

16-12

F → flex
M → mem
S →

T → theory

N → not mention

- 1 (a) → theory
- (b) → flexi
- 2 (a) → T
- (b) → F/N
- 3 (a) → F/N
- (b) → F
- 4 (a) → S
- 5 (a) → M
- (b) → M
- 6 (a) → M
- (b) → M
- 7 (a) → M
- (b) → S
- 8 (a) → S
- (b) → S

15-16

- 1 (a) → M
- (b) → M
- 2 (a) S
- (b) S
- 3 (a) S
- (b) M
- 4 (a) M
- (b) S
- 5 (a) F
- (b) F
- 6 (a) F
- (b) F
- 7 (a) F
- (b) S
- 8 (a) N
- (b) S

14-15

- 1 (a) F
- (b) F
- 2 (a) F
- (b) F
- 3 (a) S
- (b) S
- 4 (a) S
- (b) → T
- 5 (a) T
- (b) M
- 6 (a) M
- (b) M
- 7 (a) S
- (b) F
- 8 (a) S
- (b) S

15-14

- 1 (a) M
- (b) F
- 2 → F
- 3 → M
- 4 → F
- 5 → M
- 6 → F
- 7 → M
- 8 → S
- 9 → S
- 10 → S
- 11 → S
- 12 → S
- 13 → S
- 14 → F

12-13

- 1 (a) M
- (b) S
- 2 (a) M
- (b) S
- 3 (a) S
- (b) S
- 4 (a) S
- (b) F
- 5 (a) F
- (b) F/T
- 6 (a) F
- (b) F
- 7 (a) F
- (b) F
- 8 (a) F
- (b) F

11-12

- 1 (a) F
- (b) S
- 2 (a) F
- (b) S
- 3 (a) N
- (b) S
- 4 → S
- 5 (a) M
- (b) F
- 6 (a) Scope
- (b) M
- 7 (a) M
- (b) Scope

S → 4
F → 4
M → 5

S → 5
F → 5
M → 4

S → 6
F → 5
M → 3

S → 6
F → 4
M → 4

S → 4
F → 6
M → 2

S → 4
F → 3
M → 3

13-14

11 12
10 11
8 9

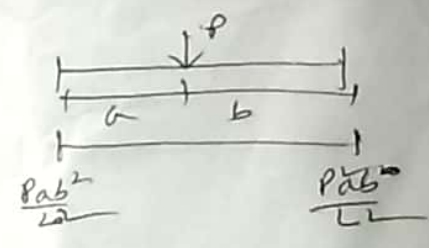
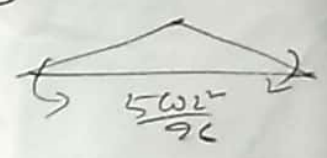
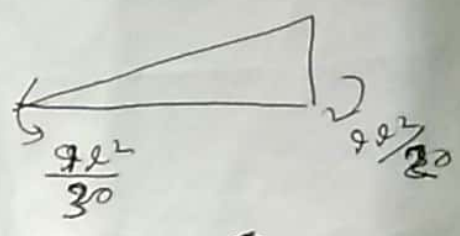
Nothing is certain.

10-11

- 1 (A) IF
- 1 (B) M
- 2 (A) S
- 1 (B) M
- 3 (A) M
- 1 (B) IF
- 4 (A) M
- 1 (B) T
- 5 (A) P
- 1 (B) S
- 6 (A) S
- 1 (B) S
- 7 (A) S
- 1 (B) S
- 8 (A) S

9-10

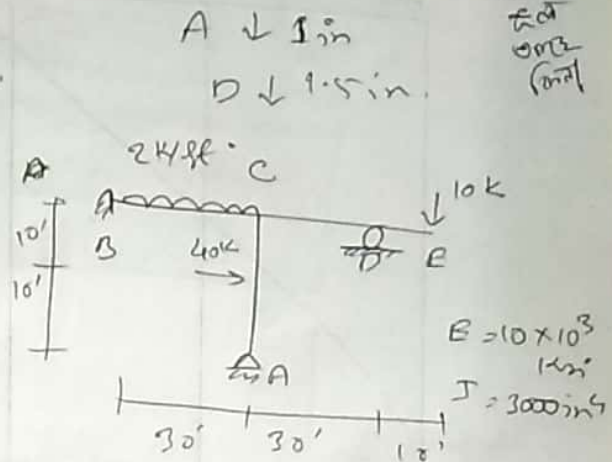
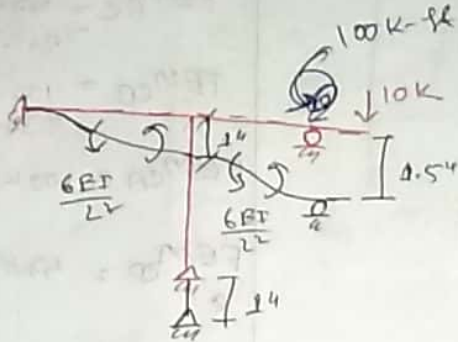
- 1 (A) F/S
- 1 (B) IF
- 2 (A) M
- 1 (B) M
- 3 (A) S
- 1 (B) M
- 4 (A) IF
- 1 (B) M
- 5 (A) S
- 1 (B) S
- 6 (A) S
- 1 (B) F
- 7 (A) S
- 1 (B) S
- 8 (A) S
- 1 (B) F



2/16/17

Frame
 GP solve
 1. 5.5
 2. 10
 3. 15
 4. 20
 5. 25
 6. 30
 7. 35
 8. 40
 9. 45
 10. 50
 11. 55
 12. 60
 13. 65
 14. 70
 15. 75
 16. 80
 17. 85
 18. 90
 19. 95
 20. 100

G (a)



$DF_{BC} = 0$

$DF_{CB} = \frac{I/30}{I/30 + I/30 \times \frac{2}{4} + I/20 \times \frac{3}{4}} = 0.35$

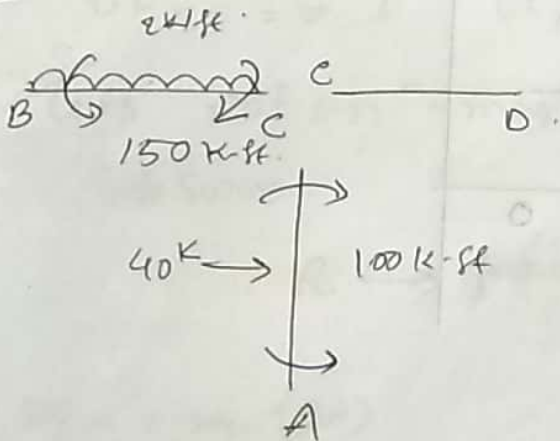
$DF_{CD} = \frac{I/30 \times \frac{3}{4}}{I/30 + I/30 \times \frac{3}{4} + I/20 \times \frac{3}{4}} = 0.26$

$DF_{CA} = 1 - 0.35 - 0.26 = 0.39$

$DF_{AC} = 1$

$DF_{DC} = 1$

FEM



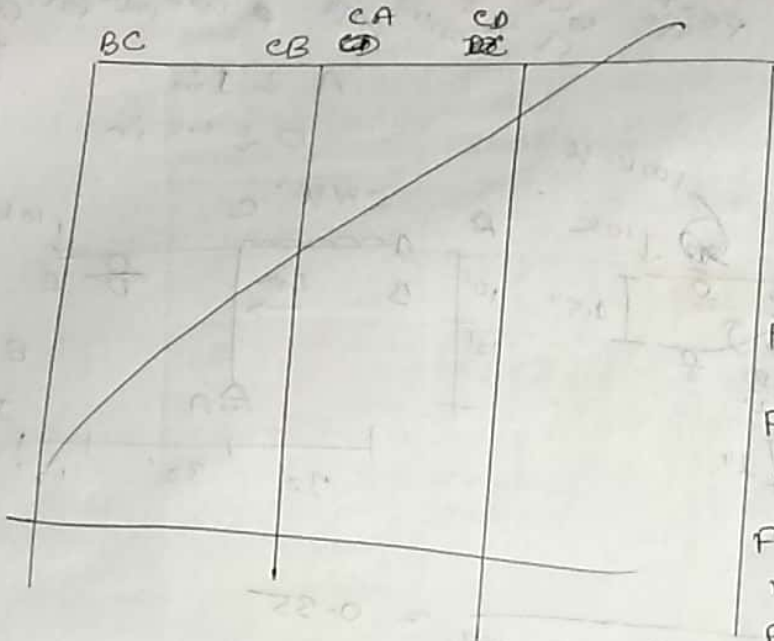
Settlement

$FEM_{BC} = FEM_{CB}$

$= \frac{6EI}{L^2} \Delta$
 $= \frac{6 \times 10000 \times 3000 \times 1}{30^2 \times 12^3}$
 $= 115.74 \text{ k-ft}$

