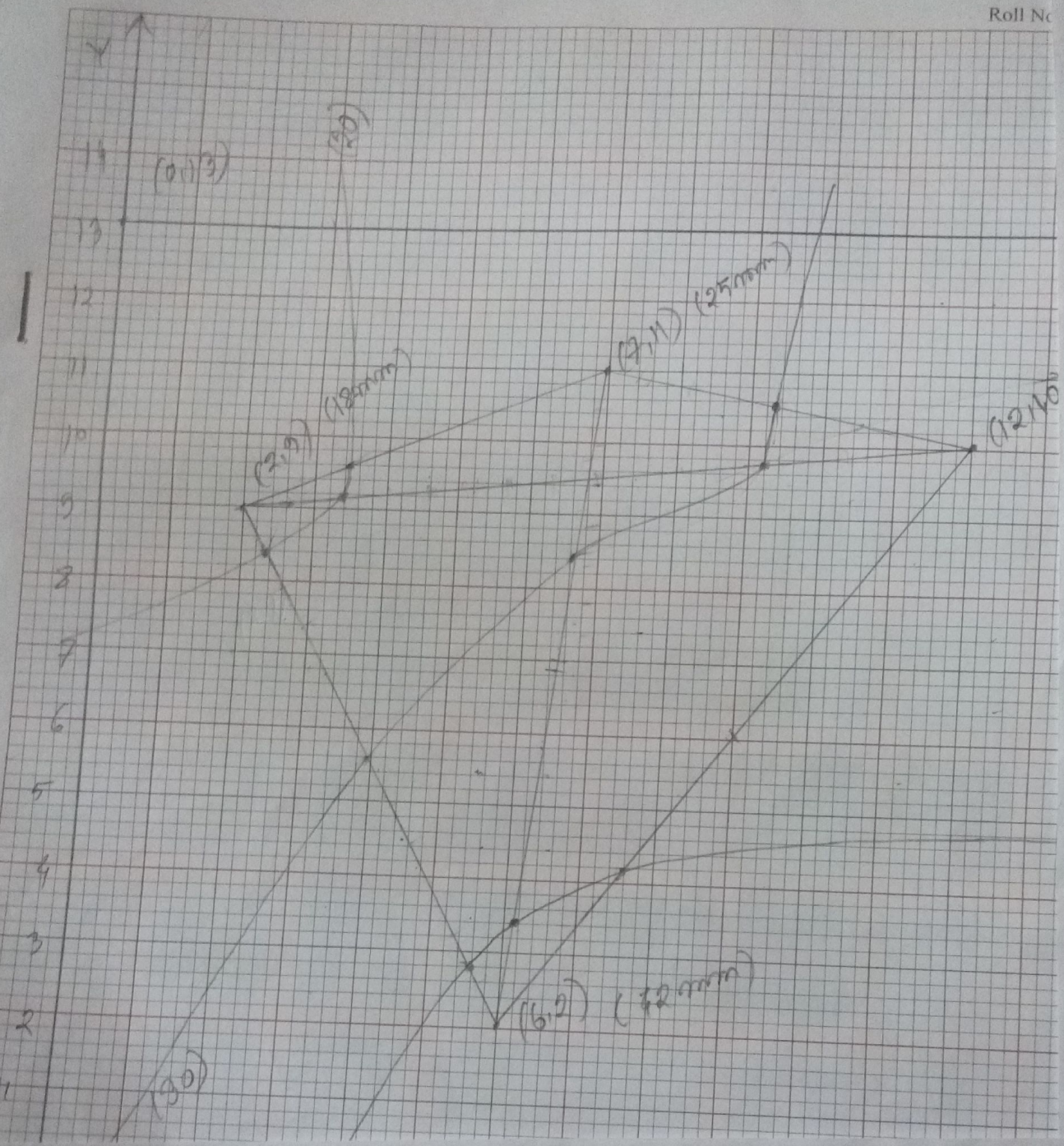
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36	15	699	669	25	16.7
38	10	699	679	20	13.3
40	5	699	689	10	6.7
42	2	701	694	7	4.7
44	0	699	699	0	(0) (2) 2
46	0	699	699	0	0
48	0	699	701	-2	(-1.3) (0) 0
50	0	699	699	0	0

2019-14 3(c) Four rain gauge gauges located within a rectangular area with four corners at (0,0), (0,13), (14,13), and (14,0) having the following coordinates and recorded rainfalls

Rain gauge location	Rainfall (mm)
(2, 9)	18
(7, 11)	25
(12, 10)	35
(6, 2)	42

All coordinates are expressed in km. Compute the average rainfall in the area by isohyetal Method (use isohyets of 20 and 40mm) Use plain graph paper.



where $L =$ Maximum length of travel of water of hose

From Graph!

Isohyets	Area enclosed	Avg rainfall	Rainfall vol ^m
	200 900	10	4000
20	1375	25	34375
30	1800	35	63000
40	975	20	19500
	<hr/> 4550		<hr/> 120875

$$\begin{aligned} \text{Average rainfall} &= \frac{120875}{4550} \\ &= 26.57 \text{ mm (Ans)} \end{aligned}$$

2013-14 (19). Consider the following two catchment areas

Catchment A

Slope = 0.002

$L = 1500 \text{ m}$

Sandy soil

High vegetative cover

$A = 2 \text{ km}^2$

Catchment B

Slope = 0.02

$L = 2000 \text{ m}$

Clay soil

No vegetative cover

$A = 3 \text{ km}^2$

Where $L =$ Maximum length of travel of water

- i) The runoff coefficients of 0.2 and 0.8. Which runoff coefficients will be applicable to which catchment and why?
- ii) Find out the time of concentration of catchment A
- iii) Compute the peak discharge for catchment A for a return period of 100 years using Rational Method. Use IDF curves shown in Fig 1.

Solve! i) Catchment A has sandy soil so infiltration will be high as a result runoff will be low. At the same time catchment B has clay soil so impermeable as a result runoff will be high. Catchment A has higher vegetative cover so lower runoff. Catchment B has no vegetative cover so higher runoff.

So, for catchment ~~area~~ A runoff coefficient $C = ~~0.8~~ 0.2$
 for catchment B runoff coefficient $C = 0.8$

ii) here, $L = 1500\text{m}$ $S = 0.002$

$$\begin{aligned} \text{time of concentration, } t_c &= 0.01947 L^{0.77} S^{-0.385} \\ &= 0.01947 \times (1500)^{0.77} \times (0.002)^{-0.385} \\ &= 59.44 \text{ minutes } \underline{\underline{(Am)}} \end{aligned}$$

iii) here, $T = 100$ and $t_c = 59.44$

$$\text{so, } i = 3.25 \text{ m/h}$$

$$= 8.255 \text{ cm/h}$$

Peak discharge, $Q = CiA$

$$= 0.27 \frac{8.255}{100 \times 3600} \times (2) \times 10^6$$

$$= 9.17 \text{ m}^3/\text{s} \text{ (Ans)}$$

Objective

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