

Influence line:

An influence line is a diagram showing the variation in the shear, moment, stress in a member, reaction or other direct function at a particular section or point or member, due to a unit load moving across the structure.

Construction of Influence Line: An influence line is constructed by plotting directly under the point where the unit load is placed and ordinate the height of which represents to some scale the value of the particular function being studied when the load is in that point.

Purpose of Influence Lines:

Influence lines can be used for two very important purposes -

1. To determine what position of live loads will lead to a maximum value of the particular function for which an influence line has been constructed.
2. To compute the value of that function with the loads so placed or in fact for any loading condition.

Theorem 1: To obtain the maximum value of a function due to a single concentrated line load, the load should be placed at the point where the ordinate to the influence line for the function is a maximum.

Theorem 02: The value of a function due to the action of a single concentrated live load equals the product of the magnitude of the load and the ordinate to the influence line for that function, measured at the point of application of load.

Theorem-03: To obtain the maximum value of a function due to a uniformly distributed live load, the load should be placed over

CE 1201 - Analysis of statically determinate arches, beams, frames, trusses and cables.

all those portions of the structure for which the ordinates to the influence line for that function have the sign of the character of the function desired.

- Analysis of statically determinate arches.
- Influence lines for statically determinate structures.
- Moving loads on beam, frames and trusses
- Cable supported structures and
- Space trusses

Kind of loads

1. Dead load:

Dead loads are loads which always fixed in position, always acting, and of unchanging magnitude.

The dead load in a building includes the weight of walls, permanent partitions, furniture, floors, roofs and all other permanent stationary construction entering into building

(a) Weight of material of which a structure is composed

b. Permanent equipments such as gas/water/sewerage pipe/electric cables etc.

2. Live loads:

The live load includes all loads ~~exp~~ except dead loads. Live loads which can move or movable

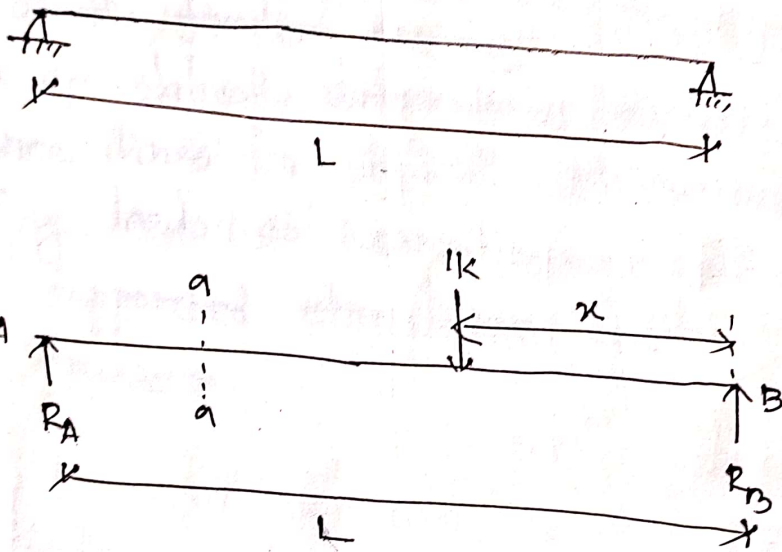
Theorem-04

preparation of Influence line

1. Select function of influence line you need
(Function - Reaction, shear force, bending moment, axial force, deflection etc)
2. Place a unit load at various locations along the structure
3. Compute the value of the function for that particular position of the unit load.
4. Locate the magnitude of the function on the structural member at current position

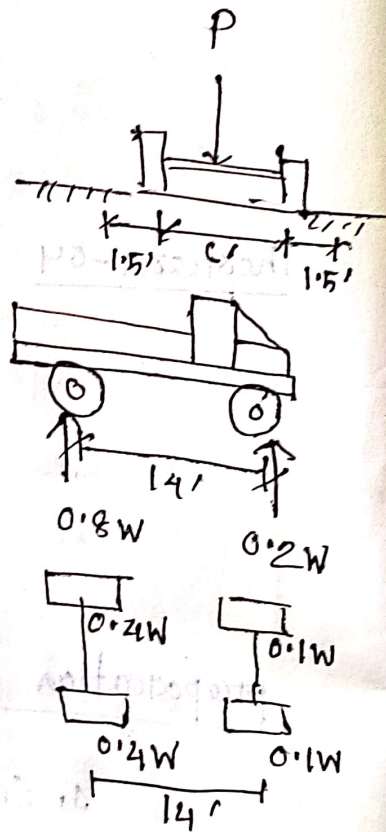
of the unit load

b. Draw a line by joining the ordinate along the members/structure.



$$R_A = \frac{x}{L}$$

$$R_B = 1 - \frac{x}{L}$$



1. Locate the magnitude of the reaction at the structural members of interest.
 2. Compute the value of the reaction for that member.
 3. Draw a unit load of various positions along the structure.
 4. Place a unit load of various positions along the structure.

Influence line for reaction:

Unit load at A

$$\sum M_B = 0; R_A \times L - 1 \times L = 0$$

$$R_A = 1k, R_B = 0k$$

$$\sum F_y = 0; R_A = 1k, R_B = 0k$$

Unit load at mid span

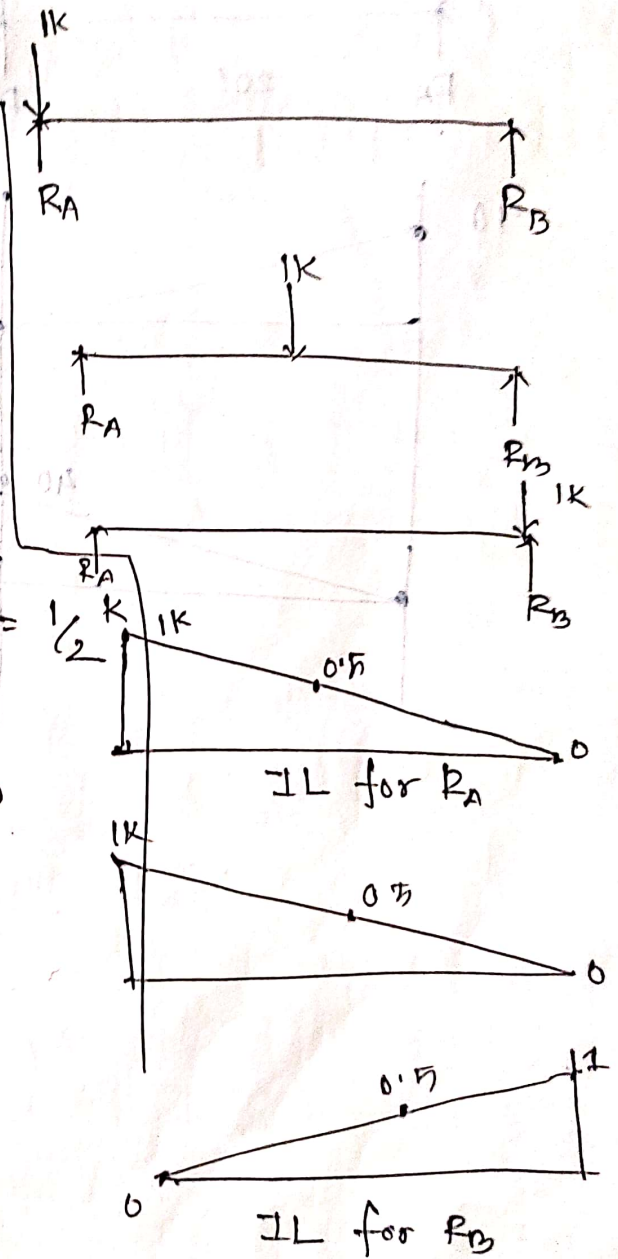
$$\sum M_B = 0; R_A \times L - 1 \times \frac{L}{2} = 0$$

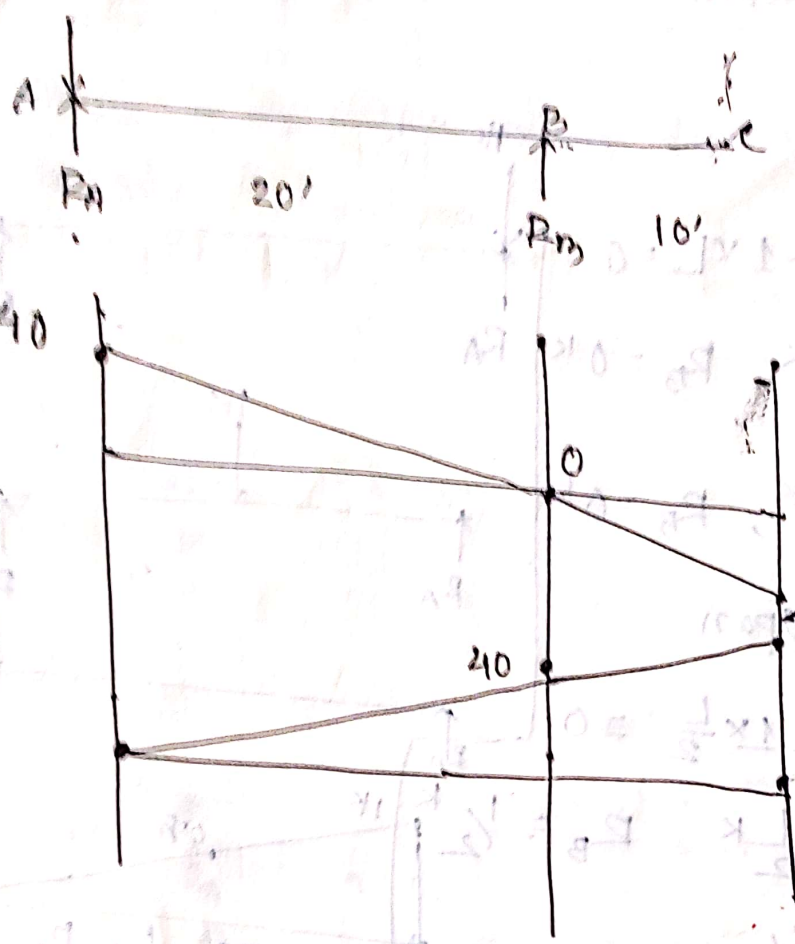
$$R_A = \frac{1}{2}k, R_B = \frac{1}{2}k$$