$FEM_{CD} = FEM_{DC} = \frac{6EI}{L^2} \Delta$

$\Delta = 1.5 \text{ in}$
 $= 0.5''$
 $= \frac{6 \times 10000 \times 3000}{30^2 \times 12^3} \times 0.5$
 $= 57.87 \text{ k-ft}$



$$FEM_{BC} = 150 + 115.74 = 265.74 (\odot)$$

$$FEM_{CB} = 150 - 115.74 = 34.26 (\ominus)$$

$$FEM_{CA} = 100k (\ominus)$$

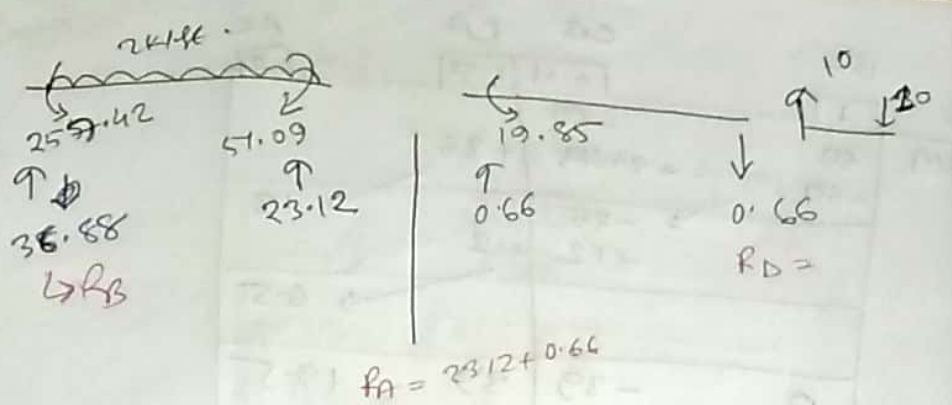
$$FEM_{CD} = 57.87 (\ominus)$$

$$FEM_{DC} = 57.87 (\ominus)$$

$$FEM_{AC} = 100k (\ominus)$$

-100 hoibe

DF	BC	CB	CA	CD	DC	AC
0	0.35	0.35	0.26	1	1	1
FEM	265.74	-34.26	100	57.87	57.87	100
		-43.26	-48.21	-32.14	-57.87	-100
	-21.63		-50	-28.94	-16.07	
		27.63	30.79	20.52	+16.07	
	1382			8.04	10.26	
		-2.81	-3.14	-2.09	-10.26	
	-1.41			-5.18	-1.045	
		+1.8	2	1.33	+1.045	
	0.9			0.53		
		-0.19	-0.24	-0.14		
	257.92	-51.09	312.3	19.85	0	0



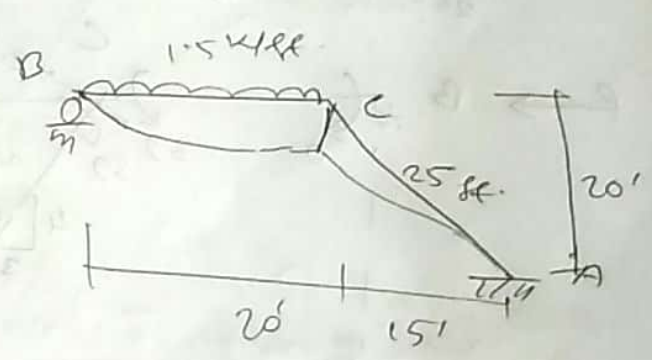
2016-17
7(a)
 Not sure

$$DF_{CB} = \frac{\frac{1}{20} \times \frac{3}{4}}{\frac{3}{4} \times \frac{1}{20} + \frac{1}{25}}$$

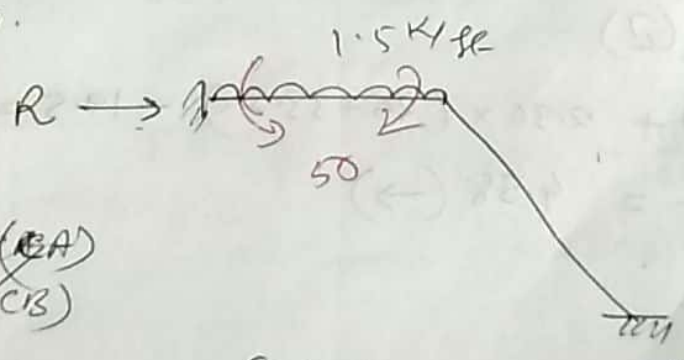
$$= 0.48$$

$$DF_{CA} = 1 - 0.48 = 0.52$$

$$DF_{BC} = 0 \quad DF_{AC} = 0$$



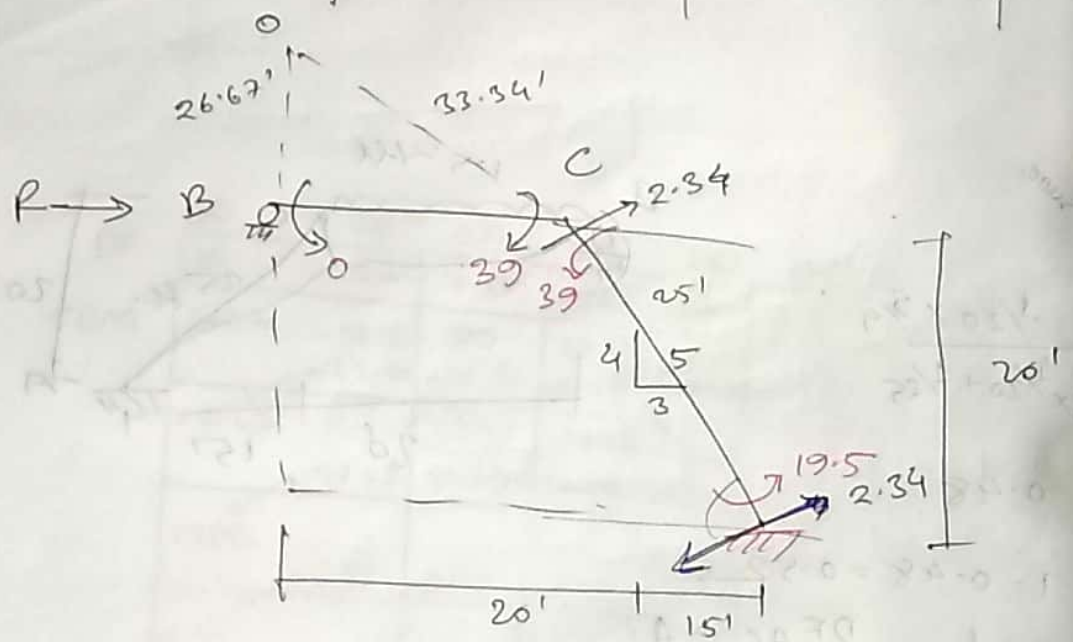
Cross
 Let's put an imaginary support to prevent side sway.



~~$DF = 0.49$ (BA)~~
 ~~$DF = 0.66$ (CB)~~

Side Sway prevented.

	BC	CB	CA	AC
DF	1	0.48	0.52	0
FEM	50 -50	-50 +24.28	+26	
		-25 +12	+13	13
				6.5
	0	-39	39	19.5



$$\frac{0B + 20}{35} = \frac{0B}{20} \Rightarrow 0B = 26.67 \text{ ft.}$$

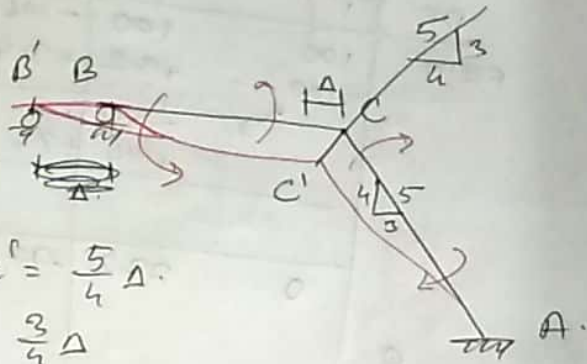
$$\therefore M_0 = 0 \quad (2)$$

$$-R \times 26.67 + 2.34 \times (25 + 33.34) - 19.5 = 0$$

$$\Rightarrow R = 4.88 \quad (\rightarrow)$$

Case 2

Swos permitted.



