

* What are the characteristics of the critical path ~~ing~~ a network? [DNCC'22]

- The longest path in the network
- Specifies the minimum project duration
- Indicates amount of scheduling flexibility
- A project can have more than one critical path.
- Total float of activities on critical path is zero
- critical path changes as the project progresses

→ any delay in any of activities in critical path results in a delay in the overall project duration.



Date: _____

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* PERT = Programme Evaluation & Review Technique

Activity	Estimated duration (weeks)		
	optimistic time (t_o)	most likely time (t_m)	Pessimistic (t_p)
1-2	1	7	13
1-6	2	5	14
2-3	2	14	26
1-2-4	2	5	8
3-5	7	10	19
4-5	5	5	17
6-7	5	8	29
5-8	3	3	9
7-8	8	17	32

You are required to -

- (1) Draw the project network
- (2) Find the expected duration & variance of each activity
- (3) Calculate the earliest & latest occurrence for each activity
- (4) Calculate expected project length
- (5) Calculate the variance and standard deviations of project length
- (6) Find the probability of the project completing in 40 days

Solng

~~Activity 1-2 1-6 2-3 2-4 3-5 4-5 6-7~~

Activity 1-2 1-6 2-3 2-4 3-5 4-5 6-7 5-8 7-8

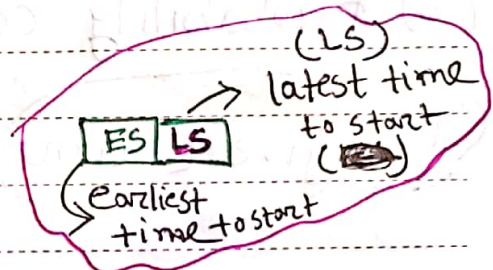
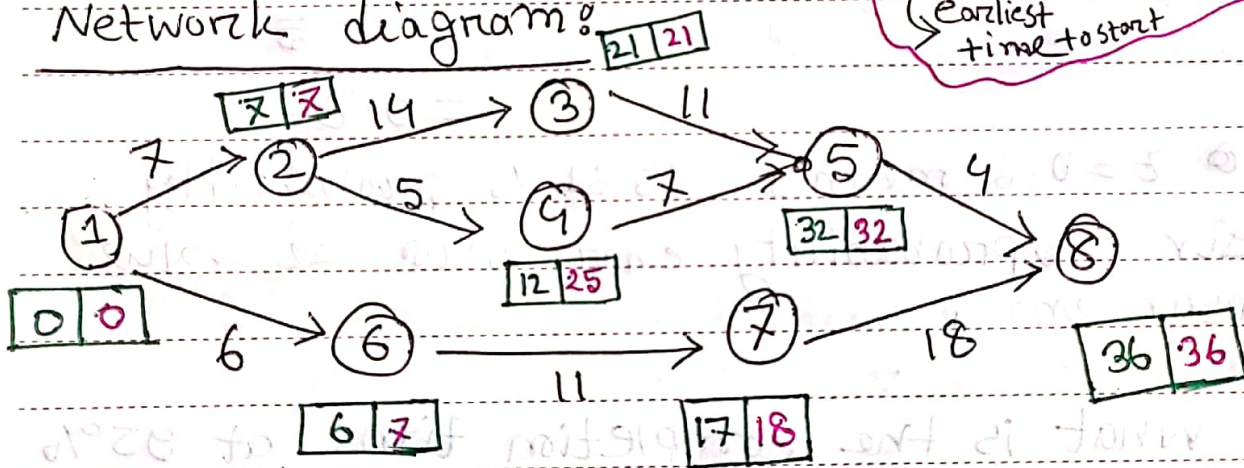
expected time 7 6 14 5 11 7 11 4 18

$$t_e = \frac{t_o + 4t_m + t_p}{6}$$

variance 4 4 16 1 4 4 16 1 16

$$\sigma^2 = \left(\frac{t_p - t_o}{6}\right)^2$$

Network diagram:



- * Earliest to (अस्य स्य प्रारंभक कालः)
- * latest to (अस्य स्य अन्तःकालः) (अन्तःकालः)
- * ES to (अस्य स्य प्रारंभक कालः) स्य प्रारंभक कालः स्य प्रारंभक कालः
- * LS to (अस्य स्य अन्तःकालः) स्य अन्तःकालः स्य अन्तःकालः
- * Float or slack = LS - ES