Unit load at B,

$$\sum M_B = 0; R_A \times L - 1 \times 0 = 0$$

$$R_A = 0; R_B = 1k$$





IL for R_A

IL for R_B

influence line for reaction

unit load at

$\sum M_B = 0$

$\sum M_A = 0$

$\sum M_B = 0$

$\sum M_A = 0$

$\sum M_B = 0$

$\sum M_A = 0$

$\sum M_B = 0$

$\sum M_A = 0$

$\sum M_B = 0$

$\sum M_A = 0$

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$\sum M_A = 0$

$\sum M_B = 0$

$\sum M_A = 0$

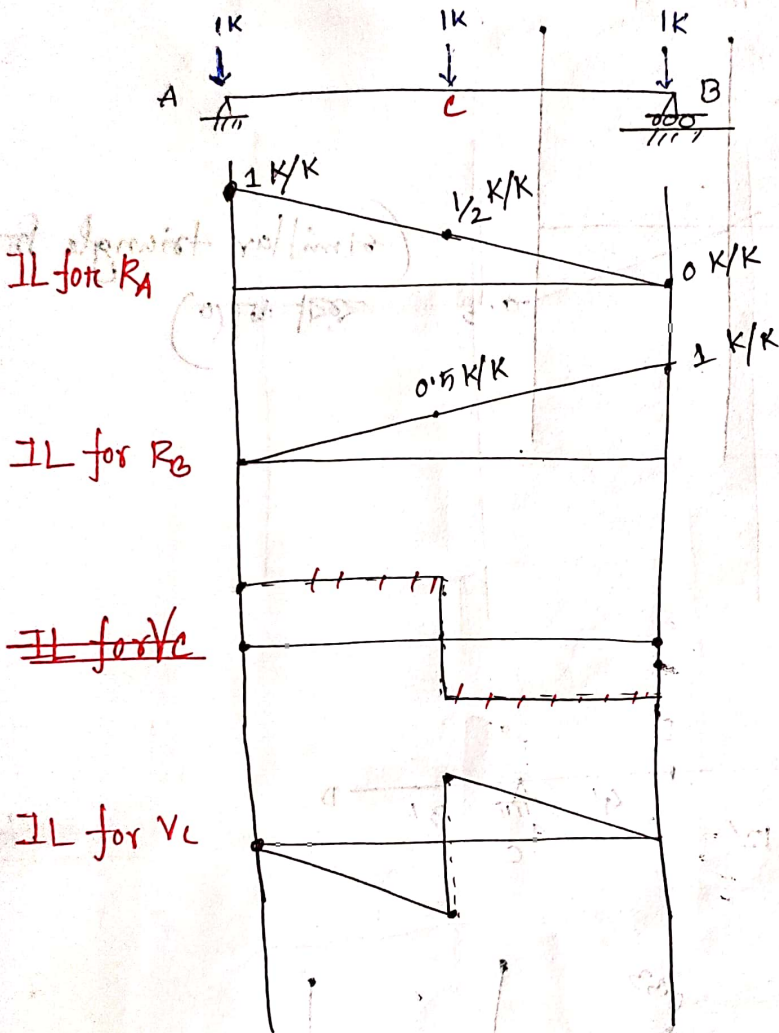
$\sum M_B = 0$

$\sum M_A = 0$

Influence Line

so-mohit

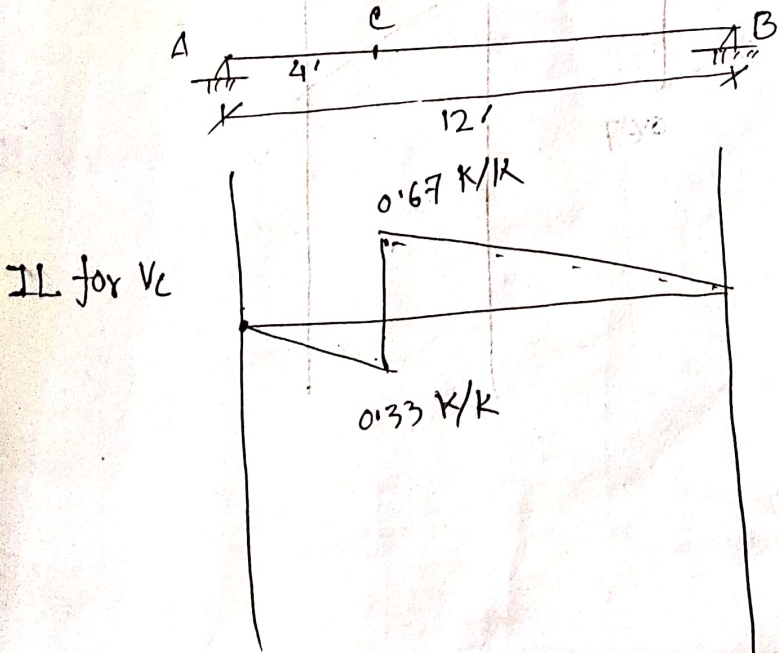
Problem-01



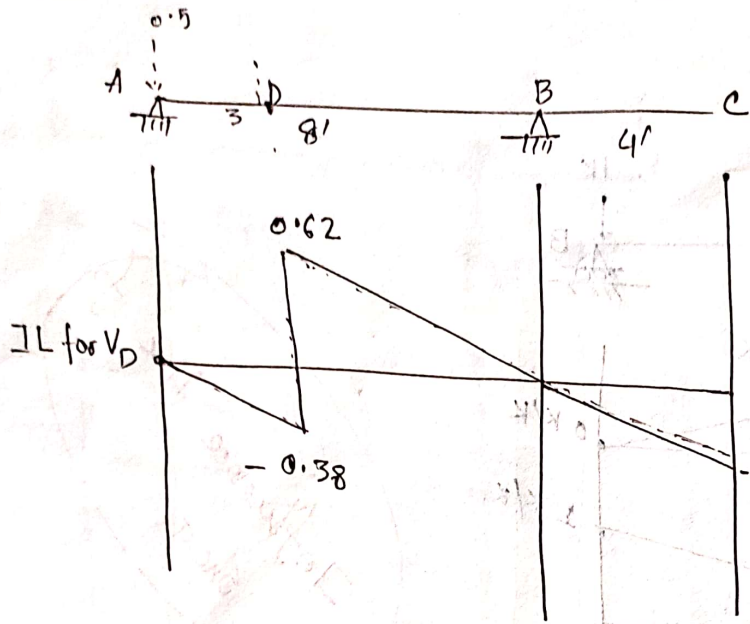
Influence line for
Sheet

so-mohit

Problem-02

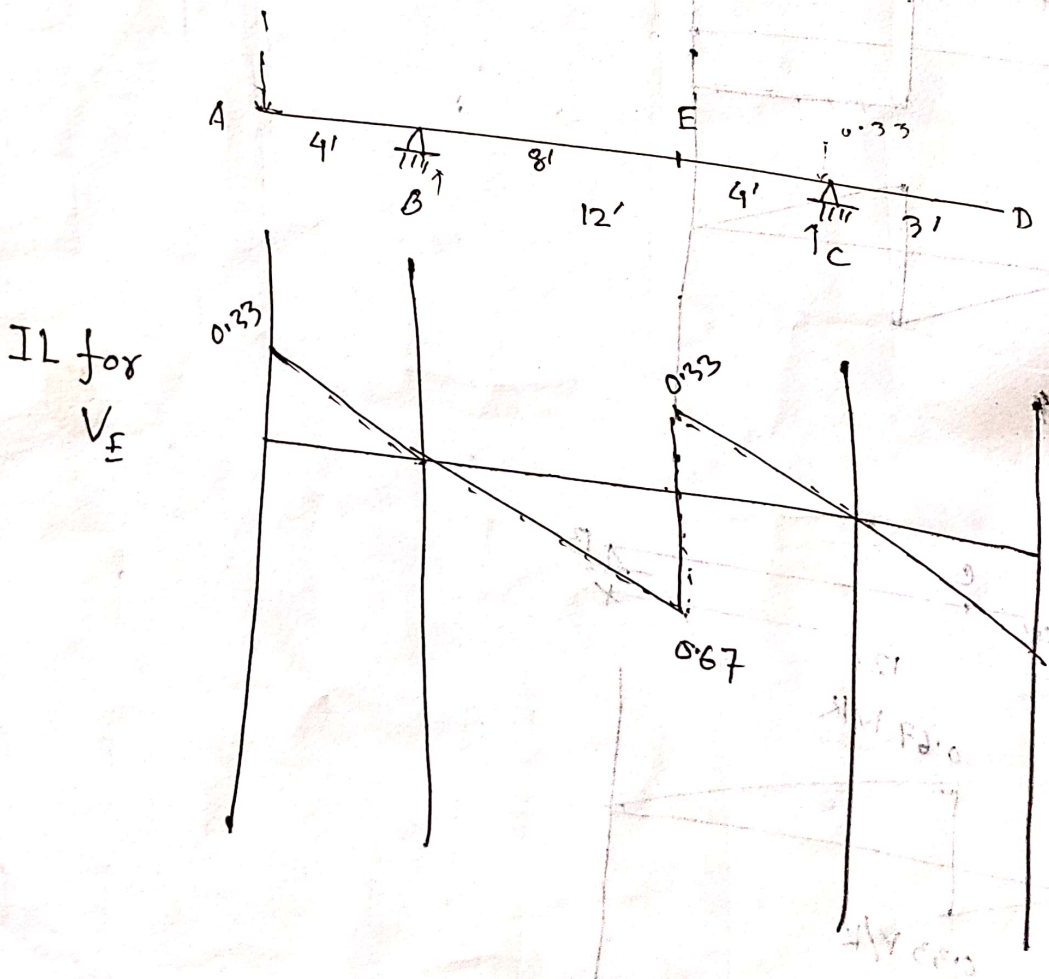


Problem-02



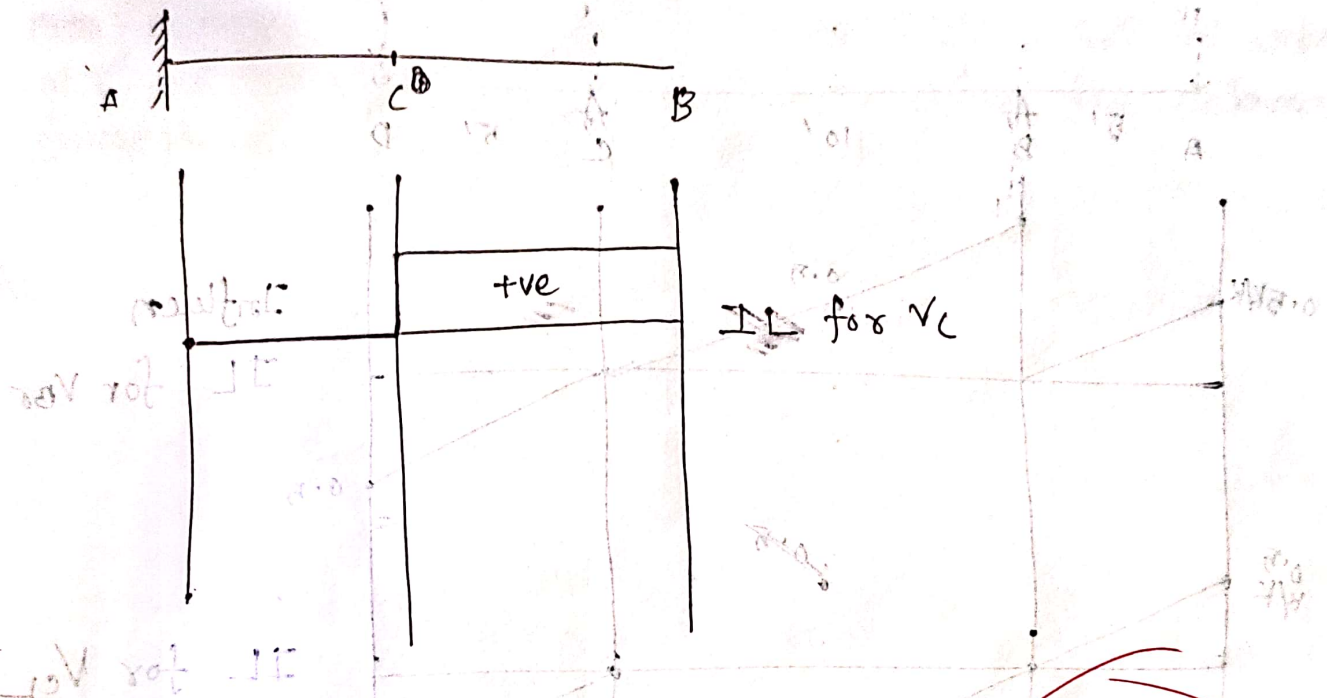
(similar triangle का प्रयोग)