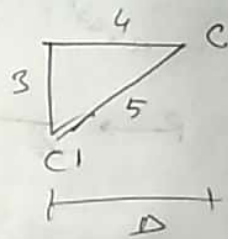
$$\Delta AC = CC' = \frac{5}{4} \Delta$$

$$\Delta BC = \frac{3}{4} \Delta$$

$$FEM_{AC} = FEM_{CA} = - \frac{6EI}{L^2} \Delta$$

$$= - \frac{6EI}{25^2} \times \frac{5}{4} \Delta$$

$$= - \frac{3}{250} EID$$



$$\textcircled{\ominus} FEM_{BC} = FEM_{CB} = \frac{6EI}{L^2} \times \Delta$$

$$= \frac{6EI}{20^2} \times \frac{3}{4} \Delta = \frac{9}{800} \times EID$$

Let

$$\cancel{FEM_{AC} = FEM_{CA} = - \frac{3}{250} EID} = -100 \text{ ksp}$$

$$\cancel{EID = 10000}$$

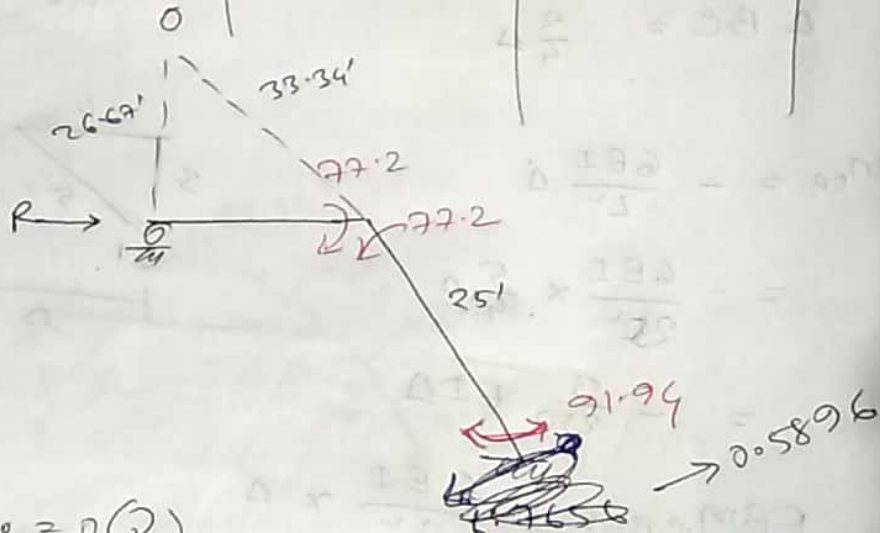
$$FEM_{BC} = FEM_{CB} = \frac{9}{800} \times EID = 100$$

$$\Rightarrow EID = 8888.89$$

$$\therefore FEM_{AC} = FEM_{CA} = - \frac{3}{250} \times 8888.89$$

$$= -106.67$$

	BC	CB	CA	AC
DF	1	0.48	0.52	0
FEEM	100	100	-106.67	-106.67
	-100	+3.2	+3.47	
		-50	+1.73	
		+24	+26	
			+13	
	0	77.2	-77.2	-91.94



$$M_0 = 0 \text{ (2)}$$

$$\Rightarrow -R \times 26.67 + 0.5896 - 6.7356 (33.34 + 25) + 91.94 = 0$$

$$\Rightarrow R = \frac{11.35}{4.73} = 2.157 \text{ (}\rightarrow\text{)}$$

Actual moment

$$M_{BC} = 0$$

$$M_{CB} = -39 + \frac{4.38}{2.157} \times 77.2 = -9.2 + 117.76$$

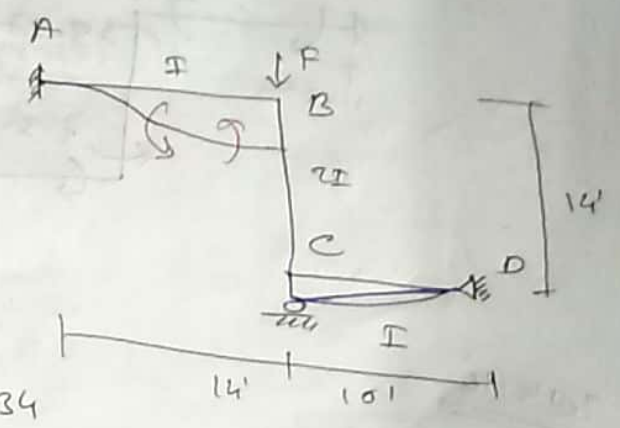
$$M_{CA} = 39 + \frac{4.38}{2.157} \times (-77.2) = -9.2 - 117.76$$

$$M_{AC} = 19.5 + \frac{4.38}{2.157} \times (-91.94) = -167.19$$

2015-16

16

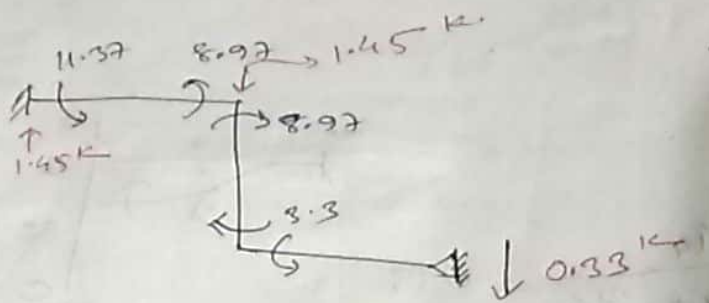
$DF_{AB} = 0$
 $DF_{BA} = \frac{I/14}{I/14 + 2I/14} = 0.33$
 $DF_{BC} = 0.67$
 $DF_{CD} = \frac{I/10 \times 3/4}{I/10 \times 3/4 + \frac{2I}{12} \times 2} = 0.34$
 $DF_{CB} = 1 - 0.34 = 0.66$
 $DF_{DC} = 1$



$FEM_{AB} = \frac{6EI}{L^2} \Delta = FEM_{BA}$
 $= \frac{6 \times 30000}{14^2} \times 0.15$
 $= 13.77 \text{ K-ft}$

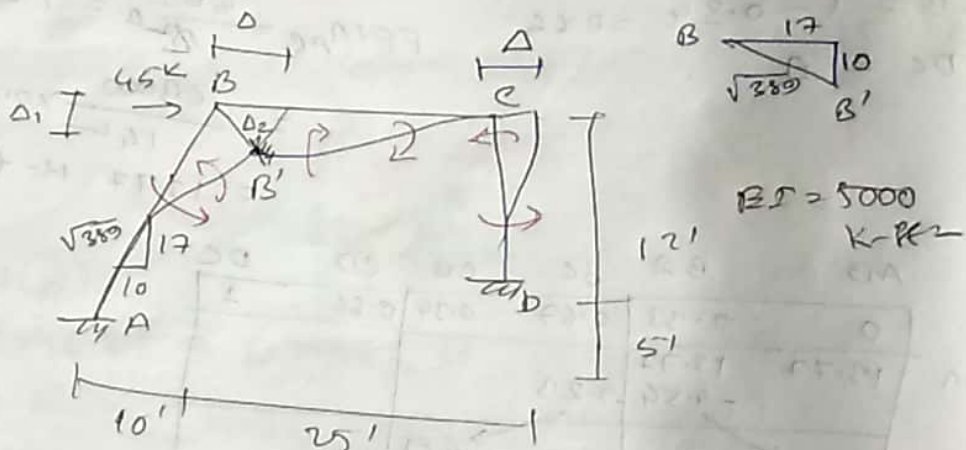
	AB	BA	BC	CB	CD	DC
DF	0	0.33	0.67	0.34	0.66	1
FEM	13.77	13.77				
		-4.54	9.23			
	-2.27			-4.61	3.04	
				+1.57		
			0.79			1.52
		-0.26	-0.55			-1.52
	-0.13			-0.26	-0.26	
	11.37	8.97	8.97	-3.3	3.3	

$\text{DF}_{CB} = 0.66$
 $\text{DF}_{DC} = 1$



2015-16

30



$$DF_{AB} = 0$$

$$DF_{BA} = \frac{1/\sqrt{389}}{1/\sqrt{389} + \Delta/25} = 0.56$$

$$DF_{BC} = 1 - 0.56 = 0.44$$

$$DF_{CB} = \frac{\Delta/25}{1/25 + 1/12} = 0.324$$

$$DF_{CD} = 1 - 0.324 = 0.676$$

$$DF_{DC} = 0$$

$$\frac{\Delta}{17} = \frac{\Delta_1}{10} = \frac{\Delta_2}{\sqrt{389}}$$

$$\rightarrow \Delta_1 = \frac{10}{17} \Delta$$

$$\Delta_2 = \frac{\sqrt{389}}{17} \Delta$$

DF

$$FEM_{AB} = FEM_{BA} = \frac{6EI}{L^2} \Delta_2 \quad EI = 5000$$

$$= \frac{6EI}{(\sqrt{389})^2} \times \frac{\sqrt{389}}{17} \Delta$$

$$= \frac{30000}{17} \Delta = \boxed{100 \text{ K-ft}} \quad \text{let}$$

$$\Delta = \frac{17}{300}$$

$$FEM_{BC} = FEM_{CB} = -\frac{6EI}{L^2} \Delta_1$$

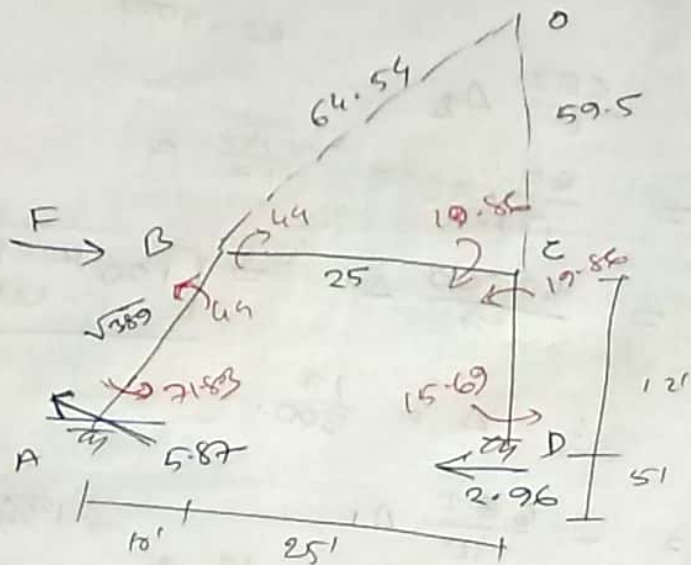
$$= -\frac{6 \times 5000}{25^2} \times \frac{10}{17} \Delta \quad \rightarrow \frac{17}{300}$$

$$= -\frac{8}{5} \text{ K-ft} = -1.6 \text{ K-ft}$$

$$FEM_{CD} = FEM_{DC} = \frac{6EI}{L^2} \Delta$$

$$= \frac{6 \times 5000}{12^2} \times \Delta = \frac{425}{36} = 11.8 \text{ K-ft} \quad \rightarrow \frac{17}{300}$$

