

Lateral earth pressure

$$K_0 = (1 - \sin \phi) \rightarrow NC$$

$$K_0 = \sigma_{cr}^{\sin \phi} \cdot (1 - \sin \phi) \rightarrow OC \quad \left. \begin{array}{l} \\ \end{array} \right\} \text{-Jaky}$$

$$K_0 = 0.19 + 0.233 \log (IP) \rightarrow NC$$

$$K_0(OC) = K_0(NC) \cdot \sqrt{OER} \rightarrow OC \quad \left. \begin{array}{l} \\ \end{array} \right\} \text{-Atterberg}$$

$(1 + 0.5 \tan \beta)^2 \rightarrow$ Correction factor. when the soil is inclined with retaining wall.

cohesionless soil

$$K_a = \frac{1 - \sin \phi}{1 + \sin \phi} = \tan^2 \left(45^\circ - \frac{\phi}{2} \right) \rightarrow \text{Active pressure}$$

$$K_p = \frac{1 + \sin \phi}{1 - \sin \phi} = \tan^2 \left(45^\circ + \frac{\phi}{2} \right) \rightarrow \text{passive}$$

partially cohesive soil:

$$P_{ac} = K_a \cdot \gamma h - 2c\sqrt{K_a}$$

$$h_c = \frac{2c}{\gamma\sqrt{K_a}} = \frac{2c}{\gamma} \tan \left(45^\circ + \frac{\phi}{2} \right)$$

critical height

theoretical unsupported height $H_u = 2h_c$

$$= \frac{4c}{\gamma\sqrt{K_a}}$$

$$P_{ac} = \frac{1}{2} K_a \cdot \gamma H^2 - 2cH\sqrt{K_a} + \frac{2c^2}{\gamma}$$

$$P_{pc} = K_p \gamma H + 2\sqrt{K_p} c$$

Lateral earth pressure

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critical height \leftarrow

theoretical unsupported height $H_u = 2h_c$

$$= \frac{4c}{\gamma\sqrt{K_a}}$$

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$$P_{pc} = K_p \gamma H + 2\sqrt{K_p} c$$

Cohesionless back filling.

$$K_a = \frac{\cos \beta - \sqrt{\cos^2 \beta - \cos^2 \phi}}{\cos \beta + \sqrt{\cos^2 \beta - \cos^2 \phi}}$$

$$P_a = \frac{1}{2} K_a \gamma H^2 \cos \beta.$$

horizontal $P_{ah} = \frac{1}{2} K_a \gamma H^2 \cos^2 \beta.$

$$K_p = \frac{\cos \beta + \sqrt{\cos^2 \beta - \cos^2 \phi}}{\cos \beta - \sqrt{\cos^2 \beta - \cos^2 \phi}}.$$

passive $P_p = \frac{1}{2} K_p \gamma H^2 \cos \beta.$

point load. $m > 0.4$

$$P_n = \frac{1.77 \gamma}{H^2} \frac{m^2 n^2}{(m^2 + n^2)^3}$$

$m \leq 0.4$

$$P_n = \frac{1.77 \gamma}{H^2} \frac{0.4^2 n^2}{(0.4^2 + n^2)^3}$$

$$P_n' = P_n \cdot \cos^2 \beta (1 -$$

Line load.

$m > 0.4$

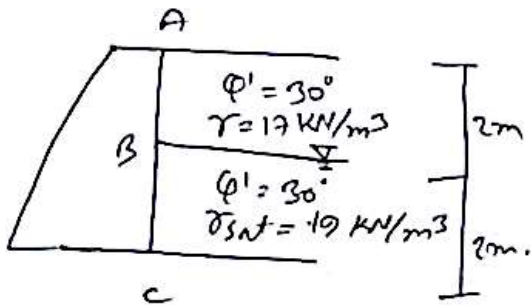
$$P_n = \frac{4 \gamma}{\pi H} \frac{m^2 n}{(m^2 + n^2)^2}$$

$m \leq 0.4$

$$P_n = \frac{4 \gamma}{\pi H} \frac{0.4^2 n}{(0.4^2 + n^2)^2}$$

AK-47

19.1 Determine the lateral earth pressure at rest per unit length of wall shown in Fig. Also determine the location of the resultant earth pressure. $K_0 = 1 - \sin \phi'$
 $\gamma_w = 10 \text{ kN/m}^3$



$$K_0 = 1 - \sin \phi'$$
$$= 1 - \sin 30^\circ = 1/2$$

At point B:

$$\bar{\sigma}_z = 2 \times 17 = 34 \text{ kN/m}^2$$

$$u = 0$$

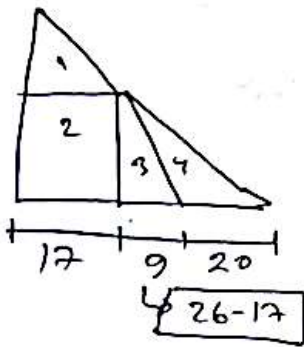
$$P_0 = K_0 \cdot \bar{\sigma}_z$$
$$= 17 \text{ kN/m}^2$$

At point C

$$\bar{\sigma}_z = 2 \times 17 + (19 - 10) \times 2 = 52 \text{ kN/m}^2$$

$$P_0 = 0.5 \times 52 = 26 \text{ kN/m}^2$$

$$u = 2 \times 10 = 20 \text{ kN/m}^2$$



$$P_1 = \frac{1}{2} \times 17 \times 2 = 17 \text{ kN}$$

$$P_2 = 2 \times 17 = 34 \text{ kN}$$

$$P_3 = \frac{1}{2} \times 9 \times 2 = 9 \text{ kN}$$

$$P_4 = \frac{1}{2} \times 20 \times 2 = 20 \text{ kN}$$

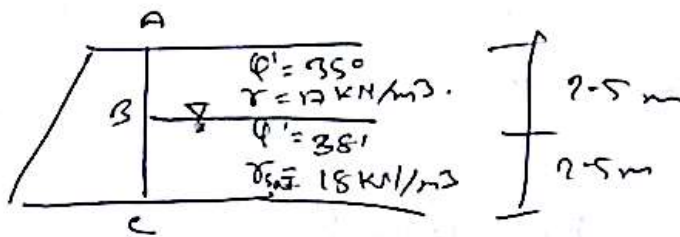
$$P = \sum P = 80 \text{ kN}$$

Line of P determined by moments about C

$$P \cdot \bar{x} = 17 \times 2.667 + 34 \times 1 + 9 \times 0.667 + 20 \times 0.667$$

$$\Rightarrow \bar{x} = 1.23 \text{ m from base}$$

17.2 Determine the active earth pressure on the retaining wall shown in figure. $\gamma_w = 10 \text{ kN/m}^3$



$$\Rightarrow K_a = \frac{1 - \sin \phi'}{1 + \sin \phi'}$$

for upper layer $K_a = \frac{1 - \sin 35}{1 + \sin 35} = 0.271$

" lower " $K_a = \frac{1 - \sin 38}{1 + \sin 38} = 0.238$

at point B.

$$\bar{\sigma}_2 = 2.5 \times 17 = 42.5 \text{ kN/m}^2$$

$$u = 0$$

$$P_a = 0.271 \times 42.5 = 11.5 \text{ kN/m}^2$$

below the interface

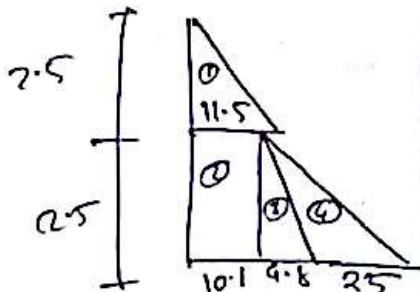
$$P_a = 0.238 \times 42.5 = 10.1 \text{ kN/m}^2$$

at point C

$$\bar{\sigma}_2 = 2.5 \times 17 + 2.5 \times (18 - 10) = 62.5$$

$$u = 2.5 \times 10 = 25$$

$$P_a = 0.238 \times 62.5 = 14.9$$



$$P_1 = \frac{1}{2} \times 2.5 \times 11.5 = 14.4$$

$$P_2 = 2.5 \times 10.1 = 25.3$$

$$P_3 = \frac{1}{2} \times 2.5 \times 4.8 = 6$$

$$P_4 = \frac{1}{2} \times 2.5 \times 25 = 31.3$$

$$\Sigma P = 77$$

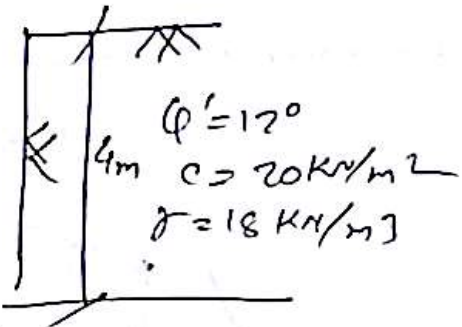
19.4 Determine the stress at the top and bottom of the cut shown in fig. Also determine the maximum depth of potential crack and maximum depth of unsupported excavation

$$P_a = K_a \cdot \gamma z - 2c' \sqrt{K_a}$$

$$K_a = \frac{1 - \sin 12^\circ}{1 + \sin 12^\circ} = 0.656$$

$$P_a = 0.656 \times 18z - 2 \times 20 \times \sqrt{0.656}$$

$$= 11.81z - 32.4$$



at $z = 0$ \cdot $P_a = -32.4 \text{ kN/m}^2$

\cdot $z = 4$ $P_a = 14.8 \text{ kN/m}^2$

depth of crack

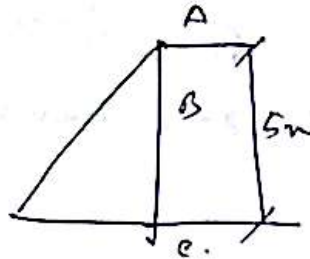
$$z_c = \frac{2c'}{\gamma \sqrt{K_a}} = \frac{2 \times 20}{18 \times \sqrt{0.656}} = 2.745 \text{ m}$$

max depth of unsupported excavation

$$H_c = \frac{2c'}{\gamma \sqrt{K_a}} = 5.490 \text{ m}$$

19.5 A 5m high retaining wall is shown in Fig.
 Determine the Rankine active pressure on the wall

- ① Before formation of crack
- ② After " " " "



$$\begin{aligned} \phi &= 30^\circ \\ c &= 5 \text{ kN/m} \\ \gamma &= 17.5 \text{ kN/m}^3 \end{aligned}$$

$$K_a = \frac{1 - \sin \phi}{1 + \sin \phi} = \frac{1 - \sin 30}{1 + \sin 30} = 0.333$$