Problem-03

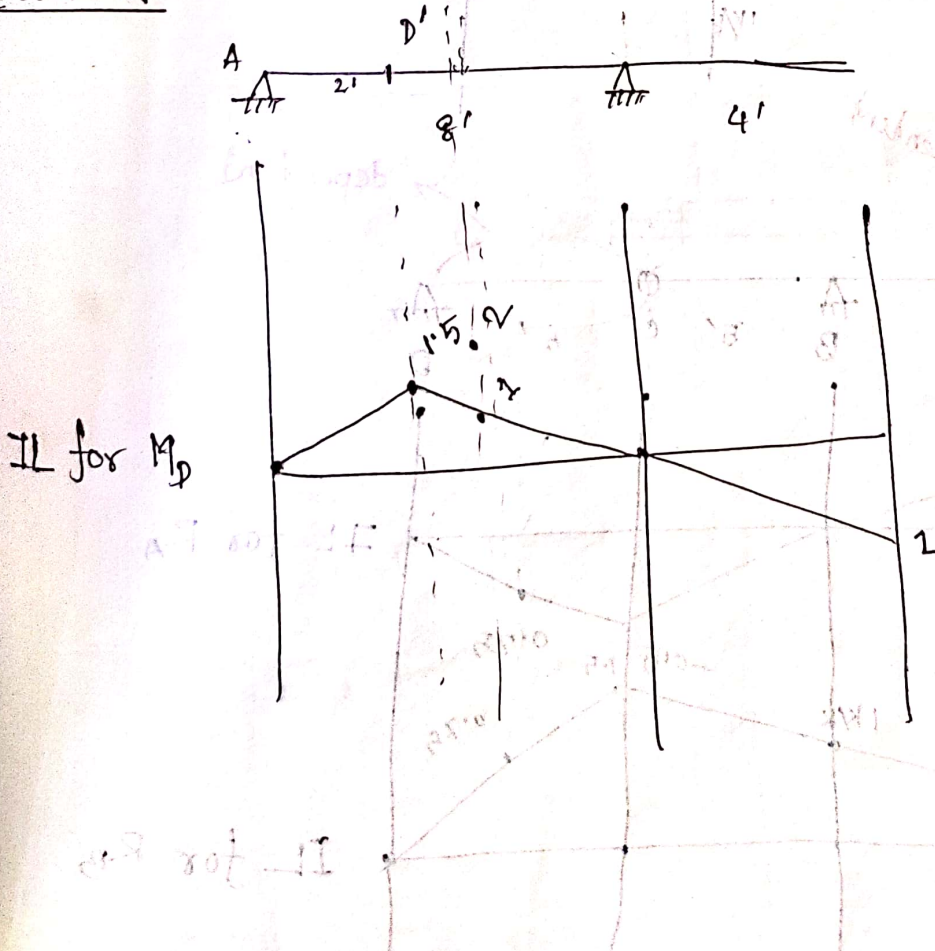


IL for V_E

Problem-04

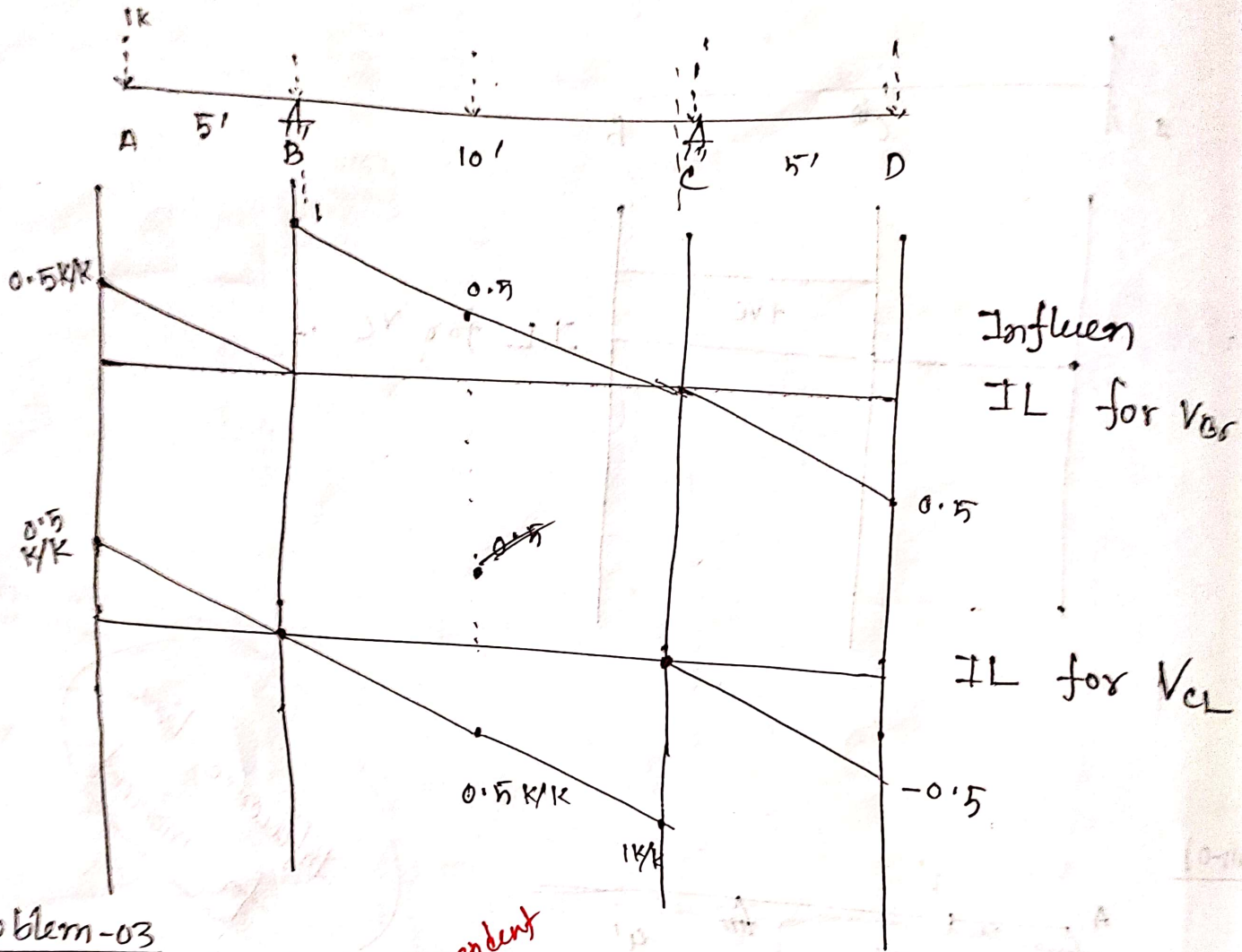


Problem-01

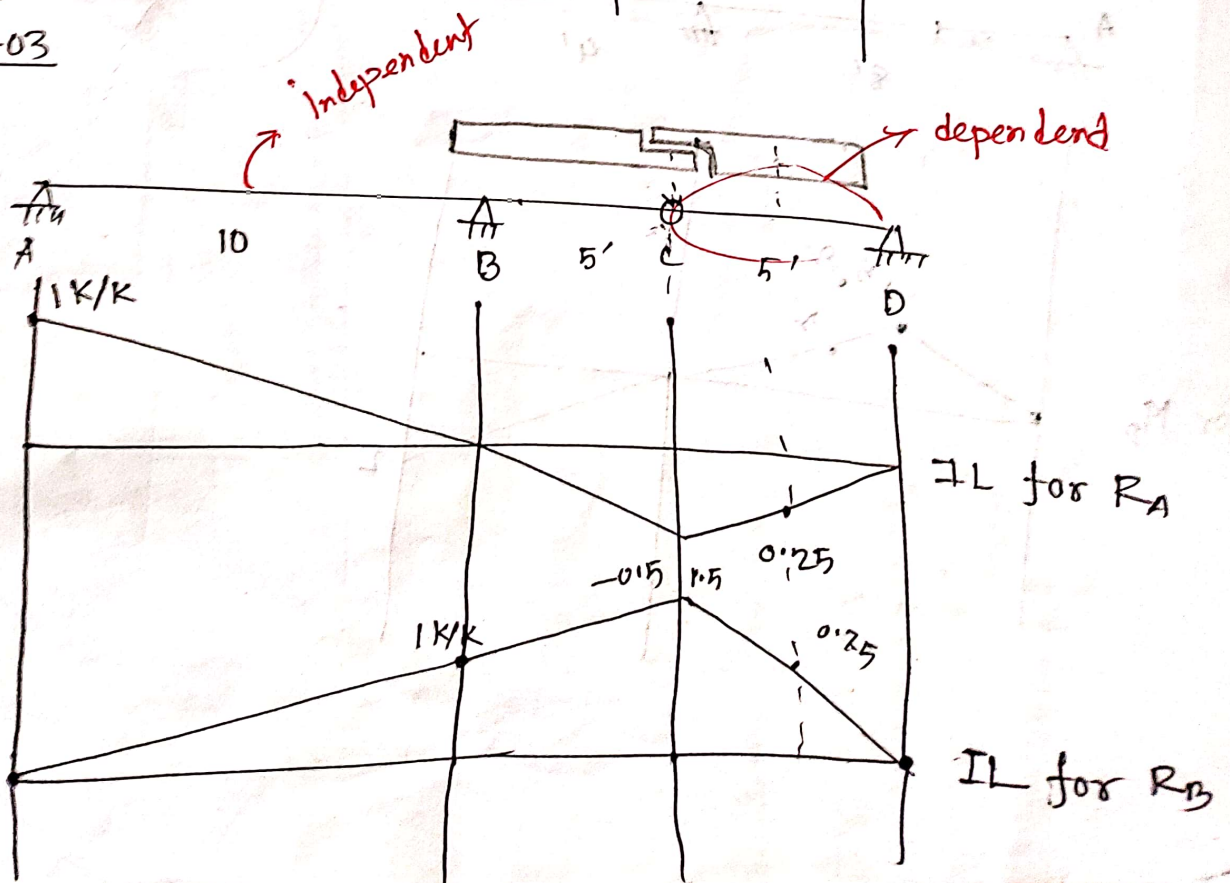


Influence line for moment

Problem-02



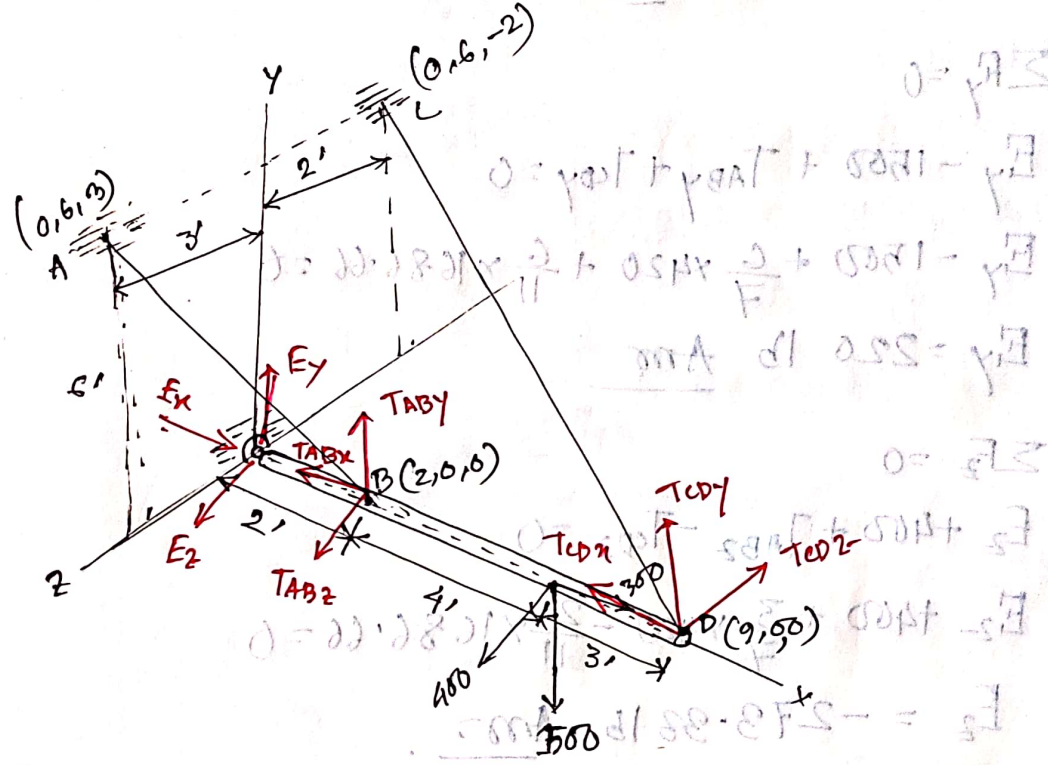
Problem-03



3D

767: The boom DE of the following figure carries a load $F = (300i - 1500j + 400k)$ lb as shown and is supported by a ball and socket at E and two wires AB and CD. Determine the five unknown forces (or components) acting on the boom.

Soln



$$T_{ABx} = \frac{2}{\sqrt{2^2 + 6^2 + 3^2}} \times T_{AB}$$

$$= \frac{2}{7} T_{AB}$$

$$T_{ABy} = \frac{6}{7} T_{AB}$$

$$T_{ABz} = \frac{3}{7} T_{AB}$$

$$T_{CDx} = \frac{9}{\sqrt{9^2 + 6^2 + 2^2}} = \frac{9}{11} T_{CD}$$

$$T_{CDy} = \frac{6}{11} T_{CD}$$

$$T_{CDz} = \frac{2}{11} T_{CD}$$

$\sum M_y = 0$

$T_{ABz} \times 2 + 400 \times 6 - T_{CDz} \times 9 = 0$

$\frac{3}{7} T_{AB} \times 2 - \frac{2}{11} T_{CD} \times 9 + 2400 = 0$

$\sum M_z = 0$

$-1500 \times 6 + T_{CDy} \times 9 + T_{ABy} \times 2 = 0$
 $\Rightarrow \frac{6}{7} T_{AB} \times 2 + \frac{6}{11} T_{CD} \times 9 - 9000 = 0$

$T_{AB} = 420 \text{ lb}$
 $T_{CD} = 1686.66 \text{ lb}$ } Ans.