	AB	BA	BC	CB	CD	DC
DF	0	0.56	0.44	0.324	0.676	0
FEM	100	100	-1.6	-1.6	11.8	11.8
		-55.27	-43.43	-3.3	-6.9	
	-27.64		-1.65	21.72	-3.45	
		0.92	0.73	+7.03	14.68	
	0.46		3.52	0.37		7.34
		-1.97	-1.55	-0.12	-0.25	
	-0.99		-0.08	-0.78		
		+0.03	0.03	0.252	0.527	
	71.83	43.71	-44	-19.86	19.86	15.69
		≈ 44				



$$\frac{0C + 17}{35} = \frac{0C}{25}$$

$$2) 0C = 59.5$$

$$\sum M_0 = 0 \quad \uparrow$$

$$\Rightarrow -F \times 64.54 + 5.87(64.54 + \sqrt{389}) + 2.96 \times (59.5 + 12) - 71.83 - 15.69$$

$$\Rightarrow F = 9.58 \quad (\rightarrow)$$

$$\therefore \Delta = \frac{17}{300} \text{ for } F = 9.58(\rightarrow)$$

$$\therefore \Delta = \frac{.45}{9.58} \times \frac{17}{300} = \boxed{0.26 \text{ ft}} \text{ for } \boxed{P = 45 \text{ k}}$$

2015-16

4(a)

$DF_{AB} = 1$

$$DF_{BA} = \frac{3/4 \times \frac{1}{12}}{\frac{3}{4} \times \frac{1}{12} + \frac{3}{4} \times \frac{1}{24} + \frac{1}{14}}$$

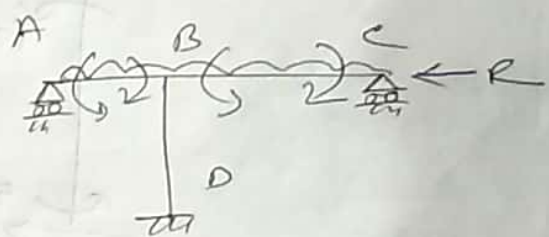
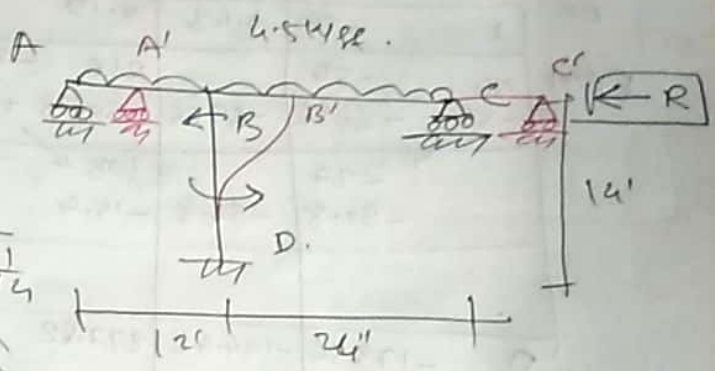
$$= 0.38$$

$$DF_{BC} = \frac{3/4 \times \frac{1}{24}}{\square} = 0.19$$

$DF_{BD} = 1 - 0.38 - 0.19 = 0.43$

$DF_{CB} = 1$

$DF_{DB} = 0$



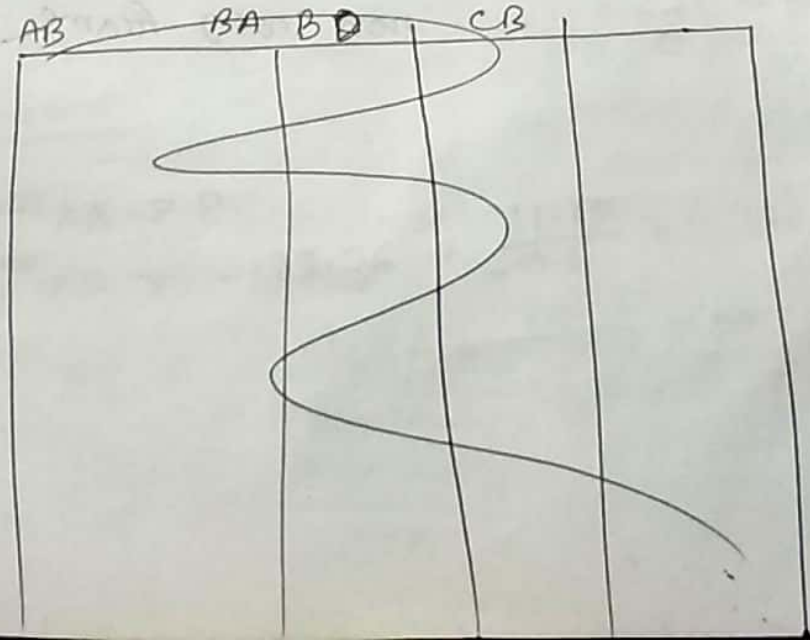
Case-1

$F_{BM} AB = -F_{BM} BA$

$$= \frac{4.5 \times 12^2}{12} = 54 \text{ k-ft}$$

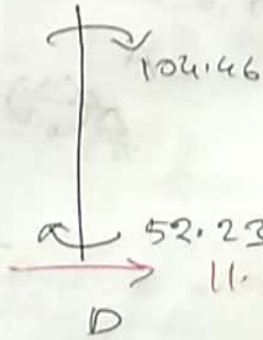
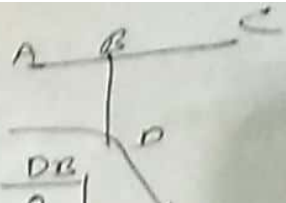
Case-1
Sway restricted.

$F_{BM} BC = -F_{BM} CB = \frac{4.5 \times 24^2}{12} = 216 \text{ k-ft}$



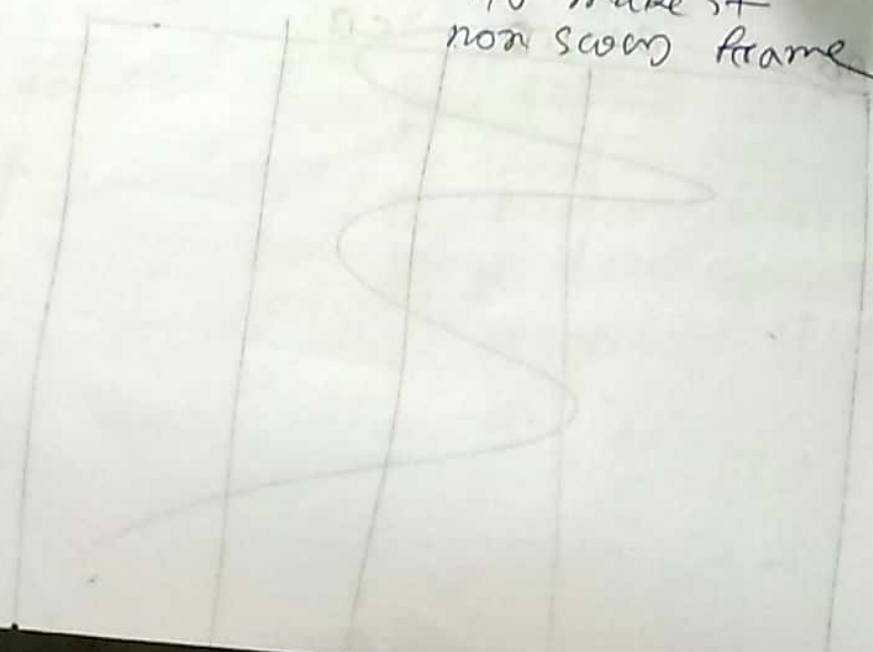
DF
FBM

	AB	BA	BD	BC	CB	DB
1	0.38	0.43	0.19	1	0	0
54	-54			216	-216	
-54	-61.56	-69.66	-30.78	+216		
	-27		108		-34.83	
	-30.8	-34.8	-15.4			
					-17.4	
0	-173.36	-104.46	277.82	0	-52.23	