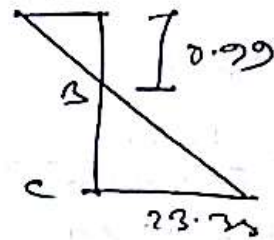
$$P_a = K_a \gamma z - 2c' \sqrt{K_a}$$

$$\begin{aligned} &= 0.333 \times 17.5 \times z - 2 \times 5 \times \sqrt{0.333} \\ &= 5.832z - 5.77 \end{aligned}$$

$$\text{at } z=0, P_a = -5.77$$

$$\text{at } z=5, P_a = 23.38$$

$$\begin{aligned} \text{at } z & \text{ at } P_a = 0, \quad 5.832z - 5.77 = 0 \\ & \Rightarrow z = 0.99 \text{ m} \end{aligned}$$



Before formation of crack.

$$\begin{aligned} \text{Negative pressure } P_1 &= \frac{1}{2} \times 0.99 \times 5.77 \\ &= 2.86 \text{ kN} \end{aligned}$$

$$\begin{aligned} \text{positive } P_2 &= \frac{1}{2} \times 4.01 \times 23.38 \\ &= 46.88 \text{ kN} \end{aligned}$$

$$\text{Net } P_a = 46.88 - 2.86 = 44.02 \text{ kN}$$

Line of action P_a is determined by taking moment about C

$$\bar{z} = \frac{46.88 \times \frac{4.01}{3} - 2.86 \times (4.01 + 0.67)}{44.02}$$

$$= 1.12 \text{ m}$$

After formation of crack

after formation of crack the -ve pressure is eliminated.

$$P_a = \frac{1}{2} \times 23.38 \times 4.01 = 46.88$$

will act at a height of $\frac{4.01}{3}$ m from above

19.6 Determine the ranking passive forces per unit length of the wall shown in fig. The water table at level B. $\gamma_w = 10 \text{ kN/m}^3$

top layer.

$$K_{p1} = \frac{1 + \sin 30}{1 - \sin 30} = 3.00$$

bottom layer.

$$K_{p2} = \frac{1 + \sin 24}{1 - \sin 24} = 2.37$$

$$P_p = K_p \gamma z + 2c' \sqrt{K_p}$$

At A. $z = 0$. $P_p = 0$

at B $z = 2\text{m}$. $\bar{\sigma}_v = 2 \times 16 = 32 \text{ kN/m}^2$

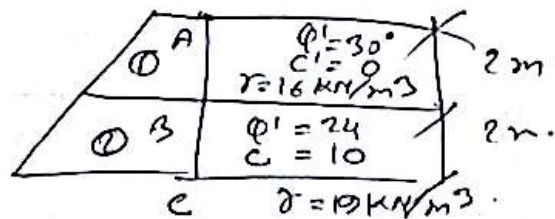
top layer $P_p = 3 \times 32 = 96 \text{ kN/m}$

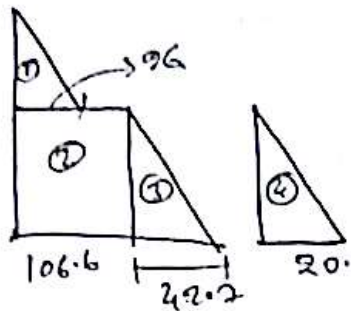
bottom $P_p = 32 \times 2.37 + 2 \times 10 \times \sqrt{2.37} = 106.6 \text{ kN/m}$

At C. $\bar{\sigma}_v = 2 \times 16 + 2 \times (19 - 10) = 50 \text{ kN/m}^2$

$P_p = 50 \times 2.37 + 2 \times 10 \times \sqrt{2.37} = 149.3$

$u = 2 \times 10 = 20 \text{ kN/m}$



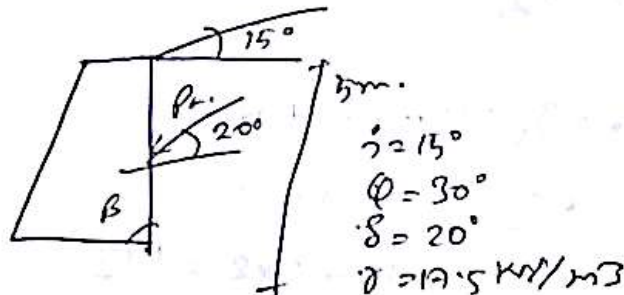


$$\text{total pressure} = P_1 + P_2 + P_3 + P_4$$

$$= \frac{1}{2} \times 2 \times 96 + 106 \times 2 + \frac{1}{2} \times 42.2 \times 2 + \frac{1}{2} \times 2 \times 20$$

$$= 371.9 \text{ kN}$$

17.2 Determine Coulomb's active force on the retaining wall shown in fig. $\gamma = 17.5 \text{ kN/m}^3$.



$$K_a = \frac{\sin^2(\beta + \phi')}{\sin^2 \beta \cdot \sin(\beta - \delta) \left[1 + \frac{\sin(\phi + \delta) \cdot \sin(\phi' - i)}{\sin(\beta - \delta) \cdot \sin(\beta + i)} \right]}$$

$$= \frac{\sin^2(75 + 30)}{\sin^2 75 \cdot \sin(75 - 20) \left[1 + \frac{\sin(30 + 20) \cdot \sin(30 - 15)}{\sin(75 - 20) \cdot \sin(75 - 15)} \right]}$$

$$= 0.548$$

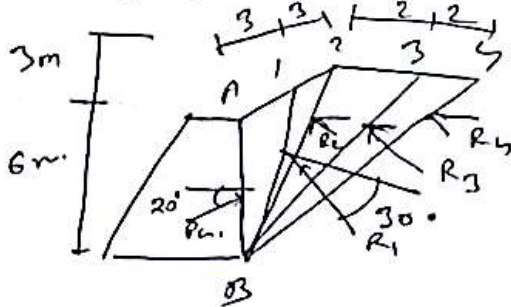
$$P_a = \frac{1}{2} K_a \gamma \cdot H^2$$

$$= \frac{1}{2} \times 0.548 \times 17.5 \times 5^2 = 119.9 \text{ kN}$$

This will act at a height of $5/3$ m from the base and inclined at 20° to normal in the direction shown.

10.8 Determine the active thrust on the retaining wall shown in Fig. The backfill is cohesionless

$$\phi = 30^\circ, \gamma = 19 \text{ kN/m}^3, \delta = 20^\circ$$



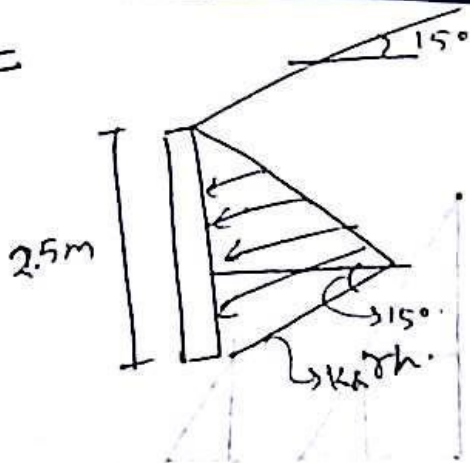
$$AB1 \quad W_1 = \frac{1}{2} (6 \times 3/2) \times 19 = 171 \text{ kN}$$

$$AB2 \quad W_2 = (6 \times 6/2) \times 19 = 342 \text{ kN}$$

$$AB3 \quad W_3 = \frac{1}{2} \times 2 \times 9 \times 19 + 342 = 513$$

$$AB4 \quad W_4 = \frac{1}{2} \times 2 \times 9 \times 19 + 513 = 684$$

A772 sheet



$$\begin{aligned} H &= 2.5 \text{ m} \\ \phi &= 35^\circ \\ \gamma &= 18 \text{ kN/m}^3 \\ OCR &= 2 \\ \beta &= 15^\circ \end{aligned}$$

Let the earth pressure is at rest

$$\begin{aligned} K_0 &= (1 - \sin \phi) OCR^{\sin \phi} \cdot (1 + 0.5 \tan^2 \beta) \\ &= (1 - \sin 35) 2^{\sin 35} (1 + 0.5 \tan^2 15) \\ &= 0.816 \end{aligned}$$

total force.

$$\begin{aligned} P_0 &= \frac{1}{2} \cdot K_0 \gamma h \cdot \cos \beta \cdot h \\ &= \frac{1}{2} \times 0.816 \times 18 \times 2.5 \times \cos 15 \times 2.5 \\ &= 44.34 \text{ kN/m} \end{aligned}$$