$$\sum F_x = 0$$

$$E_x + 300 - T_{ABx} - T_{CDx} = 0$$

$$\Rightarrow E_x + 300 - \frac{2}{7} T_{AB} - \frac{2}{11} T_{CD} = 0$$

$$\Rightarrow E_x = 1200 \text{ lb } \underline{\text{Ans.}}$$

$$\sum F_y = 0$$

$$E_y - 1500 + T_{ABy} + T_{CDy} = 0$$

$$E_y - 1500 + \frac{6}{7} \times 420 + \frac{6}{11} \times 1686.66 = 0$$

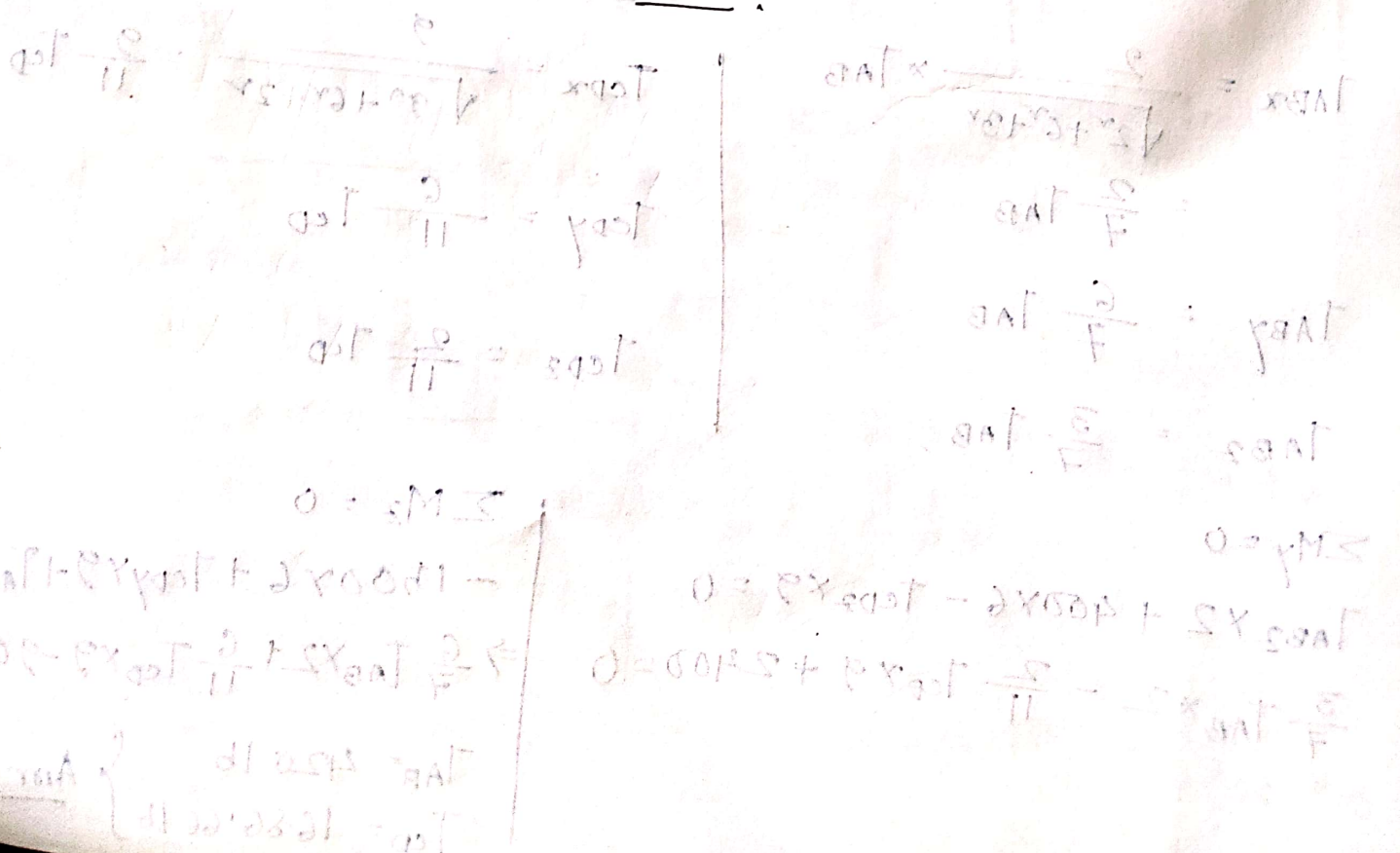
$$E_y = 220 \text{ lb } \underline{\text{Ans.}}$$

$$\sum F_z = 0$$

$$E_z + 400 + T_{ABz} - T_{CDz} = 0$$

$$E_z + 400 + \frac{3}{7} \times 420 - \frac{2}{11} \times 1686.66 = 0$$

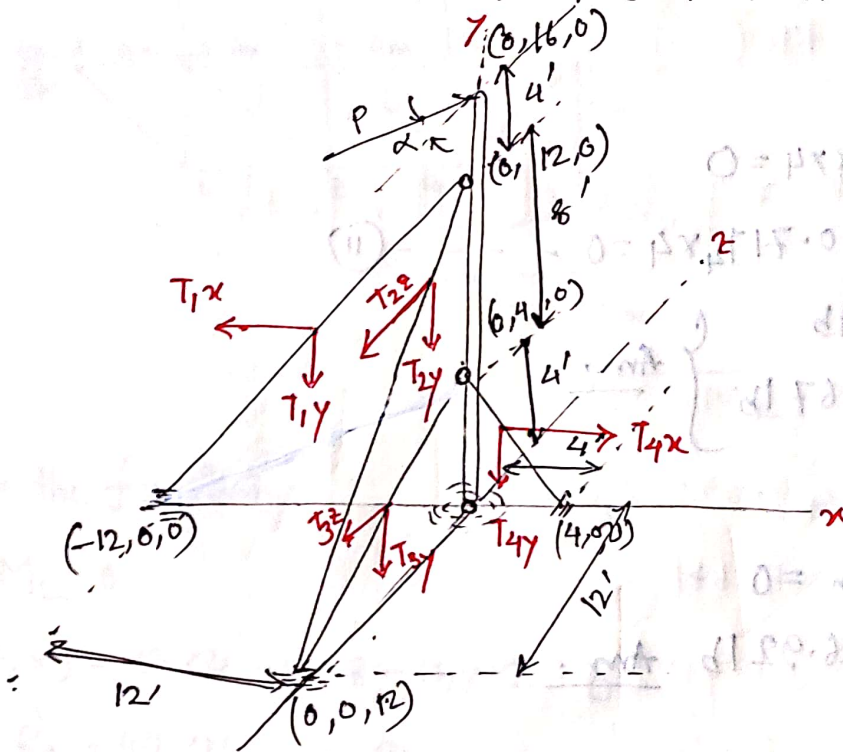
$$E_z = -273.33 \text{ lb } \underline{\text{Ans.}}$$



734

A 16 ft boom is held by a ball and socket at A and by two cables ECF and F'BG which pass around frictionless pulleys at C and B. A horizontal load P of magnitude 900 lb is applied at the top of the boom at D. If P is parallel to the z axis (x=0), determine the reaction at A and the tension in each cable.

Soln



$$T_1 = T_2 \text{ and } T_3 = T_4$$

$$\textcircled{i} T_{1x} = \frac{12}{\sqrt{12^2 + 12^2}} T_1 = 0.71 T_1$$

$$T_{1y} = \frac{12}{\sqrt{12^2 + 12^2}} T_1 = 0.71 T_1$$

$$T_{2y} = \frac{12}{\sqrt{12^2 + 12^2}} T_2 = 0.71 T_2$$

$$T_{2z} = \frac{12}{\sqrt{12^2 + 12^2}} T_2 = 0.71 T_2$$

$$\textcircled{ii} T_{3y} = \frac{4}{\sqrt{12^2 + 4^2}} T_3 = 0.32 T_3$$

$$T_{3z} = \frac{12}{\sqrt{12^2 + 4^2}} T_3 = 0.95 T_3$$

$$T_{4x} = \frac{4}{\sqrt{4^2 + 4^2}} T_4 = 0.7 T_4$$

$$T_{4y} = \frac{4}{\sqrt{4^2 + 4^2}} T_4 = 0.7 T_4$$

$$\Sigma M_x = 0$$

$$T_{22} \times 12 + T_{32} \times 4 - 900 \times 16 = 0$$

$$0.71 T_2 \times 12 + T_{32} \times 4 - 900 \times 16 = 0$$

$$\Rightarrow 0.71 \times 12 T_1 + 0.97 \times 4 T_2 - 900 \times 16 = 0 \quad \text{--- (1)}$$

$$\Sigma M_2 = 0$$

$$-T_1 \times 12 + T_4 \times 4 = 0$$

$$\Rightarrow 0.71 T_1 \times 12 - 0.71 T_4 \times 4 = 0 \quad \text{--- (2)}$$

$$T_1 = 723 \text{ lb}$$

$$T_2 = 2168.67 \text{ lb}$$

Ans.

$$\Sigma F_x = 0$$

$$T_1 \times 2 - T_4 \times 2 - A_x = 0$$

$$A_x = -1026.92 \text{ lb} \quad \text{--- Ans.}$$

$$\Sigma F_y = 0$$

$$T_{1y} + T_{2y} + T_{3y} + T_{4y} - A_y = 0$$

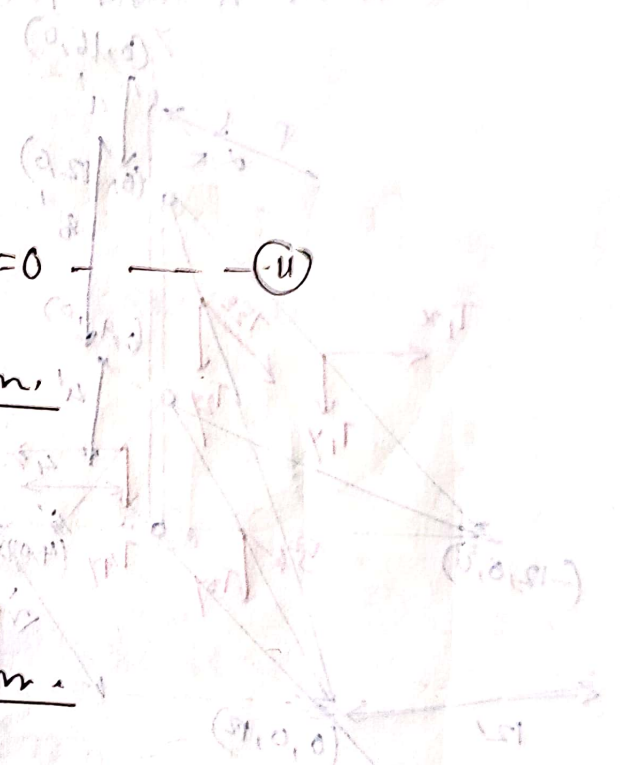
$$A_y = 3260.23 \text{ lb} \quad \text{--- Ans.}$$