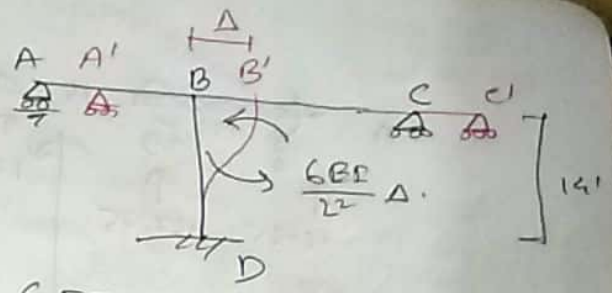


$\therefore R = 11.19 \text{ K}$

to be applied
to make it
non sway frame

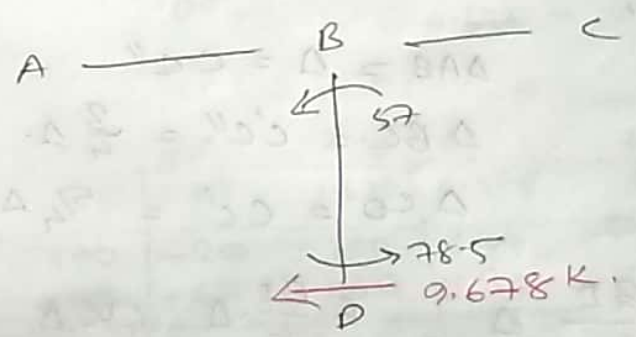


Case-2
Sway permitted



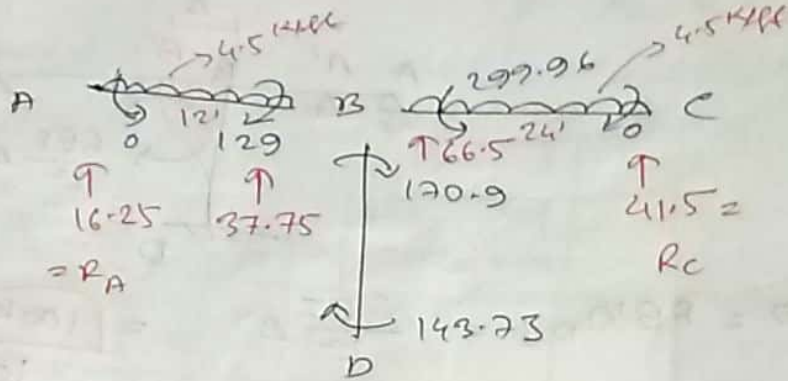
FEM_{BD} = FEM_{DB} = $\frac{6EI}{2^2} \Delta = 100K$
 $\Rightarrow BDD = 100K \times 14 = 1400K$

DF	AB	BA	BD	BC	CB	DB
1	0	-38	0	0	0	0
2	0	0	100	0	0	100
3	0	-38	-43	-19	0	-21.5
Σ	0	-38	57	-19	0	78.5



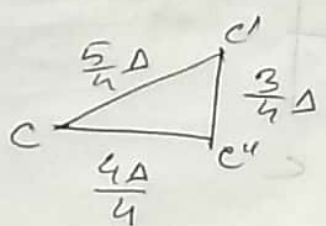
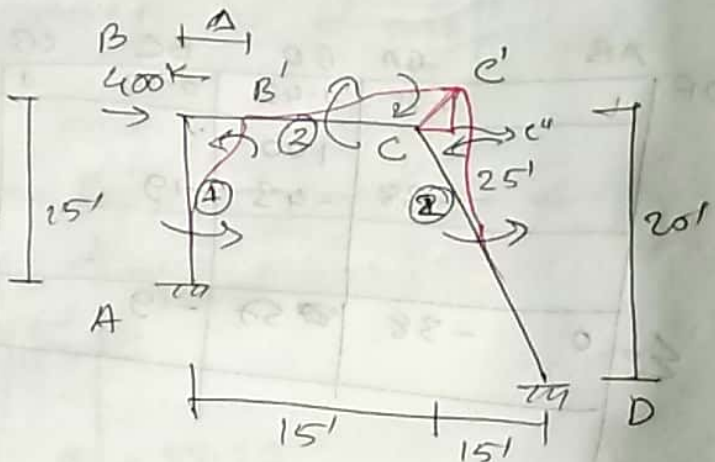
Actual moment

$M_{AB} = 0$
 $M_{BA} = -173.36 + \frac{11.19}{-9.6} \times (-38) = -129$
 $M_{BD} = -104.46 + \frac{11.19}{-9.6} \times 57 = -120.9$
 $M_{BC} = 277.82 + 11.19 \times (-19) = 299.96$
 $M_{CB} = 0$
 $M_{DB} = -52.23 + 11.19 \times (78.5) = -143.73$



2014-15

6(a)



$$\Delta_{AB} = \Delta = CC''$$

$$\Delta_{BC} = C'C'' = \frac{3}{4} \Delta$$

$$\Delta_{CD} = CC' = \frac{5}{4} \Delta$$

$$FEM = \frac{6EI}{L^2} \Delta = \frac{6EI}{L^2} \cdot \frac{3}{4} \Delta = \frac{6EI}{L} \cdot \frac{3}{4} \Delta = \frac{6EI}{L} \Delta$$

K बिना के लिये
K के value को
उपरोक्त में डालें

$$FEM_{AB} = FEM_{BA} = \frac{6EI}{L} \Delta$$

$$= \frac{6 \times 1 \times 10^4}{15} \Delta = \frac{6}{15} \Delta$$

Let $FEM_{AB} = FEM_{BA} = \frac{6}{15} \Delta = \boxed{100 \text{ K}}$
 $\Rightarrow \Delta = 250 \text{ mm}$

$\therefore FEM_{BC} = FEM_{CB} = -\frac{6KA}{L}$
 $= -\frac{6 \times 2}{15} \times 250$
 $= -200 \text{ K-ff}$

$FEM_{CD} = FEM_{DC} = \frac{6KA}{L} = \frac{6 \times 2 \times 250}{25}$
 $= 120 \text{ K-ff}$

DF

$DF_{AB} = 0$
 $DF_{BA} = \frac{I/15}{I/15 + 2I/15} = 0.33$ $DF_{BC} = 1 - 0.33 = 0.67$

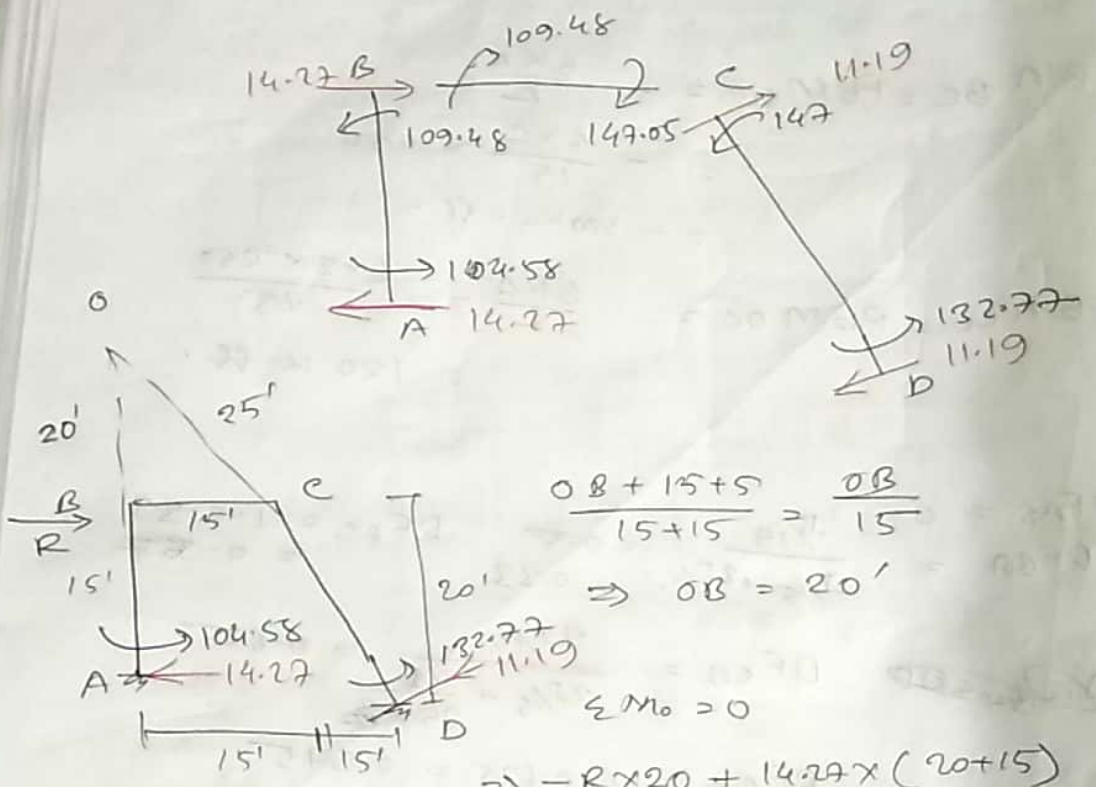
~~$DF_{CB} = \frac{2I/15}{2I/15 + 2I/15} = 0.625$~~