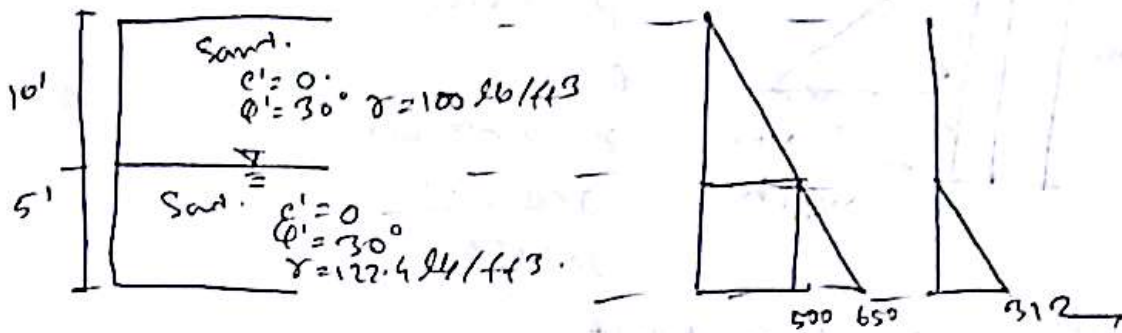
Horizontal thrust.

$$\begin{aligned} P_H &= P_0 \cos \beta \\ &= 44.34 \cos 15 \\ &= 42.83 \text{ kN/m} \end{aligned}$$

From Rankine's formula.

$$\begin{aligned} K_0 &= [0.19 + 0.233 \log I_p] \times \sqrt{OCR} \times (1 + \tan^2 \beta)^{0.5} \\ &= (1 - \sin \phi) \cdot 2^{\sin \phi} \cdot (1 + 0.5 \tan^2 \beta) \\ \Rightarrow [0.19 + 0.233 \log I_p] \sqrt{2} &= (1 - \sin 35) \times 2^{\sin 35} \\ \Rightarrow I_p &= 12.9 \end{aligned}$$

Example - 12.1 BSM DAS.



earth pressure is at rest

$$K_0 = \frac{1 - \sin 30}{1 + \sin 30} = 0.5$$

at $z = 10$: $\sigma_1' = K_0 \cdot \gamma h = \frac{1}{2} \times 100 \times 10 = 500$
 $u_1 = 0$

at $z = 15$: $\sigma_1' = 500 + \frac{1}{2} \times (122 - 62.4) \times 5$
 $= 650 \text{ lb/ft}^2$

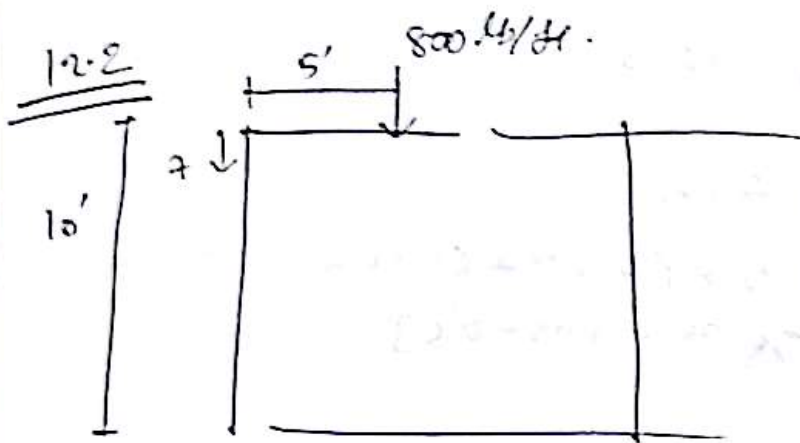
$u_2 = K_0 \cdot \gamma h \cdot 62.4 \times 5$
 $= 312$

total lateral force = $\frac{1}{2} \times 500 \times 10 + 5 \times 500 +$
 $\frac{1}{2} \times 150 \times 5 + \frac{1}{2} \times 5 \times 312$
 $= 6155$

location of \bar{x} from ground

$$= \frac{\frac{1}{2} \times 500 \times 10 \times (\frac{10}{3} + 5) + 5 \times 500 \times 2.5 + \frac{1}{2} \times 150 \times 5 \times \frac{5}{3} + \frac{1}{2} \times 5 \times 312 \times \frac{5}{3}}{6155}$$

$= 4.71 \text{ ft}$ (from the bottom).



for Line Load $m = \frac{x}{H} = \frac{5}{10} = 0.5$

$m = 0.5 > 0.4$

divide the height into 8 equal parts.

$z = 0, 1.25, 2.5, 3.75, 5, 6.25, 7.5, 8.75, 10$

$n = \frac{z}{H}$

for $n = \frac{0}{10} = 0$ $p_{h_0} = 0$

$n = \frac{1.25}{10} = 0.125$ $p_{h_1} = \frac{49 \cdot m \cdot n}{\pi H (m^2 + n^2)^2} = 45.11$

$Q = 500$
 $H = 10$
 $m = 0.5$
 $n = 0.125$

$n = \frac{2.5}{10} = 0.25$ $p_{h_2} = 65.2$

$n = \frac{3.75}{10} = 0.375$ $p_{h_3} = 62.58$

$n = \frac{5}{10} = 0.5$ $p_{h_4} = 50.93$

$n = \frac{6.25}{10} = 0.625$ $p_{h_5} = 38.28$

~~$n = \frac{7.5}{10} = 0.75$ p_{h_6}~~

$n = \frac{7.5}{10} = 0.75$ $p_{h_6} = 26.93$

$n = \frac{8.75}{10} = 0.875$ $p_{h_7} = 21.6$

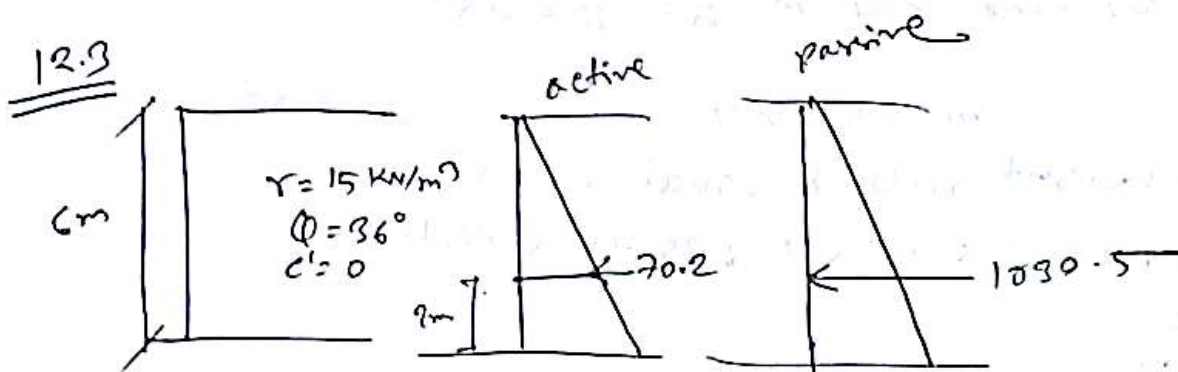
$$n = \frac{10}{10} = 1$$

$$Ph_g = 16.3$$

total increase in lateral force.

$$= \frac{1}{2} \times 1.25 \times [0 + 16.3 \times 2 \times (45.11 + 65.2 + 62.58 + 50.93 + 38.78 + 28.93 + 21.6)]$$

$$= 401.6 \text{ lb/ft}$$



(a) active force.

$$K_a = \frac{1 - \sin \phi}{1 + \sin \phi} = \frac{1 - \sin 36}{1 + \sin 36} = 0.26$$

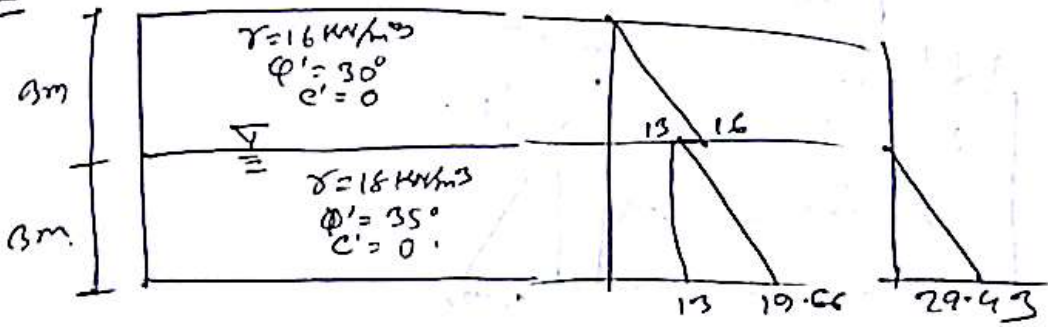
$$P_{ac} = \frac{1}{2} K_a \cdot \gamma \cdot h \cdot h = \frac{1}{2} \times 0.26 \times 15 \times 6^2 = 70.2 \text{ lb/ft}$$

(b) passive force

$$K_p = \frac{1 + \sin \phi}{1 - \sin \phi} = 3.85$$

$$P_{pc} = \frac{1}{2} \times 3.85 \times 15 \times 6^2 = 1039.5 \text{ lb/ft}$$

12.4



for upper layer.

$$K_a = \frac{1 - \sin \phi}{1 + \sin \phi} = \frac{1}{3}$$

$$\sigma = K_a \gamma h = \frac{1}{3} \times 16 \times 3 = 16$$

for bottom layer.

