

Hyetograph

$\phi$  index : The  $\phi$  index is the average rainfall above which the rainfall volume (intensity) is equal to the runoff volume (intensity)

$$\phi \text{ index} = \frac{P_e - R}{t_e}$$

$P_e$  = excess rainfall ( $i > f_p$ )

$t_e$  = time of excess rainfall

$R$  = total runoff

$P$  = all kind of rainfall ( $i > f_p$  or  $i < f_p$ )

\*  $\phi$  index is soil's maximum infiltration capacity.  $\phi > i > f_p$  or  $\phi < i < f_p$

## W-index

⇒ it is refined version of  $\phi$ -index

⇒ Here the initial losses\* are separated from the total losses

$$\Rightarrow W\text{-index} = \frac{P - R - \text{initial losses}}{t}$$

\* Initial losses = interception process + depression storage (SD)

interception process :  $\text{शुष्क पृष्ठ, या किसी obstacle के कारण जल की कुछ मात्रा वाष्पित हो जाती है}$   
evaporated 20% मात्रा

⇒ W-index सिस्टम  $\phi$ -index जगह जगह पर initial loss को count कर 20% or

⇒ W-index is more accurate than the  $\phi$ -index

\*\*\* In estimating the max floods for design purposes, in the absence of any other data,  $\phi$ -index value is taken as 0.10 cm/hr

## Calculation of Runoff

$$R = \sum_{i=1}^n (I_i - \phi) \Delta t$$

$\Delta t$  = time interval

$I_i$  is always greater than  $\phi$  in that case only  $I_i > \phi$  is acceptable in the case

## Math Problems :

① The rate of rainfall for the successive 30 min period of a 3 hr storm are: 1.6, 3.6, 5.0, 2.8, 2.2, 1.0 cm/hr. The surface runoff is estimated to be 3.6 cm.

Determine  $\phi$ -index & W-index  
[BIWTA'19 - BWD B 16]

Sol<sup>n</sup>:

$$P = (1.6 + 3.6 + 5.0 + 2.8 + 2.2 + 1.0) \times \frac{30}{60}$$

$$= 8.1 \text{ cm}$$

$$\therefore W = \frac{P - R - \text{initial loss}}{t}$$

$$= \frac{8.1 - 3.6 - 0}{3}$$

$$= 1.5 \text{ cm/hr}$$

$\therefore \phi\text{-index} > W\text{-index}$  ...  $P_e$  too ...

Intensity - 1.5 cm/hr ... intensity ...  
 value ...

$$P_e = 8.1 - \frac{1.0 \times 30}{60}$$

$$= 7.5 \text{ cm}$$

$$\phi \text{ index} = \frac{P_e - R}{\Delta t}$$

$$= \frac{7.5 - 3.6}{2.5}$$

[30 minute ...]

$$= 1.6 \text{ cm/hr}$$

(2) The intensity/rate of rainfall for successive 20min period of a storm 10.0, 7.5, 1.25, 1.25, 5 cm/hr. Assume  $\phi$  index = 3.2 cm/hr. Find net runoff, total rainfall & W-index if initial loss is 0.96 cm.

Sol<sup>n</sup>

(i) Total rainfall,  $P = (2.5 + 2.5 + 10 + 7.5 + 1.25 + 1.25 + 5) \times \frac{20}{60} \text{ cm}$

$$= 10 \text{ cm}$$

(ii) Runoff,  $R = \sum_{i=1}^n (i - \phi) \Delta t$

$$= [(10 - 3.2) + (7.5 - 3.2) + (5 - 3.2)] \times \frac{20}{60}$$

$$= 4.3 \text{ cm}$$

$$(ii) W \text{ index} = \frac{P - R - \text{initial loss}}{t}$$

$$= \frac{10 - 4.3 - 0.06}{\frac{140}{60}}$$

$$= 2.42 \text{ cm/hr}$$

(3) Find the  $\phi$ -index if the direct runoff is 4.9 cm [BWD B-19]

Time (hr)	1	2	3	4	5
P (cm)	1.5	2.5	4.1	3	1.9

Soln: With given diagram -  $\phi$ -index for runoff  
 W-index for runoff  
 $\phi$ -index for runoff  $\phi > W$  index

$$P = 1.5 + 2.5 + 4.1 + 3 + 1.9 = 13 \text{ cm}$$

$$W \text{ index} = \frac{13 - 4.9}{5} = 1.62 \text{ cm/hr}$$

$$\text{Now, } P_e = 13 - 1.5 = 11.5 \text{ cm [1 hr \& 15 min after rain]}$$

$$\therefore \phi \text{ index} = \frac{P_e - R}{t_e} = \frac{11.5 - 4.9}{4} = 1.65 \text{ cm/hr}$$

(4) A 6h storm with hourly intensities of 7, 18, 25, 12, 10, 3 mm/h produces a runoff of 33 mm. Then  $\phi$ -index is ?

Sol<sup>n</sup>:

$$W\text{-index} = \frac{25 - 33}{6} = 7 \text{ mm/h}$$

$$\phi\text{-index} = \frac{(25 - 7) - 33}{4} = \frac{(25 - 7 - 33)}{4} = 8 \text{ mm/h} \text{ An}$$

(5) A 4h storm had 4cm of rainfall & the resulting direct run-off was 2cm. If the  $\phi$ -index remains at the same value, the runoff due to 10cm of rainfall in 8h in the catchment is what?

Sol<sup>n</sup>:  $\phi$  index =  $\frac{4 - 2}{4} = 0.5$

again,  $0.5 = \frac{10 - R}{8}$

$\Rightarrow R = 6 \text{ cm} \text{ An}$

(b) A storm with 10 cm of precipitation produced a direct runoff of 5.8 cm. The duration of the rainfall was 16 hr and its time distribution is given below. Estimate  $\phi$ -index

Time (hr)	0	2	4	6	8	10	12	14	16
Cumulative rainfall (cm)	0	0.4	1.3	2.8	5.1	6.9	8.5	9.5	10
Sol <sup>n</sup> : increment (cm)	0	0.4	0.9	1.5	2.3	1.8	1.6	1.0	0.5
intensity (cm/hr)	0	0.2	0.45	0.75	1.15	0.9	0.8	0.5	0.5

$$W \text{ index} = \frac{10 - 5.8}{16} = 0.2625 \text{ cm/hr}$$

$$\phi \text{ index} = \frac{(10 - 0.4 - 0.5) - 5.8}{12} = 0.275 \text{ cm/hr}$$

duration of rainfall excess = 12 hr



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# The intensity/rate of rainfall for successive 20min period of a 140min storm 2.5, 2.5, 10.0, 7.5, 1.25, 1.25, 5 cm/hr. Assume  $\phi$ -index = 3.2 cm/hr. Find net runoff, total rainfall & W-index if initial loss is 0.06 cm.

Sol<sup>n</sup>:

$$(i) \text{ Total rainfall, } P = (2.5 + 2.5 + 10 + 7.5 + 1.25 + 1.25 + 5) \times \frac{20}{60} \text{ cm}$$
$$= 10 \text{ cm}$$

$$(ii) \text{ Runoff, } R = \left[ (10 - 3.2) + (7.5 - 3.2) + (5 - 3.2) \right] \times \frac{20}{60}$$
$$= 4.3 \text{ cm}$$

$$(iii) \text{ W index} = \frac{P - R - \text{initial loss}}{t}$$
$$= \frac{10 - 4.3 - 0.06}{140/60}$$
$$= 2.42 \text{ cm/hr}$$

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(2) A 8 hours storm produced a surface runoff of 11.6 cm. Estimate the infiltration-index of the storm. [DMTCL Line 55]

Storm time (h)	1	2	3	4	5	6	7	8
Rainfall intensity (cm/h)	0.8	1.8	3.0	4.6	3.6	3.2	2.0	1.0

Solution:

$$\text{Total precipitation} = 0.8 + 1.8 + 3.0 + 4.6 + 3.6 + 3.2 + 2.0 + 1.0 = 20 \text{ cm}$$

$$W\text{-index} = \frac{20 - 11.6}{8} = 1.05 \text{ cm/hr}$$

1hr or 8hr storm intensity W-index (20cm) (12cm), or 2nd or 7th infiltration storm.

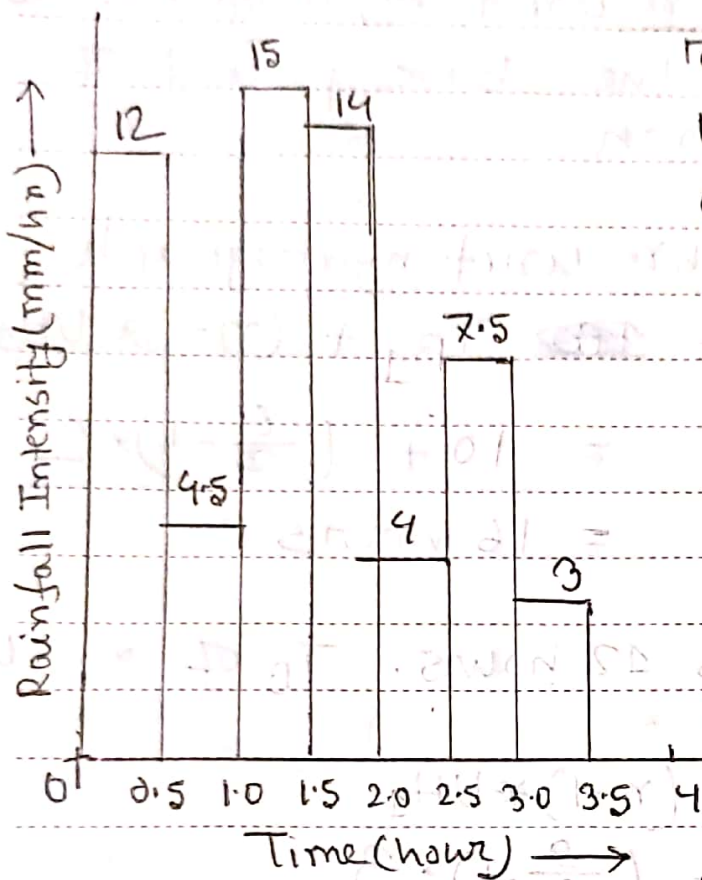
$$\therefore \text{infiltration index} = \frac{(20 - 0.8 - 1.0) - 11.6}{8 - 2} = 1.1 \text{ cm/hr } \underline{A}$$

for 1st or 2nd or 8th hour or 6th or 7th infiltration storm, 2nd or 7th (or) 6th or 7th infiltration 1.1 cm/hr

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\* Rainfall intensity with respect to time is given below:



rainfall depth is 3cm. If the rainfall event has produced a direct runoff of 1.6cm, calculate the  $\phi$ -index of the event.

$$\text{Sol}^{\text{no}} = W\text{-index} = \frac{3 - 1.6}{3.5} = 0.4 \text{ cm/hr} = 4 \text{ mm/hr}$$

$$\therefore \phi\text{-index} = \frac{(30 - \frac{4 \times 1}{2} - \frac{3}{2}) - 16}{3.5 - 1} \Rightarrow \text{mm}$$

$$= 4.2 \text{ mm/hr}$$

$\frac{210-30}{60} = 3.5 \text{ hr}$   
 discharge =  $1.2 \text{ m}^3/\text{s}$   
 base flow =  $1.2 \text{ m}^3/\text{s}$

Time (min)	Intensity (mm/h)	Discharge ( $\text{m}^3/\text{s}$ )
0	-	1.2
30	8	1.2
60	18	3.9
90	35	8.5
120	25	6
150	8	4.5
180	16	3.1
210	22	1.2

Catchment area is  $1.5 \text{ km}^2$ . Assume the rain fall amount in the first half-an-hour is the initial loss & the base flow is  $1.2 \text{ m}^3/\text{sec}$ .

determine  $\phi$ -index

Sol<sup>n</sup>:  $P = \frac{30}{60} [8 + 18 + 35 + 25 + 8 + 16 + 22] = 66 \text{ mm}$   
 Runoff volume =  $\left[ (6-1.2) + (4.5-1.2) + (3.1-1.2) + (1.2-1.2) \right] \times 60 \times 30$

$\text{m}^3/\text{s} = 60 \text{ m}^3/\text{min}$   
 $= 60 \times 30 \text{ m}^3$   
 $= 3600 \text{ m}^3$

$\frac{210-30}{60} = 3.5 \text{ hr}$

Runoff depth =  $\frac{3600 \text{ m}^3}{1.5 \times 10^6 \text{ m}^2} = 24 \text{ mm}$

$\therefore W \text{ index} = \frac{P - R - L}{t} = \frac{66 - 24 - 8}{3.5} = 12.6 \text{ mm/hr}$   
 First 30 min intensity =  $8 \text{ mm/hr}$   
 or for 30 min a  $4 \text{ mm}$

$$\therefore P_e = (18 + 35 + 25 + 16 + 22) \times \frac{30}{60} = 58$$

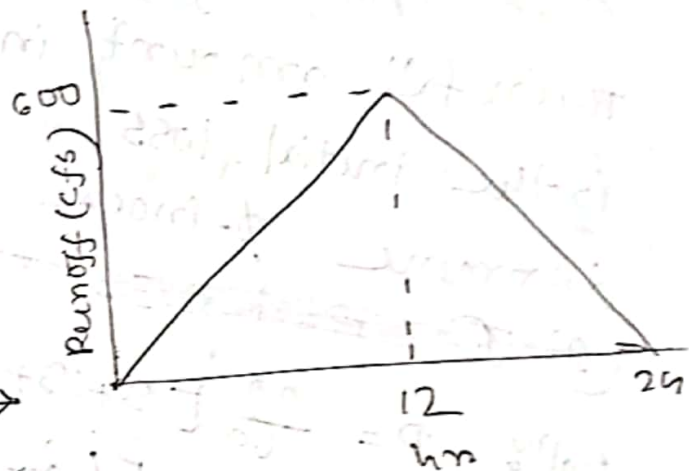
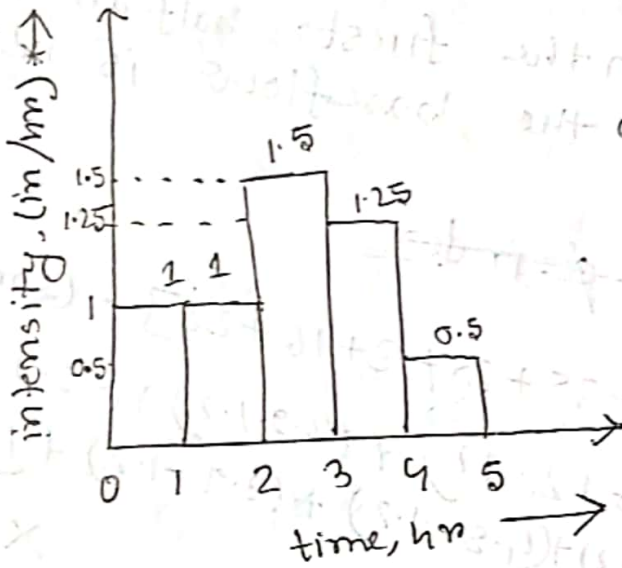
$$t_e = 3 \text{ hrs} \quad (30 \text{ min}, 30 \text{ min one way one})$$

$$\therefore \phi \text{ index} = \frac{58 - 24}{3 \times 2.5} = 13.6 \text{ mm/hr}$$

\*\*\*

Intensity vs time  $\Rightarrow$  Hyetograph

Flow vs time  $\Rightarrow$  Hydrograph  
(Runoff)



Given,  $\phi \text{ index} = 0.5 \text{ in/hr}$

Determine total volume of runoff & the watershed area.

Soln:  $P = 1 + 1 + 1.5 + 1.25 + 0.5 = 5.25 \text{ in}$

Runoff depth,  $R = (1 - 0.5) + (1 - 0.5) + (1.5 - 0.5) + (1.25 - 0.5) + (0.5 - 0.5)$   
 $= 2.75 \text{ in}$

*work*

$$\phi \cdot \phi\text{-index} = \frac{Pe - R}{te}$$

$$\Rightarrow 0.5 = \frac{5.25 - R}{5} \Rightarrow R = 5.25 - 2.5 = 2.75$$

$$\text{Runoff volume} = \frac{1}{2} \times \frac{600 \times 3600}{24} = \frac{25920000}{24} \text{ ft}^3$$

$$\therefore \frac{2.75 \text{ ft}}{12} = \frac{25920000}{\text{Area}}$$

$$\Rightarrow \text{Area} = \frac{25920000 \times 12}{2.75} = 113105454.5 \text{ ft}^2$$

## Hydrograph

DRH = Direct Runoff hydrograph

FH = Flood hydrograph

DRH = FH - base flow

~~DRH~~ \* Unit hydrograph (UH) =  $\frac{\text{DRH}}{\text{rainfall excess (cm)}}$   
↓  
runoff

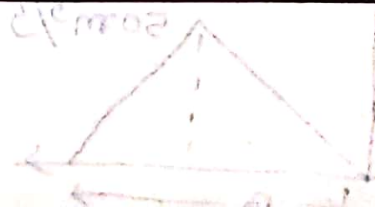
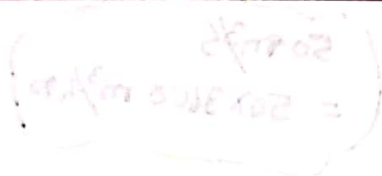
\* Peak flow of UH =  $\frac{\text{Peak of DRH}}{\text{rainfall excess (cm)}}$

\* Runoff volume = Catchment area \* runoff depth

(\* UH for 1cm or 1in (unit) runoff gives DRH)

Flood hydrograph = DRH + base flow

= UH \* runoff + base flow



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\* The peak of flood hydrograph due to a 3h duration isolated storm in a catchment is  $270 \text{ m}^3/\text{sec}$ . The total depth of rainfall is  $5.9 \text{ cm}$ . Assuming an average infiltration loss is  $0.3 \text{ cm/hr}$  and a constant ~~base~~ baseflow of  $20 \text{ m}^3/\text{s}$ . Estimate the peak of the 3-hr unit hydrograph of this catchment.

Sol<sup>n</sup>: Peak of DRH =  $270 - 20 = 250 \text{ m}^3/\text{s}$

~~Peak of UH =  $\frac{250}{3} = 83.33$~~

turnoff,  $R = P - \phi t$

$= 5.9 - 0.3 \times 3$   
 $= 5 \text{ cm}$

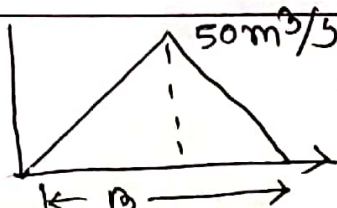
$\therefore$  Peak of UH =  $\frac{250}{5} = 50 \text{ m}^3/\text{s}$  Ans

\* From previous questions, If the area of catchment is  $567 \text{ km}^2$ , determine base width of a 3hr UH by assuming it to be a triangular shape.

Sol<sup>n</sup>: Area of UH = catchment area  $\times 0.01$  <sup>4cm</sup>

$\Rightarrow \frac{1}{2} \times B \times 50 \times 60 \times 60 = 567 \times 10^6 \times 0.01$

$\therefore B = 63 \text{ hours}$  Ans



$50 \text{ m}^3/\text{s}$   
 $= 50 \times 3600 \text{ m}^3/\text{hr}$

~~\*\* A~~

\*\* A unit hydrograph for a 200-acre watershed has a triangular shape and a duration of 4 hrs. What is the max<sup>m</sup> flow rate (cfs) in the unit hydrograph?



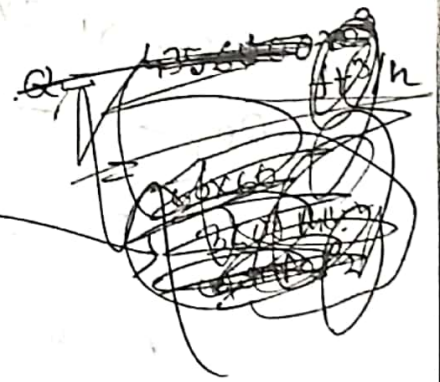
$$A = 200 \text{ acres} = 200 \times 43560 = 8712000 \text{ ft}^2$$

∴ unit hydrograph  
∴ runoff,  $R = 1 \text{ inch} = \frac{1}{12} \text{ ft}$

$$\frac{R}{Q} = \frac{\frac{1}{2} \times 4 \times Q}{8712000}$$

$$\Rightarrow \frac{1}{12} = \frac{2Q}{8712000}$$

$$\Rightarrow Q = 363000 \text{ ft}^3/\text{hr} = 100.83 \text{ ft}^3/\text{sec (cfs)}$$



\* A flood hydrograph of a river draining a catchment of  $189 \text{ km}^2$  due to a 6h isolated storm is in the form of a triangle with a base of 66h and a peak ordinate of  $30 \text{ m}^3/\text{sec}$  occurring at 20 hours from start. Assume zero base flow. Develop 6-hr unit hydrograph for this catchment.

Soln: Runoff volume =  $\frac{1}{2} \times 66 \times (30 \times 60 \times 60)$   
 $= 3564000 \text{ m}^3$

Runoff depth =  $\frac{3564000}{189 \times 10^6}$   
 $= 0.01885 \text{ m}$   
 $= 1.885 \text{ cm}$

Peak of 6hr Unit hydrograph =  $\frac{30}{1.885}$   
 $= 15.909 \text{ m}^3$

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\* A 12hr unit hydrograph of a catchment is of a triangular shape with a base width of 144 hours and a peak discharge of  $23 \text{ m}^3/\text{s}$ . Calculate the catchment area in  $\text{km}^2$ .

Sol<sup>n</sup>

$$\frac{1}{2} \times 144 \times 23 \times 60 \times 60 = \text{Area} \times 0.01 \quad \left( \begin{array}{l} 1 \text{ cm} \\ 1 \text{ m} \end{array} \right)$$

$\rightarrow \text{m}^3/\text{s} \text{ to } \text{m}^3/\text{hr}$

$$\Rightarrow \text{Area} = 59616000 \text{ m}^2 = \cancel{59.616 \text{ km}^2} = 596.16 \text{ km}^2$$

12hr unit hydrograph

$$1 \text{ m} = 0.01 \text{ cm}$$

# Math Problems

DWASA - 12

(1) Rainfall of magnitude 3.8cm & 2.8cm occurring on two consecutive 4hr durations on a catchment of area 22 km<sup>2</sup> produced the following hydrograph of flow at the outlet of the catchment. Estimate the rainfall excess and  $\phi$ -index.

Time (hr)	-6	0	6	12	18	24	30	36	42	48	54	60	66
flow (m <sup>3</sup> /s)	6	5	13	26	21	16	12	9	7	5	5	4.5	4.5

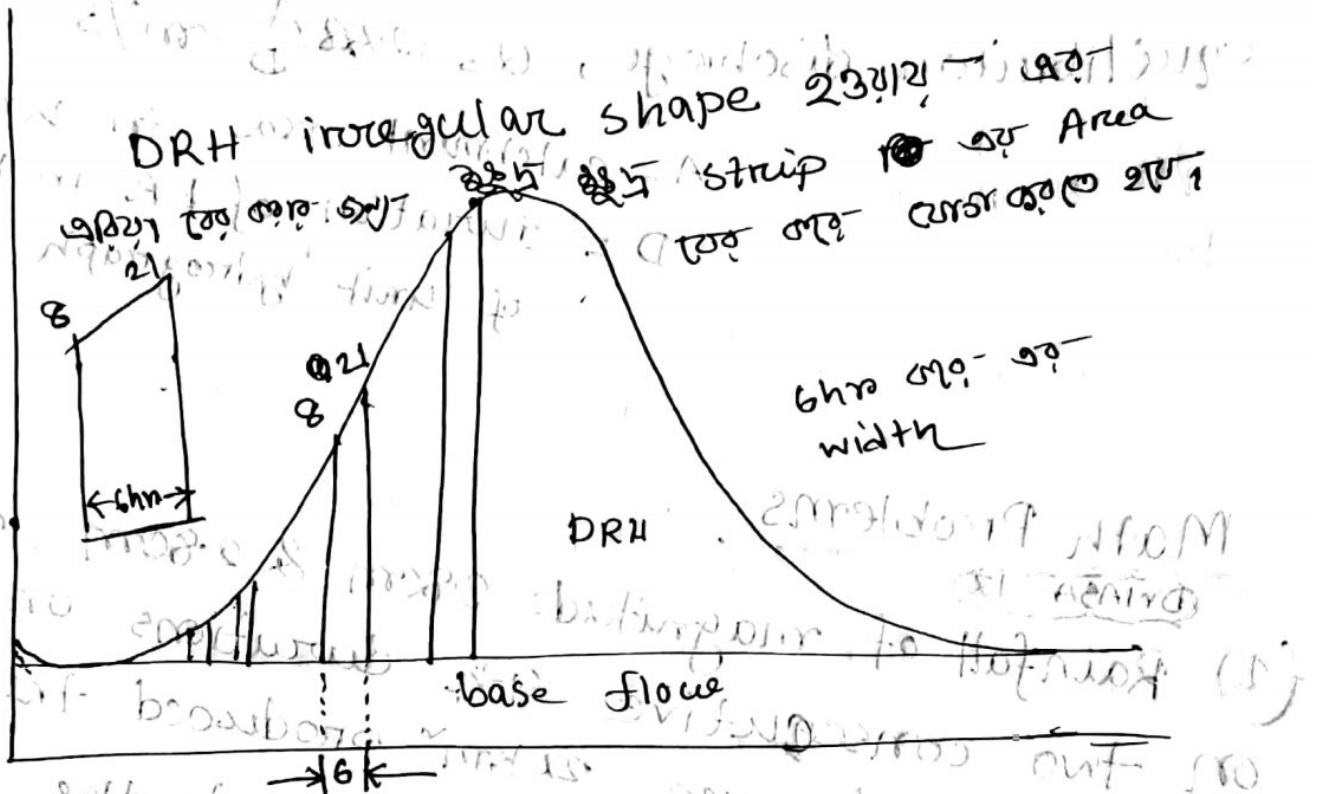
Flood hydrograph

Soln: base flow = 5 m<sup>3</sup>/s

Time (hr)	0	6	12	18	24	30	36	42	48
direct flow (m <sup>3</sup> /s)	0	8	21	16	11	7	4	2	0

[ Flood hydrograph (total flow) - base flow OR from DRH ]  
 [ zero or negative ]

Runoff volume = Area of DRH



$$\text{Runoff volume} = (6 \times 60 \times 60) \times \left[ \frac{1}{2}(0+8) + \frac{1}{2}(8+21) + \frac{1}{2}(21+16) + \frac{1}{2}(16+11) + \frac{1}{2}(11+7) + \frac{1}{2}(7+4) + \frac{1}{2}(4+2) + \frac{1}{2}(2+0) \right]$$

$$= 1.4904 \times 10^6 \text{ m}^3$$

$$\text{Runoff depth} = \frac{\text{Runoff volume}}{\text{catchment area}}$$

$$= \frac{1.4904 \times 10^6}{27 \times 10^6} = 0.0552 \text{ m}$$

$$= 5.52 \text{ cm}$$

∴ rainfall excess = 5.52 cm

$$\text{Total rainfall} = 3.8 + 2.8 = 6.6 \text{ cm}$$

$$\text{Duration} = 4 + 4 = 8 \text{ hrs}$$

$$\phi \text{ index} = \frac{6.6 - 5.52}{8} = 0.135 \text{ cm/hr An}$$

QRE 15

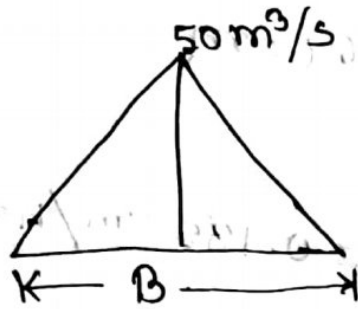
(2) The peak of flood hydrograph due to a 3h duration of isolated storm in a catchment is  $270 \text{ m}^3/\text{s}$ . The total depth of rainfall is  $5.9 \text{ cm}$ . Assuming an average infiltration loss of  $0.3 \text{ cm/h}$  & a constant base flow of  $20 \text{ m}^3/\text{s}$ , estimate the peak of the 3h unit hydrograph of this catchment. If the area of the catchment is  $56 \text{ km}^2$  determine the base width of the 3h unit hydrograph.

Soln: Peak of DRH =  $\frac{\text{Total} - \text{base}}{1} = (270 - 20) \text{ m}^3/\text{s} = 250 \text{ m}^3/\text{s}$

$$\begin{aligned} \text{runoff depth} &= 5.9 \text{ cm} - 0.3 \text{ cm/h} * 3 \text{ h} \text{ infiltration loss} \\ &= (5.9 - 0.9) \text{ cm} \\ &= 5 \text{ cm} \end{aligned}$$

$$\text{Peak of unit hydrograph} = \frac{250}{5} = 50 \text{ m}^3/\text{s} \quad [\because \text{UH area } 1 \text{ cm runoff}]$$

(b)



unit hydrograph to triangular shape  
assume

Area of UH = Volume of 1cm runoff  
Area of catchment x depth

$$\Rightarrow \frac{1}{2} \times B \times 50 \times 3600 = 562 \times 10^6 \times \frac{1}{100}$$

$$= 5620000$$

$$\Rightarrow 90,000 B$$

$$\Rightarrow B = 63 \text{ hr}$$

graph

(hr)

(hr)

$$= 50 \text{ m}^3/\text{s}$$

$$= 2.5 \text{ cm/hr} \times 0.3 \text{ cm/hr} \times 0.3 \text{ cm/hr}$$

cm

Raghunath (amr 3viro no no bhr rainfall 230)

(5) The successive three hourly ordinates of a 6hr UH for a particular basin are 0, 15, 36, 30, 17.5, 8.5, 3, 0 cumec respectively.

The flood peak observed due to a storm was 450 cumec. Assuming a constant base flow of 6 cumec & an average storm loss of 6mm/hr, determine the depth of storm rainfall and the stream flow at successive 3hr interval.

Soln: DRH Peak = flood peak - base flow  
 $= 450 - 6 = 144$  cumec

Runoff =  $\frac{\text{DRH Peak}}{\text{UH Peak}} = \frac{144}{36} = 4$  cm

$\therefore \text{UH peak} = \frac{\text{DRH peak}}{\text{Runoff}}$

depth of storm rainfall = Runoff + loss  
 $= 4 + 6\text{mm/hr} \times 6\text{hr}$   
 $= 4 + 0.6 \times 6 = 7.6$  cm

Second part:

Streamflow (or Flood Hydrograph) at successive 3hr interval =

UH or ordinate (or) DRH  
Runoff or baseflow (or) DRH  
Streamflow or flood hydrograph.

Now, streamflow at successive 3hr intervals are  $0 \times 4 + 6 = 6$ ,  $15 \times 4 + 6 = 66$ ,  $150$ ,  $126$ ,  $76$ ,  $40$ ,  $18$ ,  $6$  cumec respectively.

(6) BUET The hourly ordinate of 6h unit hydrograph for a particular basin is 36 cumec. The flood peak due to 6h storm was 130 cumec. The constant base flow is 6 cumec & avg. loss is 6mm/m. Determine depth of storm rainfall & the streamflow at successive 3hr interval.

Sol<sup>n</sup>: (i) Peak of 6h UH =  $\frac{\text{Peak of DRH}}{\text{rainfall excess}}$

$$\Rightarrow \text{rainfall excess} = \frac{(130 - 6)}{36} = 3.44 \text{ cm}$$

Storm rainfall depth =  $3.44 + 0.6 \times 6 = 7.04 \text{ cm}$  Ans

(ii) Streamflow =  $36 \times 3.44 + 6 = 129.84 \text{ m}^3/\text{sec}$

\* The ordinate of a 2hr unit hydrograph for a catchment are given as:

Time (h)	0	1	2	3	4
ordinate ( $m^3/s$ )	0	5	12	25	41

Calculate the ordinate (in  $m^3/s$ ) of a 4hr unit hydrograph for this catchment at the time of 3h.

Sol<sup>n</sup>

4hr duration  
 5hr

Time (hr)	ordinate of 2hr UH	ordinate of 2hr UH lagged by 2hr	ordinate of 4hr DRH	4hr UH = $\frac{4hr DRH}{2}$
0	0	-	0	0
1	5	-	5	2.5
2	12	0	12	6
3	25	5	30	15
4	41	12	53	26.5
		25	25	12.5
		41	41	20.5

$\therefore$  Ordinate of 4hr UH at 3hr duration is  $15 m^3/s$

2 unit UH  $\rightarrow$  4 unit UH  $\therefore n = \frac{4}{2} = 2$

$\therefore$  4hr UH =  $\frac{4hr DRH}{n}$

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\* The ordinate of a 1hr unit hydrograph at sixty minutes interval are 0, 3, 12, 8, 6, 3, & 0 m<sup>3</sup>/s. A two hour storm of 4cm excess rainfall occurred in a basin from 10AM, considering constant base flow of 20m<sup>3</sup>/s, calculate the flow of the river (in m<sup>3</sup>/s) at 1PM.