$DF_{CD} = 1 - 0.625 = 0.375$

$DF_{DC} = 0$

	AB	BA	BC	CB	CD	DC
DF	0	0.33	0.67	0.625	0.375	0
FEM	100	100 +33	-200 +67	-200 +50	120 +30	120
	16.5	-24.75	75	33.5	15	
	-12.375	+3.46	-10.47	-25.125	6.28	
	1.76	-2.59	7.85	3.5	4.21	
	-1.3	+0.36	-1.09	-2.63	-0.66	
			0.73	+1.64	+0.99	

$$\sum \begin{array}{|c|c|c|c|c|c|} \hline 104.58 & 109.48 & -109.48 & -147.05 & 147 & 132.77 \\ \hline AB & BA & BC & CB & CD & DC \\ \hline \end{array}$$



$$\frac{0.8 + 15 + 5}{15 + 15} = \frac{0.8}{15}$$

$$\Rightarrow OB = 20'$$

$$\sum M_0 = 0$$

$$\Rightarrow -R \times 20 + 14.27 \times (20 + 15) + 11.19 \times (20 + 25) - 132.77 - 104.58 = 0$$

$$\Rightarrow R = 39.88 (\rightarrow)$$

Actual moment $\rightarrow 10.03$

$$M_{AB} = \frac{400}{39.88} \times 104.58 = 1048.93$$

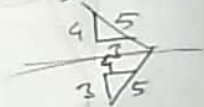
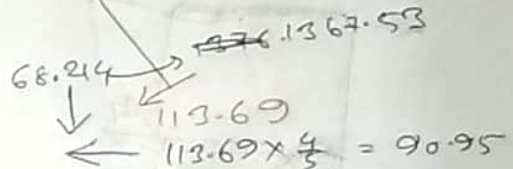
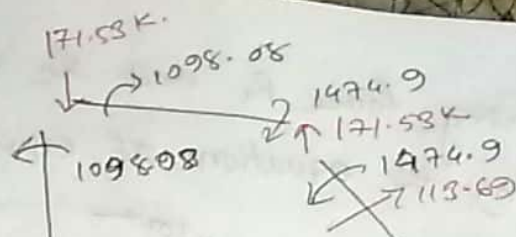
$$M_{BA} = 10.03 \times 109.48 = 1098.08$$

$$M_{BC} = 10.03 \times (-109.48) = -1098.08$$

$$M_{CB} = -147.05 \times 10.03 = -1474.9$$

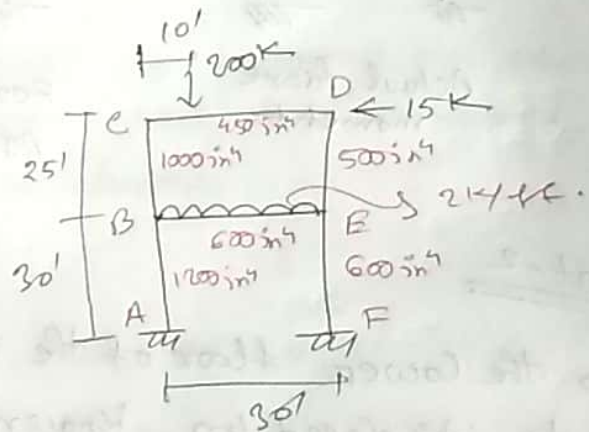
$$M_{CD} = +1474.9$$

$$M_{DC} = 132.77 \times 10.03 = 1367.53$$



2014-15
6 (b)

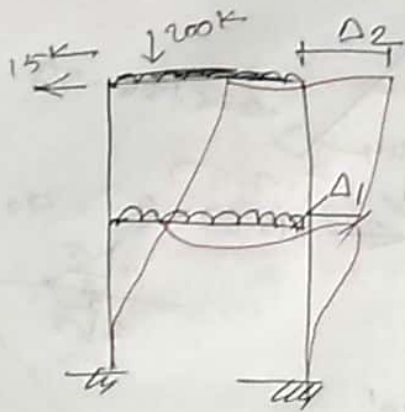
The moment distribution analysis is carried out in 3 parts.



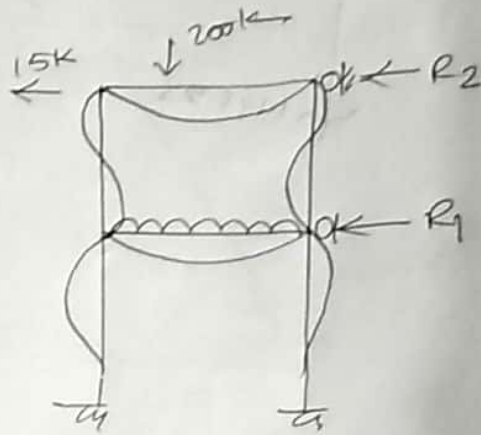
part-1

- The side sway of both floor is prevented by imaginary roller.
- The ~~moment~~ member end moments M_0 ~~are~~ which is caused by the external load is evaluated by moment distribution process

→ The restraining force R_1 and R_2 evaluated by applying the equation of equilibrium.



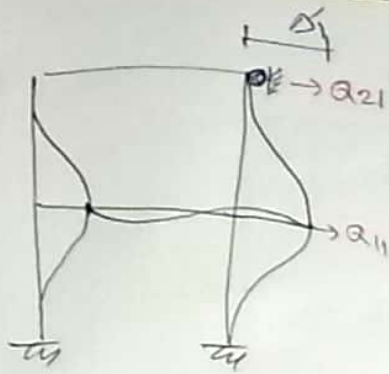
Actual frame moment



Frame with SideSway prevented.

Part-2

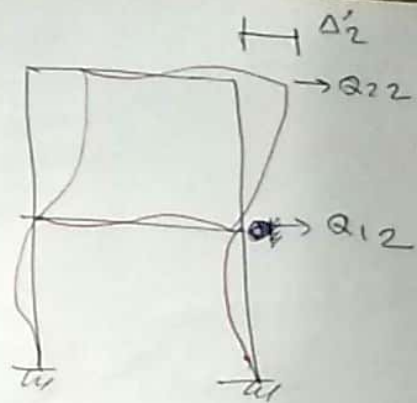
- The lower floor of the frame is allowed to displaced by known displacement Δ_1 while side-sway in upper floor is prevented.
- The FEM caused by the displacement computed and distributed to obtain the member end moments @ M_{A1} .
- With the member end moments known, the forces Q_{11} and Q_{21} at the locations of roller supports are determined by equilibrium equation.



$$\frac{\text{Part-2}}{M\Delta_1 - \Delta_1}$$

Part-3

→ Upper floor is allowed to displaced by known displacement Δ_2 and $M\Delta_2$, and force Q_{22} , Q_{12} are evaluated.



$$\frac{\text{Part-3}}{M\Delta_2 - \Delta_2}$$

The final moments

$$M = M_0 + C_1 M\Delta_1 + C_2 M\Delta_2$$

C_1 and C_2 are evaluated by

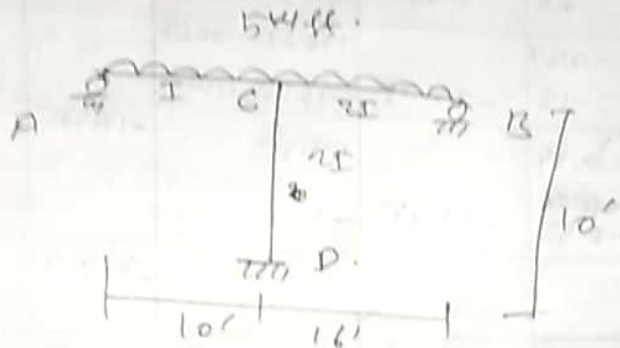
$$-R_1 + C_1 Q_{11} - C_2 Q_{12} = 0$$

$$-R_2 - C_1 Q_{21} + C_2 Q_{22} = 0$$

Frame

20/3-19

(2)

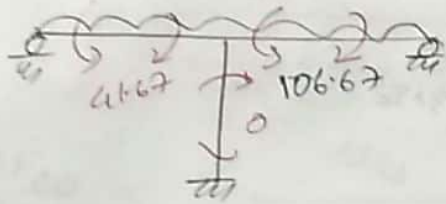


$$DF_{CA} = \frac{\frac{3}{4} \times \frac{F}{10}}{\frac{3}{4} \frac{F}{10} + \frac{3}{4} \times \frac{2F}{16} + \frac{2F}{10}} = 0.2$$