$$K_a = \frac{1 - \sin 35}{1 + \sin 35} = 0.271$$

at $z = 3$ $\sigma = K_a \gamma h = 0.271 \times 16 \times 3 = 13$

at $z = 6$ $\sigma = 13 + K_a \gamma' h = 13 + 0.271 \times (18 - 9.81) \times 3$

$$= 19.66$$

$$u = 9.81 \times 3 = 29.43$$

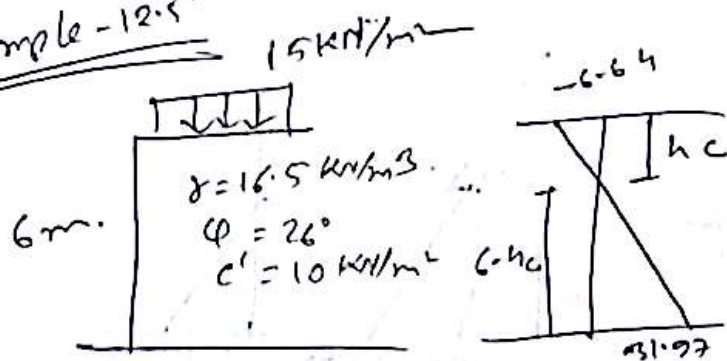
force per unit width = $\frac{1}{2} \times 16 \times 3 + 13 \times 3 + \frac{1}{2} \times (19.66 - 13) \times 3$
 $+ \frac{1}{2} \times 29.43 \times 3$

(= 117.14 kN)

$$\bar{z} = \frac{\frac{1}{2} \times 16 \times 3 \times (3+1) + (13 \times 3 \times 1.5) + \frac{1}{2} \times (19.66 - 13) \times 3 \times 1 + \frac{1}{2} \times 29.43 \times 3 \times 1}{117.14}$$

$$= 1.78 \text{ m}$$

Example - 12.5



$$K_a = \frac{1 - \sin 26}{1 + \sin 26} = 0.39$$

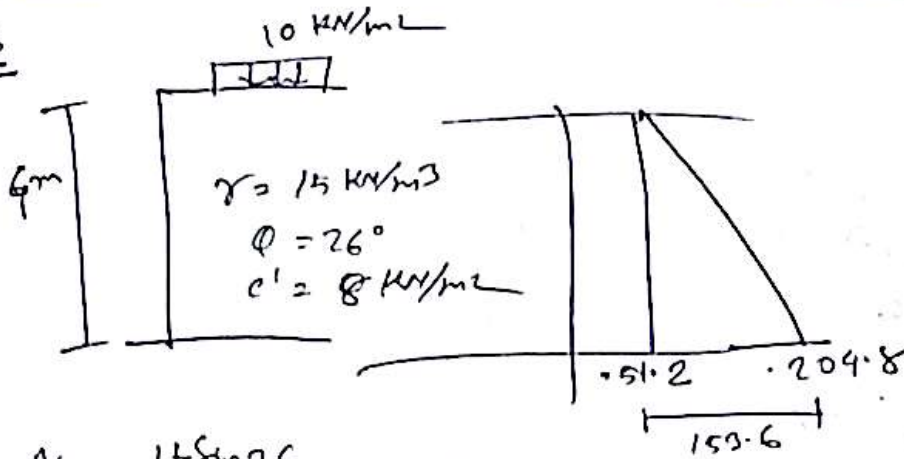
$$\begin{aligned} \text{at } z = 0: \quad \sigma_a' &= \gamma K_a - 2c\sqrt{K_a} \\ &= 15 \times 0.39 - 2 \times 10 \times \sqrt{0.39} \\ &= -6.64 \text{ kN/m}^2 \end{aligned}$$

$$\begin{aligned} \text{at } z = 6\text{m} \quad \sigma_a' &= \gamma K_a + K_a \gamma h - 2c\sqrt{K_a} \\ &= 15 \times 0.39 + 0.39 \times 16.5 \times 6 - 2 \times 10 \sqrt{0.39} \\ &= 31.97 \text{ kN/m}^2 \end{aligned}$$

$$\frac{31.97}{6 - h_c} = \frac{6.64}{h_c} \Rightarrow h_c = 1.03 \text{ m}$$

$$\begin{aligned} \text{Active force} &= \frac{1}{2} \times 31.97 \times (6 - 1.03) \\ &= 79.45 \text{ kN/m} \quad (\text{after crack}) \end{aligned}$$

12.6



$$K_p = \frac{1 + \sin 26}{1 - \sin 26} = 2.56$$

$$\begin{aligned} \text{at } z=0 \quad \sigma_p' &= qK_p + 2c\sqrt{K_p} \\ &= 10 \times 2.56 + 2 \times 8 \times \sqrt{2.56} \\ &= 51.2 \text{ kPa} \end{aligned}$$

$$\begin{aligned} z=6\text{m} \quad \sigma_p &= 51.2 + K_p \gamma h \\ &= 51.2 + 2.56 \times 15 \times 6 \\ &= 204.8 \text{ kPa} \end{aligned}$$

passive resistance per unit width.

$$\begin{aligned} P_p &= 51.2 \times 4 + \frac{1}{2} \times 159.6 \times 4 = 512 \text{ kN/m} \\ \bar{z} &= \frac{51.2 \times 4 \times 2 + \frac{1}{2} \times 159.6 \times 4 \times \frac{4}{3}}{512} \\ &= 1.6 \text{ m} \end{aligned}$$

Question:

- 2015-16 \rightarrow 4, 5
- 2014-15 \rightarrow 3, 5, 6, 7
- 2013-14 \rightarrow 2, 6, 7, 8 (90%)
- 2012-13 \rightarrow 5, 7, 6
- 2011-12 \rightarrow 3
- 2010-11 \rightarrow 1 (100%), 3, 4
- 2009-10 \rightarrow 2, 4
- 8-9 \rightarrow 1 (100%) \rightarrow shift (5), 4

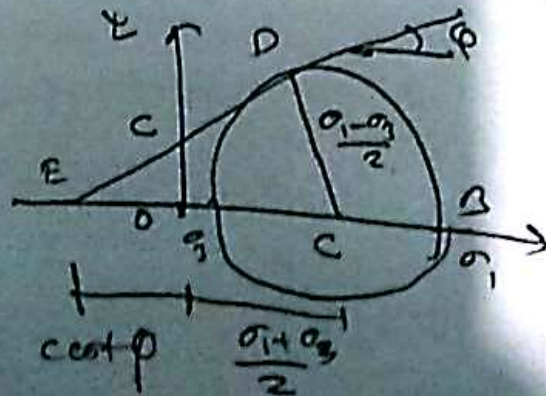
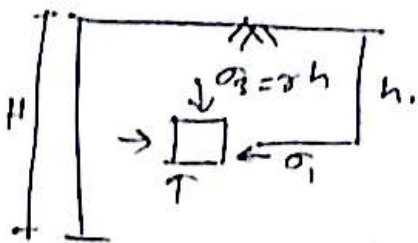
2013/14 (2) passive earth pressure in a c- ϕ

Soil: Let us assume a vertical and smooth retaining wall with a c- ϕ backfill having a horizontal surface for passive case. $\sigma_h > \sigma_v$.

At a given depth h on an element the vertical stress is $\sigma_v = \sigma_3 = \gamma h$.

Lateral stress is $\sigma_h = \sigma_1$

It is assumed that the wall has yielded sufficiently to satisfy passive earth condition such that $\sigma_1 = K_p \sigma_3$



From the Mohr circle.

$$\sin \phi = \frac{\frac{\sigma_1 - \sigma_3}{2}}{\frac{\sigma_1 + \sigma_3}{2} + c \cdot \cot \phi} = \frac{c \gamma}{c \gamma}$$

$$\Rightarrow \sin \phi = \frac{\sigma_1 - \sigma_3}{\sigma_1 + \sigma_3 + 2c \cot \phi}$$

$$\Rightarrow \sigma_1 (1 - \sin \phi) = \sigma_3 (1 + \sin \phi) + 2c \cot \phi$$

$$\Rightarrow \sigma_1 = \sigma_3 \cdot \left(\frac{1 + \sin \phi}{1 - \sin \phi} \right) + \frac{2c \cot \phi}{1 - \sin \phi}$$

$$\frac{\cot \phi}{1 - \sin \phi} = \frac{\sqrt{1 - \sin^2 \phi}}{\sqrt{(1 - \sin \phi)^2}} = \sqrt{\frac{(1 + \sin \phi)(1 - \sin \phi)}{(1 - \sin \phi)^2}} = \sqrt{\frac{1 + \sin \phi}{1 - \sin \phi}} = \sqrt{K_p}$$

$$\therefore \sigma_1 = \sigma_3 \cdot K_p + 2c \sqrt{K_p} = K_p \gamma h + 2c \sqrt{K_p}$$

$$\Rightarrow P_{ac} = K_p \gamma h + 2c \sqrt{K_p}$$

Depth of unsupported height = h_c .