$$\Sigma F_z = 0$$

$$T_{1z} + T_{2z} + T_{3z} + T_{4z} - A_z = 0$$

$$T_{22} + T_{32} + A_z - 900 = 0$$

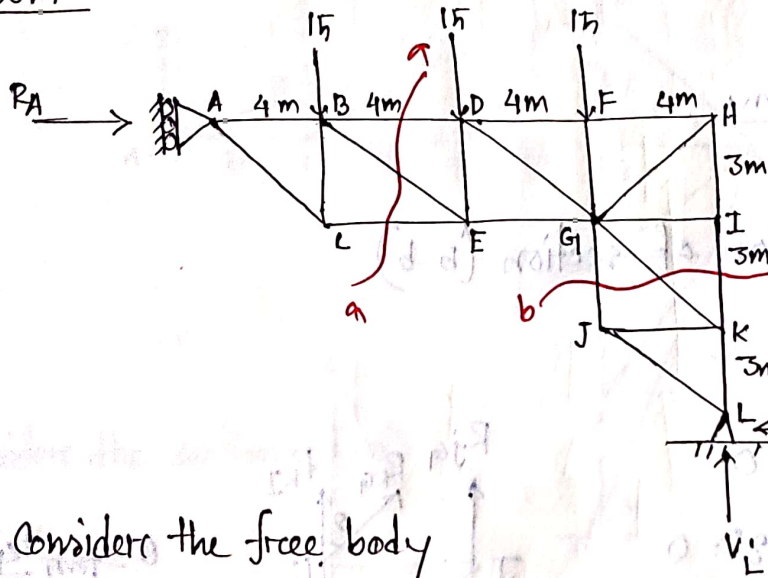
$$A_z = -1673.56 \text{ lb} \quad \text{--- Ans.}$$



TRUSS

381. Determine the force in the members BD, BE, CE, GIJ, GIK and IK of the truss shown

Soln



Consider the free body

$$\sum M_L = 0$$

$$R_A \times 9 - 15 \times 4 - 15 \times 8 - 15 \times 12 = 0$$

$$\therefore R_A = 40 \text{ kN} \text{ --- (i)}$$

$$\sum F_x = 0$$

$$H_L - R_A = 0$$

$$H_L = 40 \text{ kN} \text{ --- (ii)}$$

$$\sum F_y = 0$$

$$V_L - 15 - 15 - 15 = 0$$

$$V_L = 45 \text{ kN} \text{ --- (iii)}$$

Consider the left portion of section (A-A)

$$\sum F_y = 0$$

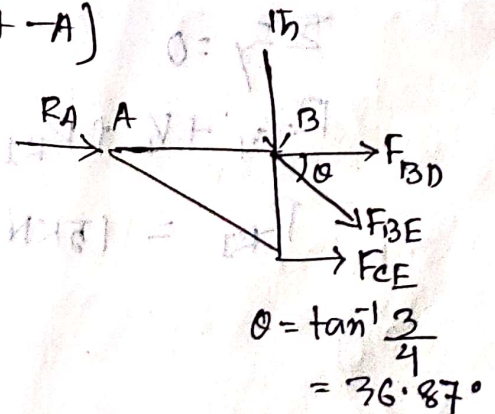
$$15 + F_{BE} \sin 36.87^\circ = 0$$

$$F_{BE} = 25 \text{ kN (C) Ans.}$$

$$\sum M_B = 0$$

$$F_{CE} \times 3 = 0$$

$$F_{CE} = 0 \text{ kN Ans.}$$



$$\sum F_x = 0$$

$$R_A + F_{CE} + F_{BD} + F_{BE} \cos 30^\circ = 0$$

$$40 + 0 + F_{BD} - 25 \cos 36.87^\circ = 0$$

$$F_{BD} = -20 \text{ kN}$$

$$F_{BD} = 20 \text{ kN (C)} \quad \underline{\text{Ans}}$$

Consider the lower portion of section (b-b)

$$\sum F_x = 0$$

$$H_L + R_{KG} \sin 53.13^\circ = 0$$

$$40 + R_{KG} \sin 53.13^\circ = 0$$

$$R_{KG} = -50 \text{ kN}$$

$$R_{KG} = 50 \text{ kN (C)} \quad \underline{\text{Ans}}$$

$$\sum M_K = 0$$

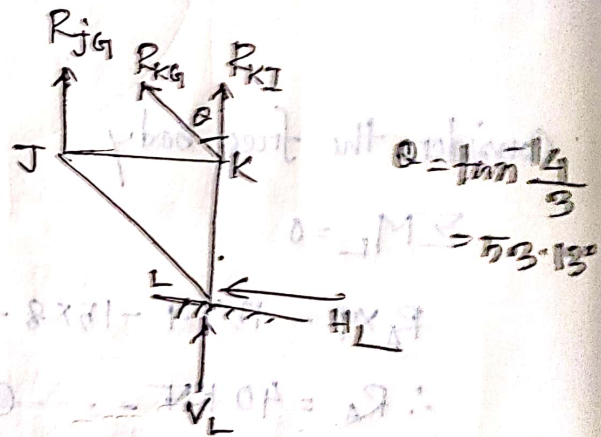
$$R_{JG} \times 4 + 3 \times H_L = 0$$

$$R_{JG} = 30 \text{ kN (C)} \quad \underline{\text{Ans}}$$

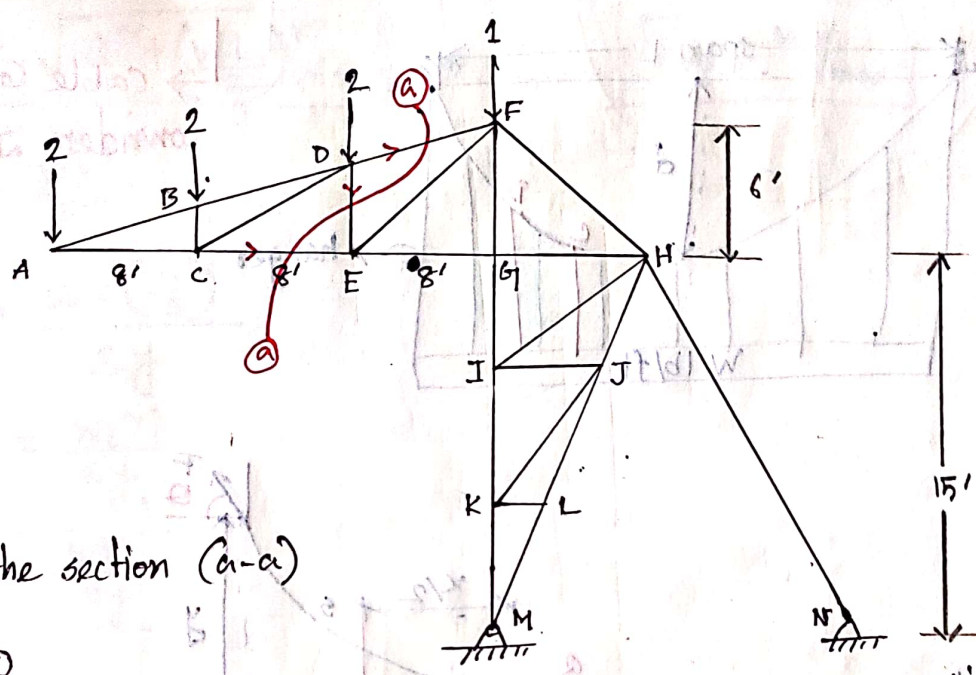
$$\sum F_y = 0$$

$$R_{JG} + V_L + R_{KI} + R_{KG} \cos 53.13^\circ = 0$$

$$R_{KI} = 15 \text{ kN (T)} \quad \underline{\text{Ans}}$$



Determine the force in members DF, DE, and CE of the truss shown.



Consider the section (a-a)

$$\sum M_D = 0$$

$$-2 \times 8 - 2 \times 16 - R_{CE} \times 4 = 0$$

$$\Rightarrow R_{CE} = -12 \text{ kips}$$

$$R_{CE} = 12 \text{ kips (comp)} \quad \underline{\text{Ans.}}$$

$$\sum F_x = 0$$

$$R_{CE} + R_{DF} \times \cos 14^\circ = 0 \quad \therefore R_{DF} = -12.86 \text{ kips (t)} \quad \underline{\text{Ans.}}$$

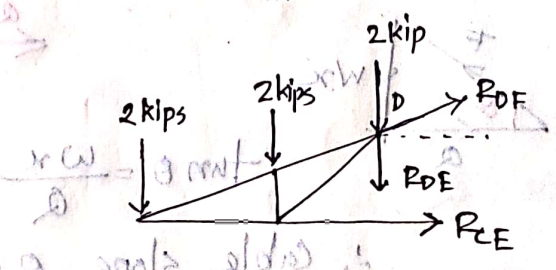
$$R_{DF} = 12.86 \text{ kips (t)} \quad \underline{\text{Ans.}}$$

$$\sum F_y = 0$$

$$-R_{DE} \sin 14^\circ + 2 + 2 + 2 + R_{DE} = 0$$

$$R_{DE} = -3 \text{ kips}$$

$$R_{DE} = 3 \text{ kips (c)} \quad \underline{\text{Ans.}}$$



① $\sum F_x = 0$
 $0 = R_{DF} \cos 14^\circ + R_{CE}$
 $0 = R_{DF} \cos 14^\circ - 12$
 $R_{DF} = 12.86 \text{ kips (t)}$