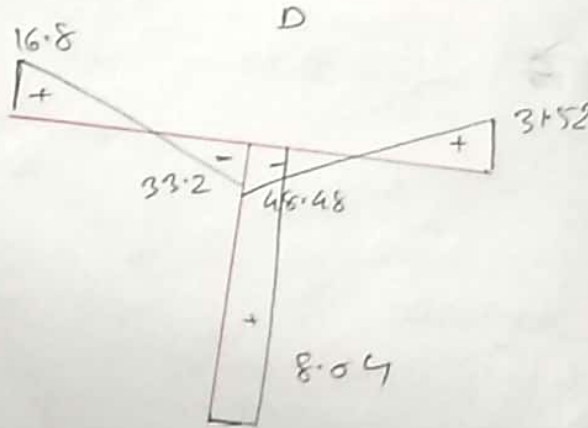
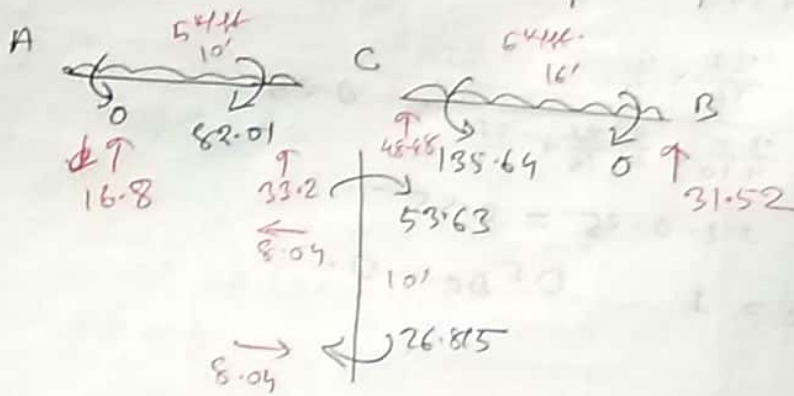
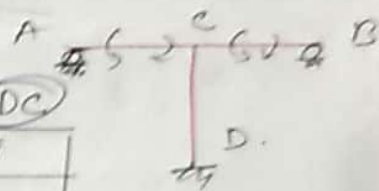
$$DF_{CB} = \frac{\frac{2F}{16} \times \frac{3}{4}}{\frac{3}{4} \frac{F}{10} + \frac{3}{4} \times \frac{2F}{16} + \frac{2F}{10}} = 0.25$$

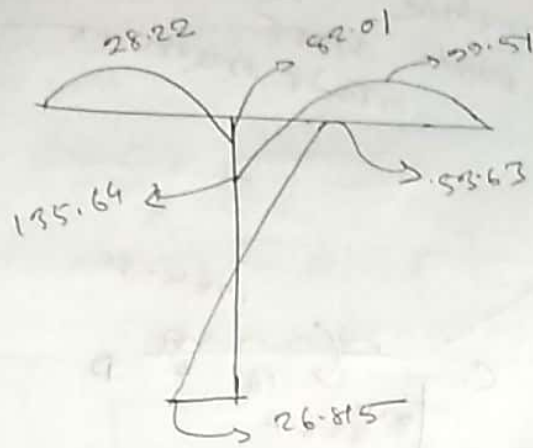
$$DF_{CD} = 1 - 0.2 - 0.25 = 0.55$$

$$DF_{AC} = DF_{BC} = 1 \quad DF_{DC} = 0$$



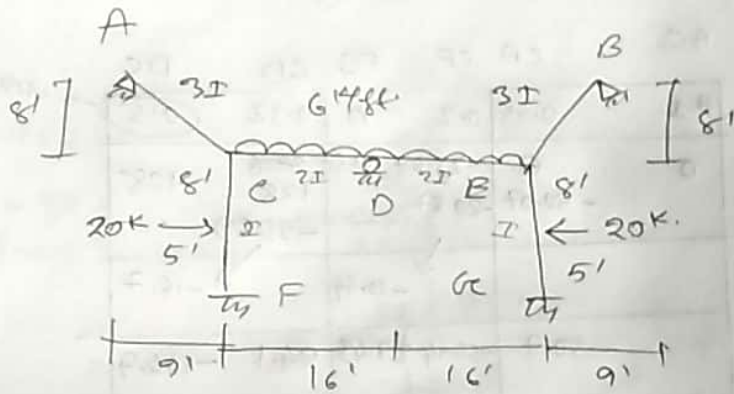
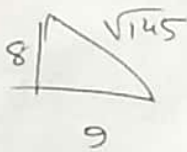
	AC	CA	CD	DC	CB	BC	DB
DF	1	0.2	0.55	0.25	1	0	0
FEM	41.67	-41.67			106.67	-106.67	
	-41.67	-13	-35.75	-16.25	+106.67		
		-20.84		53.35		-17.875	
		-16.26					
		-6.5	-17.88	-8.13			
						-8.94	
0	-82.01	-53.63	135.64	0	-26.815		





2013-14

5

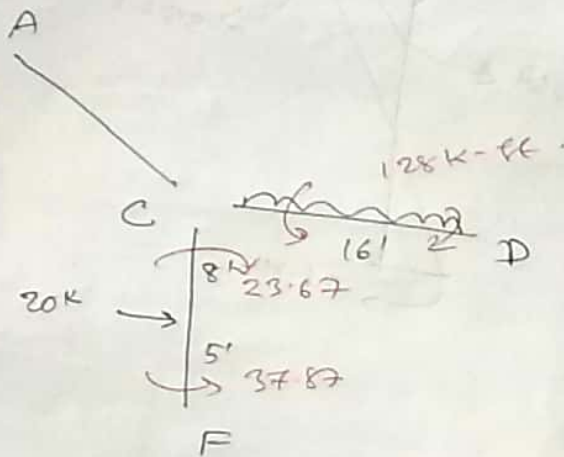


$$DF_{CA} = \frac{\frac{3I}{\sqrt{145}} \times \frac{3}{9}}{\frac{3I}{\sqrt{145}} \times \frac{3}{9} + \frac{2I}{16} + \frac{I}{13}} = 0.48$$

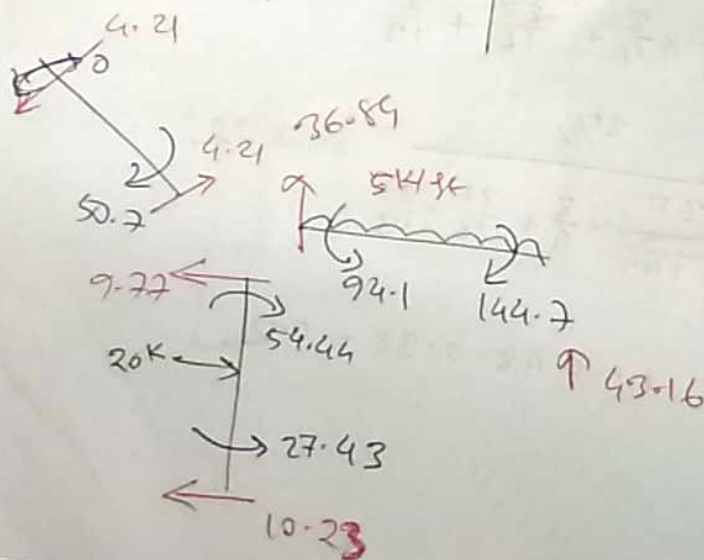
$$DF_{CD} = \frac{\frac{2I}{16}}{\frac{3I}{\sqrt{145}} \times \frac{3}{9} + \frac{2I}{16} + \frac{I}{13}} = 0.32$$

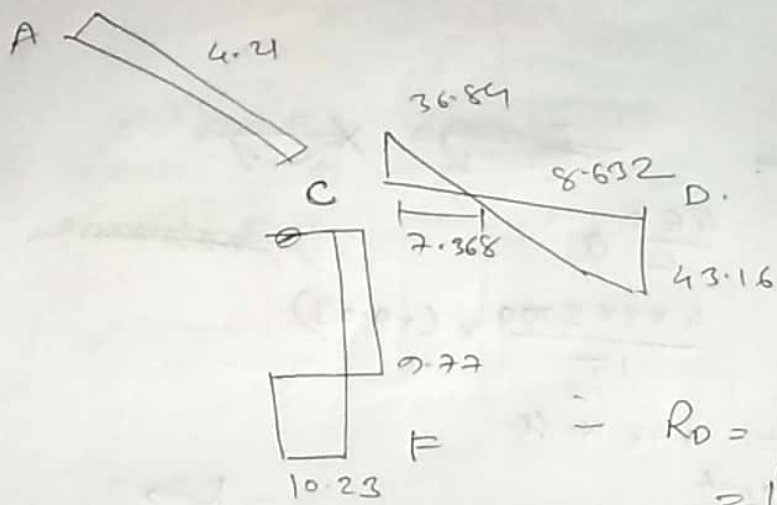
$$DF_{CF} = 1 - 0.48 - 0.32 = 0.2$$

Since it is symmetric
 So, I can do half of it



DF	AC	CA	CF	FC	CD	DC
A1	0.48	0.2	0	0.32	0.5	
D	0	-23.67	37.87	128	-128	
FEM	-50.07	-20.87		-33.39	-16.7	
		-10.44				
	-50.7	-54.44	27.43	94.1	-144.7	