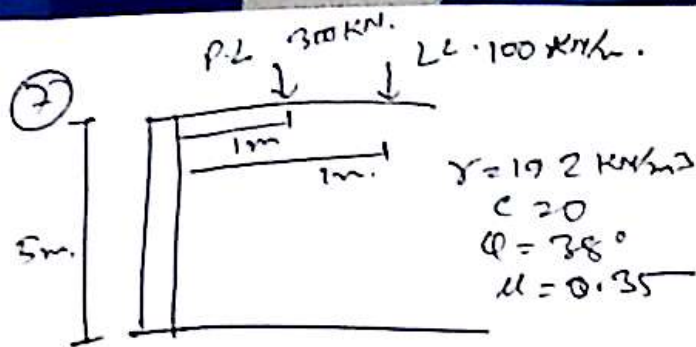
at h_c $P_{ac} = 0$.

$$0 = K_p \gamma h_c + 2c \sqrt{K_p}$$

$$\Rightarrow -h_c = \frac{2c}{\gamma \sqrt{K_p}} = \frac{2c}{\gamma \sqrt{\tan^2(45^\circ + \frac{\phi}{2})}}$$

$$\Rightarrow -h_c = \frac{2c}{\gamma \tan(45^\circ + \frac{\phi}{2})}$$

$$\text{Unsupported height } 2h_c = \frac{4c}{\gamma \tan(45^\circ + \frac{\phi}{2})}$$



$$m = \frac{x}{h} = \frac{1}{5} = 0.2 < 0.5$$

$$P_n = \frac{0.28 Q}{H^2} \frac{n^2}{(0.16 + n^2)^3}$$

0.28
 $= 1.77 \times 0.4$
 $= 0.28$

At a lateral distance of 1.5 m from wall

$$P'_n = P_n \cos^2(1.1\alpha)$$

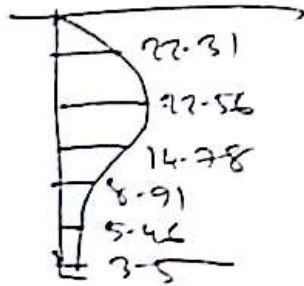
$\alpha = \tan^{-1}\left(\frac{1.5}{1}\right)$
 $= 56.31^\circ$

$$= \frac{0.28 Q}{H^2} \frac{n^2}{(0.16 + n^2)^3} \cos^2(1.1\alpha)$$

for line load. $m \leq 0.5$ $m = \frac{x}{h} = \frac{2}{5} = 0.4$

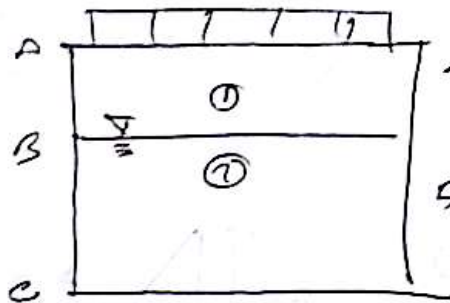
$$P_n = \frac{Q}{H} \cdot \frac{0.203 n}{(0.16 + n^2)^2} L$$

Depth \rightarrow	$n = \frac{z}{h}$	Line load. $\frac{Q}{H} \cdot \frac{0.203 n}{(0.16 + n^2)^2} L$	Point load. $\frac{0.28 Q}{H^2} \frac{n^2}{(0.16 + n^2)^3} \cos^2(1.1\alpha)$	total
0	0	0	0	0
0.833	0.167	3.12	19.19	22.31
1.667	0.333	4.15	18.41	22.56
2.5	0.5	2.70	12.28	14.98
3.333	0.667	1.5	7.91	9.41
4.167	0.833	0.833	4.63	5.46
5	1	0.48	3.02	3.5



50 KN/m

(4)



3m $\gamma_1 = 16 \text{ KN/m}^3$
 $\phi_1 = 30^\circ$ $q_0 = 50 \text{ KN/m}^2$

5m $\gamma_2 = 18 \text{ KN/m}^3$
 $\phi_2 = 33^\circ$

$c_1 = 10$
 $c_2 = 5$

For Soil 1

$$K_{a1} = \frac{1 - \sin \phi_1}{1 + \sin \phi_1} = \frac{1}{3}$$

At A, $P_{ac} = q_0 K_a + K_a \gamma_1 h - 2c_1 \sqrt{K_a}$

$$= 50 \times \frac{1}{3} + \frac{1}{3} \times 16 \times 0 - 2 \times 10 \times \sqrt{\frac{1}{3}}$$

$$= 5.12 \text{ KN/m}$$

for soil 2. $K_{a2} = \frac{1 - \sin \phi_2}{1 + \sin \phi_2} = 0.29$

At B for Soil 1.

$$P_{ac} = q_0 K_a + K_a \gamma_1 h_1 - 2c_1 \sqrt{K_a}$$

$$= 50 \times \frac{1}{3} + \frac{1}{3} \times 16 \times 3 - 2 \times 10 \sqrt{\frac{1}{3}}$$

$$= 21.1 \text{ KN/m}$$

at B, we have to consider both surcharge load and overlying soil 2.

$$\sigma_v = q_0 + \gamma_1 h_1 = 150 + 16 \times 3 = 98 \text{ kN/m}^2$$

$$\begin{aligned} p_{ac} &= K_{a2} \cdot \sigma_v - 2c_2 \sqrt{K_{a2}} \\ &= 0.29 \times 98 - 2 \times 5 \times \sqrt{0.29} \\ &= 23.03 \text{ kN/m} \end{aligned}$$

at c.

$$\begin{aligned} p_{ac} &= q_0 K_{a2} + K_{a2} \gamma_2 h_2 - 2c_2 \sqrt{K_{a2}} + \gamma_1 h_1 K_{a2} \\ &= 50 \times 0.29 + 0.29 \times (18 - 9.81) \times 5 \\ &\quad - 2 \times 5 \times \sqrt{0.29} + (10 \times 3) \times 0.29 \\ &= 34.91 \text{ kN/m} \end{aligned}$$

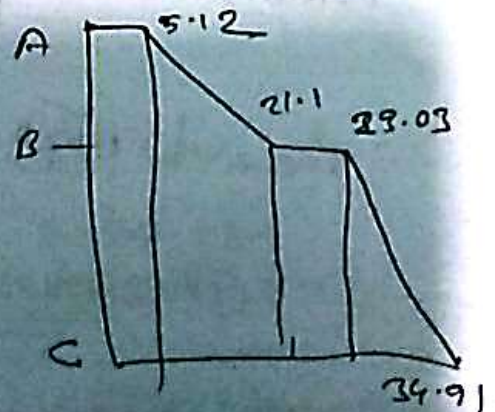
Neglecting water pressure.

Total thrust

$$\begin{aligned} &= (5.12 \times 8) + \frac{1}{2} \times (21.1 - 5.12) \times 5 \\ &\quad + (34.91 - 23.03) \times \frac{1}{2} \times 5 \\ &= 184.18 \text{ kN/m} \end{aligned}$$

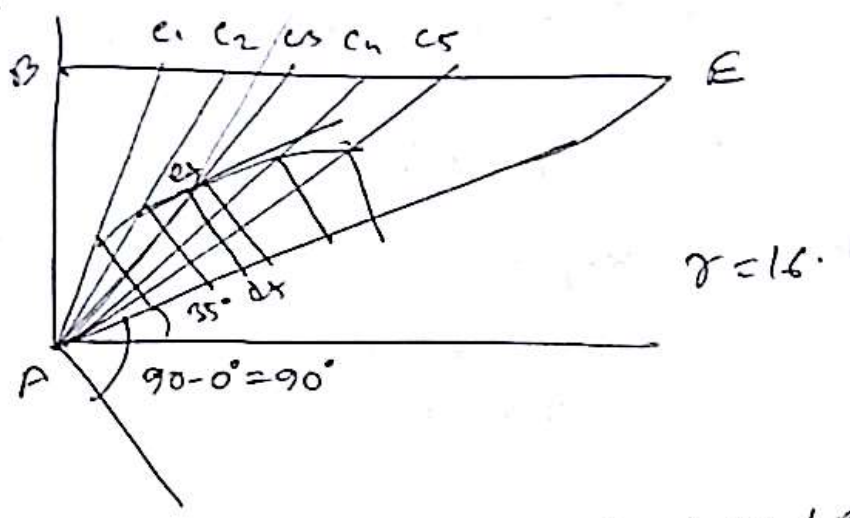
taking moment about c.

$$\begin{aligned} 184.18h &= 40.96 \times \left(\frac{8}{2}\right) + \\ &\quad 23.97 \times \left[5 + \frac{1}{3} \times 3\right] \\ &\quad + 89.55 \times \frac{5}{2} \\ &= 3.15 \text{ m} \cdot (\text{from base}) \end{aligned}$$



2012-13

⑥



⑥ weight of wedges = $\frac{1}{2} \times AB \times (BC_1 + BC_2 + BC_3 + \dots) \times \gamma$

$$W_{ABC_1} = \frac{1}{2} \times 10 \times 2 \times 16 = 160 \text{ kN}$$

$$W_{ABC_2} = \frac{1}{2} \times 10 \times 4 \times 16 = 320 \text{ kN}$$

$$W_{ABC_3} = \frac{1}{2} \times 10 \times 6 \times 16 = 480 \text{ kN}$$

$$W_{ABC_4} = \frac{1}{2} \times 10 \times 8 \times 16 = 640 \text{ kN}$$

$$W_{ABC_5} = \frac{1}{2} \times 10 \times 10 \times 16 = 800 \text{ kN}$$

800 kN = 12 cm. 1 kN = 0.015 cm.

$$e \text{ of } dx = 3.5 \text{ cm} = \frac{800}{12} \times 3.5 = 233.33 \text{ kN/m}$$

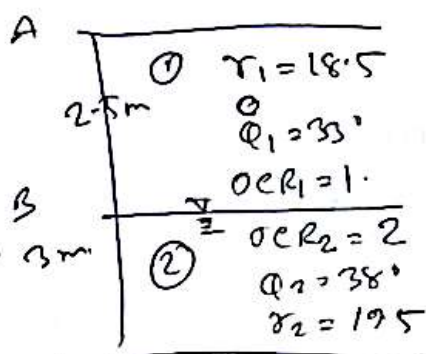
Rankine formula.

$$K_a = \frac{1 - \sin \phi}{1 + \sin \phi} = 0.22$$

$$P_{ac} = \frac{1}{2} \gamma H K_a = \frac{1}{2} \times 16 \times 10 \times 0.22 = 216 \text{ kN/m}$$

② Basic consideration.

Rankin considered the equilibrium of a soil element for Coulomb's theory → Coulomb considered the equilibrium of a soil wedge during failure in a soil mass.