Sol<sup>n</sup>:

Time always zero

$2 \div 1 = 2$

Time (hr)	1hr UH	UH of 1hr lagged by 1hr	2hr DRH	2hr UH = $\frac{2 \times \text{DRH}}{2}$
10AM	0	—	0	0
11AM	3	0	3	1.5
12PM	12	3	15	7.5
1PM	8	12	20	10
2PM	6	8	14	7
3PM	3	6	9	4.5
4PM	0	3	3	1.5
		0	0	0

River flow at 1PM = DRH + baseflow

= Rainfall excess  $\times$  UH + baseflow

=  $10 \times 4 + 20$

=  $60 \text{ m}^3/\text{s}$

con & unit

flow value m<sup>3</sup>/s of area



\* ~~If baseflow of 2hr unit hydrograph is~~

\* If base period of 2hr unit hydrograph is 10 hours, calculate the base period of 8hr unit hydrograph.

Sol<sup>n</sup>: base period of 8hr unit hydrograph

$$= \cancel{10} T_{B1} + (n-1) * UH_1$$

$$= 10 + \left(\frac{8}{2} - 1\right) * 2$$

$$= 16 \text{ hours}$$

$$\begin{aligned} & (10 + (8-2)) \\ & = 16 \text{ hrs} \end{aligned}$$

\*  $T_B$  of 3hr UH is 12 hours.  $T_B$  of 9hrs UH is \_\_\_\_\_?

Sol<sup>n</sup>:  $T_{B2} = T_{B1} + (n-1) * UH_1$

$$= 12 + \left(\frac{9}{3} - 1\right) * 3$$

$$= 12 + 2 * 3 = 18 \text{ hrs}$$

\*  $T_B$  of 4hr UH  $\rightarrow$  16 hours

$$T_B \text{ of } 8 \text{ hr UH} = 16 + \left(\frac{8}{4} - 1\right) * 4$$

$$= 20 \text{ hrs}$$

$$(16 + (8-4)) = 20 \text{ hrs}$$

# Maximum Flood Estimation

**Rational Method**

$$Q = \frac{CIA}{3.6}$$

Q = discharge (m<sup>3</sup>/sec)

C = runoff coefficient

I = intensity (mm/hr)

A = Area (km<sup>2</sup>)

$Q = \frac{CIA}{360}$  if A in hectare, I in mm/hr

runoff volume, Yield = CAP

P = Precipitation (rainfall depth)

Yield = runoff volume (m<sup>3</sup>)

Time of concentration: The time of concentration of a drainage basin is the time required by the water to reach the outlet from the most remote point of the drainage area.

Problems BWDB 2016

(1) The value of total direct runoff volume of catchment is  $6 \times 10^6 \text{ m}^3$ . If rainfall depth is 8 cm & runoff coefficient 0.5. Determine the catchment area in  $\text{km}^2$ .

Sol<sup>n</sup>:

$$\text{Yield} = \text{C} \times \text{A} \times \frac{I}{100}$$

$$6 \times 10^6 = 0.5 \times A \times \frac{8}{100}$$

$$\Rightarrow A = 15 \times 10^7 \text{ m}^2$$

$$\Rightarrow A = 150 \text{ km}^2$$

(2) calculate  $\phi$ -index of rain water available for a family having a roof area of  $20 \text{ m}^2$ . Assume  $c = 0.70$ .

Sol<sup>n</sup>:

$$\text{Yield} = \text{C} \times \text{A} \times P$$

$$\Rightarrow P = \frac{\text{Yield}}{\text{C} \times \text{A}}$$

$$= \frac{30}{0.7 \times 20}$$

$$= 2.14 \text{ m}$$

$\phi$  index =  $0.3 \times 214$   
 $= 0.642 \text{ m/year}$   
 \* assume 1 year time duration  
 \* 0.70 of Rainfall runoff  
 21.4 or 0.3 infiltration

(3) Determine the rainwater availability for a roof area of  $5\text{m} \times 5\text{m}$ . Intensity  $25\text{cm/year}$  & runoff coefficient  $0.70$ . (WASA '19)

Sol<sup>n</sup>:

$$A = 5 \times 5 = 25 \text{ m}^2$$

$$I = 25 \text{ cm/year}$$

Rainwater availability

$$Q = CIA$$

$$= 0.7 \times 25 \times 25$$

$$= 437.5 \text{ cm}^3/\text{year}$$

(4) A catchment of area 200 hectare has a runoff coefficient 0.5. A storm duration larger than the time of concentration of the catchment and of intensity  $3.6 \text{ cm/h}$  causes a peak discharge of?

Sol<sup>n</sup>:

$$Q = \frac{CIA}{360}$$

$$= \frac{0.5 \times 36 \times 200}{360}$$

$$= 10 \text{ m}^3/\text{sec}$$

(5) Rainfall intensity 2.4 m/yr. Runoff coefficient 0.2. Find the minimum catchment area of the daily water demand is 15 lpcd of 7 people.

Sol<sup>n</sup>:

$$\begin{aligned}
 Q &= 15 \text{ lpcd} \text{ - daily} \times 7 \\
 &= 15 \text{ litre/day} \times 7 \\
 &= 15 \times 10^{-3} \text{ m}^3/\text{day} \times 7 \\
 &= 105 \times 10^{-3} \text{ m}^3/\text{day}
 \end{aligned}$$

$$Q = CIA$$

$$\begin{aligned}
 \Rightarrow A &= \frac{Q}{CI} \\
 &= \frac{105 \times 10^{-3} \times 365}{0.2 \times 2.4} \\
 &= 22.81 \text{ m}^2
 \end{aligned}$$

DNCC '16

(6) Rainfall were applied at constant rate to an impervious surface area of 6 acre. Using rational method calculate peak rate of rainfall (in cfs). Intensity of rainfall 1.5 inch/hr

Soln:

Impervious,  $C = 1$   
 $Q = CIA$

$$\frac{R}{P_{10}} = 1$$

$$1 \text{ acre} = 43560 \text{ ft}^2$$

$$\Rightarrow Q = 1 \times \frac{1.5}{12} \times 6 \times 43560$$

$$= 19820 \text{ ft}^3/\text{hr}$$

$$= 32670 \text{ ft}^3/\text{hr}$$

$$= 9.075 \text{ cfs}$$

\* A watershed of 1500 ha is discharging through a drain at an average rate of  $2.5 \text{ m}^3/\text{sec}$ . Calculate the drainage coefficient. If the drainage coefficient is  $3 \text{ cm}/\text{day}$ , what would be the discharge through the drain?

Sol<sup>n</sup>: (i) Drainage coefficient,  $c = \frac{2.5 \times 3600 \times 24 \text{ m}^3/\text{day}}{1500 \times 10^4 \text{ m}^2}$

$$= 0.0144 \text{ m}/\text{day}$$

$$= 1.44 \text{ cm}/\text{day} \quad \underline{A}$$

~~(ii) Drainage coefficient,  $c = \frac{3}{100} = \frac{3}{1500 \times 10^4}$~~

$$Q = \frac{3}{100} \times 1500 \times 10^4$$

(ii)  $Q = AC$

$$= (1500 \times 10^4) \times \frac{0.03 \text{ m}}{24 \times 3600}$$

$$= 5.21 \text{ m}^3/\text{sec} \quad \underline{A}$$

$$Q = A \frac{1}{m} AR^{2/3} S^{1/2}$$

(4) A culvert is designed for a flood frequency of 100 years & a useful life of 20 years. Risk?

Sol<sup>n</sup>:  $T = 100, n = 20$

$$\begin{aligned} \text{Risk} &= 1 - q^n \\ &= 1 - (1 - P)^n \\ &= 1 - \left(1 - \frac{1}{100}\right)^{20} \\ &= 18.2\% \end{aligned}$$

(5) The probability that the annual max<sup>m</sup> flood discharge will exceed 25000 m<sup>3</sup>/s, at least once in next 5 years is 0.25. what is the return period?

Sol<sup>n</sup>:

$$\begin{aligned} \text{Risk} &= 0.25 \\ \Rightarrow 1 - q^n &= 0.25 \\ \Rightarrow 1 - (1 - P)^n &= 0.25 \\ \Rightarrow 1 - \left(1 - \frac{1}{T}\right)^n &= 0.25 \\ \Rightarrow 1 - \left(1 - \frac{1}{T}\right)^5 &= 0.25 \\ \Rightarrow T &= 18 \text{ years} \end{aligned}$$

(6) A bridge has an expected life of 25 years and is designed for a flood magnitude of return period 400 years. What is the risk of the hydraulic design? If a 10% risk is acceptable what return period will have to be adopted? **WRE 15**

Sol<sup>n</sup>:  $n = 25$  years  
 $T = 100$   
 $P = 0.01$

$$\text{Risk} = 1 - (1 - P)^n$$

$$= 1 - (1 - 0.01)^{25}$$

$$= 0.22$$

$$= 22\%$$

Part b: Risk = 10%

$$\Rightarrow 0.10 = 1 - (1 - P)^{25}$$

$$\Rightarrow (1 - P)^{25} = 1 - 0.10 = 0.9$$

$$\Rightarrow 1 - P = 0.995$$

$$\Rightarrow P = 0.004$$

$$\Rightarrow T = 237.78 \text{ years}$$

(8) Determine the percentage chance that a 25 years storm may occur

(i) In the next 10 years (b) In the next year

(iii) may not occur in another 15 years

Sol<sup>n</sup>:

$$\begin{aligned} \text{(i) Risk} &= 1 - (1 - \frac{1}{25})^{10} \\ &= 1 - (1 - 0.04)^{10} \\ &= 1 - (0.96)^{10} \\ &= 33.5\% \end{aligned}$$

$$\text{(ii) Risk} = 1 - (1 - \frac{1}{25})^1 = 4\%$$

$$\begin{aligned} \text{(iii) Reliability} &= (1 - \frac{1}{25})^{15} \\ &= (0.96)^{15} \\ &= 54.21\% \end{aligned}$$

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\* A culvert is designed for a flood frequency of 100 years and a useful life of 20 years. Calculate the risk involved in the design of the culvert.

Sol<sup>n</sup>

$$\text{Risk} = 1 - \left(1 - \frac{1}{T}\right)^n$$

$$= 1 - \left(1 - \frac{1}{100}\right)^{20}$$

$$= 0.182$$

$$= 18.2\%$$

\* The probability that the annual max<sup>m</sup> flood discharge will exceed 25000 m<sup>3</sup>/s, at least once in next 5 years is found to be 0.25. Calculate the return period of this flood event.

Sol<sup>n</sup>

$$\text{Risk} = 1 - \left(1 - \frac{1}{T}\right)^n$$

$$\Rightarrow 0.25 = 1 - \left(1 - \frac{1}{T}\right)^5$$

$$\Rightarrow \left(1 - \frac{1}{T}\right)^5 = 1 - 0.25 = 0.75$$

$$\Rightarrow 1 - \frac{1}{T} = \sqrt[5]{0.75} = 0.94408$$

$$\Rightarrow \frac{1}{T} = 1 - 0.94408 = 0.056$$

$$\therefore T = 17.885 \text{ years}$$

(9) For a river valley project, the following results were obtained from flood frequency analysis using Gumbel's method.

<u>Return Period</u>	<u>Peak flood (m<sup>3</sup>/sec)</u>
40	22000
80	31000

Estimate the flood magnitude with a return period of 240 years. **BWDB 2020, SGFL 23**

Soln: Try solving using  $k = 0.28 \ln T - 0.45$

$$x_T = \bar{x} + (0.28 \ln T - 0.45) \sigma_{n-1} \quad \text{--- (i)}$$

$$\Rightarrow 22000 = \bar{x} + (0.28 \ln 40 - 0.45) \sigma_{n-1} \quad \text{--- (ii)}$$

$$\Rightarrow 31000 = \bar{x} + (0.28 \ln 80 - 0.45) \sigma_{n-1} \quad \text{--- (iii)}$$

$$(iii) - (ii) \Rightarrow 9000 = \sigma_{n-1} \left( 0.28 \ln \frac{80}{40} \right)$$

$$\Rightarrow \sigma_{n-1} = \frac{9000}{0.541} = 7398.436$$

Now from eq<sup>n</sup> (i),  $\bar{x} = 22000 - (0.28 \ln 40 - 0.45) * 7398.436$   
 $= 3041.584$

$$\therefore x_{240} = \bar{x} + (0.28 \ln 240 - 0.45) * 7398.436 = 37340 \text{ m}^3/\text{sec}$$

(12) The annual floods for a large period were statically analysed by Gumbel's method, which yielded  $\bar{Q} = 19000$  cumec,  $\sigma = 3200$  cumec

Determine

- (i) the probability of flood magnitude of 30,000 cumec occurring in the next year -  
 (ii) The flood magnitude of 5 yr return period

Sol<sup>n</sup>: (i) ~~2.4~~

$$30,000 = 19000 + (0.2817 - 0.45) * 3200$$

$$\Rightarrow T = 146.05$$

$$\begin{aligned} \text{Risk} &= 1 - 2^{-T} \\ &= 1 - (1 - P)^{1/T} \\ &= 1 - \left(1 - \frac{1}{146.05}\right) \\ &= 1 - 0.99 \\ &= 0.01 = 1\% \end{aligned}$$

(ii)  $x_5 = 19000 + (0.28175 - 0.45) * 3200$   
 $= 21572 \text{ m}^3/\text{sec}$  Ans

(13) Statistical analysis of the annual floods of the river Tapti using Gumbel's method yielded the 100-yr & 10 yr floods as 42800 & 22700 cumec respectively. Determine

- (a) the magnitude of a 20 yr flood  
 (b) the probability of a flood magnitude 3500 cumec (i) occurring in next 10 years  
 (ii) in the next year itself

Sol<sup>n</sup>:

$$42800 = \bar{x} + (0.78 \ln 100 - 0.45) \sigma_{n-1} \quad (i)$$

$$22700 = \bar{x} + (0.78 \ln 10 - 0.45) \sigma_{n-1} \quad (ii)$$

$$(i) - (ii) \Rightarrow 20100 = \sigma_{n-1} \left( 0.78 \ln \frac{100}{10} \right)$$

$$\Rightarrow \sigma_{n-1} = 1191.43$$

From eq<sup>n</sup> (i)

$$\bar{x} = 42800 - (0.78 \ln 100 - 0.45) * 1191.43$$

$$= 2636.15$$

(a)  $x_{20} = 2636.15 + (0.78 \ln 20 - 0.45) * 1191.43$   
 $= 28750 \text{ cumec}$   
 $= 78.750 \text{ tcm}$

$$(b) \quad 35000 = 2636.15 + (0.78 \ln T - 0.45) * 11191.43$$

$$\Rightarrow T = 4.1 \text{ years}$$

(i) occurring in next 10 years

$$\text{Risk} = 1 - (1 - P)^{10}$$

$$= 1 - \left(1 - \frac{1}{4.1}\right)^{10}$$

$$= 22\%$$

(ii) occurring in next year

$$\text{Risk} = 1 - \left(1 - \frac{1}{4.1}\right)^1 = 0.244\%$$

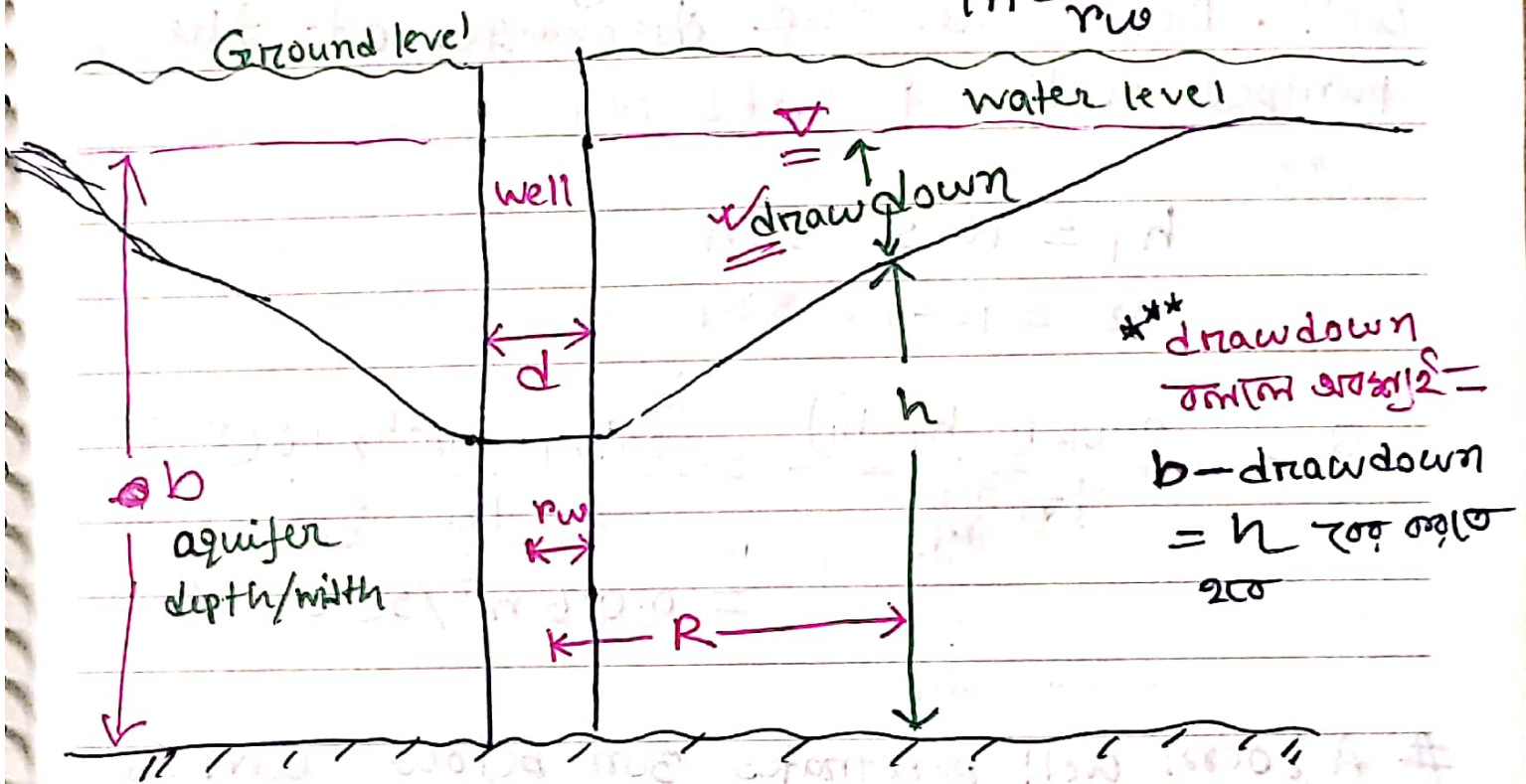
$$= 2.44\% \quad \text{Ans}$$

discharge in unconfined aquifer,

$$Q = \frac{\pi K (H^2 - H_w^2)}{\ln \frac{R}{r_w}}$$

discharge in confined aquifer,

$$Q = \frac{2\pi K b (H - H_w)}{\ln \frac{R}{r_w}}$$



\*  $T = \text{Transmissibility (unit: mm}^2/\text{hr)}$   
 $= K b$   $\leftarrow$   $\begin{matrix} \text{depth} \\ \text{width} \end{matrix}$  of aquifer

$K = \text{hydraulic conductivity}$   
 unit mm/hr

\* artesian = confined aquifer

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# An artesian aquifer 10m thick with piezometric surface 40m above the bottom confining layer is being pumped by a fully penetrating well. The aquifer is medium sand ( $k = 1.5 \times 10^{-4} \text{ m/s}$ ) steady state drawdown of 5m & 1m are observed at two non-pumping wells located 20m & 200m respectively from the pumped well. Determine the discharge at the pumped well [SGFL'17]

Sol<sup>n</sup>:

$$h_1 = 10 - 5 = 5 \text{ m}$$

$$h_2 = 10 - 1 = 9 \text{ m}$$

$$Q = \frac{2\pi k B (h_2 - h_1)}{\ln \frac{r_2}{r_1}} = \frac{2\pi \times 1.5 \times 10^{-4} \times 10 (9 - 5)}{\ln \frac{200}{20}}$$
$$= 0.016 \text{ m}^3/\text{sec} \quad \underline{\underline{A}}$$

# A 20cm well penetrates 30m below GWT. After a long period of pumping at a rate of 1800 lpm, the drawdowns in the observation wells at 12m & 36m from the pumped well are 1.2m & 0.5m respectively. Determine transmissibility of the aquifer.

Sol<sup>n</sup>:

$$Q = \frac{\pi k (h_2 - h_1)}{\ln \frac{r_2}{r_1}}$$

$$h_1 = (30 - 1.2) \text{ m}$$
$$= 28.8 \text{ m}$$

$$h_2 = (30 - 0.5) \text{ m}$$
$$= 29.5 \text{ m}$$



$$= \frac{1.8}{60}$$

$$= \frac{\pi k (29.5 - 28.8)}{\ln \frac{36}{12}}$$

$$\Rightarrow k = 2.57 \times 10^{-4} \text{ m/s}$$

$$= 22.2 \text{ m/day}$$

$$\therefore T = kH$$

$$= 22.2 \times 30$$

$$= 666.14 \text{ m}^2/\text{day}$$

∴ math of  
artesian well  
w/ thickness of  
aquifer,  $2H$   
∴ unconfined  
aquifer

# A well fully penetrates a 25m thick confined aquifer. After a long period of pumping at a constant rate of  $0.05 \text{ m}^3/\text{sec}$ , the drawdowns at a distance of 50m & 150m from the well ~~were~~ were observed to be 3 & 1.2m respectively. Determine hydraulic conductivity & transmissibility.

$$\frac{Q}{2\pi k} = \frac{2\pi k \times 25 (23.8 - 22)}{\ln\left(\frac{150}{50}\right)}$$

$$\therefore k = 1.94 \times 10^{-4} \text{ m/sec}$$

$$T = 1.94 \times 10^{-4} \times 25 = 4.85 \times 10^{-3} \text{ m}^2/\text{sec}$$

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# A 100mm diameter tube well is sunk ~~40m~~<sup>40m</sup> below static groundwater level. The depth & water in tubewell while pumping is 33m. The radius of drawdown is 30m & the coefficient of permeability of the aquifer = 0.50 lps/m<sup>2</sup>. Calculate the [BWD B'22]

Sol<sup>n</sup>:

$$Q = \frac{\pi k (h_w - h_0)}{\ln \frac{R}{r_w}}$$

$$= \frac{\pi \times 0.50 \times 10^{-3} \times (40 - 33)}{\ln \left( \frac{30}{0.05} \right)}$$

$$= 0.125 \text{ m}^3/\text{s} \quad \underline{\underline{A}}$$

$$r_w = \frac{100}{2} = 50 \text{ mm} = 0.05 \text{ m}$$

$$k = \frac{0.50 \times 10^{-3} \text{ m}^3/\text{s}}{\text{m}^2} = 0.50 \times 10^{-3} \text{ m/s}$$

A tube-well of 20cm dia fully penetrates a horizontal, homogeneous and isotropic confined aquifer of infinite horizontal extent. The aquifer is of 30m uniform thickness. A steady pumping at the rate of 40 litres/sec from the well for a long time results in a steady drawdown of 4m at the well face. The subsurface flow to the well due to pumping is steady, ~~horizontal~~ and the radius of influence line is 245m. Calculate the hydraulic conductivity of the aquifer in m/day.

Sol<sup>n</sup>

$$Q = \frac{2\pi k b (h_2 - h_1)}{\ln\left(\frac{R}{r}\right)}$$

$$\Rightarrow 40 \times 10^{-3} \text{ m}^3/\text{s} = \frac{2\pi \times k \times 30 \times 4}{\ln\left(\frac{245}{\frac{0.2}{2}}\right)}$$

drawdown

$$\begin{aligned} \text{dia} &= 0.2 \text{ m} \\ \therefore r &= \frac{0.2}{2} \end{aligned}$$

$$\Rightarrow k = 4.14 \times 10^{-4} \text{ m/s}$$

$$\Rightarrow k = 4.14 \times 10^{-4} \times 60 \times 60 \times 24 \text{ m/day}$$

$$\Rightarrow \textcircled{\ast} k = 35.77 \text{ m/day} \quad \text{A}$$

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\* A 100mm diameter tube well is sunk to 35m below in an unconfined aquifer. The depth of water in the tube well while pumping is 30m and the radius of influence is 30m. If the discharge is 33.4 lps, calculate the co-efficient of permeability of the aquifer. [WARPO'2017]

Sol<sup>n</sup>:

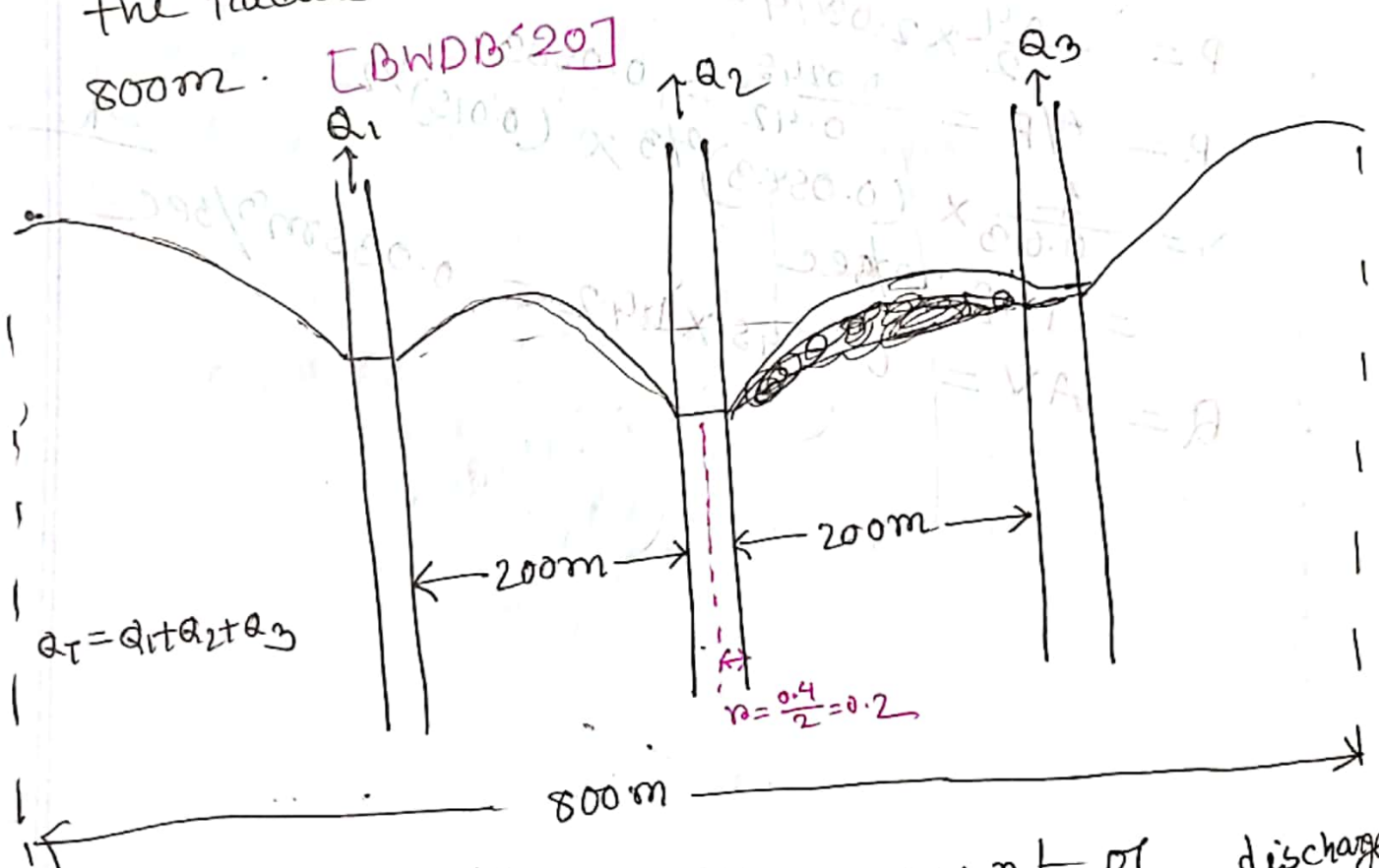
$$Q = \frac{\pi k (H^2 - H_w^2)}{\ln\left(\frac{R}{r_w}\right)}$$

$$\Rightarrow 33.4 \times 10^{-3} = \frac{\pi k \times (35^2 - 30^2)}{\ln\left(\frac{30}{\frac{0.1}{2}}\right)}$$

$$\Rightarrow k = 5 \times 10^{-4} \text{ m/s} = 3 \text{ cm/min}$$

$$Q = 33.4 \text{ l/s} \\ = 33.4 \times 10^{-3} \text{ m}^3/\text{s}$$

\* Three pumping wells located along a straight line are spaced at 200m apart. What should be the steady-state pumping rate from ~~which~~ each well so that the near steady-state drawdown in each well will not ~~exceed~~ exceed 2m? The transmissibility of the confined aquifer is  $2400 \text{ m}^2/\text{day}$  and all the wells are  $\frac{40\text{cm}}{}$  in dia. The thickness of the aquifer is 40m and the radius of influence of each well is 800m.



~~The~~ For the same amount of discharge ( $Q_T$ ), draw down in the middle well (2) will

$$T = KB$$

be more. Therefore, the draw down in this well governs.