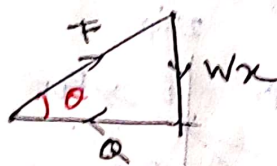
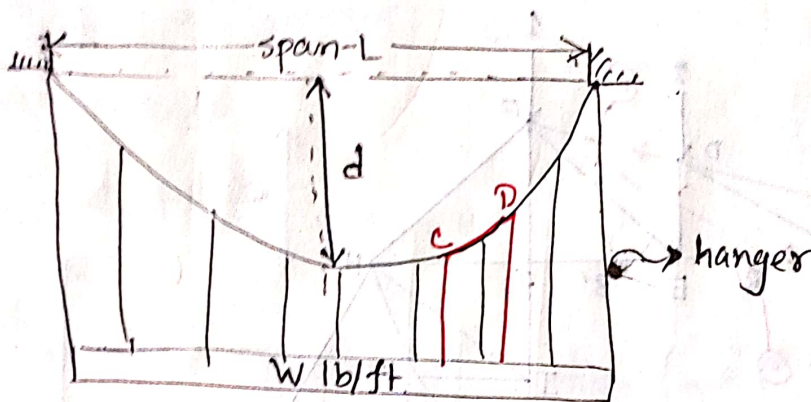
② $\sum F_y = 0$
 $0 = R_{DE} \sin 14^\circ + 2 + 2 + 2 + R_{DE}$
 $0 = R_{DE} \sin 14^\circ + R_{DE} + 6$
 $R_{DE} (\sin 14^\circ + 1) = -6$
 $R_{DE} = -3 \text{ kips}$
 $R_{DE} = 3 \text{ kips (c)}$

Cable:

Cable take only Hemiion

(Parabolic)

↳ cable का weight consider ना करे



$$\tan \theta = \frac{wx}{Q}$$

∴ cable slope, $\theta = \tan^{-1} \frac{wx}{Q}$

$$\therefore \theta = \tan^{-1} \frac{WL}{2Q}$$

$$[L = 2x]$$

$$\sum F_x = 0$$

$$\Rightarrow Q = F \cos \theta \quad \text{--- (i)}$$

$$\sum F_y = 0$$

$$wx = F \sin \theta \quad \text{--- (ii)}$$

$$\sum M_c = 0$$

$$-Q \times y + wx \times \left(\frac{x}{2}\right) = 0$$

$$\Rightarrow y = \frac{wx^2}{2Q}$$

s = half length of cables

Tension

$$F = \sqrt{Q^2 + (Wx)^2}$$

$$F_{\max} = \sqrt{Q^2 + \left(\frac{WL}{2}\right)^2} \quad \text{--- (1)}$$

$$F_{\max} = W y_{\max}$$

$$Q = \frac{Wx^2}{2y}$$

$$= \frac{Wx \left(\frac{L}{2}\right)^2}{2y}$$

$$= \frac{WL^2}{8y}$$

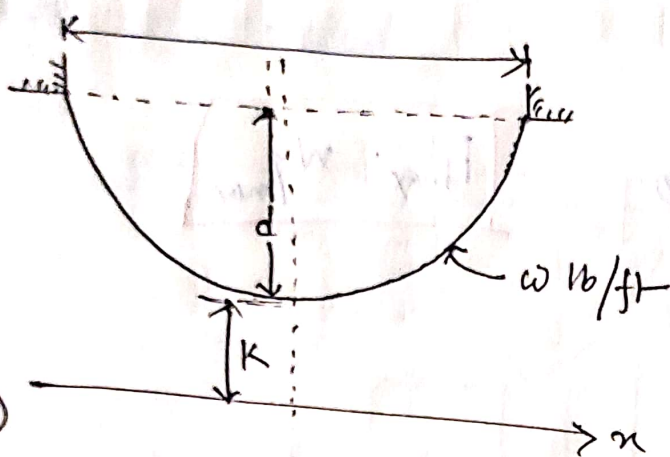
$$\therefore Q = \frac{WL^2}{8y}$$

length of the cable

$$s = L + \frac{8d^2}{3L} - \frac{32d^4}{5L^3}$$

$$(1) \text{ } d^2 = 0$$

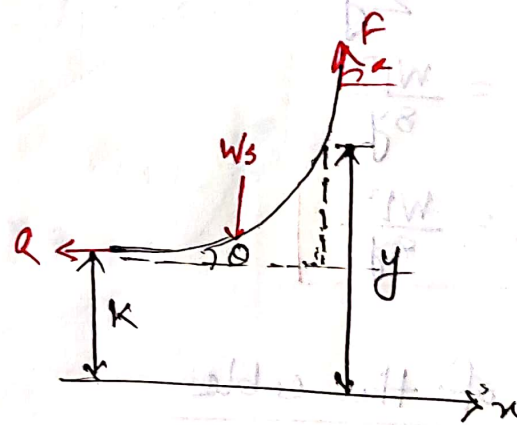
$$(2) \text{ } d^2 = 1$$



Parabolic
 (समतल)
 catenary
 (बुलबुल)
 (बुलबुल)

(Catenary)

→ Cable का निम्न weight consider करें



$$\sum F_x = 0$$

$$F \cos \theta = Q \quad \text{--- (1)}$$

$$\sum F_y = 0$$

$$F \sin \theta = ws \quad \text{--- (2)}$$

$$(2) \div (1)$$

$$\tan \theta = \frac{ws}{Q} \quad \left(\frac{Q}{w} = k, \text{ let} \right)$$

$$\therefore \tan \theta = \frac{s}{k} = \frac{dy}{dx}$$

$$Q = wk$$

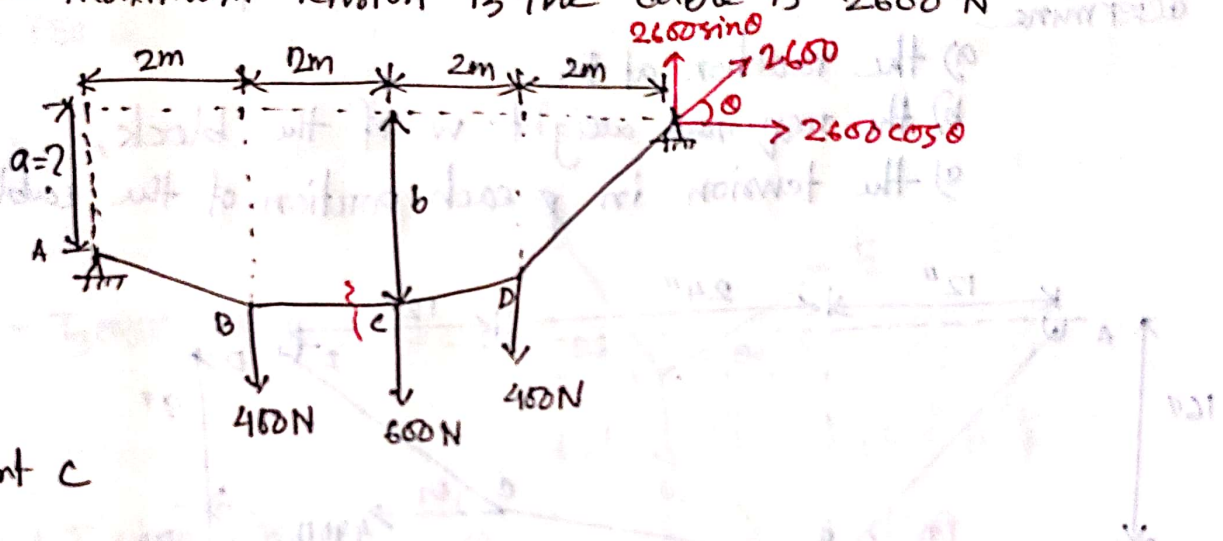
$$F = wy = w \sqrt{s^2 + k^2}$$

$$s = k \sinh\left(\frac{x}{k}\right)$$

$$y = k \cosh\left(\frac{x}{k}\right)$$

Problem 1348:

Determine the distance a if the portion BC of the cable is horizontal and if the maximum tension in the cable is 2600 N



At point C

$$F_y = 0$$

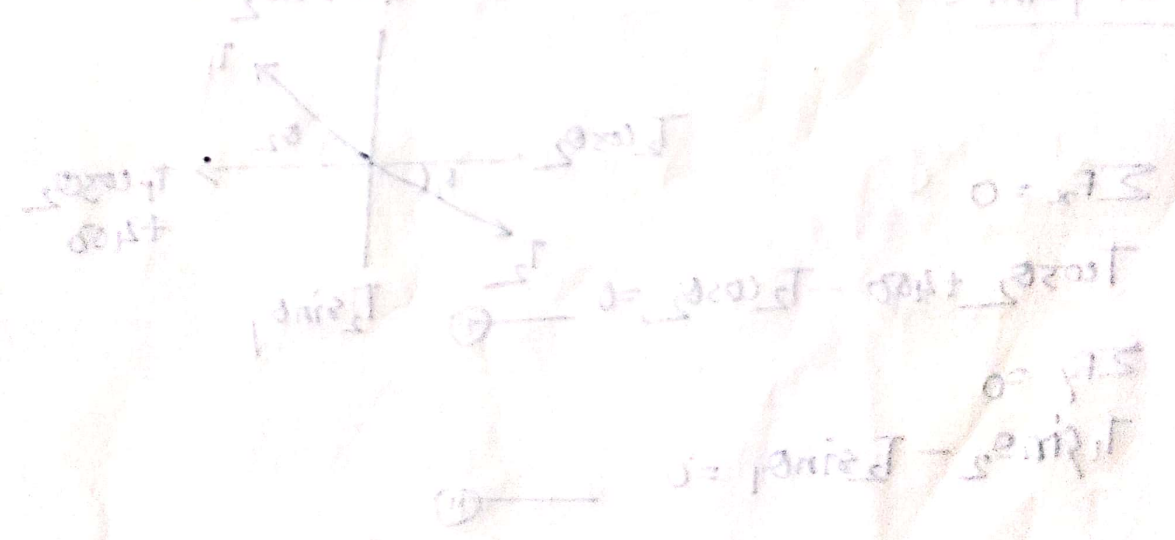
$$400 + 600 = 2600 \sin \theta$$

$$\theta = 22.62^\circ$$

$$\sum M_A = 0$$

$$a \times 2600 \cos 22.6^\circ - 8 \times 2600 \sin 22.6^\circ + 400 \times 2 + 600 \times 4 + 400 \times 6 = 0$$