Critical path to slack/float always zero to



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∴ critical path 1-2-3-5-8

∴ Expected project duration = $7 + 14 + 11 + 4 = 36$ weeks

∴ project length variance, $\sigma^2 = 4 + 16 + 4 + 1 = 25$

∴ project length standard deviation, $\sigma = 5$

(6) probability coefficient, $z = \frac{T_s - T_e}{\sigma}$

$T_s = \text{given time}$

$$= \frac{40 - 36}{5}$$

$$= 0.8$$

∴ $z = 0.8$ means 78.81% probability.

∴ a probability chart gives z value

* What is the completion time at 95% confidence level?

for 95% confidence level, $z = 1.96$

$$z = \frac{T_s - 36}{5}$$

$$\Rightarrow T_s = 5z + 36 = 5 \times 1.96 + 36 = 45.8 \text{ weeks}$$

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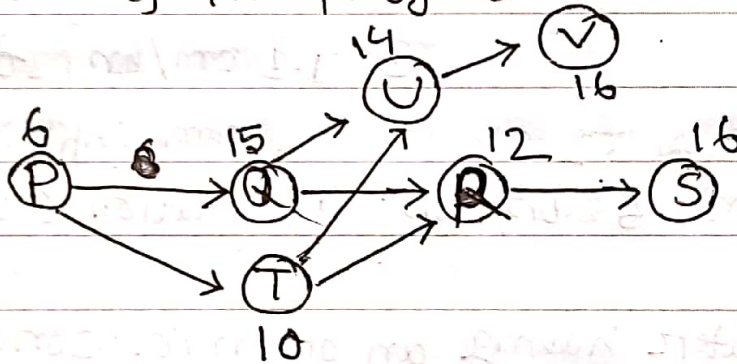
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(4) The activity details of a project are given below:

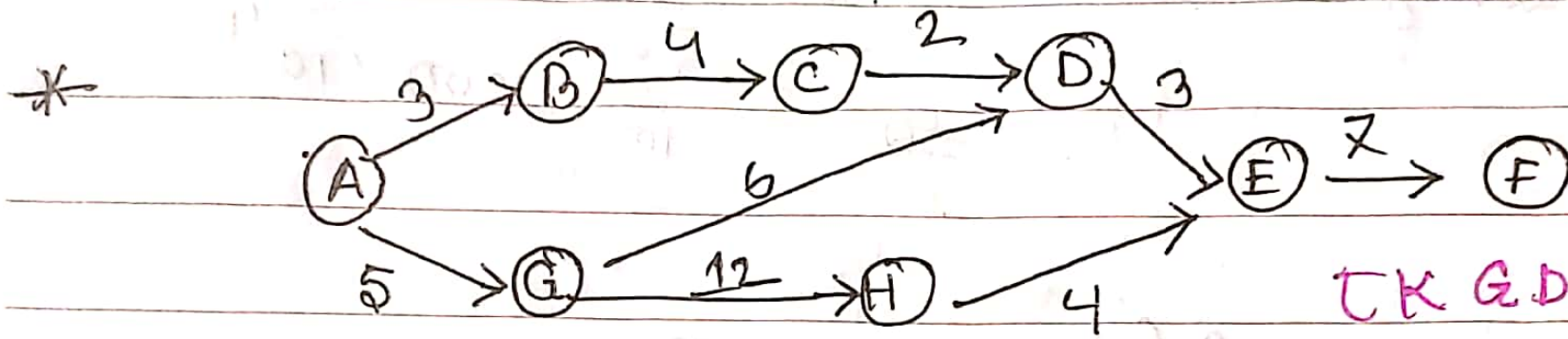
Activity	Depends on	Duration (in days)
P	--	6
Q	P	15
R	Q, T	12
S	R	16
T	P	10
U	Q, T	14
V	U	16

The estimated minimum time (in days) for the completion of the project will be what?

Ans:



$$\therefore \text{Critical path} = 6 + 15 + 14 + 16 = 51 \text{ days}$$



[KGDCL'21]

Critical path \rightarrow A \rightarrow G \rightarrow H \rightarrow E \rightarrow F

$$\text{Time} = 5 + 12 + 4 + 7 = 28 \text{ days}$$