The drawdowns in well 2 due to pumping in wells 1, 2 & 3 are respectively.

$$S_{22} = \frac{Q}{2\pi T} \ln \frac{800}{0.2}$$

$$= \frac{Q}{2\pi \times \frac{2400}{24}} \ln \frac{800}{0.2}$$

$$= 0.0132 Q$$

$$Q = \frac{2\pi T s_w}{\ln \frac{R}{r_0}}$$

$$S_{21} = \frac{Q}{2\pi \times \frac{2400}{24}} \ln \frac{800}{200} = 0.0022 Q$$

$$S_{21} = S_{23} = 0.0022 Q \text{ in well (2)}$$

$$\therefore \text{Total draw down } (S) = 0.0132 + 0.0022 Q + 0.0022 Q$$

$$= 0.0176 Q$$

$$\therefore Q = \frac{2}{0.0176} = 113.55 \text{ m}^3/\text{hr} \times \frac{\text{A}}{\text{hr}}$$

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\* Residence time ~~is~~ is the average duration of a particle of water to pass through a phase of the hydrological ~~cycle~~ cycle. ~~is~~  
~~as the~~ [BIWTA '23]

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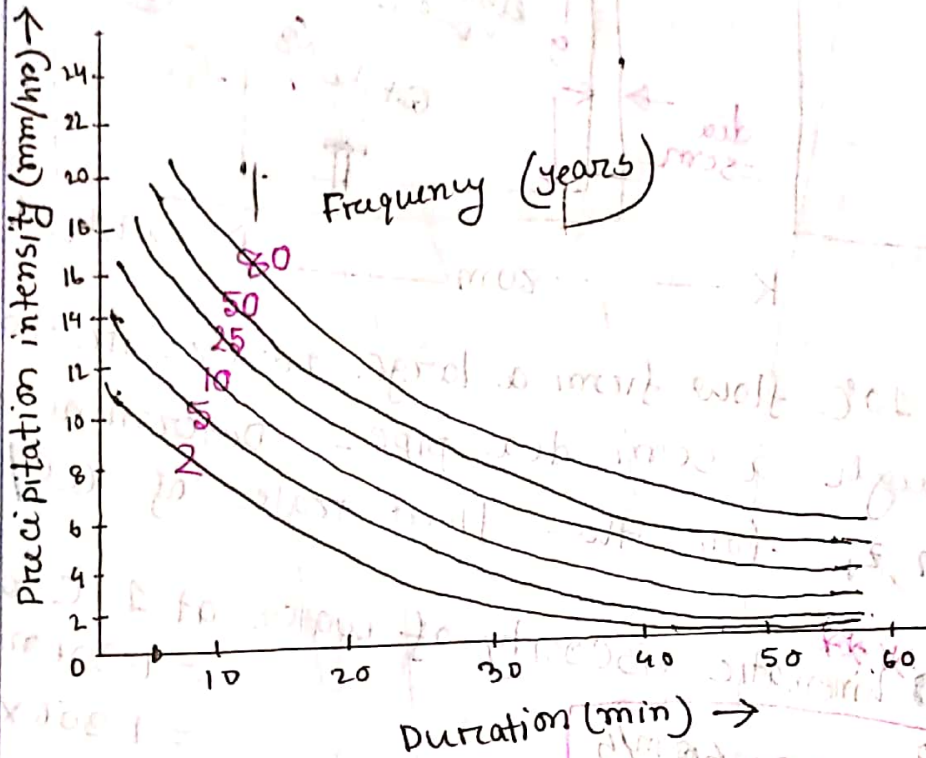
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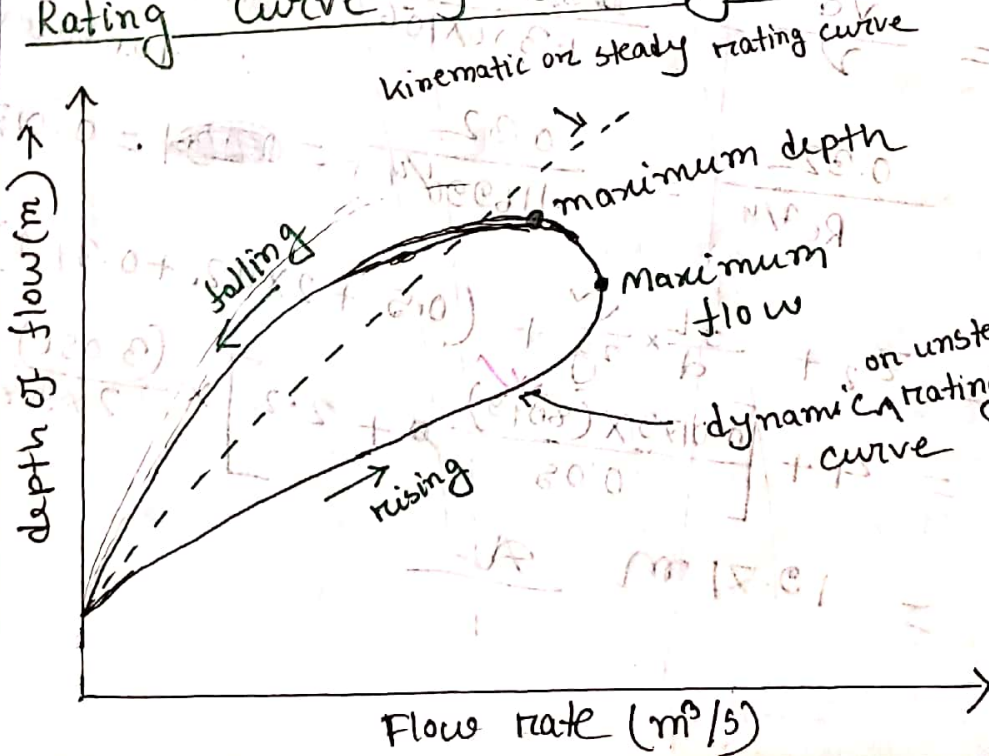
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## Intensity - Duration - Frequency (IDF) curves:

[DWASA '21]



## Rating Curve of Unsteady flow: [DWASA '21]



\* Why using a manometer is important?

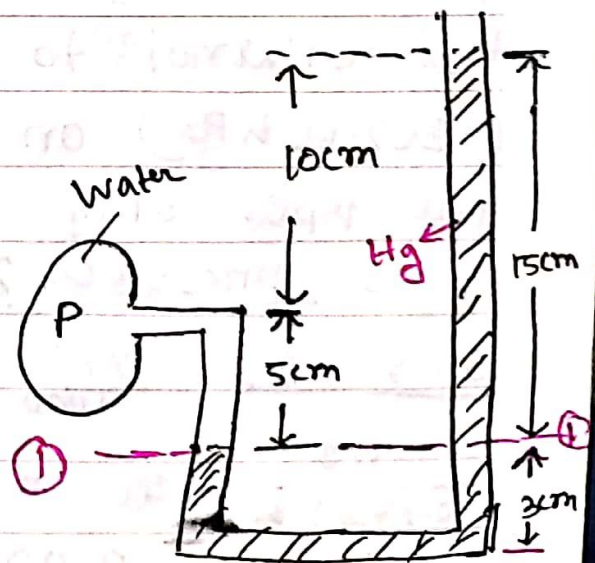
A manometer is an instrument which is widely used for many industrial applications, this device can be used to measure the pressure difference between two points in a pipe or it can also be used to determine the pressure difference between two pipes.

\* A U-tube manometer containing Hg (sp. gr 13.6) has its right limb open to the atmosphere, the left limb is full of water and is connected to a pipe containing water under pressure. Find the pressure of water in the pipe above the atmosphere for the manometer ~~read~~ below —

Sol<sup>n</sup> At section (1-1)

$$P + \frac{5 \times 9.81}{100} = \frac{15}{100} \times 13.6 \times 9.81$$

$$\Rightarrow P = 19.52 \text{ kN/m}^2$$

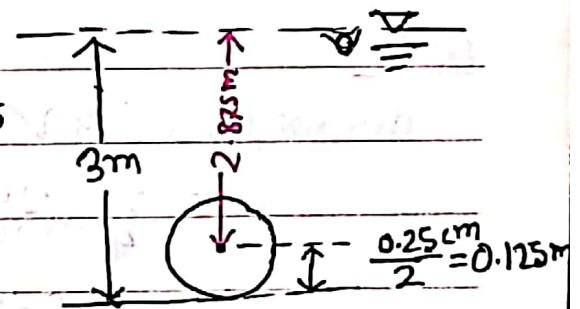


\* A rectangular tank of 5m length, 3m width and 2.5m height. Calculate pressure force at the bottom of the tank. [BPDB'21]

Sol<sup>n</sup>: Force,  $F = A \gamma h$   
 $= (5 \times 3) \times 9.81 \times 2.5 = 367.875 \text{ N}$

# What is the resultant force on one side of a 25cm diameter vertical circular plate standing at the bottom of 3m pool of water? [SGFL'17]

Sol<sup>n</sup>:  $F = A \gamma \bar{x}$   
 $= \frac{\pi}{4} \times (0.25)^2 \times 9.81 \times 2.875$   
 $= 1.38 \text{ kN}$



# Determine the total pressure on a circular plate of diameter 1.5m which is placed vertically in water in such a way that the centre of the plate is 3m below the free surface of water. Find the position of centre of pressure also.

Sol<sup>n</sup>:  $F = \frac{\pi}{4} \times (1.5)^2 \times 9.81 \times 3 = 52 \text{ kN}$



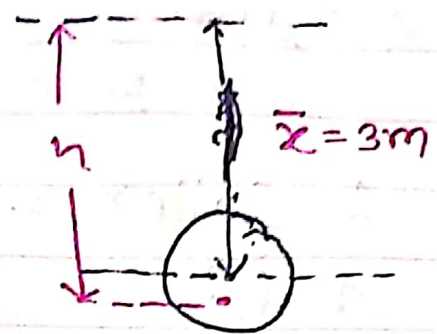
P.T.O

Position of centre of pressure,

$$h = \frac{I_G}{A \bar{x}} + \bar{x}$$

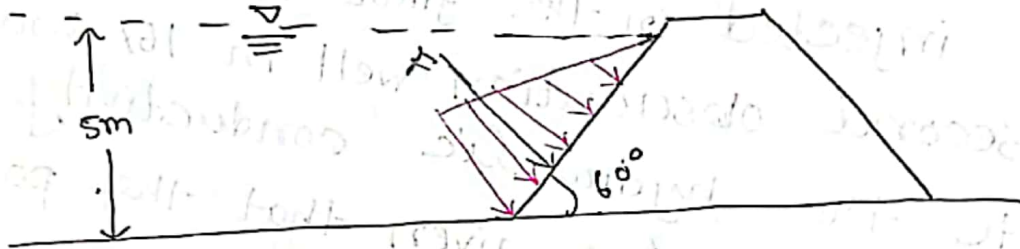
$$= \frac{\frac{\pi}{64} \times (1.5)^4}{\frac{\pi}{4} \times (1.5)^2 \times 3} + 3$$

$$= 3.05 \text{ m}$$



Ans, resultant force is 52 kN and its position is 3.05 m from the top surface of water.

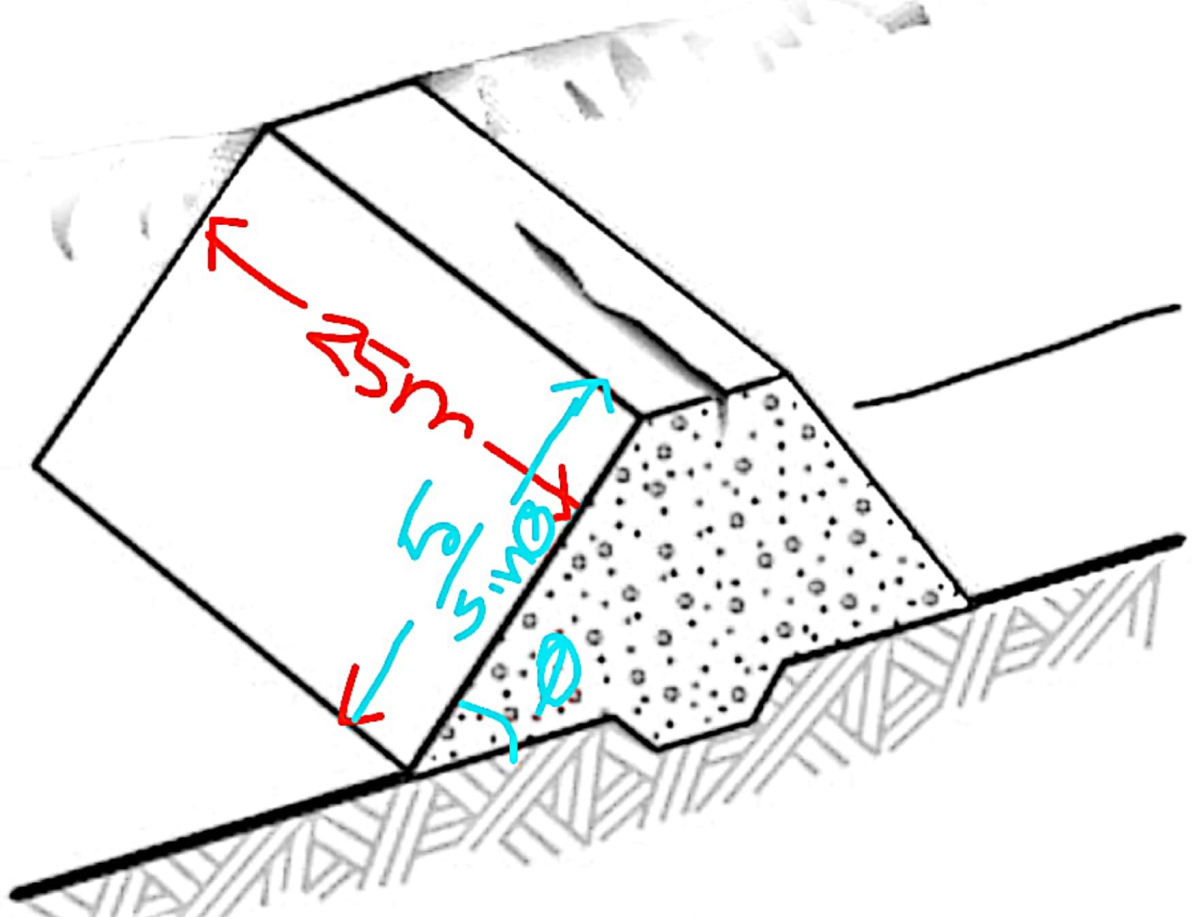
\* Determine the hydrostatic force and the location of the center of pressure on the 25m long dam shown below. The face of the dam is at an angle of  $60^\circ$ .

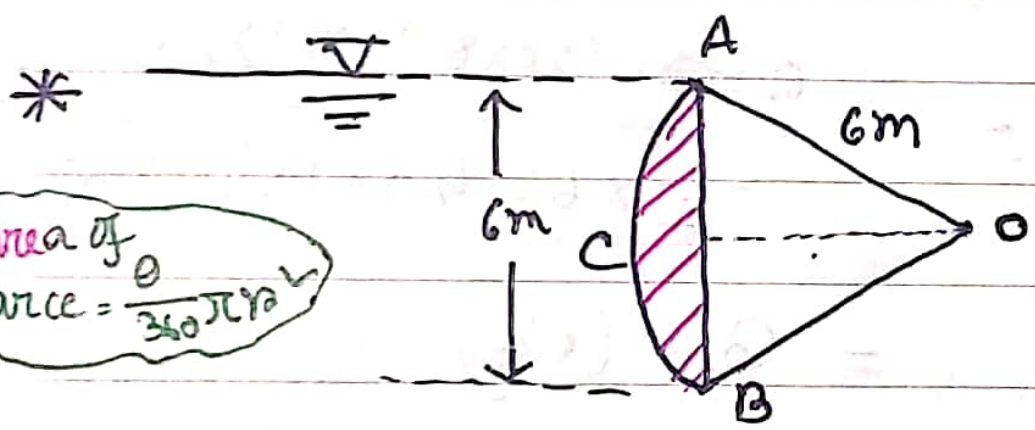
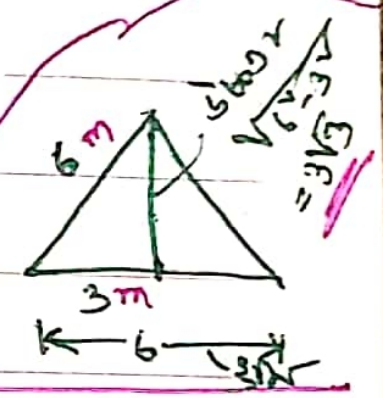


Sol<sup>n</sup>:  $A = 25 \times \frac{5}{\sin 60^\circ} = 144.3376 \text{ m}^2$

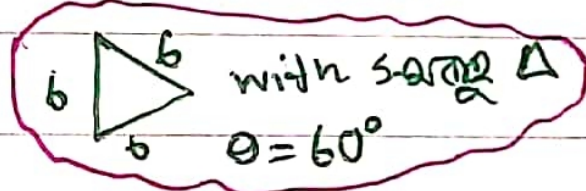
Force,  $F = \rho \bar{x} A = 9.81 \times \frac{5}{2} \times 144.3376$   
 $= 3539.88 \text{ kN}$   
 $= \text{3539.88 kN}$

Center of pressure  $= \frac{2}{3} \times 5 = 3.33 \text{ m}$





Calculate resultant force  
[BEPZA'16]



area of  
arc =  $\frac{\theta}{360} \pi r^2$

Sol<sup>n</sup>:  $F_x = \frac{1}{2} \gamma h^3 = \frac{1}{2} \times 9.81 \times 6^3 = 176.58$  kN

$F_y = \gamma \times \text{area} \times \text{width}$   
 $= \gamma \times \text{volume}$

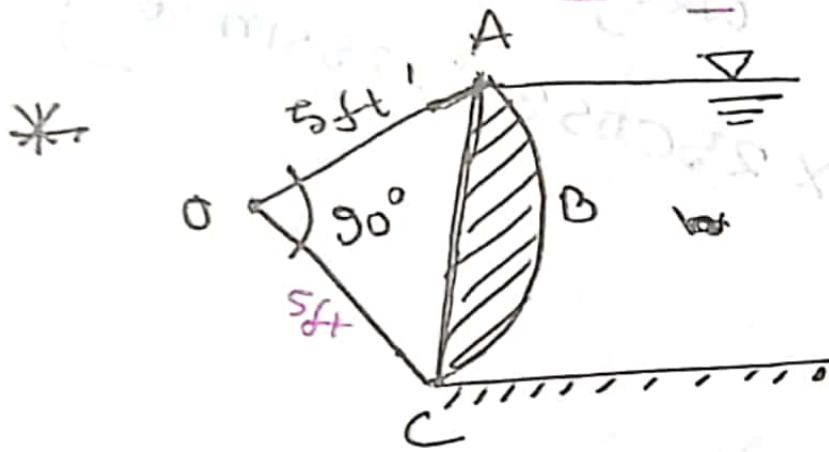
$F_y = \text{self weight of water of ABC equivalent}$   
 $= \text{width} \times [\text{area of arc OACB} - \text{area of OAB}] \times 9.81$

taking  
1m width

$= 1 \times \left[ \frac{60}{360} \times \pi \times 6^2 - \frac{1}{2} \times 6 \times 3\sqrt{3} \right] \times 9.81$   
 $= 32$  kN

$\therefore$  Resultant,  $R = \sqrt{(176.58)^2 + (32)^2} = 179.45$  kN,  $\theta = \tan^{-1} \frac{32}{176.58} = 10.27^\circ$





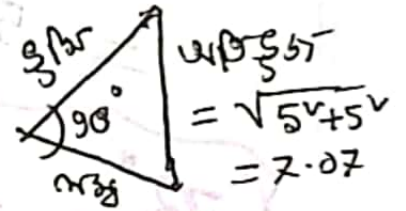
Curved wall ABC

width 9 ft

compute horizontal, vertical & Resultant force.

Sol<sup>n</sup>

$$F_H = \gamma A \bar{x} = 62.43 \times (7.07 \times 9) \times \frac{7.07}{2} = 14046.75 \text{ lb}$$



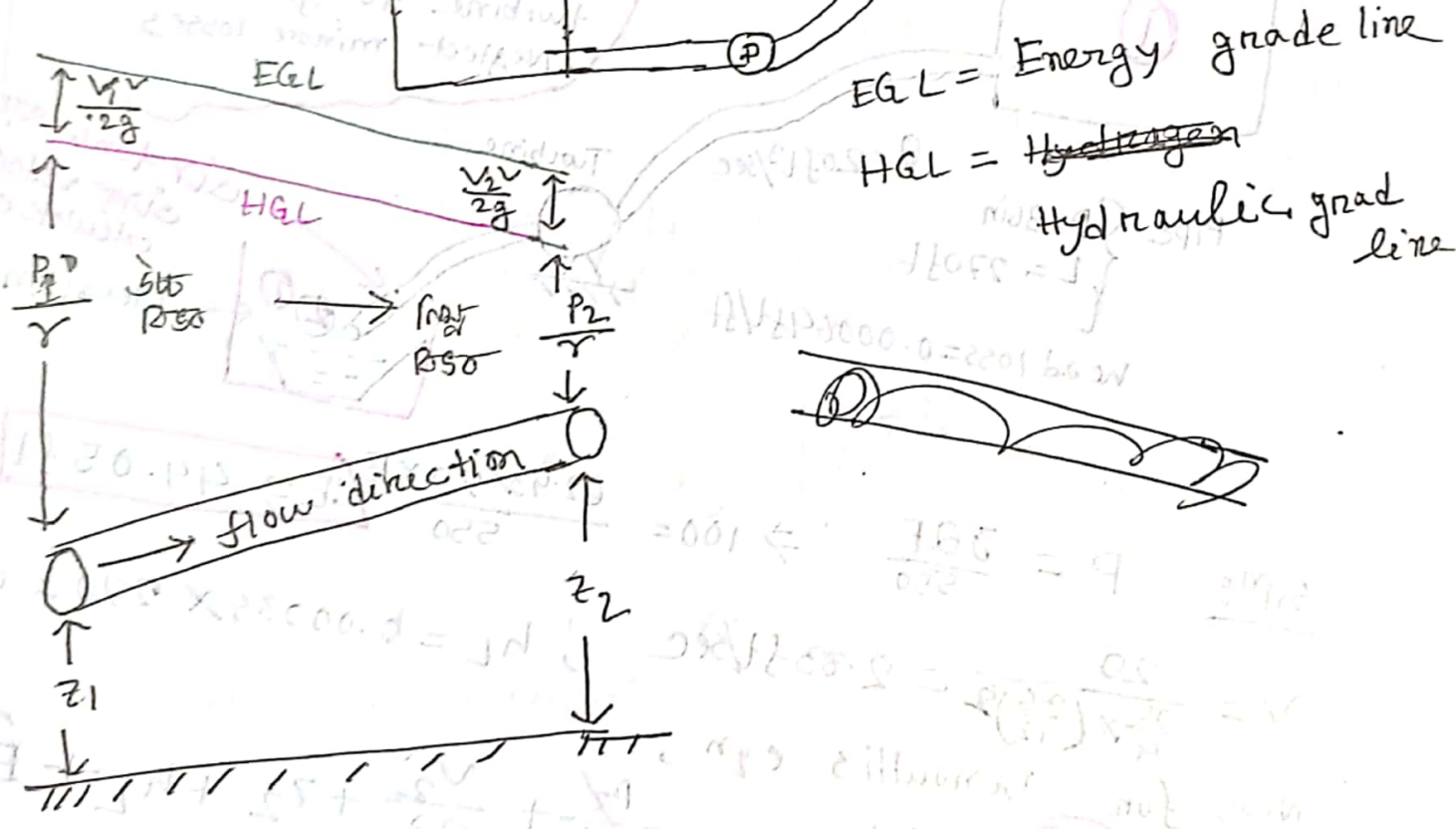
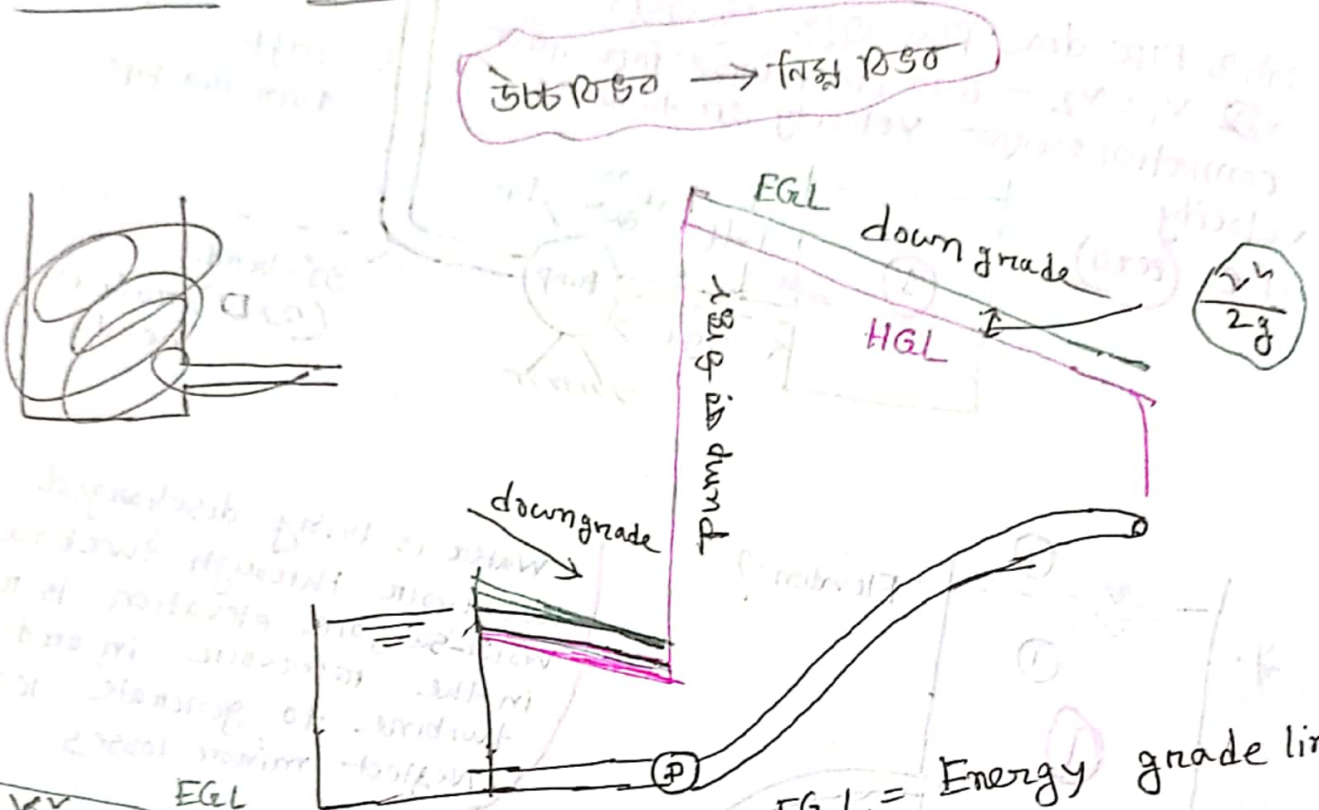
$F_V =$  weight of (imaginary) water in hatched area

$$= \cancel{62.43} \times \left[ \frac{\pi \times 5^2}{4} - \frac{1}{2} \times 5 \times 5 \right] \times \text{width}$$

$$= \text{unit weight} \times \left[ \text{ARC AOCB} - \Delta AOC \right] \times \text{width}$$

$$= 62.43 \times \left[ \frac{\pi \times 5^2}{4} - \frac{1}{2} \times 5 \times 5 \right] \times 9 = 4008.91 \text{ lb}$$

ARC AOCB  
=  $\frac{\text{circle}}{4}$



# Pizometer is what? uses?

→ Pizometer is a device which measures the height at which a column of liquid ~~is~~ rises against gravity in a system.

In geotechnical engineering, pizometer is used to measure pore water pressure in the soil, earth/rock fills, foundations & concrete structures.

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\* The reading of pitot tube ~~is~~ and piezometer are 40cm and 30cm respectively. calculate the velocity of the pipe. [BIWIA '23]

Sol<sup>n</sup>:

Pitot tube =  $\frac{v^2}{2g}$  head

Piezometer = Pore water pressure head

∴ Velocity head = (Pitot tube - Piezometer) reading

$$\Rightarrow \frac{v^2}{2g} = (40 - 30) \text{ cm} = 0.1 \text{ m}$$

$$\therefore v = \sqrt{2 \times 9.81 \times 0.1} = 1.4 \text{ m/s}$$

# A water reservoir is under a pressure of 490 kN/m<sup>2</sup>. Find the theoretical rate at which water in it is escaped through a circular orifice of 2.5cm dia.

Sol<sup>n</sup>:

$$H = \frac{p}{\gamma} = \frac{490}{9.81} = 49.95 \text{ m}$$

Orifice dia  
2.5 cm

$$\therefore Q = A\sqrt{2gh}$$

$$= \frac{\pi}{4} \times \left(\frac{2.5}{100}\right)^2 \times \sqrt{2 \times 9.81 \times 49.95}$$

$$\text{premiaflex} = 0.0154 \text{ m}^3/\text{s} \quad \underline{A}$$

# A circular pipe with 10 cm diameter having flow with an average velocity of  $10 \text{ m s}^{-1}$ .

Calculate the discharge in lps. Also calculate the velocity of another end of the pipe with gradual diameter of 20 cm. [BPDB'21]

Sol<sup>n</sup>

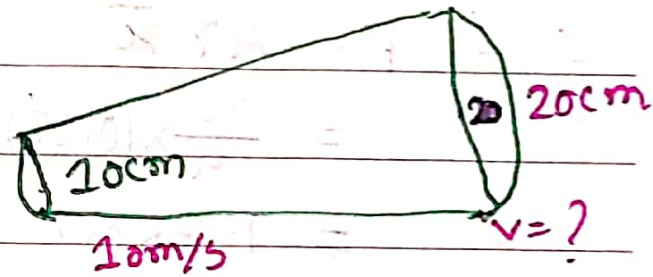
$$\text{discharge, } Q = AV$$

$$= \frac{\pi}{4} \times \left(\frac{10}{100}\right)^2 \times 10$$

$$= 0.0785 \text{ m}^3/\text{s}$$

$$= 0.0785 \times 10^3 \text{ lps}$$

$$= 78.5 \text{ lps}$$



Discharge throughout the pipe is constant.

$$\therefore A_1 V_1 = A_2 V_2$$

$$\Rightarrow V_2 = \frac{A_1}{A_2} \times V_1$$

$$= \frac{10^2}{20^2} \times 10 = 2.5 \text{ m/s}$$



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# A pipe discharge  $40 \text{ m}^3/\text{s}$ . Head loss is 10% of the velocity head difference. Find out pressure at point B.

	Point A	Point B
elevation	1011m	1050m
Pipe dia	50cm	100cm
Pressure	50 kPa	?

[BWDB'18]

Sol<sup>n</sup>:

$$z_A + \frac{P_A}{\gamma} + \frac{V_A^2}{2g} = z_B + \frac{P_B}{\gamma} + \frac{V_B^2}{2g} + h_L$$

~~$$\Rightarrow \frac{P_B}{\gamma} = (z_A - z_B) + \frac{V_A^2 - V_B^2}{2g} + \frac{P_A}{\gamma} - h_L$$~~

$$\Rightarrow \frac{P_B}{\gamma} = (z_A - z_B) + \frac{V_A^2 - V_B^2}{2g} + \frac{P_A}{\gamma} - h_L$$

$$\Rightarrow \frac{P_B}{\gamma} = (z_A - z_B) + 0.9 \left( \frac{V_A^2 - V_B^2}{2g} \right) + \frac{P_A}{\gamma} - 0.1 \left( \frac{V_A^2 - V_B^2}{2g} \right)$$

$$\Rightarrow \frac{P_B}{\gamma} = (1011 - 1050) + 0.9 \times \frac{(203.72)^2 - (50.93)^2}{2 \times 9.81}$$

$$+ \frac{50}{9.81} = 1750.86$$

$$\therefore P_B = 1750.86 \times 9.81 = 17176 \text{ kN} \text{ Ans}$$

$$V_A = \frac{40}{\frac{\pi}{4} \times 0.5^2}$$

$$= 203.72 \text{ m/s}$$

$$V_B = \frac{40}{\frac{\pi}{4} \times 1^2}$$

$$= 50.93 \text{ m/s}$$



velocity  $v = \frac{Q}{A}$  मीटर  
 velocity तदा एतः मिटर १००, नरुणरु इत्यं शक्ये!