For Soil 1.

$$K_0(1) = (1 - \sin \phi_1) \cdot OCR_1^{\sin \phi_1}$$

$$= (1 - \sin 33) \cdot 1^{\sin 33}$$

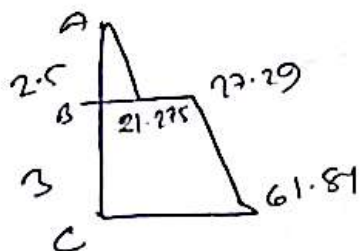
$$= 0.46$$

At B, for Soil 1.

$$P_0 = K_0 \cdot \gamma_1 H_1$$

$$= 0.46 \times 18.5 \times 2.5$$

$$= 21.275 \text{ kN/m}^2$$



at B for Soil 2

$$K_0(2) = (1 - \sin \phi_2) \cdot OCR_2^{\sin \phi_2}$$

$$= (1 - \sin 38) \cdot 2^{\sin 38}$$

$$= 0.59$$

$$\sigma_v = \gamma_1 H_1 = 18 \times 2.5 = 46.25$$

$$\sigma_h = K_0 \cdot \sigma_v = (0.59 \times 46.25)$$

$$= 27.29 \text{ kN/m}^2$$

at C.

$$P_0 = 27.29 + K_0 \cdot \gamma_2 H_2$$

$$= 27.29 + 0.59 \times 19.5 \times 3 = 61.81 \text{ kN/m}^2$$

$$\text{Total lateral thrust} = \left[\frac{1}{2} \times 2.5 \times 21.275 + 3 \times 27.29 + \frac{1}{2} \times (61.81 - 27.29) \times 3 \right]$$

$$= 160.24 \text{ kN/m}$$

Water pressure not?

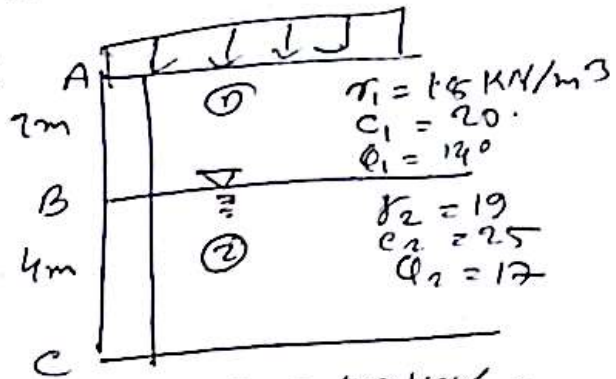
→ maybe procedure of soil mass.

passive pressure.

q_0

(8)

$$P_{pc} = K_p \gamma h + 2c \sqrt{K_p}$$



At A.

$$P_{pc} =$$

for soil 1.

$$K_p(1) = \frac{1 + \sin 14}{1 - \sin 14}$$

$$= 1.64$$

$$\text{at A } P_{pc} = q_0 K_p(1) + 2c_1 \sqrt{K_p(1)}$$

$$= 50 \times 1.64 + 2 \times 20 \times \sqrt{1.64}$$

$$= 133.22 \text{ kN/m}^2$$

at B for soil 1.

$$P_{pc}(B) = 133.22 + K_p(1) \gamma_1 H_1$$

$$= 133.22 + 1.64 \times 18 \times 2$$

$$= 192.26 \text{ kN/m}^2$$

at B for soil 2

$$K_p(2) = \frac{1 + \sin 17}{1 - \sin 17}$$

$$= 1.83$$

$$\sigma_v(B) = q_0 + \gamma_1 h_1$$

$$= 50 + 18 \times 2 = 86 \text{ kN/m}^2$$

$$P_{pc}(B) = K_p(2) \cdot \sigma_v(B) + 2c_2 \sqrt{K_p(2)}$$

$$= 1.83 \times 86 + 2 \times 25 \times \sqrt{1.83}$$

$$= 225.6$$

at C for soil 2

$$P_{pc}(C) = 225.6 + K_p(2) \gamma_2' H_2$$

$$= 225.6 + 1.83 \times (19 - 9.81) \times 4$$

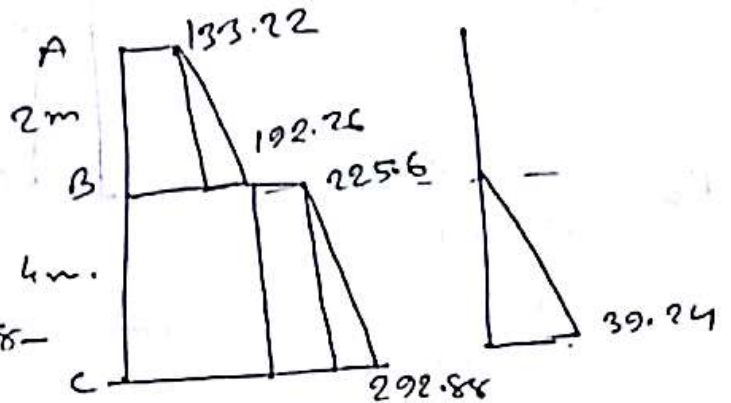
$$= 292.88 \text{ kN/m}^2$$

water pressure at c.

$$P_w = \gamma_w h_2 = 9.81 \times 4 \\ = 39.24 \text{ kN/m}$$

Total thrust

$$= 133.22 \times 2 + \\ \frac{1}{2} \times 2 \times (192.26 - 133.22) \\ + 225.6 \times 4 + \frac{1}{2} \times 4 \times (292.84 - \\ 225.6) \\ + \frac{1}{2} \times 4 \times 39.24 \\ = 1440.92 \text{ kN/m}$$

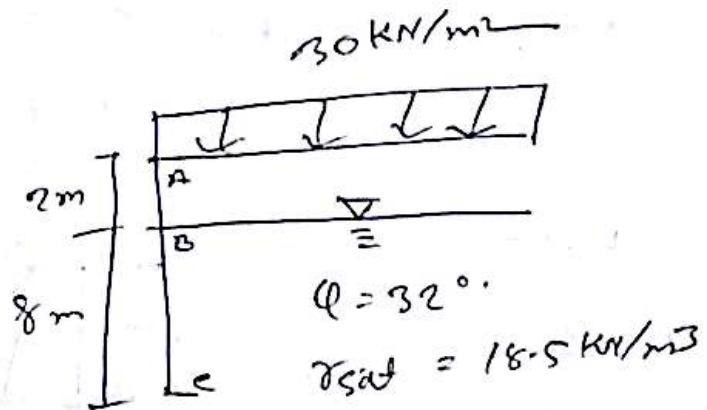


taking moment about C.

$$1440.92 \times h = 266.44 \times (4+1) + 59.04 \times (2 + \frac{2}{3}) + \\ 902.4 \times \frac{4}{2} + 134.56 \times \frac{4}{3} + 78.48 \times \frac{4}{3}$$

$$\Rightarrow h = 2.57 \text{ m from base.}$$

2011-12
3 (b)



$$K_a = \frac{1 - \sin \phi}{1 + \sin \phi}$$

$$= \frac{1 - \sin 32}{1 + \sin 32} = 0.307$$

at A. $\sigma_v = 30 \text{ kN/m}^2$

$$P_{ac}(A) = K_a \cdot \sigma_v = 0.307 \times 30 = 9.21 \text{ kN/m}^2$$

at B.

$$P_{ac}(B) = 9.21 + K_a \cdot \gamma_{sat} \cdot h_1$$

$$= 9.21 + 0.307 \times 18.5 \times 2$$

$$= 20.57$$

at C pressure by soil

$$P_{ac}(C) = 20.57 + K_a (\gamma_{sat} - \gamma_w) \times h_2$$

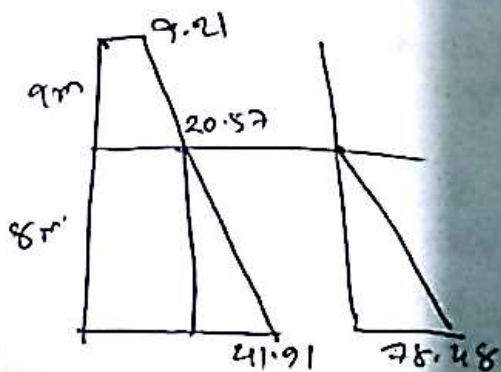
$$= 20.57 + 0.307 \times (18.5 - 9.81) \times 8$$

$$= 41.91 \text{ kN/m}^2$$

at C pressure by water

$$P_w(C) = \gamma_w h_2$$

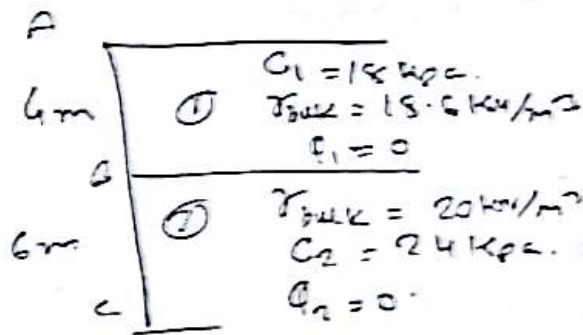
$$= 9.81 \times 8 = 78.48 \text{ kN/m}^2$$



Lateral thrust

$$\begin{aligned}
 &= (9.21 \times 2) + \frac{1}{2} \times 2 \times (20.52 - 9.21) + 20.52 \times 8 \\
 &\quad + \frac{1}{2} \times 8 \times (41.91 - 20.52) + \frac{1}{2} \times 8 \times 78.45 \\
 &= 18.42 + 11.36 + 164.16 + 55.52 + 512.92 \\
 &= 593.62 \text{ kN/m}
 \end{aligned}$$

2010-11



layer 1 and layer 2

$$K_a = \frac{1 - \sin \phi}{1 + \sin \phi} = 0.1$$

depth of tension zone to $Q = 0$.