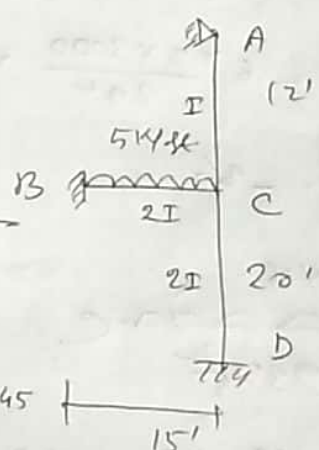


2013-14
7

B 20.03 cm

D $\rightarrow 0.4 \text{ ft}$

BE = 3000 K-ft²



$$DF_{CB} = \frac{\frac{2I}{15}}{\frac{2I}{15} + \frac{2I}{20} + \frac{I}{12} \times \frac{3}{4}} = 0.45$$

$$DF_{CA} = \frac{\frac{I}{12} \times \frac{3}{4}}{\frac{2I}{15} + \frac{2I}{20} + \frac{I}{12} \times \frac{3}{4}} = 0.21$$

$$DF_{CD} = 1 - 0.45 - 0.21 = 0.34$$

Support B rotation

$$M_{BC} = \frac{4EI}{L} \theta$$

$$= \frac{4 \times 2 \times 3000}{15} \times (+0.03)$$

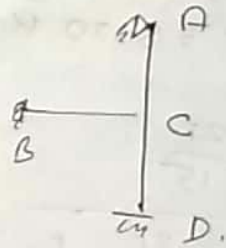
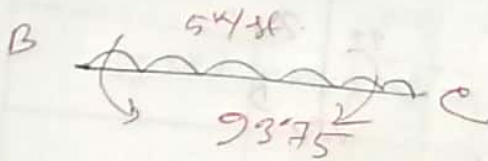
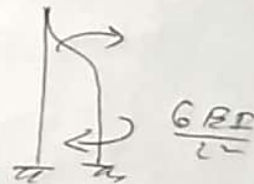
$$= +48 \text{ k-ft}$$

Support D movement

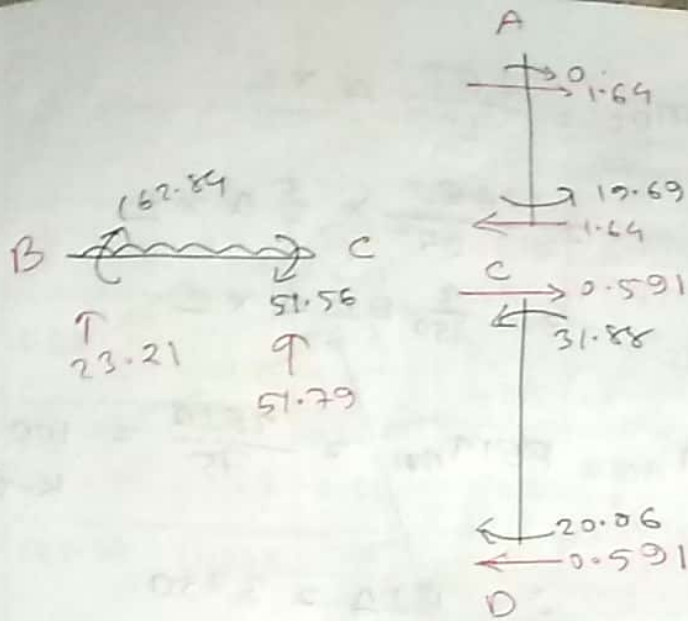
$$M_{DC} = -\frac{6EI}{L^2} \Delta$$

$$= -\frac{6 \times 2 \times 3000}{20^2} \times 0.4$$

$$= -36$$



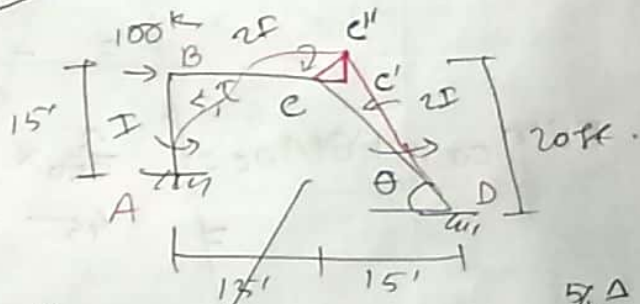
DF	AC	CA	CB	CD	DC	BC
0	0.21	0.45	0.34	0	0	0
	+19.69	+42.19	31.88	-36	93.75+48	
				15.94		
0	19.69	51.56	31.88	-20.06	21.09	$\rightarrow \frac{42.19}{2}$
					62.84	



2012-13

①

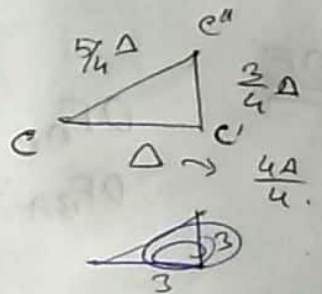
2014-15
6②
Same type



$$\Delta_{AB} = \Delta = CC'$$

$$\Delta_{BC} = \frac{3}{4}\Delta = C'C''$$

$$\Delta_{CD} = \frac{5}{4}\Delta = CC''$$



$$FEM_{AB} = FEM_{BA} = + \frac{6EI}{L^2} \Delta$$

$$= \frac{6EI}{15^2} \times \Delta = \frac{2EI\Delta}{75}$$

$$FEM_{BC} = FEM_{CB} = - \frac{6EI}{L^2} \Delta \times 2$$

$$= - \frac{6EI}{15^2} \times \frac{3}{4}\Delta = - \frac{EI\Delta}{50} \times 2$$

$$FEM_{CO} = FEM_{OC} = \frac{6EI}{L^2} \Delta \times 2$$

$$= \frac{6EI}{25^2} \times \frac{5}{4} \Delta \times 2$$

$$= \frac{3}{250} EI \Delta \times 2$$

Let assume

$$FEM_{AB} = FEM_{BA} = \frac{2EI\Delta}{75} = 100 \text{ K-}\cancel{ft}$$

$$\Rightarrow EI\Delta = 3750$$

$$\therefore FEM_{BC} = FEM_{CB} = -\frac{EI\Delta}{50} \times 2$$

$$= -\frac{3750}{50} \times 2 = -75 \times 2 = -150$$

$$FEM_{CO} = FEM_{OC} = \frac{3}{250} \times 3750 \times 2$$

$$= 45 \times 2 = 90$$

DF

$$DF_{AB} = 0$$

$$DF_{BA} = \frac{I/15}{I/15 + \frac{2I}{15}} = \frac{1}{3}$$

$$DF_{BC} = 1 - \frac{1}{3} = \frac{2}{3}$$

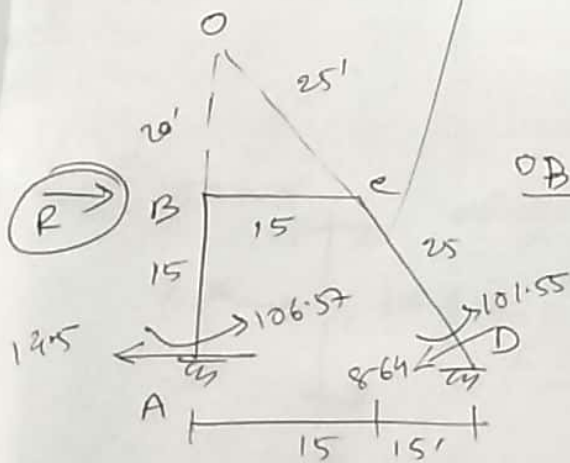
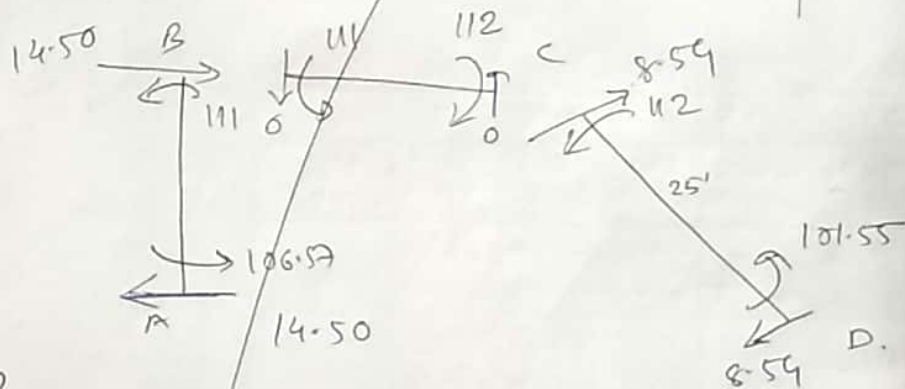
$$DF_{CB} = \frac{\frac{2I}{15}}{\frac{2I}{15} + \frac{2I}{25 \times \frac{3}{5}}} = \frac{1}{2}$$

$$DF_{CD} = 1 - \frac{1}{2} = \frac{1}{2}$$

$$DF_{DC} = 0$$

DF	AB	BA	BC	CB	CD	DC
FEM	0	0.35	0.67	0.5	0.5	0
	100	100	-150	-150	90	90
		+16.5	+37.5	+30	+30	
	+8.25		+15	18.75		+15
		-4.95	-10.05	-9.4	-9.4	
	-2.48		-4.7	-5		-4.7
		1.55	3.15	+2.5	+2.5	
	0.8		1.25	1.58		1.25
		-0.41	-0.84	-0.8	-0.8	
	106.57	112.69	-109.14	-111.97	112.3	101.55
		≈ 111	-111	≈ -112	+112	

more precisely
106.57



$$\frac{0B + 15 + 5}{30} = \frac{0B}{15} \Rightarrow 0B = 20'$$

$$\sum M_0 = 0$$

$$\Rightarrow 106.57 - 101.55 + 14.5 \times 35 + 8.64 \times 50 - R \times 20 = 0$$

$$\Rightarrow R = \frac{6.63}{20} + 36.56$$

(→)