# A pipe lying at a head of 625 in one end P and other end at elevation of 520m. Diameter of P & Q are 50cm & 75cm respectively. Discharge from P to Q is 0.02 m<sup>3</sup>/sec. If the pressure at P is 1000 kN/m<sup>2</sup>, determine the pressure at Q. Head loss is 1m [DWASA'17] [BWB'16] [MSc WRE'14]

Soln:

$$V_P = \frac{0.02}{\frac{\pi}{4} \times 0.5^2} = 0.102 \text{ m/s}$$

$$V_Q = \frac{0.02}{\frac{\pi}{4} \times 0.75^2} = 0.045 \text{ m/s}$$

$$\therefore \underline{z_P} + \frac{V_P^2}{2g} + \frac{P_P}{\gamma} = \underline{z_Q} + \frac{V_Q^2}{2g} + \frac{P_Q}{\gamma} + h_L$$

$$\Rightarrow \frac{P_Q}{\gamma} = (625 - 520) + \frac{0.102^2 - 0.045^2}{2 \times 9.81} - 1 + \frac{1000}{9.81}$$

$$\Rightarrow \frac{P_Q}{9.81} = 205.94$$

$$\Rightarrow P_Q = 2020.24 \text{ kN/m}^2 \underline{A}$$

\* Area of point A is  $20\text{cm}^2$  and area of point B is  $80\text{cm}^2$ . If height B from A is  $0.5\text{m}$ , headloss  $0.05\text{m}$  and pressure of point A  $P_A = 50\text{Pa}$ ,  ~~$Q = 80\text{l/sec}$~~  discharge from point A to B is  $80\text{l/sec}$ , find pressure at point B [PGCB'22] [PGCB'21]

Sol<sup>n</sup> A  $\longrightarrow$  B flow

$\therefore$  headloss to B is  $5\text{m}^2/5$

$$\frac{Q^2}{2gA^2} = \frac{v^2}{2g}$$

$$\frac{50}{9.81 \times 1000} + \frac{(80 \times 10^{-3})^2}{2 \times 9.81 \times (20 \times 10^{-4})^2} = \frac{P_B}{9.81 \times 1000} + \frac{(80 \times 10^{-3})^2}{2 \times 9.81 \times (80 \times 10^{-4})^2} + 0.5 + 0.05$$

W to N

$$\Rightarrow P_B = 744654.5 \text{ Pa}$$

$$= \underline{744.65 \text{ kPa}}$$

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hose pipe

(4) Water is flowing in a fire ~~nozzle~~ with a velocity of 4 m/s & pressure of 200 kPa. At the nozzle, the pressure decreases to atmospheric pressure (101.325 kPa), there is no change in height. Calculate the velocity of the water exiting the nozzle. [ELDL 2022]

Sol<sup>n</sup>:

$$\frac{200}{9.81} + \frac{4^2}{2 \times 9.81} = \frac{101.325}{9.81} + \frac{v^2}{2 \times 9.81}$$

$$\Rightarrow v = 14.012 \text{ m/s } \underline{A}$$

# A pipe 15cm in dia carries oil (sp. gr. = 0.75) at a rate of 70 lps. At a section 12cm above datum, the pressure is equivalent to 2cm of mercury vacuum. If the kinetic energy correction factor for the section is 1.1, the total head at that section in meters of oil is? [BIWTA'19]

Sol<sup>n</sup> Total head =  $z + \frac{P}{\gamma} + \alpha \frac{V^2}{2g}$

$= 0.12 - 0.02 \left( \frac{13.6}{0.75} - 1 \right) + 1.1 \times \frac{\left[ \frac{70 \times 10^{-3}}{\frac{\pi}{4} \times 0.15^2} \right]^2}{2 \times 9.81}$

$= 0.66 \text{ m of oil}$

vacuum 2cm of Hg

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Pressure head = gauge difference  $\times \left[ \frac{\text{test liquid SG (heavy)}}{\text{pipe liquid}} - 1 \right]$

$= \text{gauge diff} \times \left[ 1 - \frac{\text{SG of test liquid (light)}}{\text{pipe liquid}} \right]$

test liquid stasur 2 kora 2kora, 1 unna 2kora  
(5/1/20 20)

### \* Related math

Through a refinery, fuel ethanol is flowing in a pipe at a velocity of  $1 \text{ m/s}$  and a pressure of  $101.325 \text{ Pa}$ . The refinery needs the ethanol to be at a pressure of  $2 \text{ atm}$  ( $202.65 \text{ kPa}$ ) on a lower level. How far must the pipe drop in height in order to achieve this pressure? (density of ethanol is  $789 \text{ kg/m}^3$ )

Sol<sup>n</sup>:  $G_e = \frac{789}{1000} = 0.789$

$$\frac{101.325}{0.789 \times 9.81} + \cancel{0} = \frac{202.65}{0.789 \times 9.81} + h$$

$$\Rightarrow h = -13.09 \text{ m}$$

— the drop  $13.09 \text{ m}$

$13.09 \text{ m}$  drop  $13.09 \text{ m}$

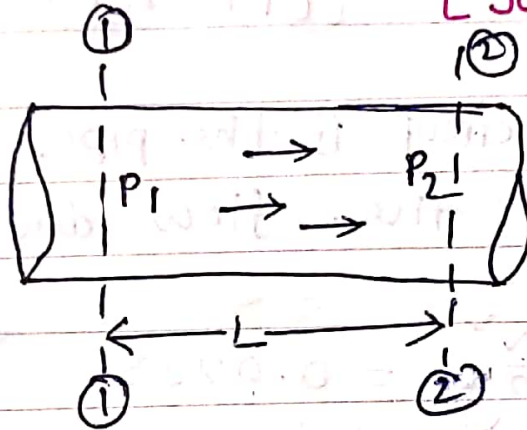
velocity  
 $1 \text{ m/s}$ , or extra  
no consider  
any extra



# Prove that, for constant discharge and constant ~~the~~ value of frictional resistance of a pipe, the head loss is inversely proportional to the 5th power of the pipe diameter.

[JGITDSL'21] [SGFCL'21]

Soln<sup>o</sup>



Applying Bernoulli's eq<sup>n</sup>,

$$\frac{P_1}{\gamma} = \frac{P_2}{\gamma} + h_f$$

[∵ constant diameter]  
[∵ ~~constant diameter~~  
∵ constant velocity]

$$\Rightarrow h_f = \frac{P_1 - P_2}{\gamma}$$

$$\Rightarrow \Delta P = \gamma h_f$$

$$\Rightarrow \frac{F}{A} = \gamma h_f$$

$$\Rightarrow \frac{f \times \pi d L \times v^2}{\frac{\pi}{4} \times d^2} = \gamma h_f$$

$$\Rightarrow h_f = \frac{4fLv^2}{\gamma d}$$

Force = frictional  
resistance \* wet area  
\* velocity<sup>2</sup>

$$= \frac{4fL \times \left(\frac{Q}{\frac{\pi}{4} \times d^2}\right)^2}{\gamma d}$$

$$= \frac{64fLQ^2}{\gamma \pi d^5}$$

$$\therefore h_f \propto \frac{1}{d^5}$$

Proved

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\*  $\Rightarrow$  Oil with  $\rho = 900 \text{ kg/m}^3$  & kinematic coefficient of viscosity,  $\nu = 0.00001 \text{ m}^2/\text{s}$ , flows at  $Q = 0.2 \text{ m}^3/\text{s}$  through 500m of 200mm dia cast-iron pipe. Take,  $f = 0.0225$   
 Determine - [ERL'22] [GTCL'22]

(i) The head loss

(ii) The pressure drop if the pipe slopes down at 1 in 10 in the flow direction

Sol<sup>n</sup>

$$(i) h_f = f \frac{L}{d} \frac{v^3}{2g} = 0.0225 \times \frac{500}{0.2} \times \frac{\left[\frac{0.2}{\frac{\pi}{4} \times 0.2^2}\right]^3}{2 \times 9.81}$$

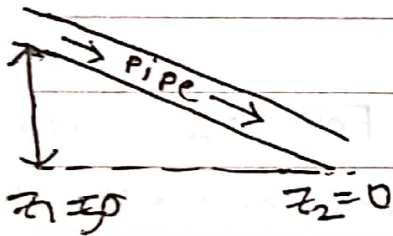
$$= 116.2 \text{ m}$$

(b)  $\Delta P = \Delta h \rho g$  [same dia pipe, velocity ~~change~~ same]

$$= (116.2 - \frac{500}{10}) \times 900 \times 9.81$$

$$= 584479.8 \text{ N/m}^2$$

$$= \underline{584.48 \text{ kN/m}^2}$$



or  $z_1 + \frac{P_1}{\rho} = z_2 + \frac{P_2}{\rho} + h_f$   
 use eqn for energy

or pressure,  $P = h \rho g$  use

$$h_f = f \frac{L}{d} \frac{v^3}{2g}$$

नाबलिन मरु 2000 (अन्य) शतमान  $f \rightarrow 0.02, 0.03, 0.04$

नाबलिन मरु 2000 (अन्य) शतमान  $f \rightarrow 0.004, 0.008,$

\* A turbine is located at an elevation 200m below that of the surface of the water intake. The friction loss in the pipeline leading to it is 8m and the turbine efficiency is 90%. What is the power ~~input~~ delivered by the turbine if the flow is  $3 \text{ m}^3/\text{s}$  in ~~kw~~ kW?

[M&MCL'22]

Sol<sup>n</sup>:

$$\text{Power, } P = \eta \rho Q h_f$$

$$= 0.9 \times 9.81 \times 3 \times (200 + 8)$$

plus 201

$$= 5085.504 \text{ kW}$$

$$= 5509.296 \text{ kW}$$

\* A reaction turbine is supplied with water through a 1500mm diameter pipe ( $\lambda = 0.011 \text{ mm}$ ) that is 50m long. The water surface in the reservoir is 27m above the draft-tube inlet that is 4.1m above the water level in the tailrace. If the turbine efficiency is 92% and the discharge is  $12 \text{ m}^3/\text{sec}$ , what is the power output of the turbine in kW?

Sol<sup>n</sup>: Head loss,  $H_L = \lambda \frac{L}{D} \frac{v^2}{2g}$

9mm motor Ans.  
 oru gnu or HL Anshu  
 222

$$= \frac{0.011}{1000} \times \frac{50}{1.5} \times \frac{\left\{ \frac{12}{2 \times 0.81} \right\}^2}{2 \times 9.81}$$

$$= 8.6177 \times 10^{-4}$$



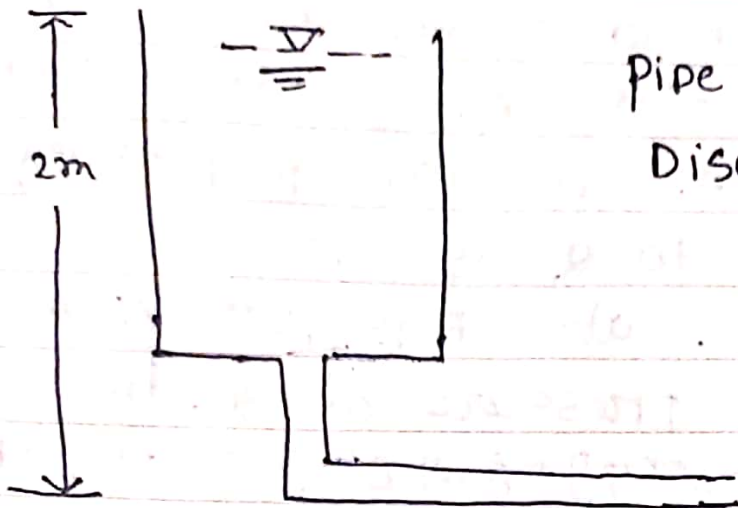
$$\therefore P = \eta \rho Q h_f$$

$$= 0.92 \times 9.81 \times 12 \times \left( 27 + 4.1 - 8.6177 \times 10^{-4} \right) = 3368.11 \text{ kW}$$

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Pipe dia 1cm.

Discharge,  $Q = ?$

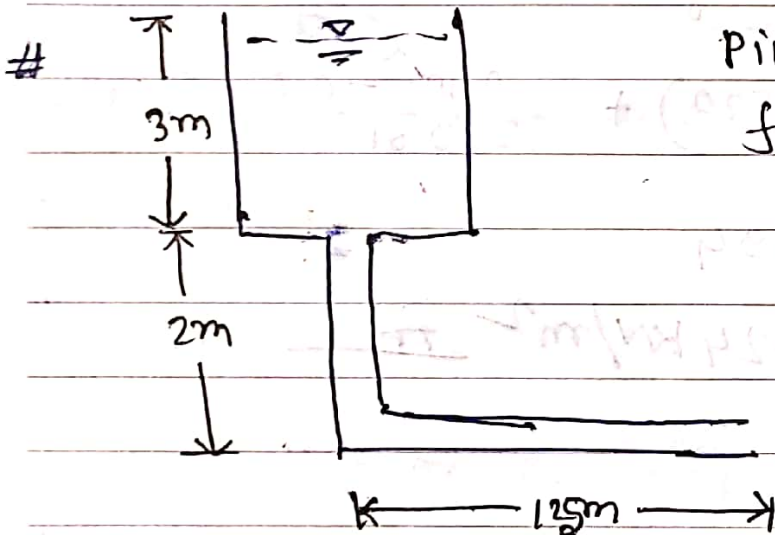
[DSCC '19]

$$v = \sqrt{2gh}$$

Sol<sup>n</sup>  $Q = A\sqrt{2gh}$

$$= \frac{\pi}{4} \times (100)^2 \times \sqrt{2 \times 9.81 \times 2}$$

$$= 4.92 \times 10^{-4} \text{ m}^3/\text{sec}$$



Pipe dia = 600mm

frictional factor,  $f = 0.04$

calculate discharge

Sol<sup>n</sup>  $v = \sqrt{\frac{2gh}{1 + f \frac{L}{d}}} = \sqrt{\frac{2 \times 9.81 \times 5}{1 + 0.04 \times \frac{125}{0.6}}}$

$$L = 125 + 2 - 0.6 = 126.4$$

$$= 3.226 \text{ m/s}$$

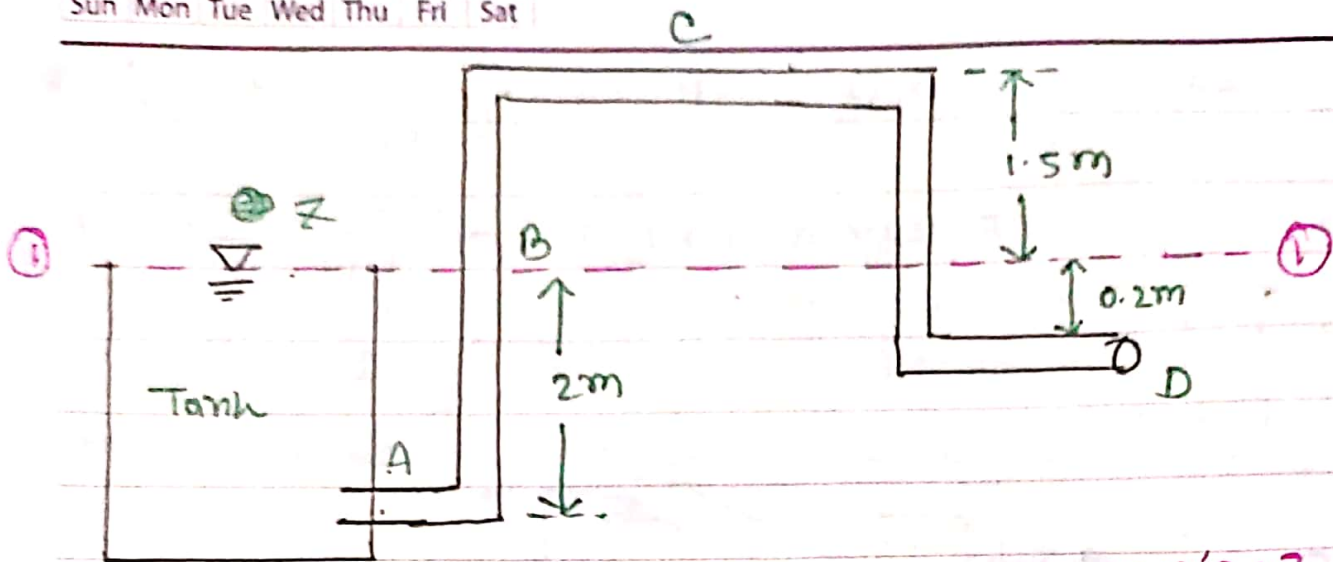
$$\therefore Q = \frac{\pi}{4} \times 0.6^2 \times 3.226 = 0.912 \text{ m}^3/\text{s}$$

A



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Find pressure at A, B, C, D [BWB'20]

Sol<sup>n</sup>:

velocity at point D,  $v = \sqrt{2 \times 9.81 \times 0.2} = 1.98 \text{ m/s}$

(∴ pipe velocity = 1.98 or 2 uniform pipe or velocity  
A to D to or,)

Applying Bernoulli's eq<sup>n</sup> at point z & C,

$$\Rightarrow 0 = 1.5 + \frac{P_C}{9.81} + \frac{1.98^2}{2 \times 9.81}$$

$$\therefore P_C = -16.675 \text{ kN/m}^2$$

Applying Bernoulli's eq<sup>n</sup> at point z & B,

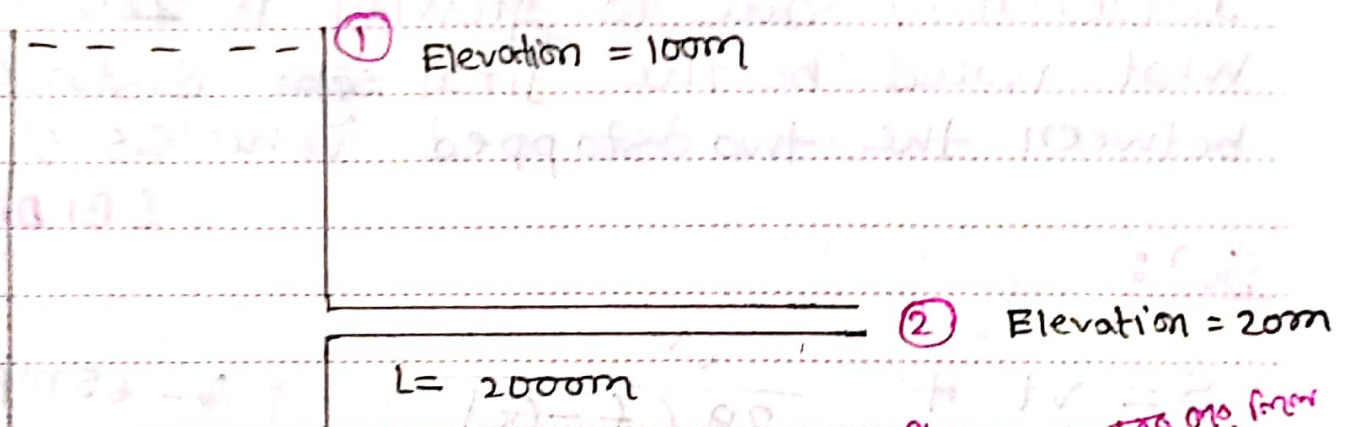
$$\Rightarrow 0 = \frac{P_B}{9.81} + \frac{1.98^2}{2 \times 9.81} \therefore P_B = -1.96 \text{ kN/m}^2$$

At point A,

$$\Rightarrow 0 = -2 + \frac{P_A}{9.81} + \frac{1.98^2}{2 \times 9.81} \therefore P_A = 17.66 \text{ kN/m}^2$$

Pressure at D,  $P_D = 0$  [atmospheric pressure]

\* The water flows from a thermal power plant through a pipe having diameter of 20cm. Flow velocity rate is  $0.06 \text{ m}^3/\text{sec}$  & frictional coefficient of the pipe is 0.02. Find the pressure at point 2. [BPPDS'23]



Soln: velocity,  $v = \frac{0.06}{\frac{\pi}{4} \times (0.2)^2} = 1.91 \text{ m/s}$

*Velocity too low from 2m 250 m/s*

*\*\*\* V of 200 m/s is wrong*

Now,

$$100 = \frac{P}{9.81} + \frac{1.91^2}{2 \times 9.81} + 20 + 0.02 \times \frac{2000}{0.2} \times \frac{1.91^2}{2 \times 9.81}$$

$$\Rightarrow \frac{P}{9.81} = 42.6264$$

$$\therefore P = 418.16 \text{ kPa}$$

A

\* Determine the coefficient of velocity of a small circular orifice in the side of a vessel. The orifice is 20cm below the vessel. The horizontal & vertical coordinates of water jet from vena contracta is 86cm & 96cm respectively.

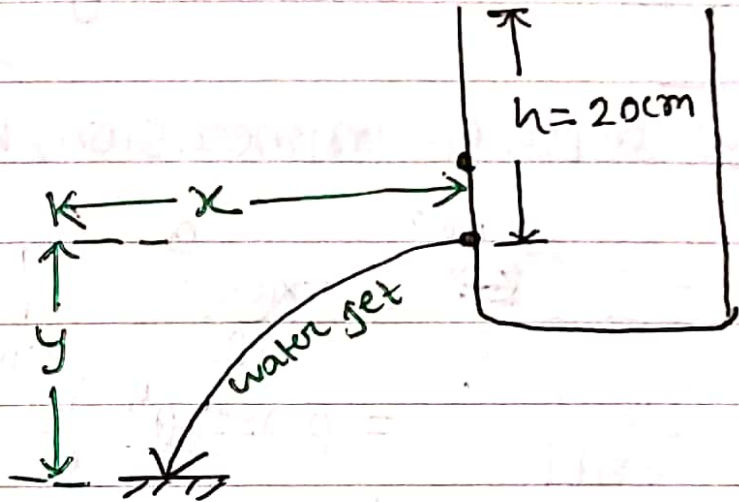
Soln<sup>o</sup>

$$x = C_v \sqrt{4yH}$$

$$\Rightarrow 86 = C_v \sqrt{4 \times 96 \times 20}$$

$$\therefore C_v = 0.98$$

A



Similarly, coefficient of discharge =  $C_d$

$$Q = C_d \cdot A \sqrt{2gh} ; C_c = \frac{C_c}{C_v}$$

# Calculate the total & effective pressure of swimming pool having 5m of water level from ground

[CPG&CBZ'15] [BPDB'16]

Soln<sup>o</sup> Total pressure =  $9.81 \times 5 = 49.05 \text{ m}$

Effective pressure = Total pressure - water pressure  
= 0 A



\* A man is spraying water onto a car at a speed of  $4\text{ m/s}$ . The diameter of the water jet is  $2.5\text{ cm}$ . If the jet hits the car surface perpendicularly, calculate the force on the car surface due to the water jet. Neglect all losses. [RPGEL'22]

Sol<sup>no</sup>

$$\text{Thrust/Force} = \rho A V^2$$

$$= 1000\text{ kg/m}^3 \times \frac{\pi}{4} \times \left(\frac{2.5}{100}\right)^2 \times (4\text{ m/s})^2$$

$$\frac{\text{kg}}{\text{m}^3} \times \text{m}^2 \times \frac{\text{m}^2}{\text{s}^2}$$

$$= 7.854\text{ N}$$

$$\boxed{\text{kg m s}^{-2} = \text{N}}$$

# Water flows steadily through the  $90^\circ$  reducing elbow shown in the figure. At the inlet to the elbow, the absolute pressure is 220 kPa and the x-sectional area is  $0.01 \text{ m}^2$ . At the outlet, the x-sectional area is  $0.0025 \text{ m}^2$  and the velocity is  $16 \text{ m/s}$ . The elbow discharges to the atmosphere. Determine the force required to hold the elbow in place. [ISGCL'17]

Sol<sup>n</sup>

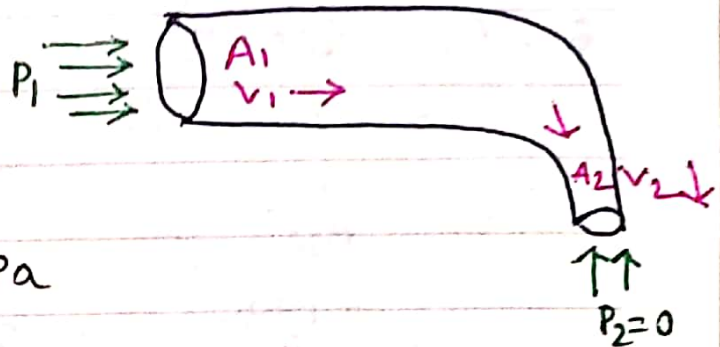
$$v_1 = \frac{A_2}{A_1} \times v_2$$

$$= \frac{0.0025}{0.01} \times 16 = 4 \text{ m/s}$$

$$P_1 = P_{abs} - P_{atm}$$

$$= 220 - 101.325 = 118.675 \text{ kPa}$$

$$P_2 = 0$$



→

$$\sum F_x = \rho Q \Delta v$$

$v_2$  is  $\times$  component zero

$$\Rightarrow R_x + P_1 A_1 = \rho Q (v_{2x} - v_{1x})$$

$$\Rightarrow R_x = -P_1 A_1 + \rho Q (-v_{1x})$$

force KN  $\rightarrow$  total force  
 $\rho = 1000$

$$\Rightarrow R_x = -118.675 \times 0.01 - 1 \times (0.01 \times 4) \times 4$$

$$= -1.35 \text{ kN} \quad \therefore R_x = 1.35 \text{ kN} (\leftarrow)$$

$$\downarrow \sum F_y = \rho Q (v_{2y} - v_{1y})$$

$$\Rightarrow R_y - P_2 A_2 = 1 \times (0.01 \times 4) \times 16$$

$$\Rightarrow R_y = 0.64 \text{ kN} (\downarrow)$$

$v_2$  into into into into  
 into positive dir<sup>n</sup>

$$\therefore R = \sqrt{(-1.35)^2 + (0.64)^2} = 1.494 \text{ kN} \quad \text{Ans.}$$

$$\Delta v = \text{out velocity} - \text{in velocity}$$

$$\text{out } v_2 = 16 \text{ m/s} \text{ so } \Delta v = 16 \text{ m/s}$$



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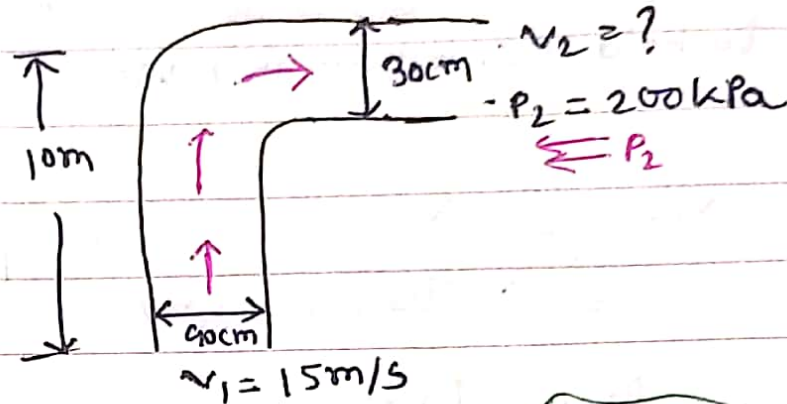
# A 90° reducing elbow is in the vertical plane and water flows through it. What is the horizontal force required to hold the reducer elbow in a stationary position?

Soln

$$Q = A_1 V_1 = \frac{\pi}{4} \times (0.4)^2 \times 15$$
$$= 1.885 \text{ m}^3/\text{s}$$

$$\therefore V_2 = \frac{Q}{A_2}$$

$$= \frac{1.885}{\frac{\pi}{4} \times (0.3)^2} = 26.67 \text{ m/s}$$



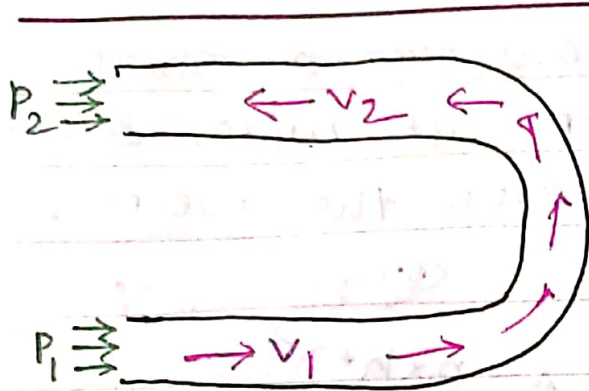
$$V_2 = 26.67 \text{ m/s}$$
$$V_2 - V_1 = 26.67 - 15 = 11.67 \text{ m/s}$$

$$\sum F_x = \rho Q (V_{2x} - V_{1x})$$

$$\Rightarrow R_x - P_1 A_1 = \rho Q V_{2x}$$

$$\Rightarrow R_x = 200 \times \frac{\pi}{4} \times (0.3)^2 + 1 \times 1.885 \times 26.67$$
$$= 64.41 \text{ kN } (\rightarrow)$$

for kN unit  
 $\rho = 1$



$$P_1 = 100 \text{ kN/m}^2$$

$$P_2 = 80 \text{ kN/m}^2$$

180° ~~bend~~ ~~bend~~  
bend

Petroleum

(density  $900 \text{ kg/m}^3$ )

flow rate =  $150 \text{ m}^3/\text{hr}$

pipe dia =  $200 \text{ mm}$

Determine force exerted by the liquid on the bend.

Sol<sup>n</sup>:  $A = \frac{\pi}{4} \times 0.2^2 = 0.03 \text{ m}^2$

$$Q = 150 \text{ m}^3/\text{hr} = \frac{150}{3600} = 0.04167 \text{ m}^3/\text{s}$$

$$v = \frac{0.04167}{0.03} = 1.389 \text{ m/s}$$

→

$$\Sigma F_x = 0$$

$$\Rightarrow R_x + P_1 A_1 + P_2 A_2 + \rho Q (v_2 - v_1) = 0$$

$$\Rightarrow R_x + 100 \times 0.03 + 80 \times 0.03 + 0.9 \times 0.04167 \times [-1.389 - 1.389] = 0$$

KN + m<sup>2</sup>

direction ← v

$$\Rightarrow R_x + 5.3 = 0$$

$$\therefore R_x = -5.3 \text{ kN}$$

$$\therefore R_x = 5.3 \text{ kN} \quad (\leftarrow)$$

\* A nozzle is so shaped that the velocity of flow along the centre line changes linearly from A to B is  $2.5 \text{ m/sec}$  to  $16 \text{ m/sec}$  in a distance of  $3.75 \text{ m}$ . Determine the magnitude of convective acceleration at point B.

Sol<sup>n</sup>:

[JOC'22]

$$\text{convective acceleration at point A} = \frac{16-2.5}{3.75} \times 2.5$$

$$= 9 \text{ ms}^{-2}$$

$$\text{at point B, } a_B = \frac{16-2.5}{3.75} \times 16$$

$$= 57.6 \text{ ms}^{-2}$$



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2m दूरी पर A point पर 2m दूरी पर convective acceleration का मान ज्ञात करें।

$$\therefore \text{A point पर 2m दूरी पर velocity} = 2.5 + \frac{16-2.5}{3.75} \times 2$$

$$= 9.7 \text{ ms}^{-1}$$

$$\therefore \text{2m दूरी पर acceleration} = \frac{16-2.5}{3.75} \times 9.7$$

$$= 34.92 \text{ ms}^{-2}$$

If the velocity distribution over a plate is given by  $u = \frac{2}{3}y - y^2$  in which  $u$  is the velocity in m/s at a distance  $y$  meter above the plate. Determine the shear stress at  $y = 0.15$ . Take dynamic viscosity of fluid as 8.63 poise.

[BWDB'16]

Sol<sup>n</sup>

$$\text{here, } u = \frac{2}{3}y - y^2$$

$$[1 \text{ poise} = 0.1 \text{ N s/m}^2]$$

$$\therefore \frac{du}{dy} = \frac{2}{3} - 2y$$

$$\text{at } y = 0.15, \quad \frac{du}{dy} = \frac{2}{3} - 2 \times 0.15 = 0.367$$

$$\text{Shear stress} = \mu \times \frac{du}{dy} = 0.1 \times 8.63 \times 0.367 = 0.3167 \text{ N/m}^2$$

2MT pipe length 1000m dia 4cm shear stress resistance

$$2T = 0.3167 \times \pi d l = 0.3167 \times \frac{\pi}{100} \times 4 \times 1000 = 39.8 \text{ N}$$

# A plate 0.025mm distant from a fixed plate moves at 60cm/s and requires a force of 2N per unit area to maintain this speed. Determine fluid viscosity between the plates.

$$\text{Sol<sup>n</sup> shear stress, } \tau = \frac{2 \text{ N}}{1 \text{ m}^2} = 2 \text{ N/m}^2$$

$$dy = 0.025 \text{ mm} = 0.025 \times 10^{-3} \text{ m}$$

$$du = 60 \text{ cm/sec} = 0.6 \text{ m/sec}$$

$$\text{we know, } \tau = \mu \frac{du}{dy} \therefore \mu = \tau \times \frac{dy}{du}$$

$$\therefore \mu = 2 \times \frac{0.025 \times 10^{-3}}{0.6} = 8.33 \times 10^{-5} \text{ N s/m}^2 = 8.33 \times 10^{-4} \text{ poise}$$


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# A log of wood 6 in wide, 12 in high & 60 in long floats on the surface of water. Assuming that its specific gravity is 0.74. If the log floats on its 6-in side, determine -

- (a) the depth of immersion
- (b) The righting moment for a 5° tilt
- (c) The metacentric height

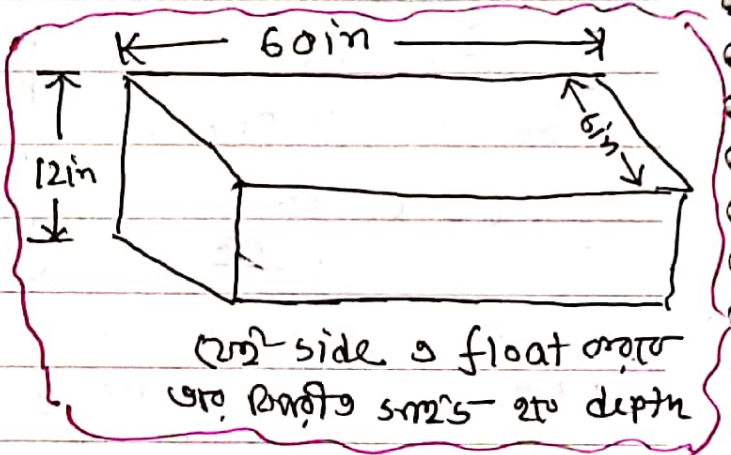
Soln:

(a) depth of immersion,  $h = 0.74 \times 12 = 8.88 \text{ in}$

(b)  $I = \frac{Lw^3}{12} = \frac{5 \times (0.5)^3}{12} = 0.0521 \text{ ft}^4$

60 in = 5 ft  
6 in = 0.5 ft

moment of inertia about depth axis



60 in side of float on its 6 in side

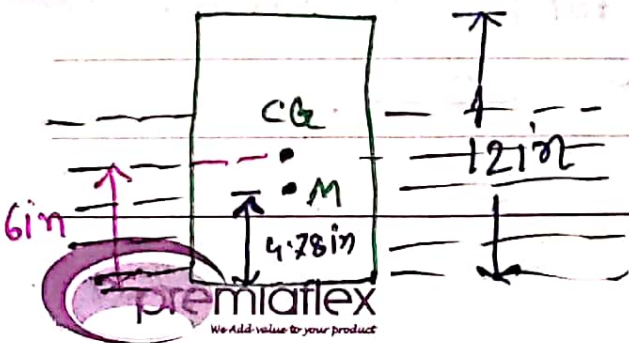
Righting moment for 5° tilt,

$M = 5^\circ * \gamma_w I$

$= \frac{5\pi}{180} \times 62.43 \times 0.0521 = 0.284 \text{ lb-ft}$

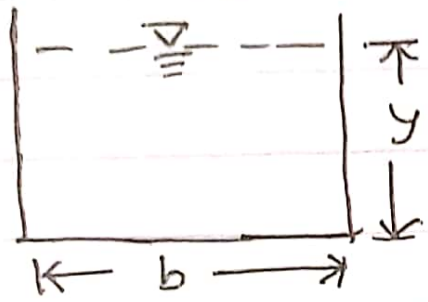
(c) Submerged volume,  $V_{sub} = \frac{8.88 \times 6 \times 60}{12 \times 12 \times 12} = 1.85 \text{ ft}^3$

Metacentric height from bottom,  $h_m = \frac{0.0521 \text{ ft}^4}{1.85 \text{ ft}^3} \times 12 + \frac{8.88}{2} = 4.78 \text{ in}$



metacentric height CG to M is 2.07 in < stable, but 2.07 in < unstable. ∴ is unstable

# Open Channel Shapes



Area,  $A = by$

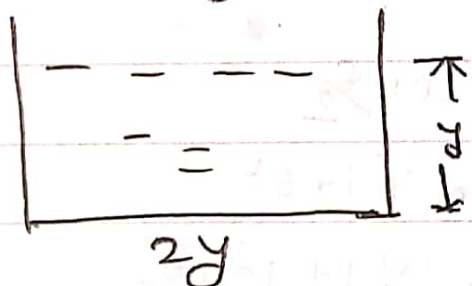
Perimeter,  $P = b + 2y$

Hydraulic Radius,  $R = \frac{A}{P} = \frac{by}{b + 2y}$

Rectangular

\* For most efficient Rectangular channel.