$$h_c = \frac{2c}{\gamma} (\tan 45^\circ + \phi/2) = \frac{2 \times 18}{18.6} = 1.94 \text{ m}$$

at A.

$$\begin{aligned}
 p_{ac}(A) &= K_a \gamma h_1 - 2c \sqrt{K_a} \\
 &= 0 - 2 \times 18 \times \sqrt{0.1} \\
 &= -36
 \end{aligned}$$

at B for layer ①

$$P_{ac}(B) = K_a \gamma_1 h_1 - 2c \sqrt{K_a}$$
$$= 1 \times 18.6 \times 4 - 2 \times 18 \sqrt{1} = 38.4$$

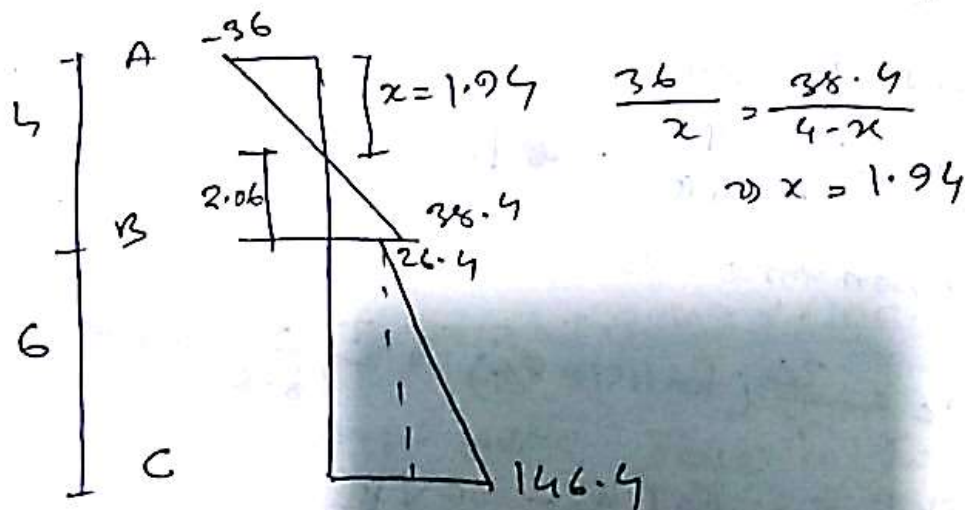
at B for layer 2

$$\sigma_v = \gamma_1 h_1 = 18 \times 6 = 72.4 \text{ kN/m}$$

$$P_{ac}(B) = K_a \sigma_v - 2c \sqrt{K_a}$$
$$= 1 \times 72.4 - 2 \times 24 \sqrt{1} = 26.4$$

at C for layer 2

$$P_{ac}(C) = 26.4 + K_a \gamma_2 h_2$$
$$= 26.4 + 20 \times 6 \times 1 = 146.4$$



Total thrust

$$\begin{aligned} &= \left(\frac{1}{2} \times 2.06 \times 38.4\right) + (26.4 \times 6) + \left(\frac{1}{2} \times 6 \times (146.4 - 26.4)\right) \\ &= 39.55 + 158.4 + 360 \\ &= 557.95 \end{aligned}$$

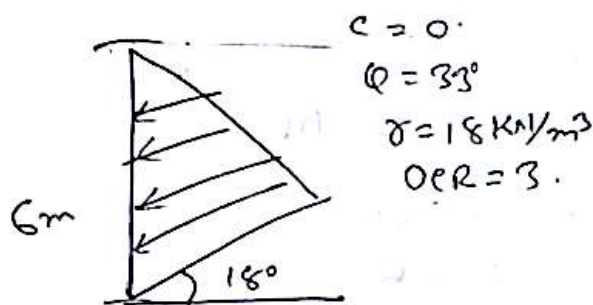
Taking moment about C

$$557.95 \times h = 39.55 \times \left(6 + \frac{2.06}{3}\right) + 158.4 \times \frac{6}{2} + 360 \times \frac{6}{3}$$

$$\Rightarrow h = 2.62$$

↳ from base.

3 b



① Earth pressure at rest

$$K_0 = (1 - \sin \phi) \cdot OCR^{\sin \phi} = (1 - \sin 33) \times 3^{\sin 33} = 0.83$$

Lateral pressure

$$= K_0 (1 + 0.5 \tan^2 \phi)^2 \gamma h$$

$$= 0.83 (1 + 0.5 \tan^2 18) \times 18 \times 6 \cos 18$$

$$= 115.2 \text{ kN/m}^2$$

$$\text{Lateral thrust} = \frac{1}{2} \times 6 \times 121.13 \times (\cos 18)^\perp \\ = 328.69$$

(ii) Soil moving outward and downward direction

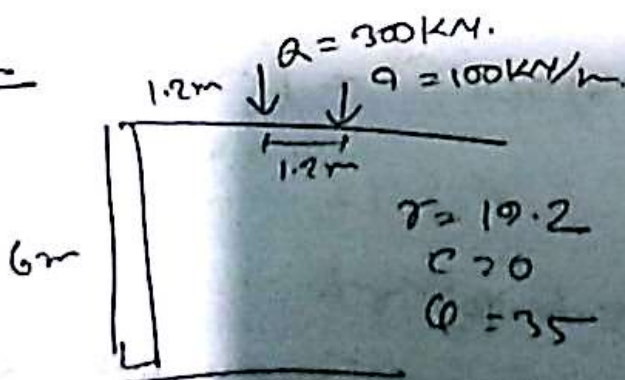
$$K_a = \frac{\cos \beta - \sqrt{\cos^2 \beta - \cos^2 \phi}}{\cos \beta + \sqrt{\cos^2 \beta - \cos^2 \phi}} \\ = \frac{\cos 18 - \sqrt{\cos^2 18 - \cos^2 33}}{\cos 18 + \sqrt{\cos^2 18 - \cos^2 33}} = 0.36$$

$$\text{Lateral pressure} = K_a \gamma h \cos \beta \\ = 0.36 \times 18 \times 6 \times \cos 18 = 37$$

$$\text{Lateral thrust} = \frac{1}{2} K_a \gamma h^2 \cos \beta \\ = \frac{1}{2} \times 37 \times 6 = 111$$

$$\text{Horizontal thrust} = 111 \cos 18 \\ = 105.6$$

4(a)



For point load

$$m = \frac{z}{H} = \frac{1.2}{6} = 0.2 \leq 0.4$$

$$P_n = \frac{1.27R}{H^2} \times \frac{0.4^2 n^2}{(0.16 + m^2)^3}$$

$$= \frac{0.28R \text{ n}^2}{H^2 (0.16 + m^2)^3}$$

For line load:

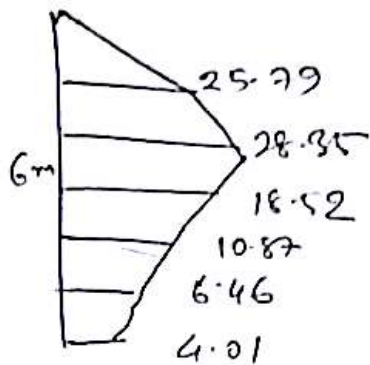
$$m = \frac{z}{H} = \frac{2.4}{6} = 0.4 \leq 0.4$$

$$P_n = \frac{4q}{\pi H} \cdot \frac{2.4 \cdot 0.4^2 n}{(0.16 + m^2)^2}$$

$$= \frac{q}{H} \cdot \frac{0.208n}{(0.16 + m^2)^2}$$

$$R = 300 \text{ kN} \quad q = 100 \text{ kN/m}$$

depth z	$m = \frac{z}{H}$	$P_n = \frac{0.28R}{H^2} \frac{n^2}{(0.16+m^2)^3}$	$P_n = \frac{q}{H} \frac{0.208n}{(0.16+m^2)^2}$	total
0	0	0	0	0
1	1/6	9.79	16.00	25.79
2	2/3	13.01	15.34	28.35
3	1/2	8.46	10.06	18.52
4	2/3	4.70	6.17	10.87
5	5/6	2.60	3.86	6.46
6	1	1.50	2.51	4.01



2009-10

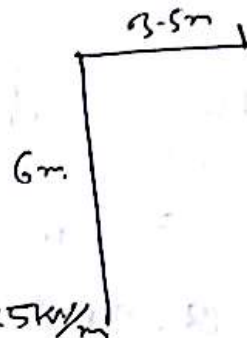
2⑥

$$m = \frac{x}{H} = \frac{3.5}{6}$$

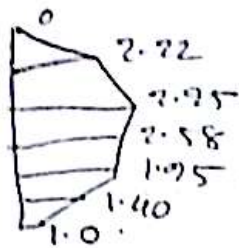
$$= 0.5833 > 0.4$$

$$P_h = \frac{1.279}{H} \cdot \frac{m^2 n}{(m^2 + n)^2}$$

$$q = 25 \text{ kN/m}$$



depth.	$n = y/H$	$P_h = \frac{1.27 \times 25}{6} \times \frac{(0.5833)^2 \times n}{((0.5833)^2 + n)^2}$
0	0	0
1	1/6	2.22
2	1/3	2.95
3	1/2	2.58
4	2/3	1.95
5	5/6	1.40
6	1	1.00



total thrust

$$= \frac{1}{2} \times 1 \times [0 + 1 + 2 \times (2.92 + 2.95 + 2.58 + 1.95 + 1.40)]$$

$$= 11.6 \text{ kN/m}$$

3(A)

Before increasing the height

$$P_h = \frac{1}{2} K_a \gamma h^2$$

$$\Rightarrow 25 = \frac{1}{2} K_a \times 16.2 \times 6.3^2$$

$$\Rightarrow K_a = 0.233$$

A

x

$$\sigma_1 = 8.2 \text{ kN/m}^3$$

$$\phi = 38.5^\circ$$

2.8m

$$\sigma_1 = 8.2 \text{ kN/m}^3$$

$$\phi = 38.5^\circ$$

B

3.5m

$$\sigma_2 = 16.2$$

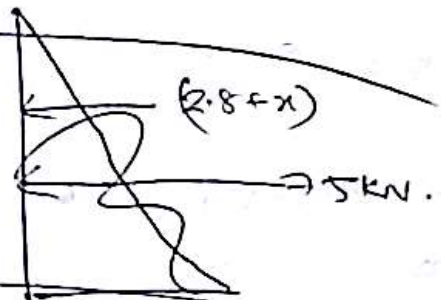
$$\phi = 38.5^\circ$$

C

$$\tan(45^\circ - \phi/2) = 0.233$$

after adding sand

$$\frac{1}{2} K_a \gamma$$



$$\tan(45^\circ - \phi/2) = 0.233$$

$$\Rightarrow \phi = 38.5^\circ$$

Let x height added.

at B. $P_{ac(B)} = K_a \sigma_1 h_1$

$$= 0.233 \times 8.2 \times (2.8 + x)$$

at B layer 2 $\sigma_v = \sigma_1 h_1 = 8.2 \times (2.8 + x)$

$$P_{ac}(B) = \gamma_1 h_1 =$$

$$P_{ac}(B) = K_a \cdot \sigma_v$$

$$= 0.233 \times 8.2 \times (2.8 + x)$$

at c.

$$P_{ac}(C) = 0.233 \times 8.2 \times (2.8 + x) + K_a \gamma_2 h_2$$

$$= 0.233 \times 8.2 \times (2.8 + x) + 0.233 \times 16.2 \times 3.5$$

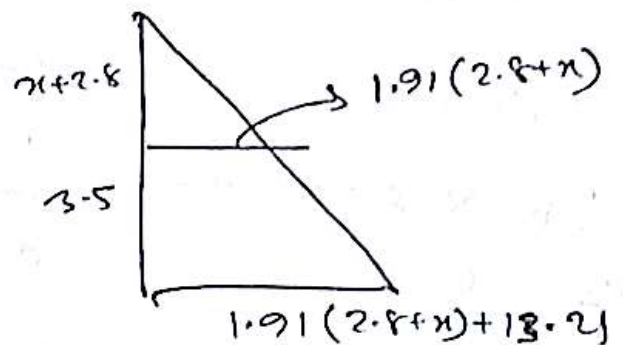
$$= 1.91(2.8 + x) + 13.02$$

total thrust

$$= \frac{1}{2} \times (2.8 + x) \times 1.91(2.8 + x)$$

$$+ 1.91(2.8) \times 3.5$$

$$+ \frac{1}{2} \times 3.5 \times 13.02$$



$$\Rightarrow 75 = 0.955(x+2.8)^2 + 6.685(x+2.8) + 23.12$$

$$\Rightarrow 0.955x^2 + 6.845x - 51.8520$$

$$\Rightarrow x = 4.66 \text{ or } -11.6$$

$$x + 2.8 = 4.66$$

$$x + 2.8 = -11.6$$

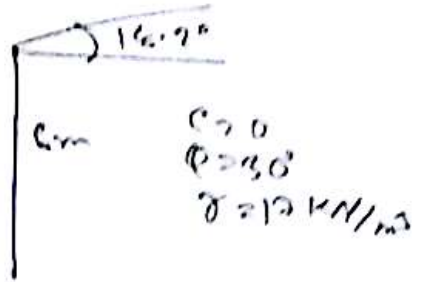
$$\Rightarrow x = -14.46$$

$$\Rightarrow x = 1.86$$

$$\boxed{x = 1.86}$$

Q10

For active pressure



$$K_a = \frac{\cos \beta - \sqrt{\cos^2 \beta - \cos^2 \phi}}{\cos \beta + \sqrt{\cos^2 \beta - \cos^2 \phi}}$$

$$= \frac{\cos 18.2^\circ - \sqrt{\cos^2 18.2^\circ - \cos^2 30^\circ}}{\cos 18.2^\circ + \sqrt{\cos^2 18.2^\circ - \cos^2 30^\circ}} = 0.477$$

horizontal

$$\text{Active thrust} = \frac{1}{2} K_a \cdot \gamma H^2 \cos \beta \times \cos \beta$$

$$= \frac{1}{2} \times 0.477 \times 17 \times 6^2 \times \cos(18.2^\circ) \times \cos(18.2^\circ)$$

$$= 121.2 \times \cos(18.2^\circ) = 115.13$$

For passive pressure

$$K_p = \frac{1 + \sin \phi}{1 - \sin \phi} = \frac{1 + \sin 30^\circ}{1 - \sin 30^\circ} = 3$$

$$\text{Passive thrust} = \frac{1}{2} \times K_p \cdot \gamma H^2$$

$$= \frac{1}{2} \times 3 \times 17 \times D^2$$

$$\therefore 25.5 D^2 = 115.13$$

$$\Rightarrow D = 2.13 \text{ m}$$

2008-09

Q ①

For loose state.

$$e_1 = 0.5$$

$$\gamma_{d1} = 17.8 \text{ kN/m}^3$$

$$\phi = 30^\circ$$

$$K_p = \frac{1 + \sin 30^\circ}{1 - \sin 30^\circ} = 3$$

$$\begin{aligned} \text{passive thrust} &= \frac{1}{2} K_p \gamma_d H^2 \\ &= \frac{1}{2} \times 3 \times 17.8 \times 8^2 \\ &= 1708.8 \text{ kN/m} \end{aligned}$$

For dense state. $\gamma_d = 18.8 \text{ kN/m}^3$

$$\phi = 35^\circ$$

$$K_p = \frac{1 + \sin 35^\circ}{1 - \sin 35^\circ} = 3.69$$

$$\begin{aligned} \text{passive thrust} &= \frac{1}{2} K_p \gamma_d H^2 \\ &= \frac{1}{2} \times 3.69 \times 18.8 \times 8^2 \\ &= 2219.9 \end{aligned}$$

$$\text{Ratio} = \frac{1708.8}{2219.9} = 0.77:1$$

According to Aritz

$$\frac{v_2}{v_1} = \frac{1 + e_2}{1 + e_1} \Rightarrow \frac{H_2 \times A}{H_1 \times A} = \frac{1 + 0.9}{1 + 0.5}$$

$$\Rightarrow H_2 = 7.42 \text{ m}$$

$$P_2 = \frac{1}{2} \times 3.69 \times 18.8 \times 7.42^2 = 1940.72$$

1 (a)

$\gamma = 22 \text{ kN/m}^3$

Unrestrained height = 4 m.

$$H_u = \frac{4e}{10} \gamma_{\text{dom}} \left(4.5 + \frac{e}{2} \right)$$

$$\Rightarrow 4 = \frac{4e}{22} \Rightarrow e = 22 \text{ kN/m}^3$$

1 (b)

$$I_p = LL - PL = 40 - 25 = 15 \text{ t}$$

$$OCR = 2.5$$

$$K_o(\text{net}) = K_o(\text{gross}) \cdot 0.19 + 0.233 \log(I_p) \\ = 0.19 + 0.233 \log(15) = 0.46$$

$$K_o(\text{acc}) = K_o(\text{net}) \times \sqrt{OCR} = 0.46 \sqrt{2.5} \\ = 0.73$$

$$\text{Thrust} = \frac{1}{2} K_o \gamma H^2 = \frac{1}{2} \times 0.734 \times 8 \times 6^2 \\ = 13.2128$$

2 (a) γ_{net}

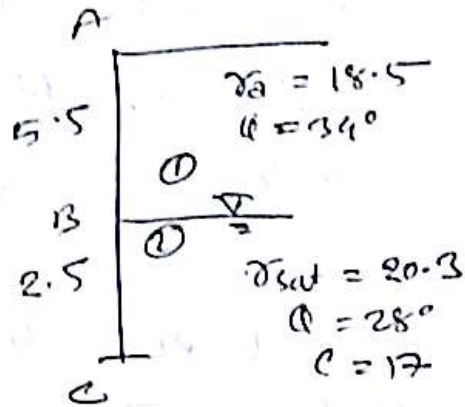
4 (a)

For layer ①

$$K_{a(1)} = \frac{1 - \sin 34^\circ}{1 + \sin 34^\circ} \\ = 0.28$$

For layer 2

$$K_{a2} = \frac{1 - \sin 28^\circ}{1 + \sin 28^\circ} \\ = 0.36$$



at B for layer 1.

$$P_{ac}(B) = K_{a(1)} \gamma_1 h_1 \\ = 0.28 \times 18.5 \times 5.5 = 28.5$$

at B for layer 2

$$\sigma_v = \gamma_1 h_1 = 18.5 \times 5.5 = 101.75$$

$$P_{ac}(B) = K_{a(2)} \cdot \sigma_v - 2c \sqrt{K_{a(2)}} \\ = 0.36 \times 101.75 - 2 \times 17 \times \sqrt{0.36} \\ = 16.23 \text{ kN/m}$$

At C.

$$P_{ac}(C) = 16.23 + K_{a(2)} (\gamma_{sat} - \gamma_w) h_2 \\ = 16.23 + 0.36 \times (20.3 - 9.81) \times 2.5 \\ = 25.67$$

$$\text{Water pressure } P_w = \gamma_w h_2 \\ = 9.81 \times 2.5 \\ = 24.5$$

Total thrust

$$= \left(\frac{1}{2} \times 5.5 \times 28.5 \right) + (7.75 \times 16.23) + \frac{1}{2} \times 2.5 (25.67 - 16.23) + \frac{1}{2} (2.5 \times 24.5)$$

$$= 161.4$$