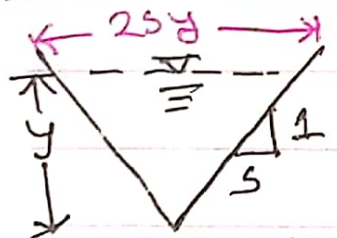
$b = 2y$



Area,  $A = 2y^2$

$P = 4y$

$\therefore R = \frac{y}{2}$



Triangular

Top width =  $2sy$

$A = sy^2$

$P = 2y\sqrt{1+s^2}$

$R = \frac{sy^2}{2y\sqrt{1+s^2}}$

For most efficient ~~rectangular~~ Triangular channel,  $s = 1$

$\therefore A = y^2$   
 $R = \frac{y}{2\sqrt{2}}$

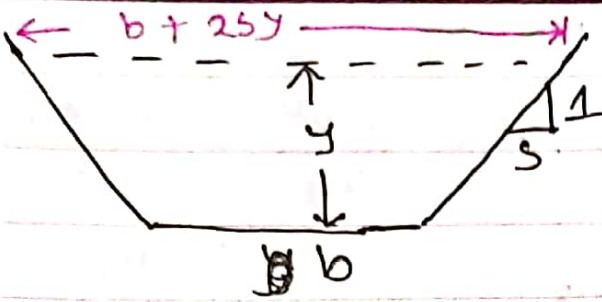
\*  $s$  slopes horizontal to depth 2 to 1  
vertical slopes 1 to 2 to 1



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Triangle cuts Trapezoidal same. Just Trapezoid is extra  $b$  cm.



Trapezoidal channel

$$A = (b + sy)y$$

$$P = b + 2y\sqrt{1+s^2}$$

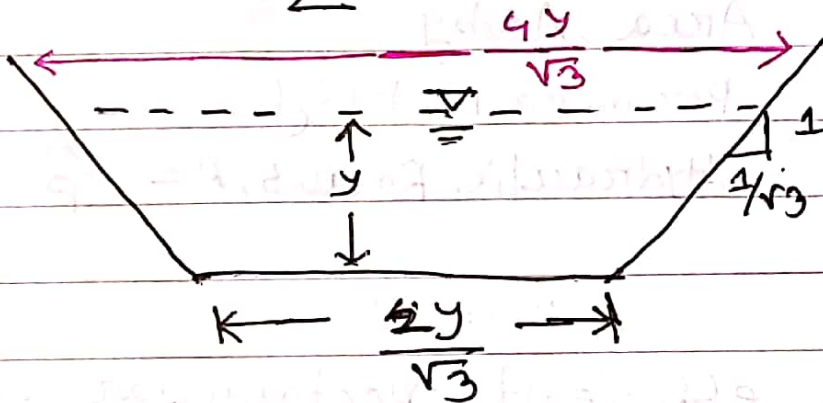
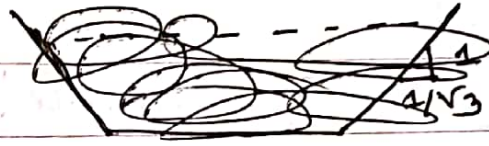
$$R = A/P$$

$$\text{Top width} = b + 2sy$$

For best trapezoidal channel,  $s = \frac{1}{\sqrt{3}}$

$$A = \sqrt{3}y^2$$

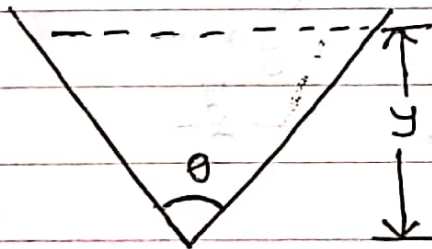
$$R = \frac{y}{2}$$



best section

angle  $\theta$  for  $\theta = 90^\circ$

$$* s = \tan \frac{\theta}{2}$$



$$A = y^2 \tan \frac{\theta}{2}$$

$$P = 2y\sqrt{1+s^2}$$

$$= 2y\sqrt{1+\tan^2 \frac{\theta}{2}}$$

$$= 2y \sec \frac{\theta}{2}$$

$$= 2y$$

$$= 2y$$

$$\cos \frac{\theta}{2}$$

$$\text{Top width, } T = 2sy$$

$$= 2y \tan \frac{\theta}{2}$$

\* For best section,

$$\theta = 90^\circ$$

$$R = \frac{A}{P}$$



Channel Design Formulae:

• Chezy's formula -

$$V = C\sqrt{RS}$$

\*  $C$  = Chezy's coefficient

Manning's formula -

$$V = \frac{1}{n} R^{2/3} S^{1/2} \quad [\text{SI unit}]$$

$$= \frac{1.486}{n} R^{2/3} S^{1/2} \quad [\text{FPS unit}]$$

→ स्टोकिंग और डिचार्ज -  
ft से मीटर  
2.540 250 1

Relation between Chezy's  $C$  & Manning's  $n$ 

$$C\sqrt{RS} = \frac{1}{n} R^{2/3} S^{1/2}$$

$$\Rightarrow CR^{1/2} = \frac{1}{n} R^{2/3}$$

$$\Rightarrow C = \frac{1}{n} R^{2/3 - 1/2} = \frac{1}{n} R^{1/6}$$

$$\Rightarrow \boxed{C = \frac{1}{n} R^{1/6}}$$

\* for wide channel,  $R = y$  (depth)

[चौड़ाई  $b = 1$  unit हो तो  $R = y$  wide channel का]

\* चौराहा discharge  $m^3/s$  पर  $y$  wide channel का  
discharge का unit  $m^3/s/m$  चौराहा  $m^2/s$

Flow Type in channel

$$\text{Froude Number, } Fr = \frac{V}{\sqrt{g \frac{A}{T}}}$$

\*  $A$  = Area

$T$  = Top width

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For rectangular channel,  $Fr = \frac{V}{\sqrt{gy}}$

For triangular channel,  $Fr = \frac{V}{\sqrt{gy/2}}$

$Fr > 1 \rightarrow$  Supercritical flow

$Fr < 1 \rightarrow$  Subcritical flow

$Fr = 1 \rightarrow$  critical flow

$\Rightarrow$  Velocity for critical flow in rectangular channel

$$Fr = 1 = \frac{V}{\sqrt{gy_c}}$$

$$\therefore V = \sqrt{gy_c}$$

Here,  
 $y = y_c =$  critical depth

$\Rightarrow$  Flow depth in different types of flow:

----- Subcritical flow

----- Critical flow

----- Supercritical flow

Channel bed

\* Critical flow to same or energy not and same total discharge and

\* Supercritical flow to  $2y_c$  depth

same or  $2y_c$  - same discharge and

same total and



⇒ Super critical flow को सामान्य तौर पर प्रकृत flow depth लाया जाये, इसके बाद, जहाँ **hydraulic jump** रहने। सामान्य तौर पर प्रकृत velocity का 2गुना, जो discharge constant तब flow depth बढ़े super critical को subcritical में आये।

⇒ Natural प्रवाह प्रकृत flow exists की, प्रकृत flow को subcritical. इस depth को प्रकृत depth, velocity का 1/2, जहाँ सामान्य तौर पर प्रकृत side को बढ़े चले आये, velocity को अधिकतम 2गुना।

### Critical depth calculation:

$$\boxed{\frac{Q^3}{g} = \frac{A^3}{T}}$$

T = Top width

← universal formula for any section

For rectangular channel,  $y_c = \left( \frac{q^3}{g} \right)^{1/3}$

\*  $q =$  unit discharge.

$$= \frac{Q}{\text{width, } B}$$

For triangular channel,

$$y_c = \left( \frac{2Q^3}{gS^3} \right)^{1/5}$$

✓ critical velocity for rectangular channel,

$$v_c = \sqrt{gy_c}$$

For triangular channel, ~~critical~~

$$\text{critical velocity, } v_c = \sqrt{8gy_c/2}$$

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# A wide channel has  $n = 0.026$  &  ~~$S_0 = 0.0028$~~   
 $S_0 = 0.0028$ . Calculate the normal depth & velocity of the flow if discharge is  $30 \text{ m}^3/\text{sec}/\text{m}$ . [BPDB'16]

Soln<sup>o</sup>  $Q = \frac{1}{n} A R^{2/3} S^{1/2}$

~~$Q = \frac{1}{n} b y^{3/2} S^{1/2}$~~

$\Rightarrow Q = \frac{1}{n} y \cdot y^{2/3} S^{1/2}$

$\Rightarrow 30 = \frac{1}{0.026} y^{5/3} \sqrt{0.0028}$

$\therefore y = 5.025 \text{ m}$

velocity =  $\frac{30}{5.025} = 5.97 \text{ m/s}$

# Calculate normal depth of earthen channel if discharge is  $10 \text{ m}^3/\text{sec}$  & channel slope is  $1 \text{ cm}/\text{km}$ . Assume best triangular channel. [BIWTA]  
take,  $n = 0.025$  19

Soln<sup>o</sup>  $10 = \frac{1}{0.025} y^2 \cdot \left(\frac{y}{2\sqrt{2}}\right)^{2/3} \cdot \sqrt{10^{-5}}$

~~$10 = \frac{1}{0.025} y^2 \cdot \left(\frac{y}{2\sqrt{2}}\right)^{2/3} \cdot \sqrt{10^{-5}}$~~

$\Rightarrow y \frac{6}{3} = \frac{10 \times 0.025 \times (2\sqrt{2})^{2/3}}{\sqrt{10^{-5}}}$

$\therefore y = 6.67 \text{ m}$

For best section,

$A = y^2$

$R = \frac{y}{2\sqrt{2}}$

$S = \frac{1 \text{ cm}}{1 \text{ km}}$

$= \frac{10^{-5} \text{ km}}{\text{km}}$

$= 10^{-5}$

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\* A wide channel having longitudinal slope 0.001, Manning's roughness coefficient 0.02 & velocity  $1.6 \text{ m s}^{-1}$ . Calculate normal depth.

Sol<sup>n</sup>  $1.6 = \frac{1}{0.02} \times y^{2/3} \times \sqrt{0.001}$

$\therefore y = 1.02 \text{ m}$

\* wide channel & ~~depth~~  $R = y$

\*  $2.12$   $\text{ft}$   $\text{or}$   $2.12 \text{ m}$   $\frac{1.486}{n}$

$2.12$  inch  $2.12 \text{ m}$   $1$   $\text{or}$   $2.12 \text{ ft}$   $\text{or}$   $2.12$

$2.12$   $\text{m}$

\* A wide channel discharge  $3 \text{ m}^3/\text{sec}$  and longitudinal slope  $0.0025$  and Manning's  $n=0.025$ . Calculate the normal depth & velocity.

[PGCB'20] [DPDC'20] [BIFPC'21]

Sol<sup>n</sup>  $Q = \frac{1}{0.025} \times (1 \times y) \times y^{2/3} \times \sqrt{0.0025}$

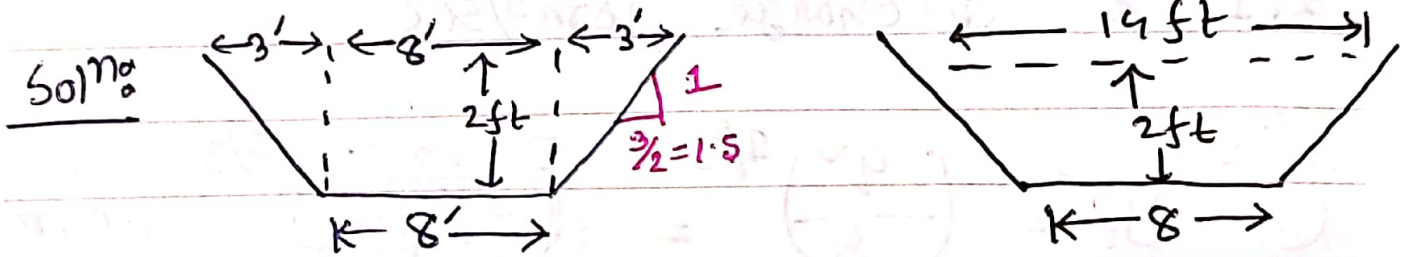
$$\therefore y^{5/3} = \cancel{0.4} 1.5$$

$$\therefore \cancel{y = 0.32 \text{ m}}$$

$$\therefore y = 1.275 \text{ m}$$

$$\text{velocity, } v = \frac{3}{1 \times 1.275} = 2.35 \text{ m/s} \quad \star$$

# The trapezoidal channel shown below has a Manning's coefficient of  $n = 0.013$  & is laid at a slope of  $0.0028$ , the depth of flow is 2ft. What is the flow rate? [SAFL'17]



$$\text{Area} = (b + sy) y$$

$$= (8 + 1.5 \times 2) \times 2 = 22 \text{ ft}^2$$

$$\text{Perimeter, } P = 8 + 2 \times 2 \sqrt{1 + 1.5^2} = 15.21 \text{ m}$$

$$\therefore R = \frac{22}{15.21} = 1.44 \text{ m}$$

$$\therefore Q = \frac{1.486}{0.013} \times 22 \times (1.44)^{2/3} \times \sqrt{0.0028}$$

$$= 170 \text{ ft}^3/\text{sec} \quad \underline{\underline{A}}$$

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\* Compute the critical depth & velocity in

(i) a rectangular channel with width of 6m & discharge  $20 \text{ m}^3/\text{sec}$

(ii) Triangular channel with side slope 2:1 & discharge  $10 \text{ m}^3/\text{sec}$

Soln

$$(i) y_c = \left( \frac{Q^2}{g} \right)^{1/3} = \left[ \frac{(20)^2}{9.81 \times 6} \right]^{1/3} = 1.04 \text{ m}$$

critical velocity,  $v_c = \sqrt{gy_c} = \sqrt{9.81 \times 1.04} = 3.2 \text{ m/s}$

$$(ii) y_c = \left( \frac{2Q^2}{gS^2} \right)^{1/5} = \left( \frac{2 \times 10^2}{9.81 \times 2^2} \right)^{1/5} = 1.385 \text{ m}$$

critical velocity,  $v_c = \sqrt{gy_c/2}$  \*\*\*

$$= \sqrt{9.81 \times \frac{1.385}{2}} = 2.61 \text{ m/s}$$



\*\*\* Trapezoidal  
 A ~~rectangular~~ channel has a width of ~~4m~~ 4m & side slopes of 1.5:1 carries a certain discharge.

(a) If the critical depth is 1.7m, calculate the discharge in the channel

(b) If this discharge was observed to be flowing at a depth of 2.50m in a reach, estimate the froude number of the flow.

Sol<sup>n</sup> We know,

$$\frac{Q^3}{g} = \frac{A^3}{T}$$

$$\Rightarrow \frac{Q^3}{9.81} = \frac{[4 + 1.5 \times 1.7] \cdot 1.7^3}{4 + 2 \times 1.5 \times 1.7}$$

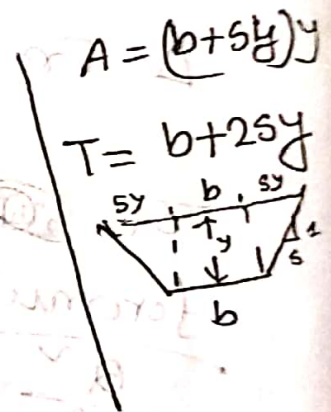
$$\Rightarrow Q = 38.58 \text{ m}^3/\text{s}$$

$$(b) v = \frac{Q}{A} = \frac{38.58}{(4 + 1.5 \times 2.5) \times 2.5} = \frac{38.58}{1.99} = 1.99$$

$$\frac{A^3}{T} = \frac{(4 + 1.5 \times 2.5)^3 \times 2.5^3}{4 + 2 \times 1.5 \times 2.5} = 1.68$$

$$Fr = \frac{v}{\sqrt{g \frac{A}{T}}} = \frac{1.99}{\sqrt{9.81 \times 1.68}} = 0.99$$

∴ subcritical flow



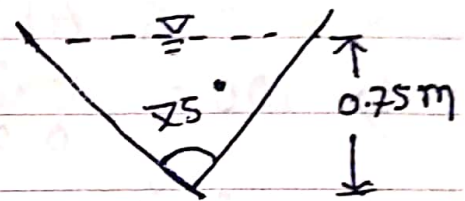
\* A triangular channel with an apex angle of  $75^\circ$  carries a flow of  $1.2 \text{ m}^3/\text{s}$  at a depth of  $0.75 \text{ m}$ . If the bed slope is  $0.009$ , find the roughness coefficient ( $n$ ) of the channel. What is the corresponding value of Chezy's coefficient ( $C$ ). Also calculate velocity ( $v$ ). [BWDB '22]

Soln:

$$A = y^2 \tan^2 \frac{\theta}{2}$$

$$= (0.75)^2 \tan^2 \frac{75}{2}$$

$$= 0.43 \text{ m}^2$$



$$P = 2y \sqrt{1 + \tan^2 \frac{\theta}{2}}$$

$$= 2 \times 0.75 \sqrt{1 + \tan^2 \frac{75}{2}}$$

$$= 1.89 \text{ m}$$

$$* s = \tan^2 \frac{\theta}{2}$$

$$\therefore R = A/P = 0.227 \text{ m}$$

$$Q = \frac{1}{n} A R^{2/3} S^{1/2}$$

$$\Rightarrow 1.2 = \frac{1}{n} \times 0.43 \times (0.227)^{2/3} \times \sqrt{0.009}$$

$$\Rightarrow n = \frac{0.43 \times (0.227)^{2/3} \times \sqrt{0.009}}{1.2}$$

$$= 0.0126$$

$$v = \frac{Q}{A} = \frac{1.2}{0.43} = 2.8 \text{ m/s}$$

\*\*\*

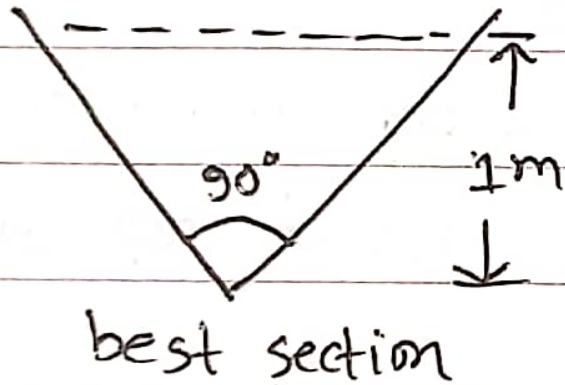
$$V_c = C \sqrt{RS}$$

$$\Rightarrow C = \frac{2.8}{\sqrt{0.227 \times 0.009}} = 61.94$$



\* Determine the top width of best triangular channel section if flow depth is 1m [DMTCL'22]

Soln:



$$\begin{aligned}\text{Top width} &= 2Sy \\ &= 2 \times \tan \frac{90}{2} \times 1 \\ &= 2m\end{aligned}$$

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\* A rectangular channel is to carry 100 cusec water. Calculate the dimensions of the best hydraulic x-section if the channel is lined with cement & is laid on a slope of 0.0001. Assume,  $n = 0.012$

Sol<sup>n</sup>

$$\text{Cusec} = 1 \text{ft}^3/\text{sec}$$

$$Q = \frac{1.49}{n} AR^{2/3} S^{1/2}$$

$$\Rightarrow 100 = \frac{1.49}{0.012} \times (2y^2) \times \left(\frac{y}{2}\right)^{2/3} \times \sqrt{0.0001}$$

$$\Rightarrow y^{2 + \frac{2}{3}} = 63.92$$

$$\Rightarrow y^{8/3} = 63.92$$

$$\therefore y = 4.75 \text{ ft}$$

For best rectangular section

$$A = 2y^2$$

$$R = \frac{y}{2}$$

∴ width,  $B = 2y = 2 \times 4.75 = 9.5 \text{ ft}$

\* A cement lined rectangular channel 20ft wide carries water at a rate of 400ft<sup>3</sup>/sec. Determine the slope required to maintain a depth of 4ft. Take,  $n = 0.012$

$$\Rightarrow 400 = \frac{1.486}{0.012} \times (4 \times 20) \times \left( \frac{4 \times 20}{4 + 20 + 2 \times 4} \right)^{2/3} \times \sqrt{S}$$

$$\Rightarrow \sqrt{S} = 0.02$$

$$\therefore S = 0.0004$$

A long channel with a triangular cross section has a ~~side~~ slope of 1:1 and a constant bed slope of  $0.343^\circ$ . What is the water depth when the channel carries 14 cfs? Take  $n=0.012$ . Is the channel slope mild or steep?

Sol<sup>n</sup>

$$14 = \frac{1.486}{0.012} \times (1 \times y^2) \times \left( \frac{1 \times y^2}{2y\sqrt{1+1}} \right)^{2/3} \times (\tan 0.343) \times y^{3/2}$$

$$\Rightarrow y^{2+\frac{2}{3}} = \frac{14 \times 0.012 \times (2\sqrt{2})^{2/3}}{1.486 \times \sqrt{\tan 0.343}} = 2.922$$

$$\therefore y^{8/3} = 2.922$$

$$\therefore y = 1.495 \text{ ft}$$

$$\text{again } y_c = \left( \frac{2Q^2}{gS^3} \right)^{1/5} = \left( \frac{2 \times 14^2}{9.81 \times 1} \right)^{1/5} = 1.65 \text{ ft}$$

$\therefore y < y_c$   $\therefore$  supercritical flow & slope is steep slope (32.2)

# Determine the dimensions of the most economical trapezoidal channel to carry  $200 \text{ m}^3/\text{s}$  with a slope of  $0.0004$ . Take  $n=0.016$ .

Sol<sup>n</sup>

$$200 = \frac{1}{0.016} \times (\sqrt{3}y^2) \times \left( \frac{y}{2} \right)^{2/3} \times \sqrt{0.0004}$$

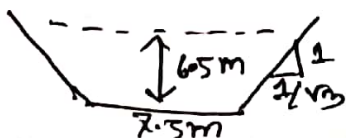
$$y^{8/3} = \frac{200 \times 0.016 \times 2^{2/3}}{\sqrt{3} \times \sqrt{0.0004}} = 146.64$$

$$\therefore y^{8/3} = 146.64$$

$$\therefore y = 6.5 \text{ m} \quad \therefore \text{depth } y = 6.5 \text{ m}$$

$$\text{bottom width} = \frac{2y}{\sqrt{3}} = \frac{2 \times 6.5}{\sqrt{3}} = 7.5 \text{ m}$$

$$\text{side slope} = \frac{1}{\sqrt{3}} : 1$$



## Energy head in Open Channel Flow:

ଅମ୍ବର ଶେକ୍ସନ ଓ total energy head same

$$y + \frac{v^2}{2g} + (\text{elevation ଅର୍ଥ ଅନୁ ଉପର hump})$$

critical depth ଅର୍ଥ ଅନୁ ଓ, energy ସାଫତା  
ଅନୁ ଅନୁ ଅନୁ, ଓ total energy head

$$E_{min} = 1.5 y_c \quad [\text{rectangular channel}]$$

$$= 1.25 y_c \quad [\text{Triangular channel}]$$

## Hydraulic Jump:

Flow ଅର୍ଥ super critical ~~ଅନୁ~~ ଅନୁ ଓ ଏହା  
ଅନୁ ଅନୁ ଓ ଏହା flow jump ଅନୁ  
subcritical ଅନୁ ଅନୁ।

ଅନୁ ଅନୁ ଓ ଏହା ଓ ଏହା ଓ depth ଅନୁ  
sequent depth ଅନୁ।

$$y_2 = \frac{y_1}{2} \left[ \sqrt{1 + 8F_1^2} - 1 \right]$$

$$\text{Jump height} = y_2 - y_1$$

$$\text{Energy loss in jump} = \frac{(y_2 - y_1)^3}{4y_1 y_2}$$

\* 4m wide rectangular channel with a sluice gate has an u/s water depth of 2.5m and down stream water depth of 0.4m. Calculate discharge through the channel. Neglect all losses

Soln:  $y_1 + \frac{v_1^2}{2g} = y_2 + \frac{v_2^2}{2g}$  [RPGCL '22]

$$\Rightarrow 2.5 + \frac{Q^2}{2g \times 4^3 \times 2.5^3} = 0.4 + \frac{Q^2}{2g \times 4^3 \times 0.4^3}$$

$$\Rightarrow \frac{Q^2}{2g \times 16} * \left( \frac{1}{0.4^3} - \frac{1}{2.5^3} \right) = 2.5 - 0.4$$

$$\Rightarrow \frac{Q^2}{313.92} = 0.34483$$

$$\Rightarrow Q = 10.4 \text{ m}^3/\text{s}$$



VESTAR MR<sup>®</sup>  
\* TRIMETAZIDINE

# A cement lined rectangular channel 20ft wide carries water at a rate of  $400 \text{ ft}^3/\text{sec}$ . Calculate the critical height of a rise for depth 4ft.

Sol<sup>n</sup> critical depth,  $y_c = \left[ \frac{\left(\frac{400}{20}\right)^2}{32.2} \right]^{2/3}$

$$= 2.32 \text{ ft}$$

$\therefore$  Energy head at critical depth  $= 1.5 \times 2.32$   
 $= 3.47 \text{ ft}$

Energy head at 4ft depth  $= y + \frac{v^2}{2g}$

$$= 4 + \frac{\left(\frac{400}{20 \times 4}\right)^2}{2 \times 32.2}$$

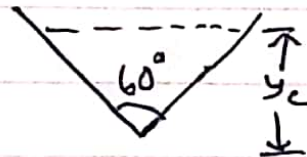
$$= 4.39 \text{ ft}$$

$\therefore$  rise  $= \cancel{4.39 - 3.47} = \cancel{0.92} \text{ ft}$

rise  $= (4.39 - 3.47) \text{ ft}$   
 $= 0.92 \text{ ft}$  Ans

\* Compute the critical depth for flow at  $0.4 \text{ m}^3/\text{s}$  through the x-section of below figure. If the normal depth is 1.2m, whether the flow is subcritical or supercritical?

Sol<sup>n</sup>  $y_c = \left( \frac{2Q^2}{gS^3} \right)^{1/5}$  ;  $S = \tan \theta / 2$   
 $= \tan 30$



$\therefore y_c = \left( \frac{2 \times 0.4^2}{9.81 \times \tan^3 30} \right)^{1/5}$

$$= 0.628 \text{ m}$$

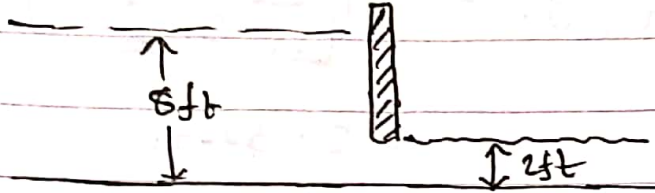
Since normal depth  $= 1.2 \text{ m} > 0.628 \text{ m} \therefore$  subcritical

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U/S  $\rightarrow$  upstream  
d/S  $\rightarrow$  downstream

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# The U/S & d/S depth of a sluice gate are 8ft & 2ft respectively. The channel is of rectangular shape & 10ft wide. Find the discharge under the gate.



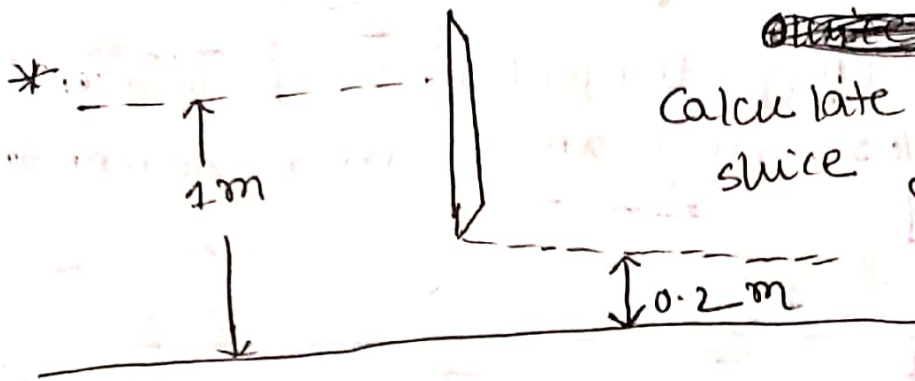
$$y_1 + \frac{v_1^2}{2g} = y_2 + \frac{v_2^2}{2g}$$

$$\Rightarrow 8 + \frac{Q^2}{2g b^2 y_1^3} = 2 + \frac{Q^2}{2g b^2 y_2^3}$$

$$\Rightarrow 6 = \frac{Q^2}{2g b^2} \left( \frac{1}{y_2^3} - \frac{1}{y_1^3} \right)$$

$$\Rightarrow Q^2 = \sqrt{\frac{2 \times 32.2 \times 10^2 \times 6}{\frac{1}{2^3} - \frac{1}{8^3}}}$$

$$\therefore Q = 406.03 \text{ ft}^3/\text{sec}$$



Calculate discharge of this sluice gate

[DNCC'22  
MIST]

Sol<sup>n</sup>:  $y_1 + \frac{v_1^2}{2g} = y_2 + \frac{v_2^2}{2g}$

$$\Rightarrow y_1 + \frac{Q^2}{2gy_1^3} = y_2 + \frac{Q^2}{2gy_2^3}$$

$$\Rightarrow 1 + \frac{Q^2}{2g \cdot 1^3} = 0.2 + \frac{Q^2}{2g \cdot (0.2)^3}$$

$$\Rightarrow \frac{Q^2}{2g} \left( \frac{1}{0.2^3} - \frac{1}{1^3} \right) = 1 - 0.2$$

$$\Rightarrow Q^2 = \frac{0.8 \cdot 2g}{\frac{1}{0.2^3} - \frac{1}{1^3}}$$

$$\therefore Q = \sqrt{\frac{2 \times 9.81 \times 0.8}{\frac{1}{0.2^3} - \frac{1}{1^3}}}$$

$$= 0.81 \text{ m}^3/\text{s}/\text{m width}$$

A

$$Q = \frac{v_1}{A}$$

$$= \frac{v_1}{b y_1}$$

$$= \frac{v_1^2}{y_1}$$

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Day

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\* A typical venturi flume of rectangular cross section has width of 2.5m at its upstream and 0.8m at its throat. For a particular flow through the flume, the upstream depth is measured as 1.2m. If the theoretical discharge is  $1.730 \text{ m}^3/\text{sec}$ , calculate the d/s water depth at the throat of the flume. ~~under~~ sub [RRI'11]

Soln<sup>g</sup>

$$y_1 + \frac{Q^2}{2gA_1^3} = y_2 + \frac{Q^2}{2gA_2^3}$$

$$\Rightarrow 1.2 + \frac{(1.73)^2}{2 \times 9.81 \times (2.5 \times 1.2)^3} = y_2 + \frac{(1.73)^2}{2 \times 9.81 \times (0.8 y_2)^3}$$

$$\Rightarrow 1.217 = y_2 + \frac{0.24}{y_2^3}$$

$$\Rightarrow y_2^3 - 1.217 y_2 + 0.24 = 0$$

Solving the eqn,  $y_2 = 0.952 \text{ m}$  A

In a rectangular channel, the discharge is  $40 \text{ ft}^3/\text{sec}$  per ft width. If a hydraulic jump occurs at a depth of 3 ft, calculate the height of the jump and the energy dissipated per foot width.

Soln

$$F_1 = \frac{V}{\sqrt{gy}} = \frac{\frac{40}{3}}{\sqrt{32.2 \times 3}} = 1.35$$

$$\begin{aligned} \therefore y_2 &= \frac{y_1}{2} \left[ \sqrt{1 + 8F_1^2} - 1 \right] \\ &= \frac{3}{2} \left[ \sqrt{1 + 8 \times (1.35)^2} - 1 \right] \\ &= 4.42 \text{ ft} \end{aligned}$$

$$\therefore \text{Jump Height} = (4.42 - 3) \text{ ft} = 1.42 \text{ ft} \quad \text{***} \quad \text{[BWB'16]}$$

$$\begin{aligned} \therefore \text{Energy head loss in jump, } \Delta H &= \frac{(y_2 - y_1)^3}{4y_1y_2} \\ &= \frac{(1.42)^3}{4 \times 4.42 \times 3} \\ &= 0.054 \end{aligned}$$

$$\begin{aligned} \therefore \text{Energy dissipated} &= \gamma Q \Delta H \\ &= 62.43 \times 40 \times 0.054 \\ &= 134.85 \text{ lb-ft/sec} \end{aligned}$$

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\* Water flows in a horizontal rectangular channel 6m wide at a depth of 0.52m and a velocity of 15.2m/s. If a hydraulic jump forms in the channel, determine the power dissipation in the jump in HP unit.

Sol<sup>n</sup>  $Fr_1 = \frac{15.2}{\sqrt{9.81 \times 0.52}} = 6.73$

$$y_2 = \frac{y_1}{2} \left[ \sqrt{1 + 8Fr_1^2} - 1 \right]$$
$$= \frac{0.52}{2} \left[ \sqrt{1 + 8 \times (6.73)^2} - 1 \right]$$
$$= 4.7 \text{ m}$$

Energy head loss,  $\Delta H = \frac{(4.7 - 0.52)^3}{4 \times 4.7 \times 0.52}$

$$= 7.47 \text{ m}$$

Power dissipation =  $\frac{\gamma Q \Delta H}{746}$  kW  $\rightarrow$  W

$$= \frac{9.81 \times 10^3 \times (6 \times 0.52 \times 15.2) \times 7.47}{746}$$

$$= 4658.53 \text{ HP}$$

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A hydraulic jump takes place in a 0.4 m wide laboratory flume. The initial depth of the jump is 20 mm and the flow rate is 3 l/sec. The flume is horizontal, rectangular & smooth. Calculate the sequent depth of the jump. If the dissipated power could be transformed into electricity, how many 40 W bulbs could be lighted?

Sol<sup>n</sup>o  $F_1 = \frac{3 \times 10^{-3}}{0.4 \times 20 \times 10^{-3}} = 8.75$  [B&DCL'21]

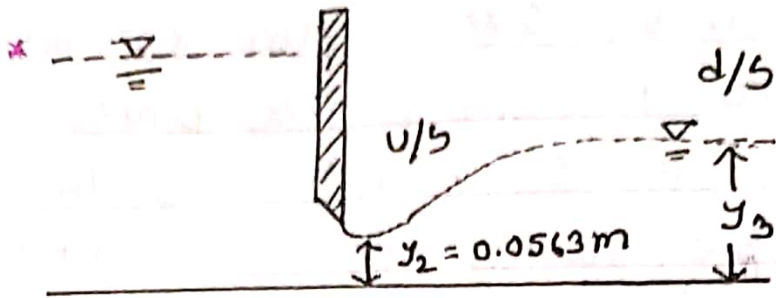
$$\therefore y_2 = \frac{20 \times 10^{-3}}{2} \left[ \sqrt{1 + 8 \times (8.75)^2} - 1 \right]$$

$$= 0.237 \text{ m}$$

$$\therefore \text{head loss} = \frac{(0.237 - 0.02)^3}{4 \times 0.237 \times 0.02} = 0.54 \text{ m}$$

$$\therefore \text{power dissipated} = 9.81 \times 10^3 \times \frac{3 \times 10^{-3}}{0.4} \times 0.54 = 164.22 \text{ watt}$$

$$\text{No of bulbs} = \frac{164.22}{40} \approx 4 \text{ Nos}$$



Determine the depth of flow downstream of the jump if the velocity under the gate is  $5.33 \text{ m/s}$

Sol<sup>n</sup>  $Fr_2 = \frac{5.33}{\sqrt{9.81 \times 0.0563}} = 7.17$

$$y_3 = \frac{y_2}{2} \left[ \sqrt{1 + 8Fr_2^2} - 1 \right]$$

$$= \frac{0.0563}{2} \left[ \sqrt{1 + 8 \times (7.17)^2} - 1 \right]$$

$$= 0.54 \text{ m} \quad \underline{\text{Ans}}$$

\* Water flows from a lake into a steep rectangular channel of  $3 \text{ m}$  wide. Determine the lake level above the channel bed at the outfall if discharge is  $40 \text{ m}^3/\text{sec}$ .

Sol<sup>n</sup> lake (or) rectangular channel is critical depth is  $2.627 \text{ m}$ .

$$\therefore \text{lake level at the outfall, } y_c = \left[ \frac{\left(\frac{40}{3}\right)^2}{9.81} \right]^{1/3}$$

$$= 2.627 \text{ m}$$

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\* A rectangular channel 2m wide carries 2.2m<sup>3</sup>/sec of water in subcritical uniform flow at a depth of 1m. What is the lowest transverse hump in the bottom such that <sup>critical depth</sup> is attained at the peak?

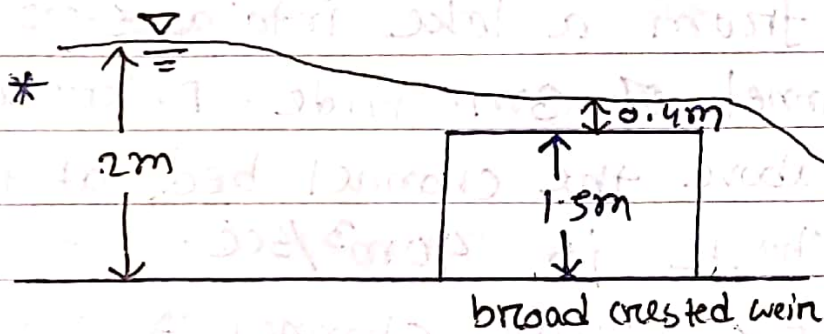
Sol<sup>n</sup>

$$y_1 + \frac{v^2}{2g} = E_{min} + z$$

critical depth  $1.5 \times 0.4$   
minimum head  $2.0$

$$\Rightarrow 1 + \frac{\left(\frac{2.2}{2 \times 1}\right)^2}{2 \times 9.81} = 1.5 \times 0.4 \left[ \frac{\left(\frac{2.2}{2}\right)^2}{9.81} \right]^{1/3} + z$$

$$\Rightarrow z = 0.315 \text{ m} \quad \underline{A}$$

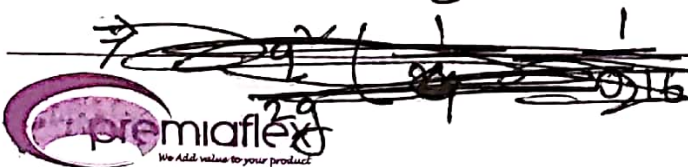


(6) What is the upstream velocity?

Sol<sup>n</sup>: width  $1.5 \text{ m}$ ,  $0.4$  unit width

$$y_1 + \frac{v_1^2}{2g} = y_2 + \frac{v_2^2}{2g} + z$$

$$\Rightarrow 2 + \frac{q^2}{2g \times 2^2} = 0.4 + \frac{q^2}{2g \times 0.4^2} + 1.5$$



$$\Rightarrow \frac{q^2}{2g} \left( \frac{1}{0.16} - \frac{1}{4} \right) = 2 - 0.4 - 1.5 = 0.1$$

$$\Rightarrow q^2 = \sqrt{\frac{0.1 \times 2 \times 9.81}{\frac{1}{0.16} - \frac{1}{4}}} = 0.572 \text{ m}^3/\text{s}/\text{m}$$

$$\therefore \text{upstream velocity} = \frac{0.572}{2} =$$

$$= 0.286 \text{ m/s}$$

Shortcut

\* unit discharge in

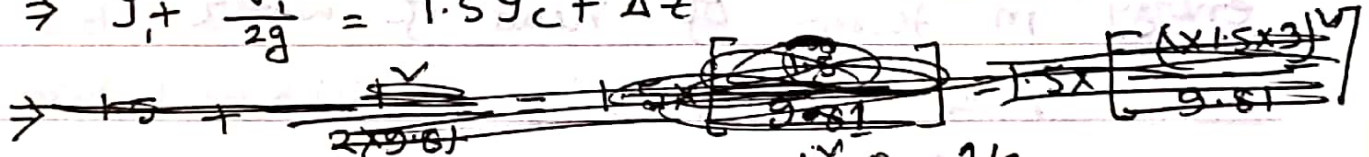
$$\text{a channel } q = \sqrt{\frac{2g \Delta H}{\frac{1}{y_2^2} - \frac{1}{y_1^2}}} \therefore \text{Discharge, } Q = q \times B$$

$$v = \frac{\text{discharge}}{\text{Area}}$$

\* Water flows at a velocity of 1 m/s and a depth of 1.5 m in a long rectangular channel of 3 m width. Compute the height of a smooth upward step in the channel bed to produce critical flow and the change in water level [BWD 19] [JB 17]

Soln  $E = E_{\text{critical}} + \Delta z$   $q = v \times y = 1.5 \times 1$  \*\*\*

$$\Rightarrow y_1 + \frac{v_1^2}{2g} = 1.5 y_c + \Delta z$$



$$\Rightarrow 1.5 + \frac{1^2}{2 \times 9.81} = 1.5 \times \left[ \frac{(1 \times 1.5)^2}{9.81} \right]^{1/3} + \Delta z$$

$$\Rightarrow \Delta z = 0.63 \text{ m}$$

$$* y_c = \left[ \frac{(1 \times 1.5)^2}{9.81} \right]^{1/3} = 0.612 \text{ [critical depth]}$$

$$\text{Change in water level, } \Delta H = (1.5 - 0.612 - 0.63) = 0.258 \text{ m}$$

\* A rectangular channel has a width of 2m and carries a discharge of  $4.8 \text{ m}^3/\text{sec}$  with a depth of 1.6m. At a certain cross-section, a small smooth hump with a flat top and a height 0.10m is proposed to be built. Calculate the likely change in the water surface. Neglect the energy loss.

Soln: Energy head at u/s

$$E_1 = 1.6 + \frac{\left(\frac{4.8}{2 \times 1.6}\right)^2}{2 \times 9.81} = 1.715 \text{ m}$$

at section 2,  $E_2 = 1.715 - 0.10 = 1.615$

$$\therefore E_2 = 1.615 = y_2 + \frac{\left(\frac{4.8}{2 \times y_2}\right)^2}{2 \times 9.81}$$

$$\Rightarrow 1.615 = y_2 + \frac{0.2935}{y_2^2}$$

$$\Rightarrow 1.615 y_2^2 = y_2^3 + 0.2935$$

Solving,  $y_2 = 1.48 \text{ m}$  or  $y_2 = 0.512 \text{ m}$

but  $y_c = \left(\frac{q^2}{g}\right)^{1/3} = \left[\frac{\left(\frac{4.8}{2}\right)^2}{9.81}\right]^{1/3} = 0.837 \text{ m}$

$\therefore$  minimum specific energy head,  $E_c = 1.5 \times 0.837 = 1.256$

$\therefore E_2 > E_c = 1.256$

$\therefore$  The flow must be subcritical, hence,  $y_2 = 1.48 \text{ m} > 0.837 \text{ m}$

∴ The drop at water surface elevation is,  
 $\Delta y = 1.6 - (1.48 + 0.10) = 0.02 \text{ m}$  A

\* A rectangular channel 2.5m wide carries  $6 \text{ m}^3/\text{sec}$  of flow at a depth of 0.50m. Calculate the height of a flat topped hump required to be placed at a section to cause critical flow. The energy loss due to the ~~obstruction~~ obstruction by the hump can be taken as 0.1 times the upstream velocity head.

Sol<sup>n</sup>  $V_1 = \frac{6}{2.5 \times 0.5} = 4.8 \text{ m/s}$

$$E_1 = 0.5 + \frac{(4.8)^2}{2 \times 9.81} = 0.5 + 1.1743 = 1.6743 \text{ m}$$

depth at  $y_c = \sqrt[3]{\frac{q^2}{g}}$   $= 0.837 \text{ m}$

$$\therefore E_2 = 1.5 \times 0.837 = 1.256 \text{ m}$$

$$\therefore E_1 = E_2 + \Delta z + HL$$

$$\Rightarrow 1.6743 = 1.256 + \Delta z + 0.1 \times 1.1743$$

$$\Rightarrow \Delta z = 0.3 \text{ m}$$
 A

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\* Water flows at a velocity of  $1\text{ m/s}$  and a depth of  $1.5\text{ m}$  in a long rectangular channel  $3\text{ m}$  wide. Compute the height of a smooth upward step in the channel bed to produce critical flow & the change in water level.

$$y_c = \left( \frac{Q^2}{gB^3} \right)^{1/3}$$

Sol<sup>n</sup>o

$$y_c = \left( \frac{4.5^3}{9.81 \times 3^3} \right)^{1/3} = 0.61\text{ m}$$

$$1.5 + \frac{1^2}{2 \times 9.81} = 1.5 \times 0.61 + \Delta z$$

$$\therefore \Delta z = 0.635\text{ m}$$

$$\therefore \text{hump height} = 0.635\text{ m}$$

$$\text{Change in water level} = 1.5 - 0.61 - 0.635 = 0.255\text{ m}$$

\* A trapezoidal channel has a bottom width of  $6\text{ m}$  & side slope  $1:1$ . The depth of flow is  $1.5\text{ m}$  at a discharge of  $15\text{ m}^3/\text{s}$ . Determine specific energy in terms of head of water [BUET '12]

Sol<sup>n</sup>o

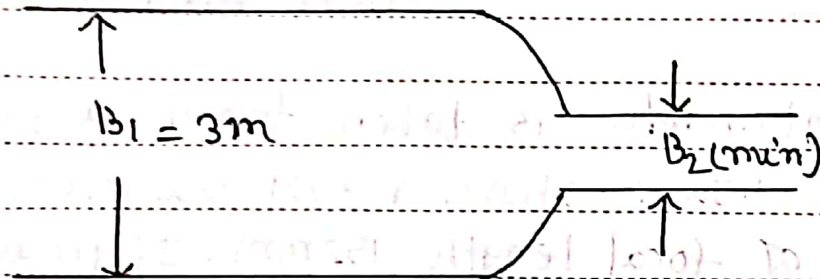
$$A = (b + sy)y = (6 + 1 \times 1.5)1.5 = 11.25\text{ m}^2$$

$$\therefore \text{Energy} = 1.5 + \frac{15^2}{2 \times 9.81 \times (11.25)^2} = 1.59\text{ m}$$

$$y + \frac{q^2}{2gAy}$$



\* Depth of water flowing in a 3m wide rectangular channel is 2m. The channel carries a discharge of  $12 \text{ m}^3/\text{s}$ . Calculate the minimum <sup>bed</sup> width at contraction which just causes the critical flow without ~~the~~ changing the upstream water level.



Sol<sup>n</sup>: Specific energy at section 1,

$$E_1 = y_1 + \frac{v_1^2}{2g}$$

$$= 2 + \frac{\left(\frac{12}{3 \times 2}\right)^2}{2 \times 9.81} = 2.2038 \text{ m}$$

at section 2, depth is critical,

$$\therefore E_c = \frac{3}{2} y_c = 2.2038$$

$$\Rightarrow y_c = \frac{2}{3} \times 2.2038 = 1.47 \text{ m}$$

again,  $\Rightarrow \left(\frac{q^2}{g}\right)^{1/3} = 1.47$



$$\Rightarrow \frac{q^2}{g} = 3.17$$

$$\Rightarrow q^2 = 31.114$$

$$\Rightarrow q = 5.578$$

$$\Rightarrow \frac{Q}{B_2(\text{min})} = 5.578$$

$$\Rightarrow B_2(\text{min}) = \frac{Q}{5.578} = \frac{12}{5.578} = 2.15 \text{ m}$$

Q. A rectangular channel is 3.50m wide conveying a discharge of 15m<sup>3</sup>/sec at a depth of 2m. It is proposed to reduce the width of the channel at a hydraulic structure. Determine the minimum width which does not cause choking.

Sol<sup>n</sup>: Specific energy at  $V/5$

$$E_1 = 2 + \frac{\left(\frac{15}{3.5 \times 2}\right)^2}{2 \times 9.81} = 2.234 \text{ m}$$

for no choking condition, ~~Maximum depth which will not cause~~

~~Choking~~  $y_c = \frac{2}{3} E$  [  $E_c = \frac{3}{2} y_c$  ]

again ~~at~~

$$= \frac{2}{3} \times 2.234$$

$$= 1.489 \text{ m}$$

again,  $y_c = \left[ \frac{(Q/B)^2}{g} \right]^{1/3}$

$$\Rightarrow (1.489)^3 = \frac{15^2}{B^2 \times 9.81}$$

$$\Rightarrow \therefore B_{\min} = 2.635 \text{ m}$$

$\therefore$  minimum width = 2.635m

## Force acting on hydraulic wall structure

$$F = \frac{1}{2} b \gamma (y_1^2 - y_2^2) - \rho Q \Delta V$$

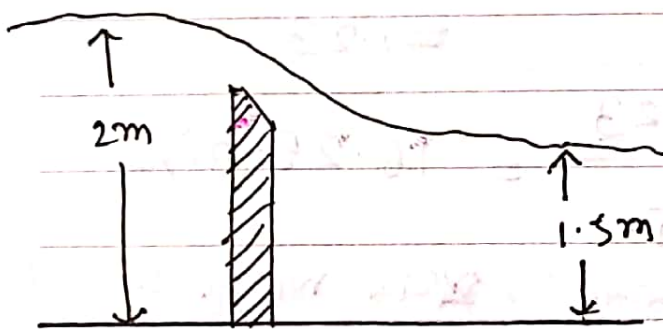
\*  $\Delta V$  ~~ଅବକାଶ~~ positive ଥାଏ ଥାଏ ।

\*  $\gamma = 9.81 \times 10^3 \text{ N/m}^3$  ନିର୍ଦ୍ଦିଷ୍ଟ ଥାଏ ।  
 $= 62.43 \text{ lb/ft}^3$

Water density,  $\rho = 1000 \text{ kg/m}^3$

$= 1.94 \text{ slugs/ft}^3$  \*\*\*

$$\rho = \frac{\gamma}{g} = \frac{62.43}{32.2} = 1.94$$



If unit discharge is  $4 \text{ m}^2/\text{s}$ .

Estimate energy loss & force on weir.

Soln:  $v_1 = \frac{4}{2} = 2 \text{ m/s}$ ,  $v_2 = \frac{4}{1.5} = 2.67 \text{ m/s}$

Applying energy eq<sup>n</sup>,

$$2 + \frac{2^2}{2 \times 9.81} = 1.5 + \frac{(2.67)^2}{2 \times 9.81} + h_L$$

$$\Rightarrow h_L = 0.34 \text{ m}$$

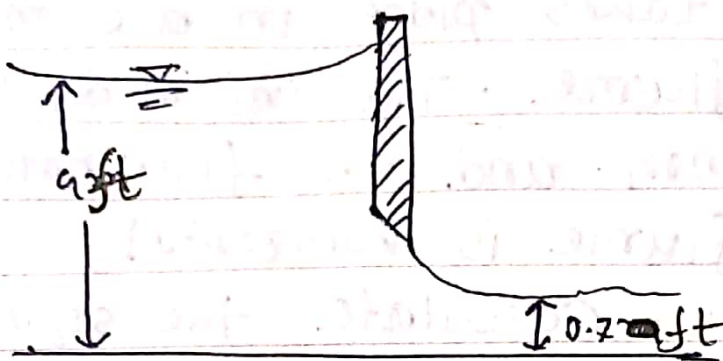
$$\text{Force} = \frac{1}{2} \gamma (y_1^2 - y_2^2) - \rho Q \Delta V$$

$$= \frac{1}{2} \times 9.81 \times 1000 \times (2^2 - 1.5^2) - 1000 \times 4 \times (2.67 - 2)$$

$$= 5903.75 \text{ N}$$

A





compute the force per unit width

~~Sol<sup>no</sup> 9 =  $\sqrt{2 \times 9.81 \times (4 - 0.7)}$~~

Sol<sup>no</sup> 0

$$q = \sqrt{\frac{2 \times 32.2 \times (4 - 0.7)}{\frac{1}{0.7^2} - \frac{1}{4^2}}} = 10.36 \text{ ft}^2/\text{sec}$$

$$\therefore v_1 = \frac{10.36}{4} = 2.6 \text{ ft/sec} ; v_2 = 14.8 \text{ ft/sec}$$

$$\therefore F = \frac{1}{2} \gamma (y_1^2 - y_2^2) - \rho q \Delta v$$

$$= \frac{1}{2} \times 62.43 (4^2 - 0.7^2) - \frac{62.43}{32.2} \times 10.36 \times (14.8 - 2.6)$$

$$= 238.4 \text{ lb-ft/sec/m width}$$

~~238.4~~  
= 238.4

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# calculate the rate of flow over a sharp crested rectangular weir 6ft wide & 3ft height, If the head over the weir is 10 in &  $C_d = 0.63$

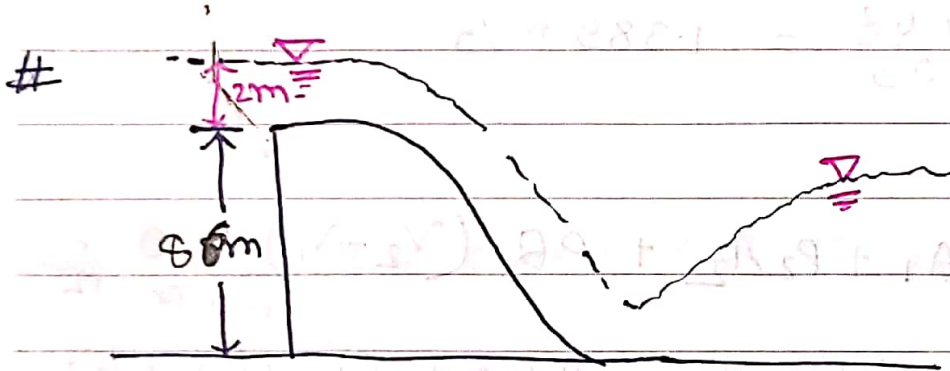
Height 3ft

Sol<sup>n</sup>:  $Q = \frac{2}{3} C_d A V$

$A = b \times \text{head}$

$$= \frac{2}{3} \times 0.63 \times (6 \times \frac{10}{12}) \times \sqrt{2 \times 32.2 \times \frac{10}{12}}$$

$$= 15.4 \text{ ft}^3/\text{sec}$$



# The length of spillway is 100m.  $C_d = 2.4$   
Compute discharge.

Sol<sup>n</sup>:

$$Q = \frac{2}{3} C_d (bn) \times \sqrt{2gh}$$

$$= \frac{2}{3} \times 2.4 \times (100 \times 2) \times \sqrt{2 \times 9.81 \times 2}$$

$$= 2004.54 \text{ m}^3/\text{sec}$$

\* The head regulator of a canal has three openings each 3m wide. The water is flowing between the upper and lower gates. The vertical opening of the gate is  $w = 1.0m$ . The head on the regulator is  $0.45m$ . If the upstream water level rises by  $0.2m$ , how much the upper gates must be lowered to maintain the canal discharge unaltered. Use  $C_d = 0.62$ . [MSc WRE '19]

Sol<sup>n</sup>: total width of regulator openings =  $3 \times 3$   
 $b = 9m$

$$\text{discharge, } Q = C_d \cdot b \cdot w \cdot \sqrt{2gy}$$

$$= 0.62 * 9 * 1 * \sqrt{2 * 9.81 * 0.45}$$

In second case, when u/s water level rises by  $0.20m$ , let the gate opening be  $xm$  to keep the discharge unaltered. — (i)

$$\therefore Q = 0.62 * 9 * x * \sqrt{2 * 9.81 * (0.45 + 0.20)} \quad \text{--- (ii)}$$

$\therefore$  from eq<sup>n</sup> (i) & (ii),

$$x * \sqrt{0.65} = 1 * \sqrt{0.45}$$

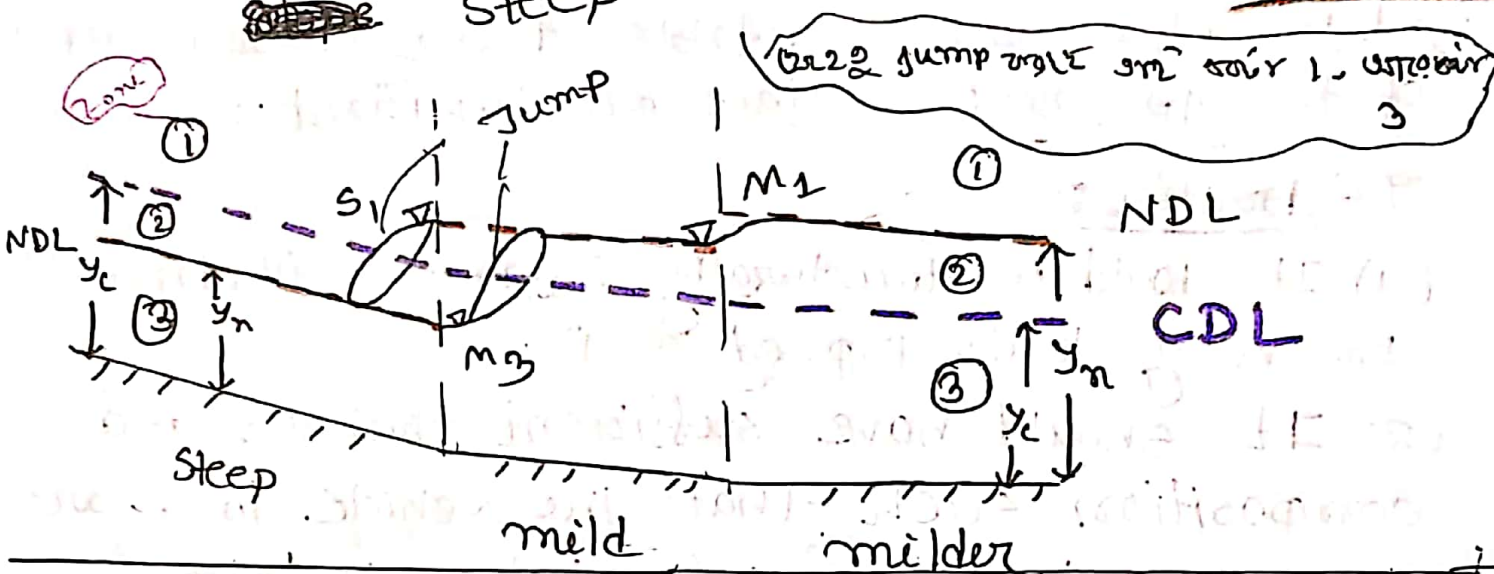
$$\Rightarrow x = 0.83m$$



Hence, the gate must be lowered by an amount of  $(1 - 0.83)m = 0.17m$

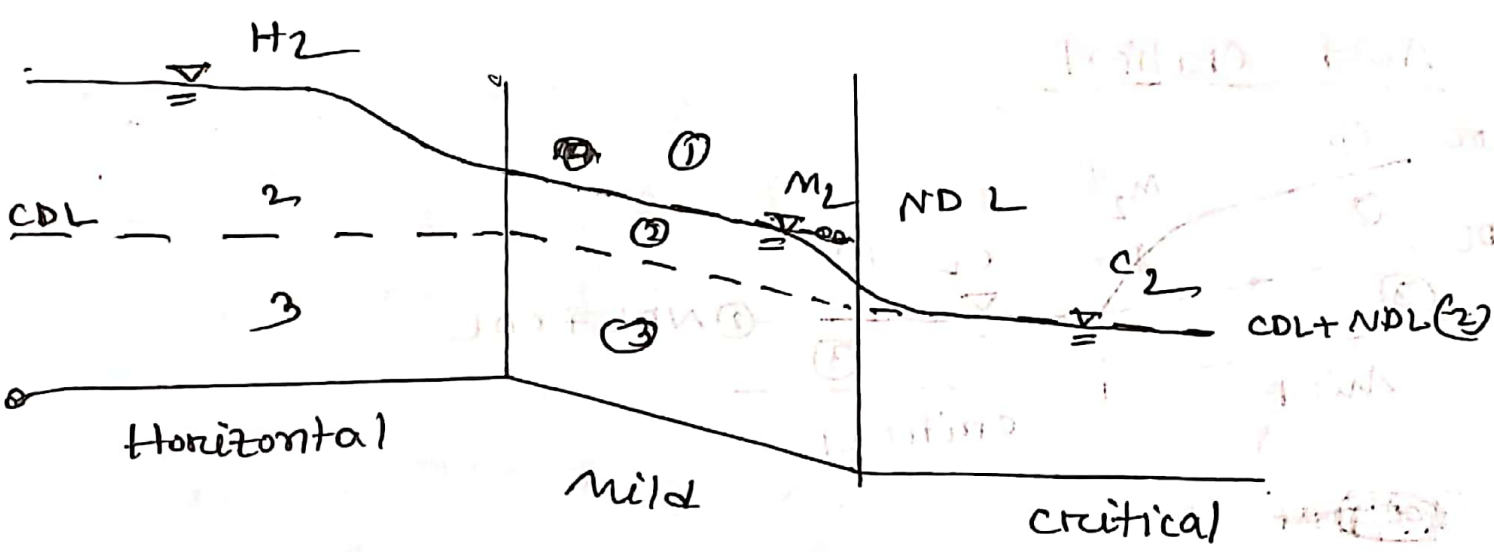
VESTAR MR<sup>®</sup>  
 TRIMETAZIDINE

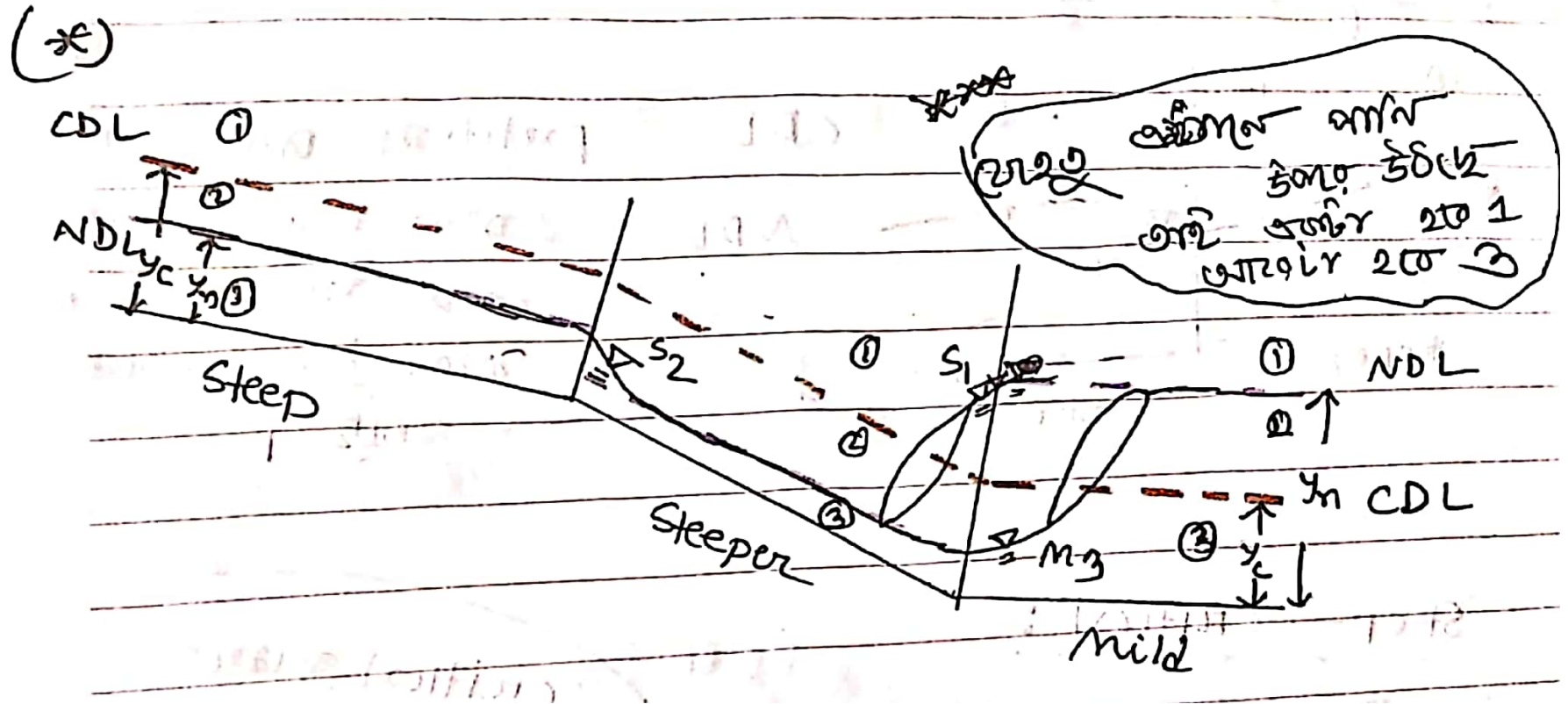
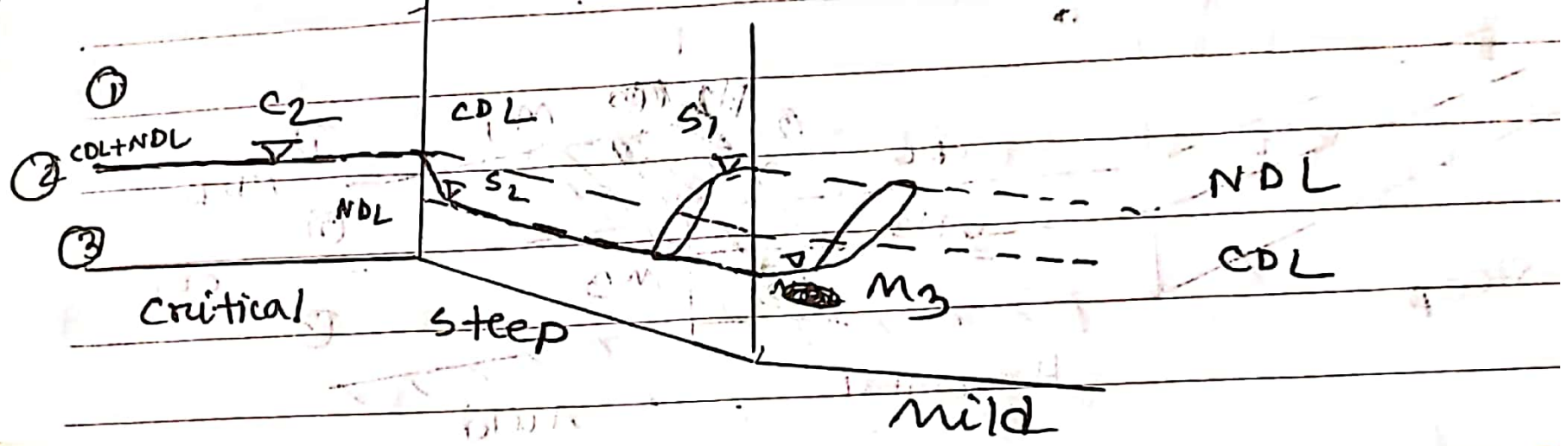
\* Draw water surface profile for the following  
 Channel slope — ~~steep~~ Steep — mild — milder EMEMCI



\* In NDL lower than NDL a water flow is CDL and jump zone.

\* Zone 1, 3 (two sections flow subcritical, zone 2 two sections flow supercritical)





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(9) A 1m wide rectangular channel has a bed slope of 0.0016 and the Manning's coefficient is 0.04. Uniform flow takes place in the channel at a flow depth of 0.5m. Determine slope type.

[DMTCL Line 55]

Sol<sup>n</sup>:

$$Q = \frac{1}{n} AR^{2/3} S^{1/2}$$

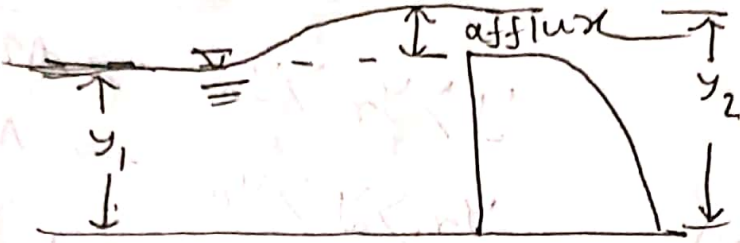
$$= \frac{1}{0.04} \times (1 \times 0.5) \times \left( \frac{1 \times 0.5}{1 + 2 \times 0.5} \right)^{2/3} \times \sqrt{0.0016}$$

$$= 0.1984 \text{ m}^3/\text{s}$$

$$\therefore y_c = \left( \frac{Q^2}{gB^3} \right)^{1/3} = \left[ \frac{(0.1984)^2}{9.81 \times 1^3} \right]^{1/3} = 0.16 \text{ m}$$

$$\therefore y_n = 0.5 > y_c = 0.16$$

$\therefore$  mild slope. Ans



length of backwater curve,  $l = \frac{E_1 - E_2}{S_b - S_e}$

$S_b$  = given bed slope

$S_e$  = energy line slope

$E_1$  = energy head at  $y_1$

$E_2$  = energy head at  $y_2$

\*\*\* A rectangular channel 8m wide, bed slope of 0.0016 &  $n = 0.0025$ . Normal & critical depth are 1m & 0.576m. Compute the length of backwater curve created by a dam which backs up a depth of 2m immediately behind the dam in a gradually varied flow. [BWD/19]

$$v_1 = \frac{1}{0.0025} \times \left( \frac{8 \times 1}{8 + 2 \times 1} \right)^{2/3} \times (0.0016)^{1/2}$$

$$= 13.8 \text{ m/s}$$

$$E_1 = 1 + \frac{(13.8)^2}{2 \times 9.81} = 10.71 \text{ m/s}$$

(width = 8m = const)

$$V_2 = \frac{V_1 y_1}{y_2} = \frac{13.8 \times 1}{2} = 6.9 \text{ m/s}$$

$$E_2 = 2 + \frac{(6.9)^2}{2 \times 9.81} = 4.43 \text{ m}$$

now,  $S_e$  calculation

$$y_{av} = \frac{1+2}{2} = 1.5 \text{ m}$$

~~$$V_{av} = \frac{13.8 \times 1}{1.5} = 9.2 \text{ m/s}$$~~

$$V_{av} = \frac{V_1 y_1}{y_{av}} = \frac{13.8 \times 1}{1.5} = 9.2 \text{ m/s}$$

$$R_{av} = \frac{8 \times 1.5}{8 + 2 \times 1.5} = 1.091 \text{ m}$$

$$V_{av} = \frac{1}{n} R_{av}^{2/3} S_f^{1/2}$$

$$\Rightarrow 9.2 = \frac{1}{0.0025} \times (1.091)^{2/3} \times \sqrt{S_f}$$

$$S_f = 0.00047$$

length of backwater curve,  $L = \frac{E_1 - E_2}{S_0 - S_f}$

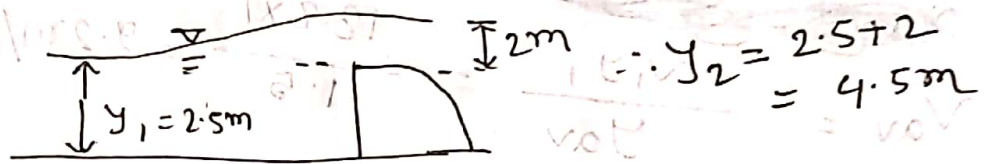
$$= \frac{10.71 - 4.43}{0.0016 - 0.00047}$$

$$= 5.552 \text{ km} \underline{A.S}$$

$V_{av} = \frac{v_1 + v_2}{2}$   
 21000 m/s  
 $V_{av}$  2m  
 avg depth  
 $S_e$  avg velocity

\* Determine the length of backwater curve caused by an afflux of 2m in a rectangular channel of width 40m & depth 2.5m. The slope of bed is given as 1 in 16000. Take Manning's  $n = 0.03$

Soln:



$$V_1 = \frac{1}{0.03} \left( \frac{40 \times 2.5}{40 + 2 \times 2.5} \right)^{2/3} \times \sqrt{\frac{1}{16000}} = 0.54 \text{ m/s}$$

$$E_1 = 2.5 + \frac{(0.54)^2}{2 \times 9.81} = 2.51 \text{ m}$$

$$V_2 = \frac{0.54 \times 2.5}{4.5} = 0.3$$

$$E_2 = 4.5 + \frac{(0.3)^2}{2 \times 9.81} = 4.5 \text{ m}$$

$$y_{avg} = \frac{2.5 + 4.5}{2} = 3.5$$

$$V_{avg} = \frac{V_1 y_1}{y_{avg}} = \frac{0.54 \times 2.5}{3.5} = 0.385 \text{ m/s}$$

$$V_{avg} = \frac{1}{n} R_{avg}^{2/3} \times \sqrt{S}$$

$$\Rightarrow 0.385 = \frac{1}{0.03} \times \left( \frac{40 \times 3.5}{40 + 2 \times 3.5} \right)^{2/3} \times \sqrt{S}$$

$$S = 0.00003$$

$$\therefore L = \frac{4.5 - 2.5}{0.0000909 - 0.00003} = 32.671 \text{ km}$$

BAPEX - 2023

Non - 36

Depth -  $6 \times 4 = 24$

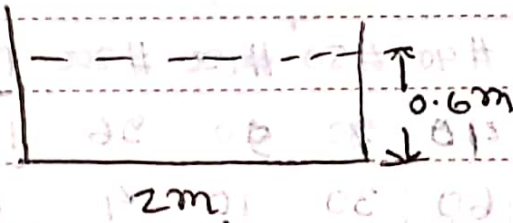
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(1) Fill in the gaps :-

(a) Pitot tube measures the total head of fluid

(b) The depth of 2m wide channel is 0.6, the hydraulic depth 0.6m.



$$* D = \frac{\text{Area}}{\text{Top width}} = \frac{2 \times 0.6}{2}$$

(c) Hydraulic depth does not depend on space ~~(length)~~/distance in uniform flow.

(d) ~~Potential~~ <sup>Specific</sup> ~~Potential~~ energy depends on hydraulic depth only.

\* Pitot tube measures velocity & pressure head & measure for 25.

\* Determine the field capacity of a soil for the following data -

Depth of root zone = 1.70m, existing moisture = 8%,  
dry density of soil =  $1450 \frac{\text{kg}}{\text{m}^3}$ , quantity of water  
applied to soil =  $650 \text{m}^3$ , water loss due to deep  
percolation and evaporation = 10%, Area of irrigation  
land =  $10000 \text{m}^2$  [BWDB'22]

Soln: Water stored in root zone depth =  $\frac{0.9 \times 650}{10000} = 0.585 \text{m}$

Water stored in root zone =  $G_s \cdot d \cdot [F.C. - M.C.]$

$\Rightarrow 0.585 = \frac{1450}{10000} * 1.70 [F.C. - 0.08]$

$\therefore F.C. = 0.317 \quad \therefore \text{Field Capacity} = 31.73\%$



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\* An irrigation field has following data -

Field capacity = 25%

Permanent wilting Point = 15%

~~Specific~~ unit weight =  $14.03 \text{ kN/m}^3$

Root zone depth = 90 cm

Calculate the available moisture holding capacity of soil [Titas '21]

Sol<sup>n</sup>: Available moisture holding capacity

$$= \frac{0.9 \times 14.03 \times [0.25 - 0.15]}{9.81}$$

$$= 0.1287 \text{ m} = 12.87 \text{ cm} \quad \underline{A}$$

\* The following data pertains to healthy growth of a crop:

→ Field capacity = 30%

→ Permanent wilting point = 11%

→ Effective depth of root zone = 200 mm

→ Porosity of soil = 39%

→ Daily consumptive use of water = 12 mm

For healthy growth moisture content must not fall below 25% of water holding capacity.

Determine the watering interval in days.

Sol<sup>n</sup>:

~~\*\*\*~~

$$G_s = \frac{\text{porosity}}{\text{field capacity}} = \frac{0.39}{0.30} = 1.3$$



$$\begin{aligned} \therefore \text{Depth of water in root zone} \\ &= 1.3 * 700 * 0.75 * (0.30 - 0.11) \\ &= 129.675 \text{ m} \end{aligned}$$

$$\therefore \text{watering interval} = \frac{700}{129.675} = \frac{129.675}{12} \approx 10.8 \text{ days} \approx 10 \text{ days}$$

11 gal per Day 5-200, 500  
more 5000 water,

\* The field capacity & moisture content at the time of irrigation are 27% and 19%. The apparent specific gravity is 1.3 & the root zone depth is 100cm. Determine the time required to irrigate 2ha with a flow of 60l/s, if the water application losses are taken to be 20% [BWD B'2016]

$$\begin{aligned} \text{Sol}^n: \text{ Net irrigation depth} &= 1.3 \times 100 \times [0.27 - 0.19] \\ &= 10.4 \text{ cm} \\ &= 0.104 \text{ m} \end{aligned}$$

$$\text{Field irrigation depth} = \frac{0.104}{0.8} = 0.13 \text{ m}$$

$$\begin{aligned} \text{Volume of irrigation water} &= 0.13 \times 2 \times 10^4 \\ &= 2600 \text{ m}^3 \end{aligned}$$

$$\begin{aligned} \text{Time required} &= \frac{2600}{60 \times 10^{-3} \times 3600 \text{ m}^3/\text{hr}} \\ &= 12.037 \text{ hr} \end{aligned}$$

## # Relation Between Duty & Delta

$$\Delta = \frac{864 B}{D}$$

Related math  
Titas '21

$\Delta$  (delta) in cm

$D$  = Duty (hectares/cumec)

$B$  = Base period (days)

\* What is the discharge capacity required at the outlet to irrigation 2600ha of sugarcane having a korz depth of 17cm & a korz period of 30 days.

Sol<sup>n</sup> Duty =  $\frac{864 B}{\Delta} = \frac{864 \times 30}{17}$   
= 1524.71 ha/cumec

$\therefore$  Discharge capacity =  $\frac{2600 \text{ ha}}{1524.71 \text{ ha/cumec}}$   
= 1.705 cumec

\* A canal commands an irrigation area of 400ha. The duty of water on the field during the peak period is 220ha/cumec. Determine the design discharge of the canal at the off take if the water loss in the canal is 30%? [BWB'16]

Sol<sup>n</sup> Discharge =  $\frac{400}{220} = 1.82 \text{ cumec}$

design discharge =  $\frac{1.82}{0.70} = 2.60 \text{ m}^3/\text{sec}$

\* A crop required 45cm of water during 120 days of base period. The total rainfall during this period is 100mm. Assume the irrigation efficiency to be 60%. Calculate the area of land which can be irrigated with a canal flow of 0.01 cumec,

$$\begin{aligned} \text{Sol}^n: \text{ Duty of irrigation water} &= \frac{864 \times B}{\Delta} \\ &= \frac{864 \times 120}{(45 - 10)} \\ &= 2962.286 \text{ ha/cumec} \end{aligned}$$

$$\text{effective canal flow} = 0.6 \times 0.01 = 0.006 \text{ cumec.}$$

$$\begin{aligned} \therefore \text{Area to be irrigated} &= 2962.286 \times 0.006 \\ &= 17.773 \text{ ha} \end{aligned}$$

\* A pump is installed on a well to lift water and to irrigate rice crop, sown over 3 hectares of land. If duty for rice is 864 hectares/cumec on the field and pump efficiency is 48%, determine the minimum required input (HP) of the pump if the water level is 8m below the ground.

$$\text{Sol}^n: \text{ Discharge required} = \frac{3}{864} = \frac{1}{288} \text{ m}^3/\text{sec}$$

$$\begin{aligned} \text{Input of the pump} &= \frac{\text{WH}}{\eta} = \frac{9.81 \times \frac{1}{288} \times 8}{0.48} = 0.567 \text{ kW} \\ &= 567 \text{ W} \end{aligned}$$

$$\begin{aligned} \frac{567}{746} \text{ HP} \\ = 0.76 \text{ HP} \end{aligned}$$



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\* If wheat requires about 7.5 cm of water in every 28 days and the base period for wheat is 140 days, find out delta.

Soln:

$$\Delta = \frac{140}{28} \times 7.5 \text{ cm} = 37.5 \text{ cm} \text{ An}$$

\* The gross commanded area for a distributory is 6000 hectares, 80% of which is culturable. The intensity of irrigation for Kharif season is 25% & that for Rabi season is 50%. If the average duty at the head of distributory is 700 hectares/cumec for ~~Rabi~~ <sup>Kharif</sup> season, <sup>& 1700 for Rabi season.</sup> find the discharge required for design at the head distributory.

Soln:

Discharge required for Kharif season,

$$Q_k = \frac{0.8 \times 6000 \times 0.25 \text{ ha}}{700 \text{ ha/cumec}} = 1.714 \text{ m}^3/\text{sec}$$

$$\text{Discharge for Rabi season} = \frac{0.8 \times 6000 \times 0.50 \text{ ha}}{1700 \text{ ha/cumec}} = 1.41 \text{ m}^3/\text{s}$$

∴ Design discharge = maximum value  
= 1.714 m<sup>3</sup>/sec



\* Determine the time required to irrigate a strip of land of 0.04 hectares in area from a tube-well with a discharge of 0.02 cumec. The infiltration capacity of the soil may be taken as 5 cm/hr & the average depth of flow on the field as 10 cm. Also determine the maximum area that can be irrigated from this tubewell.

[ WRE MSc'21 ]

Sol<sup>n</sup>:  $t = \frac{y}{f} \ln \left( \frac{Q}{Q - fA} \right)$

$$t = \frac{10}{5} \ln \left( \frac{72}{72 - 0.05 \times 400} \right)$$

$$= 0.65 \text{ hrs}$$

$$= 39 \text{ min}$$

Max<sup>m</sup> area that can be irrigated

$$i s = \frac{Q}{f} = \frac{72}{0.05} \text{ m}^2 = 1440 \text{ m}^2$$

$$y = 10 \text{ cm}$$

$$f = 5 \text{ cm/hr} = 0.05 \text{ m/hr}$$

$$Q = 0.02 \text{ m}^3/\text{sec}$$

$$= 0.02 \times 60 \times 60$$

$$= 72 \text{ m}^3/\text{hr}$$

$$A = 0.04 \text{ ha}$$

$$= 0.04 \times 10^4 \text{ m}^2$$

$$= 400 \text{ m}^2$$

A

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\* pH value for fertile soil 6.5 to 7.5\*  
[Titus'21]

\* drinking water pH 6.5 to 8.5\*

\* Salinity of water is measured by electric conductivity values [BPDB'21]

EC values (micro mhos/cm)	Class
< 250	Low salinity water (C <sub>1</sub> )
250-750	medium salinity water (C <sub>2</sub> )
750-2250	High salinity water (C <sub>3</sub> )
> 2250	Very high salinity (C <sub>4</sub> )

Sodium Absorption Ratio (SAR):

$$SAR = \frac{Na^+}{\sqrt{\frac{Ca^{2+} + Mg^{2+}}{2}}}$$

SAR value	Water type
0-10	Low sodium water (S <sub>1</sub> )
10-18	medium sodium water (S <sub>2</sub> )
18-26 (Titus'21)	High sodium water (S <sub>3</sub> )
> 26	Very high sodium water (S <sub>4</sub> )

→ what is the classification of irrigation water having the following characteristics:  
 concentration of Na, Ca & Mg are 22, 3 & 1.5 milli-equivalents per litre respectively & the electric conductivity is 200 micro mhos/cm ~~per~~ at 25°C.

(b) what problems might arise in using this water on fine textured soils?

(c) what remedies do you suggest to overcome this trouble?

Sol<sup>m</sup>

$$SAR = \frac{Na^+}{\sqrt{\frac{Ca^{2+} + Mg^{2+}}{2}}} = \frac{22}{\sqrt{\frac{3+1.5}{2}}} = 14.67$$

$10 < SAR < 18 \Rightarrow$  medium sodium water ( $S_2$ )

$EC = 200 \mu\text{mhos/cm} < 250$   
 $\Rightarrow$  low salinity water ( $C_1$ )

Hence it is classified as  $C_1 - S_2$  water

(b) Problems that might arise —

- soil becomes less permeable
- It becomes plastic & sticky when wet
- It starts crusting when dry
- Its pH increases

(c) Gypsum ( $CaSO_4$ ) addition in soil or water to overcome sodium hazards posed by the given water.



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Duty: It is defined as the area of land in hectares which can be irrigated for growing any crops if one cumec of water is supplied continuously to the land for the entire base period of crop.

Unit - hectares/cumec

Delta: The total depth of water over irrigation field required by a crop to come to maturity is called delta.

Gravity Dam: A gravity dam is such a structure which is designed in such a way that its own weight resists the external forces.

Forces acting on gravity dam [PGCB'17]

- Water pressure
- Uplift pressure
- pressure due to earthquake force
- Silt pressure
- Wave pressure
- The stabilising force (self weight of dam)

## Irrigation Channel Design:

$$\text{Manning's coefficient, } n = \frac{d_{50}^{1/6}}{21.10}$$

$$\text{or } n = \frac{d_{75}^{1/6}}{24}$$

$$\text{Max}^m \text{ hydraulic radius, } R_{\text{max}} = \frac{d}{11.5}$$

ଅର୍ଥାତ୍  $\theta, \phi$  (ଅବସର କୋଣ)  $R_{\text{max}} = \frac{kd}{0.75 \times 11.5}$

$$\text{ଅର୍ଥାତ୍ } k = \frac{\tau'_c}{\tau_c} = \sqrt{1 - \frac{\sin^2 \theta}{\sin^2 \phi}}$$

\* Irrigation canal ଗଠିବା ପାଇଁ,  $R = y$  (depth)

\* Critical shear stress,  $\tau_c = \tau^* (G_s - 1) \gamma_w D$

$\Rightarrow \tau^* = \text{dimensionless effective stress}$

again,  $\tau_c = \gamma_w R S$

$$\text{discharge, } Q = \frac{1}{n} A R^{2/3} S^{1/2}$$

$$Q = \frac{1.486}{n} A R^{2/3} S^{1/2} \quad \left[ \text{ft ସମ୍ବନ୍ଧରେ (ଅବସର କୋଣ)} \right]$$

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D (0.075) meter  $\Rightarrow R_{max}$   
 $n, R_{max}$  or  $Q$  2.82

\* An irrigation channel is to be constructed in a coarse alluvium gravel with D75 size of 5cm. The channel has to carry 3 cumecs of discharge and the longitudinal slope is 0.01. Find the minimum width of the channel.

Soln:  $R_{max} = \frac{d}{115}$   
 $= \frac{5}{115} m = 0.455 m$

$$n = \frac{d^{1/6}}{24}$$
$$n = \frac{(0.05)^{1/6}}{24}$$
$$= 0.0253$$

$$Q = \frac{1}{n} A R_{max}^{2/3} S^{1/2} = \frac{1}{n} (b \times R_{min}) \times R_{max}^{2/3} S^{1/2}$$

$$\Rightarrow 3 = \frac{1}{0.0253} \times b_{min} \times (0.455)^{2/3} \times \sqrt{0.01}$$

$$\Rightarrow b_{min} = 2.82 m \quad \underline{A}$$

\* A canal is to be designed to carry a discharge of 56 cumec. The slope of the canal is 1 in 1000. The soil grain size is 5cm. Assuming the canal to be unlined & of a trapezoidal section, determine the depth of the canal. Take  $\phi = 32^\circ$

Sol<sup>n</sup>:

let  $\theta = 30^\circ$

$$\text{Now, } \frac{\tau_c'}{\tau_c} = \sqrt{1 - \frac{\sin^2 \theta}{\sin^2 \phi}} = \sqrt{1 - \frac{\sin^2 30^\circ}{\sin^2 32^\circ}}$$

$$= 0.557$$

$$\therefore R_{\max} = \frac{0.557 \times \frac{5}{100}}{0.75 \times 11 \times \frac{1}{1000}} = 3.375 \text{ m}$$

$$\therefore \text{depth} = 3.375 \text{ m} \quad \underline{\underline{A}}$$

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\* The value of dimensionless effective stress is ~~0.045~~ 0.045. Find the value of incipient depth and effective velocity of a wide river channel with the bed sediment size of 2mm & bed slope of 0.0001 [BWB'16]

Soln:

$$\tau_c = \tau^* (G_s - 1) \gamma_w d$$
$$= 0.045 (2.65 - 1) \times 9.81 \times \frac{2}{1000}$$
$$= 1.457 \times 10^{-3} \text{ KN/m}^2$$

Take  
Sp. Gr = 2.65

again,  $\tau_c = \gamma_w R S$

$$\therefore R = \frac{\tau_c}{\gamma_w S} = \frac{1.457 \times 10^{-3}}{9.81 \times 0.0001}$$
$$= 1.485 \text{ m}$$

$\therefore$  depth,  $y = 1.485 \text{ m}$  Ans

$$\eta = \frac{d^{1/6}}{21.16} = \frac{(2 \times 10^{-3})^{1/6}}{21.16} = 0.0168$$

$$\therefore V = \frac{1}{\eta} R^{2/3} S^{1/2}$$

$$= \frac{1}{0.0168} \times (1.485)^{2/3} \times \sqrt{0.0001}$$
$$= 0.774 \text{ m/s} \quad \underline{A}$$

## Regime channel Design:

For channel or flow which is in a state of silting or scouring, the channel is in a regime state.

### True Regime:

- (1) Discharge is constant
- (2) Flow is uniform
- (3) Amount of silt is constant
- ~~(4) silt is constant grade~~
- (4) silt grade is constant
- (5) channel is flowing through a material which can be scoured as easily as it can be deposited.

### Design of Regime channel According to Lacey's Theory -

$$\Rightarrow \text{silt factor, } f = 1.76 \sqrt{d_{\text{mm}}} \quad \left[ \begin{array}{l} d \text{ (ବରଷ୍ଟା) ମି.} \\ \text{ଅନୁ ୨୦।} \end{array} \right]$$

$$\Rightarrow \text{velocity, } v = \left[ \frac{Qf^2}{140} \right]^{1/6} \text{ m/s}$$

$$\Rightarrow \text{Hydraulic mean depth, } R = \frac{5}{2} \left( \frac{v^3}{f} \right) = \text{Regime scowz depth}$$

$$\Rightarrow \text{bed slope, } S = \frac{f^{5/3}}{3340 Q^{1/6}}$$

$$\Rightarrow \text{Perimeter, } P = 4.75 \sqrt{Q} = \text{Regime width}$$

$$\Rightarrow \text{Normal scowz depth, } = 1.35 \left( \frac{Q^2}{f} \right)^{1/3}$$



Date: / /

Sun Mon Tue Wed Thu Fri Sat

\* Calculate the scour depth of a river having flow  $2500 \text{ m}^3/\text{s}$ , bed material size is  $0.15 \text{ mm}$  [BWB'22]

~~Sol<sup>n</sup>:~~

$$f = 1.76 \sqrt{0.15} = 0.68$$

~~Normal scour depth,  $R = 1.35 \left( \frac{Q}{f} \right)^{1/3}$~~   
 ~~$= 1.35 \left( \frac{2500}{0.68} \right)^{1/3}$~~

Sol<sup>n</sup>:  $f = 1.76 \sqrt{0.15} = 0.68$

$$v = \left[ \frac{Qf^2}{140} \right]^{1/6} = \left[ \frac{2500 \times (0.68)^2}{140} \right]^{1/6}$$
$$= 1.42 \text{ m/s}$$

$$\therefore \text{Scour depth} = \frac{5}{2} \left( \frac{v^2}{f} \right)$$
$$= \frac{5}{2} \times \frac{(1.42)^2}{0.68}$$
$$= 7.43 \text{ m}$$

Region scour depth  $\approx$   $7.43 \text{ m}$

\* Calculate scour depth for a rivet having width of 50m & unit discharge  $50 \text{ m}^3/\text{s}/\text{m}$ .  
 ~~$d_{50} = 0.1 \text{ mm}$~~   $d_{50} = 0.1 \text{ mm}$ . Design discharge is 80% of bank full discharge. [BWBDB'20]

⇒ Sol<sup>n</sup>

$$f = 1.76 \sqrt{0.1} = 0.537$$

$$\text{Normal scour depth} = 1.35 \left[ \frac{q^2}{f} \right]^{1/3}$$

$$= 1.35 \left[ \frac{(0.8 \times 50)^2}{0.537} \right]^{1/3}$$

$$= 19.42 \text{ m } \underline{A}$$

\* Types of scour occurs near bridge piers → (Padm bridge Project'2013)

- Aggradation & degradation scour
- contraction scour
- Local scour

Design an irrigation channel in alluvial soil according to Lacey's silt theory.

Given the following data - [PGCB'20]

discharge =  $15 \text{ m}^3/\text{sec}$  [DPDC'20]

Lacey's silt factor  $\alpha = 1.0$  [SGCL'20]

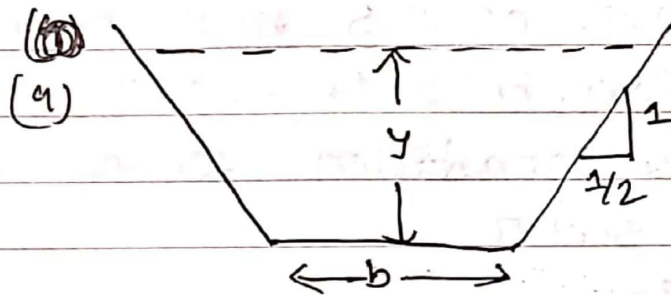
channel's side slope =  $\frac{1}{2}H : 1V$

Sol<sup>n</sup>:

(1) velocity,  $v = \left[ \frac{Q \times f^v}{140} \right]^{1/6} = \left[ \frac{15 \times 1^v}{140} \right]^{1/6} = 0.69 \text{ m/s}$

(2) Area,  $A = \frac{15}{0.69} = 21.74 \text{ m}^2$

(3) perimeter,  $P = 4.75\sqrt{A} = 4.75\sqrt{15} = 18.4 \text{ m}$



$A = (b + sy)y$   
 $= (b + \frac{1}{2}y)y$   
 $= by + \frac{y^2}{2}$

$\therefore by + \frac{y^2}{2} = 21.74$  — (i)

$P = b + 2y\sqrt{s^2 + 1}$

$\Rightarrow 18.4 = b + 2y\sqrt{\frac{1}{4} + 1}$

$\Rightarrow b + \sqrt{5}y = 18.4$  — (ii)

$\Rightarrow b = 18.4 - \sqrt{5}y$  — (ii)

from eq<sup>n</sup> (i) & (ii)

$(18.4 - \sqrt{5}y)y + \frac{y^2}{2} = 21.74$

$\Rightarrow 18.4y - \sqrt{5}y^2 + \frac{y^2}{2} = 21.74$



Solving this,  $y = 1.35 \text{ m}$

$\therefore b = 18.4 - \sqrt{5} \times 1.35 = 15.4 \text{ m}$

(5) Hydraulic radius,  $R = \frac{5v^v}{2f} = \frac{5 \times 0.69^v}{2 \times 1}$

$= 1.2 \text{ m}$

(6) Bed slope,  $s = \frac{f^{5/3}}{3340 Q^{1/6}} = \frac{1^{5/3}}{3340 \times 15^{1/6}}$

$= 0.00019$

A

## River Training:

River training covers all those engineering works which are constructed on a river so as to guide and confine the flow to the river channel and to control and regulate the river bed configuration, thus ensuring safe and effective disposal of floods and sediment loads. Stabilising and training the river along a certain alignment with a suitable waterway is therefore the first and foremost aim of river training.

### Objectives of River Training:

- (i) Provide a safe passage to flood discharge without overflowing to the bank for protection of cultivated or inhabited area.
- (ii) Prevent ~~outflanking~~ outflanking (अपसर्पण) of structures like a bridge, weir or aqueduct constructed across the river.

- (3) Protect the bank from erosion and improve the alignment by stabilizing the river channel.
- (4) Deflect the river away from the bank which it might be attacking.
- (5) Provide minimum depth of flow and a good course for navigation purpose.
- (6) Ensure effective disposal of sediment load.

### Classification of River Training: (Important)

#### (i) High Water Training:

- ⇒ Primary purpose is flood control.
- ⇒ It aims at providing sufficient river cross-section for the safe passage of maximum flood. It is also concerned with making adjoining area flood proof by construction of ~~dikes~~ levees.

#### (ii) Low Water Training:

- ⇒ Primary purpose to provide sufficient water depth for navigation during lower water period.
- ⇒ Accomplished by concentrating and enhancing

the flow in the desired channel by closing other channels.

(iii) mean water training:

⇒ aims at efficient disposal of suspended load and bed load and thus to preserve the channel in good shape

⇒ The mean water training is the most important type and forms the basis on which the former two are planned.

Methods for River Training: (UPSC)

- Important**
- (i) Marginal Embankments/levees
  - (ii) Guide banks
  - (iii) Groynes or spurts
  - (iv) Artificial cut-offs
  - (v) Pitching of banks & provision of launching aprons
  - (vi) Pitched islands
  - (vii) Sills, Bandalling etc

## Guide Bank:

স্থলকাজ ২ টি

১/ নদী যাতে গতিমত পরিবর্তন না ঘটে - অন্য দিক দিয়ে প্রবাহিত হতে না পারে। কারণ তাহলে bridge বা অন্য কোন structure গন্যে সিট useless হতে পারে।

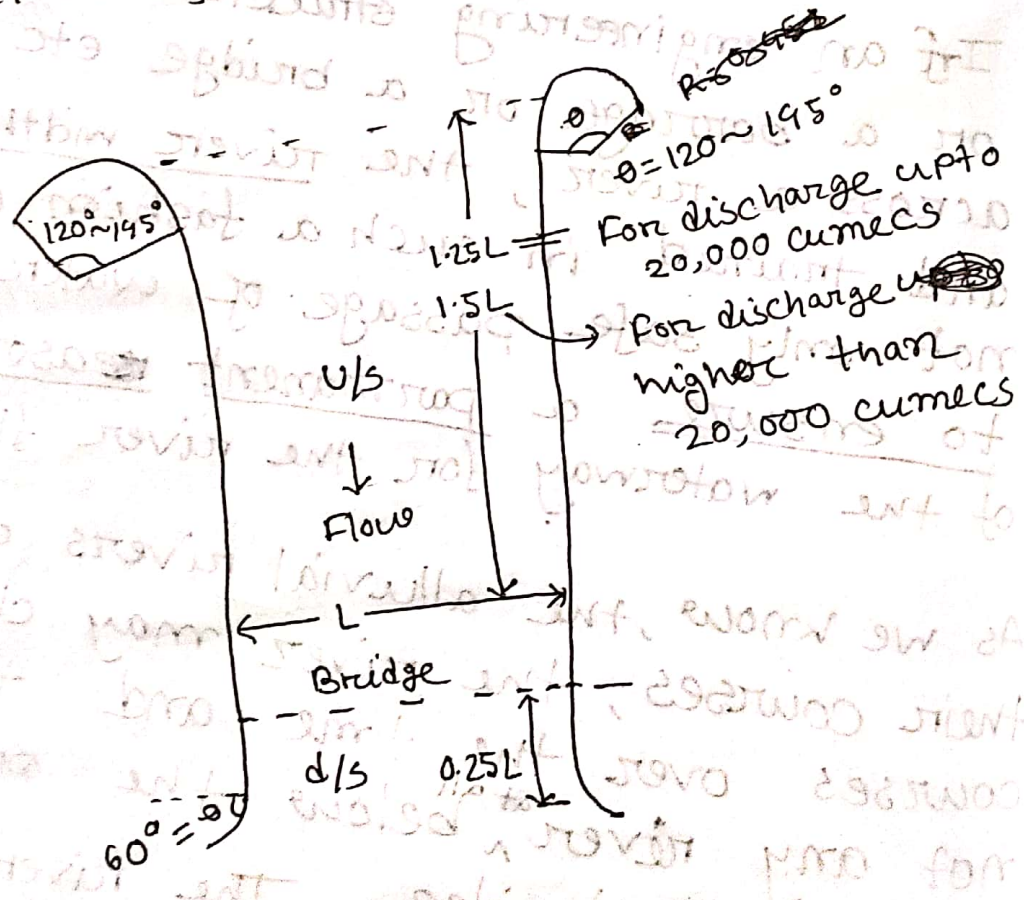
২/ নদীর width বন্ধানো। সুতরাং নদীর প্রস্থ কুট-ক্রীজ / weir / dam গন্যে সিট বুদ্ধিমানের কাজ।  
প্রচুর স্বাক্ষর হতে!

If an engineering structure, such as a weir or a barrage or a bridge etc is constructed across a river, the river width is reduced and trained in such a fashion as to ensure not only safe passage of water but also to ensure a permanent reasonable width of the waterway for the river flow.

As we know, the alluvial rivers do shift their courses, the river may change it courses over the time. and there may not any river <sup>at all</sup> below the presently constructed bridge. The river may be found to be flowing away from it,

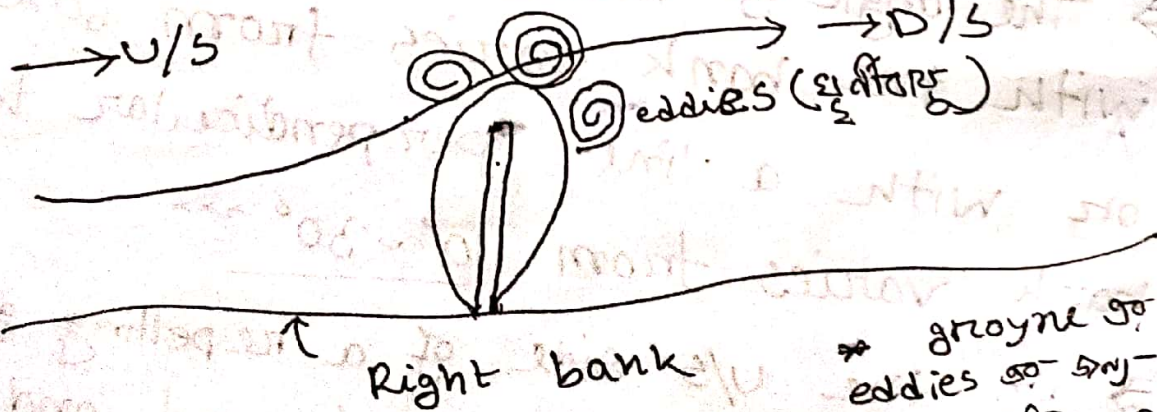
necessitating the construction of another structure.

Besides it is unwise and uneconomical to span the entire width of the river and to expose structure for deep scour. Hence, a structure such as a weir / bridge / barrage etc is extended in a smaller width of the river.



## Spurs or Groynes :

Groynes are the embankment type structures constructed <sup>(transverse)</sup> transverse to the river flow, extending from bank into the river. That is why, they may also called "Transverse Dykes". They are constructed in order to protect the bank from which they are extended, by deflecting the current away from the bank. As the water is unable to take a sharp embayment (left bank) the bank gets protected.



\* groyne nose is heavily pitched and is made of concrete or stone.

The nose of groyne is subjected to tremendous action of water and has to be heavily protected by pitching etc. The action of eddies reduces from the head towards the bank, therefore the thickness of slope pitching and apron can be reduced accordingly.

### Repelling Groynes:

⇒ A groyne pointing  $u/s$  tends to repel the river flow away from the bank on which it is provided and hence it is called a repelling groyne.

⇒ The angle of inclination of repelling groynes with the bank varies from  $60^\circ \sim 80^\circ$  or with a line perpendicular to the bank varies from  $10^\circ \sim 30^\circ$ .

⇒ On the  $u/s$  side of a repelling groyne, a still water pocket is formed and the

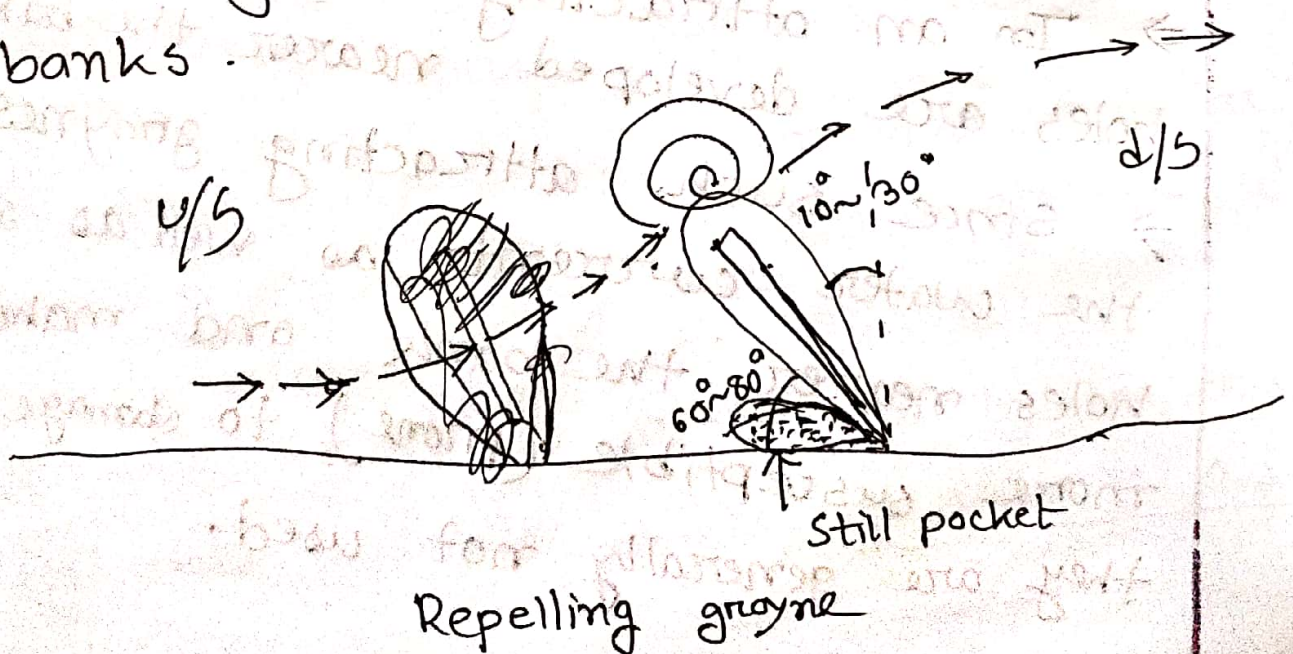
suspended sediment carried by the river gets deposited in the pocket.

⇒ The head of a repelling groyne cause disturbances in the flow at its nose.

⇒ Heavy scour occurs at the nose due to eddy formation.

⇒ The head of a repelling groyne needs a very strong protection because it is subjected to direct attack of a swirling current.

\*\*\* normal groyne (perpendicular alignment) is generally used on convex banks, repelling groyne is used on concave banks.



\*\*\* When the length of an ~~is~~ repelling groyne is small such that it changes only the direction of flow without repelling it, it is called a deflecting groyne.

### Attracting groyne:

⇒ A groyne pointing d/s tends to attract the river flow towards the bank on which it is provided. Hence it is called an attracting groyne.

⇒ The angle of inclination of an attracting groyne with the bank may be in the range of ~~30° to 60°~~  $60^\circ \sim 80^\circ$ .

⇒ In an attracting ~~hole~~ groyne, scour holes are developed nearer the bank.

⇒ Since such attracting groynes bring the water current as well as scour holes nearer the bank and make it more susceptible (prone) to damage,

they are generally not used.

## Diversion Head Works

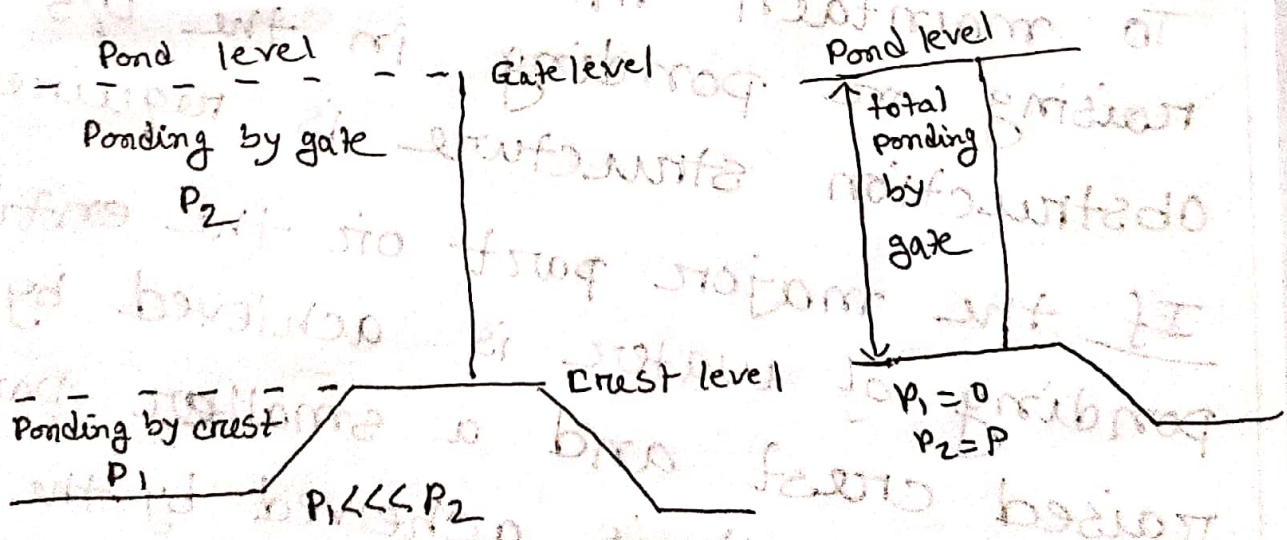
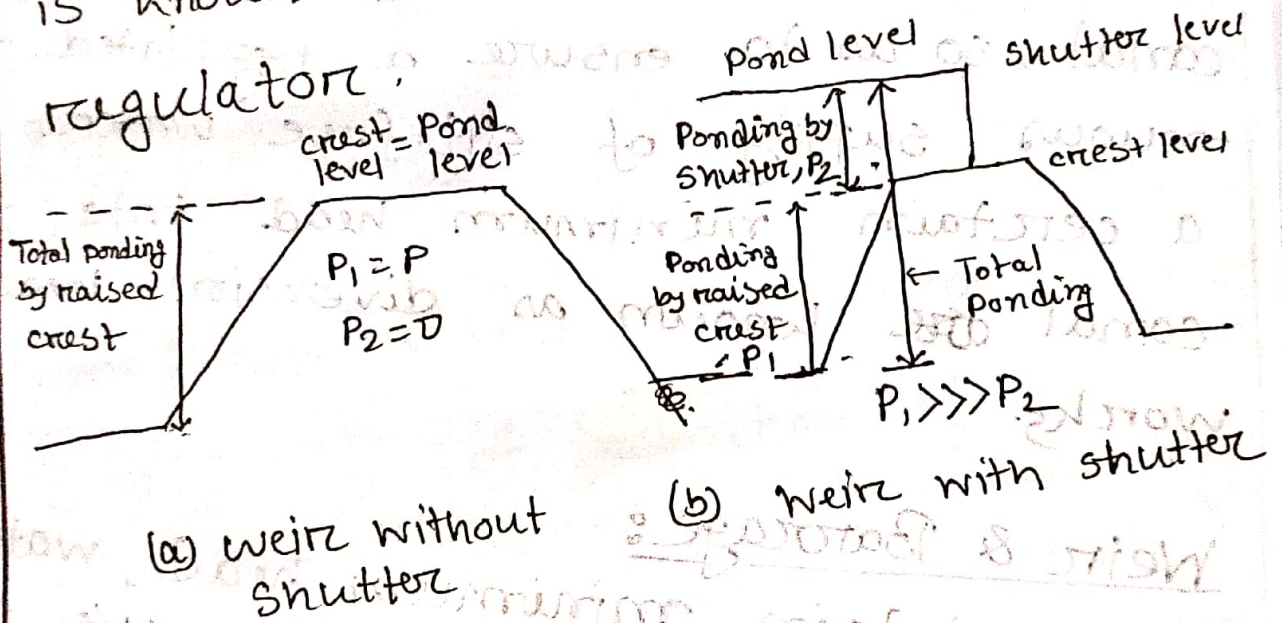
An irrigation canal takes its supply from a river or a stream. In order to divert water from the river into the canal it is necessary to construct certain works or structures across the river in order to divert the river water towards the canal, so as to ensure a regulated continuous supply of silt-free water with a certain minimum head into the canal ~~are~~ known as diversion head works.

### Weir & Barrage:

To maintain minimum head, water level raising or ponding in the u/s side of obstruction structure is required.

If the major part or the entire ponding of water is achieved by a raised crest and a smaller part or nil part of it is achieved by the shutters then ~~this~~ this barrier is known as a weir.

On the other hand, if most of the pond is done by gates/shutter and a smaller or nil part of it is done by the raised crest, then the barrier is known as a barrage or a river regulator.



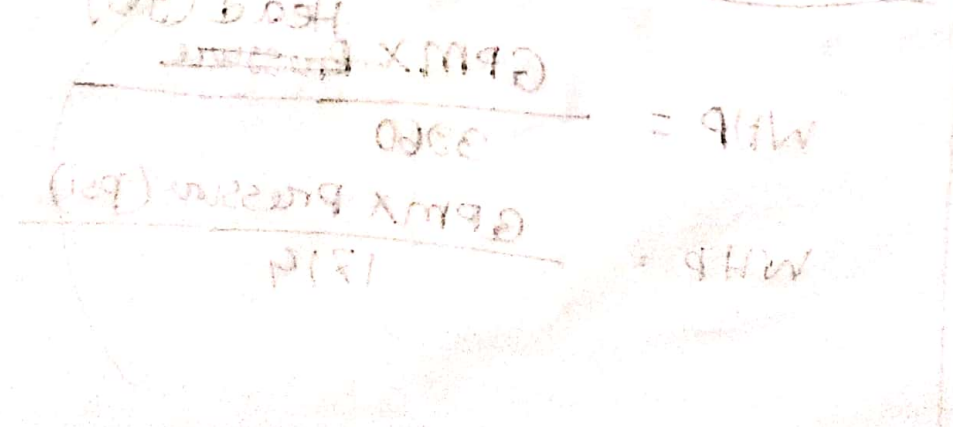
If most of the ponding or entire ponding is done by a permanent raised crest as in a weir, then the afflux caused during high flood is quite high.

on the other hand, if most of the ponding is done by gates as in a barrage, then the gates can be opened during high floods and the afflux will be nil or minimum.

Hence, barrage gives less afflux and better control upon river flow.

A weir is relatively cheaper but will lack the effective control over river flow as compared to barrage.

But a barrage can be provided with a roadway across the river at a small additional cost. (barrage cum bridge)

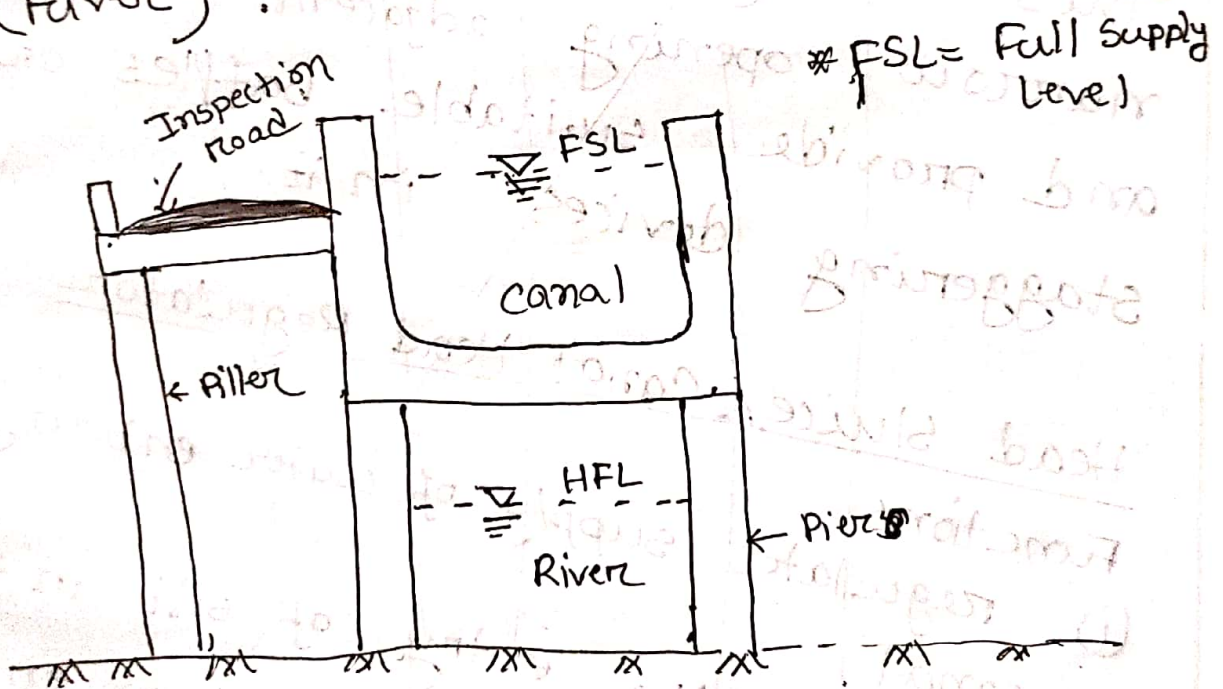


# Cross Drainage Works

## Aqueduct:

The hydraulic structure in which the irrigation canal is taken over the drainage (such as river, stream) is known as aqueduct.

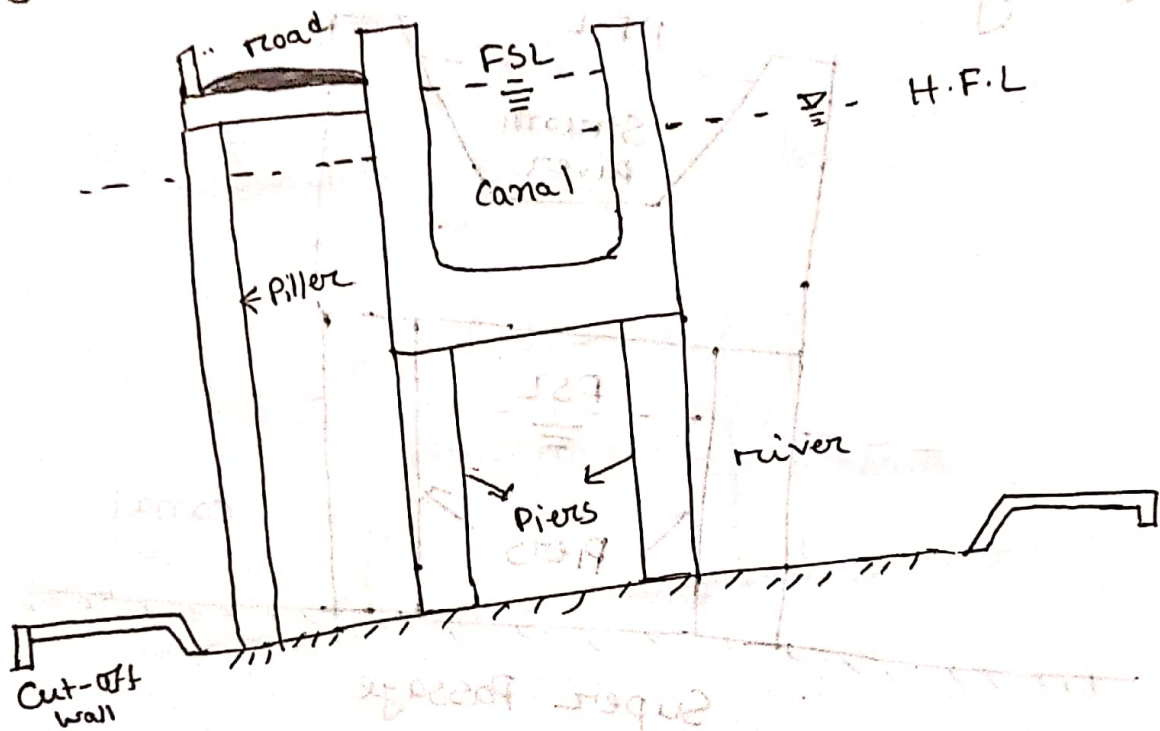
This structure is suitable when bed level of canal is above the highest flood level (HFL) of drainage (river).



Aqueduct

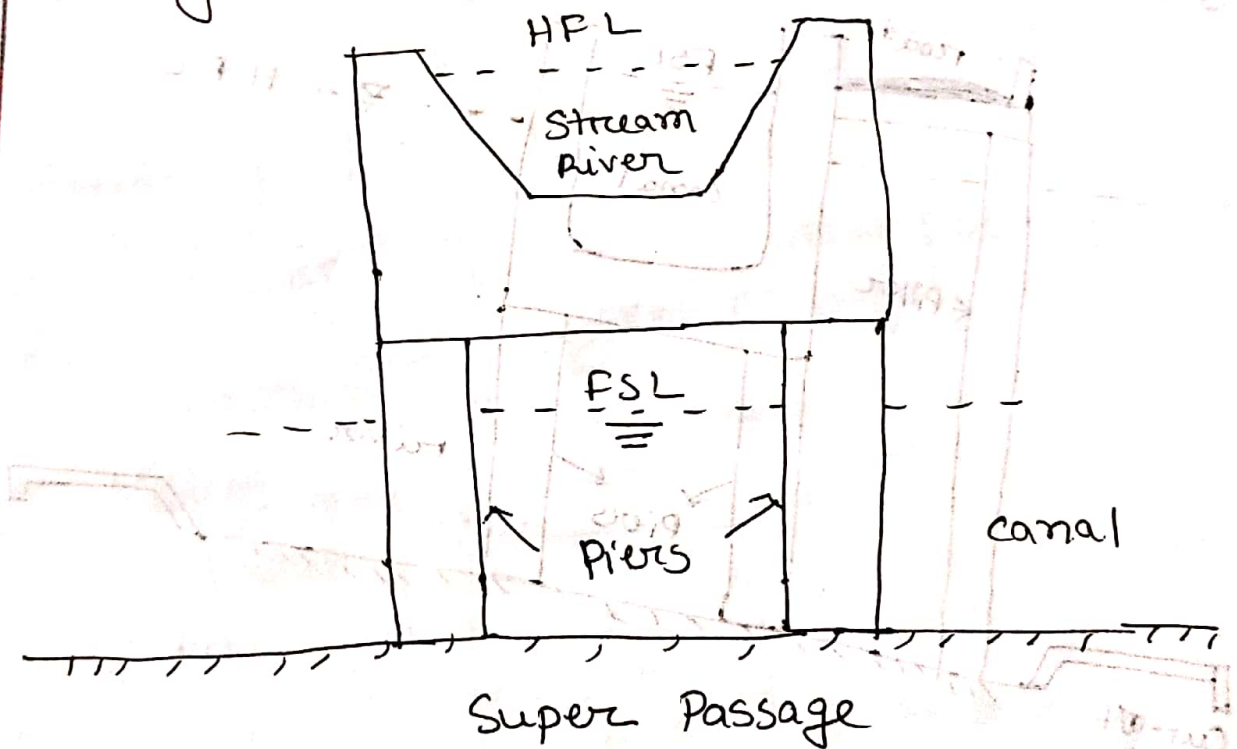
Siphon Aqueduct : In a hydraulic structure where the canal is taken over the drainage but the drainage water cannot pass clearly below the canal. It flows under siphonic action.

This structure is suitable when the bed level of canal is below the highest flood level.



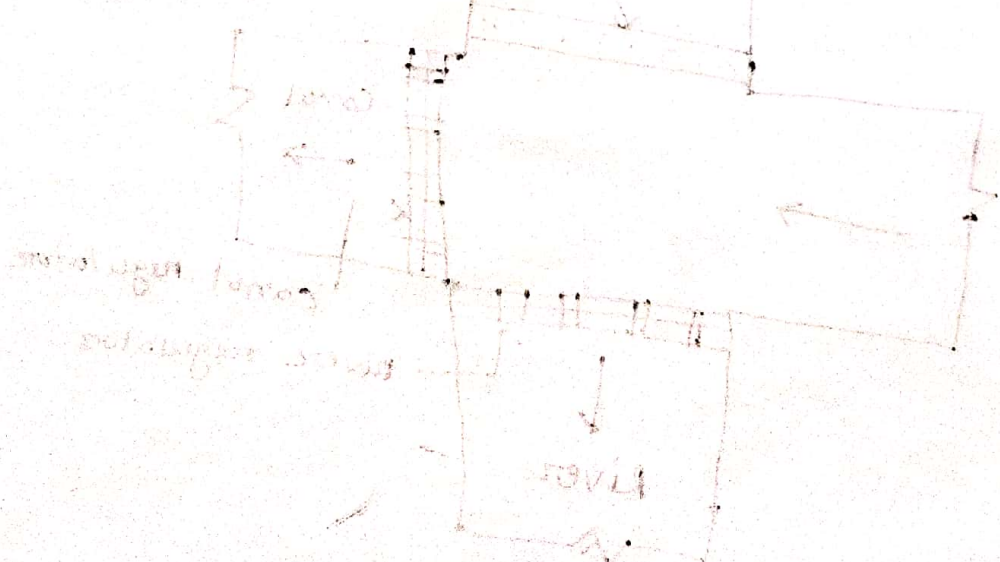
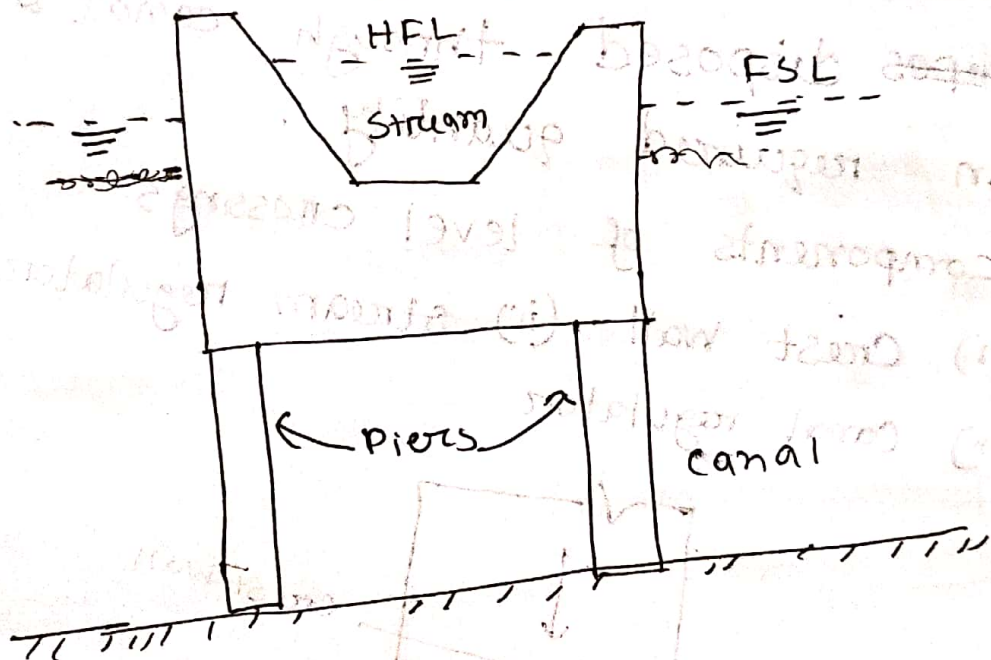
Super Passage: The hydraulic structure in which the <sup>crivory</sup> drainage is taken over the irrigation canal is known as super passage.

Bed level of drainage is above the FSL of canal. The water of the canal passes clearly below the drainage.



Siphon Super Passage: The hydraulic structure in which the drainage is taken over the irrigation canal, but the canal water passes below the drainage under siphonic action is known as siphon super passage.

This structure is suitable when the bed level of drainage is below the full supply level of the canal.



Level Crossings: When the bed level of canal and the stream are approximately the same and quality of water in canal & stream is almost same, the ~~cross~~ level crossing is constructed where water of canal & stream is allowed to mix.

With the help of regulators, water is ~~dis~~ disposed through canal & stream in required quantity.

Components of level crossings

- (i) Crest wall
- (ii) stream regulator
- (iii) Canal regulator