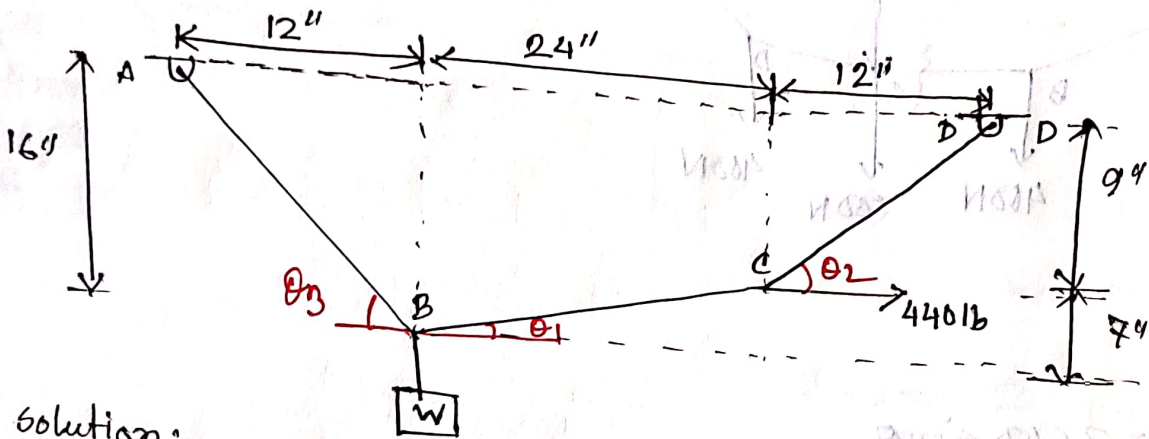
$$a = 1\text{ m} \quad \underline{\underline{A.m.}}$$



Problem 1405:

knowing that the 400 lb force applied at C and the block attached at B maintain the cable in the position shown, determine

- the reaction at D,
- the required weight w of the block,
- the tension in each portion of the cable.



Solution:

$$\theta_1 = \tan^{-1} \frac{7}{24} = 16.26^\circ$$

$$\theta_2 = \tan^{-1} \frac{9}{12} = 36.87^\circ$$

$$\theta_3 = \tan^{-1} \frac{16}{12} = 53.13^\circ$$

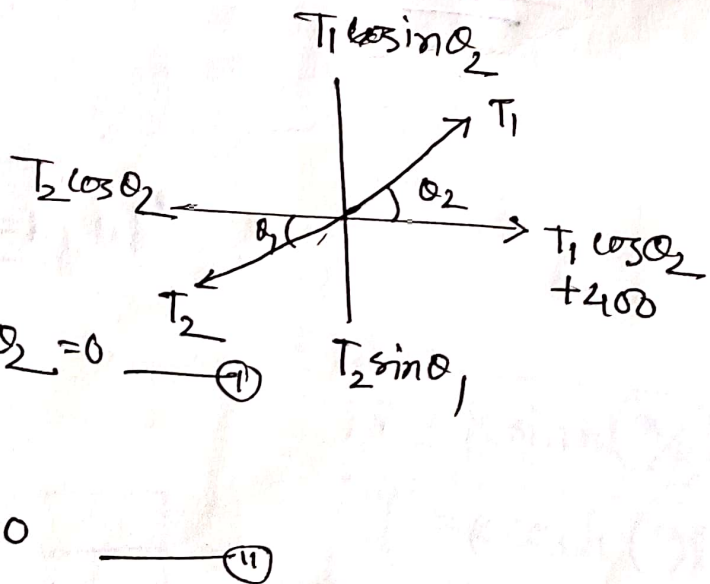
At point C

$$\sum F_x = 0$$

$$T_1 \cos \theta_2 + 400 - T_2 \cos \theta_1 = 0 \quad \text{--- (I)}$$

$$\sum F_y = 0$$

$$T_1 \sin \theta_2 - T_2 \sin \theta_1 = 0 \quad \text{--- (II)}$$



From equation (i) and (ii)

$$T_1 = 350 \text{ lb} \quad \text{f Ann.}$$

$$T_2 = 750 \text{ lb}$$

At point B,

$$\sum F_x = 0$$

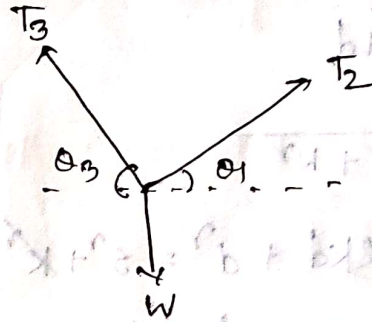
$$\Rightarrow T_2 \cos \theta_1 - T_3 \cos \theta_3 = 0 \quad \text{--- (iii)}$$

$$\sum F_y = 0$$

$$T_2 \sin \theta_1 + T_3 \sin \theta_3 - W = 0 \quad \text{--- (iv)}$$

Solving (iii) and (iv)

$$\left. \begin{array}{l} T_3 = 1200 \text{ lb} \\ W = 1170 \text{ lb} \end{array} \right\} \text{ Ann.}$$



Problem-1802

A 60ft cable which weight - 360 lb and $d=15$ ft. Find the tension at support and span.

Solution:

we know,

$$y = k + d$$

$$y = \sqrt{s^2 + kr}$$

$$\Rightarrow \cancel{y} + 2kd + d^2 = s^2 + \cancel{kr}$$

$$\Rightarrow 2kd = s^2 - d^2$$

$$\Rightarrow k = \frac{s^2 - d^2}{2d}$$
$$= \frac{30^2 - 15^2}{2 \times 15}$$

$$= 22.5$$

$$y = k + d$$

$$= 22.5 + 15$$

$$= 37.5$$

$$\therefore F = wy$$

$$= 6 \times 37.5$$

$$= 225$$

$$s = \frac{L}{2} = \frac{60}{2} = 30 \text{ ft}$$

$$w = \frac{360}{60} = 6 \text{ lb/ft}$$

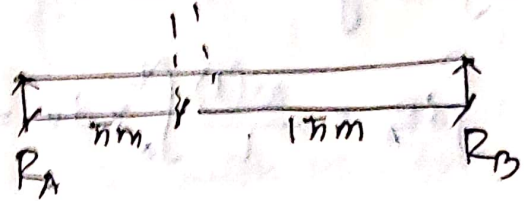
Problem (class)

If $a = 5\text{m}$, $b = 15\text{m}$, draw influence line diagrams for reactions R_A and R_B as well as V_1 and M_1 at section 1.

soln

When a unit load at A

$$R_A = 1\text{KN}, R_B = 0, V_1 = 0, M_1 = 0$$



When a unit load at just left of section 1. Using equilibrium equation

$$R_A = 0.75\text{KN}, R_B = 0.25, V_1 = -0.25$$

$$M_1 = 0.75 \times 5 = 0.25 \times 15 = 3.75\text{N}\cdot\text{m}$$

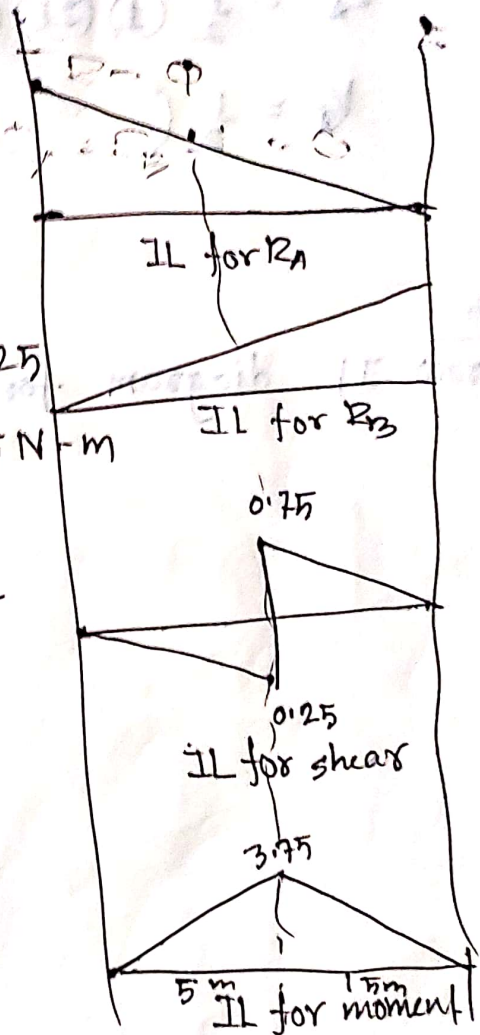
When a unit load at just right of section 1

$$R_A = 0.75, R_B = 0.25\text{KN}$$

$$V_1 = +0.75\text{KN},$$

$$M_1 = 0.75 \times 5 = 3.75\text{N}\cdot\text{m}$$

When a unit load at B.



Integrating

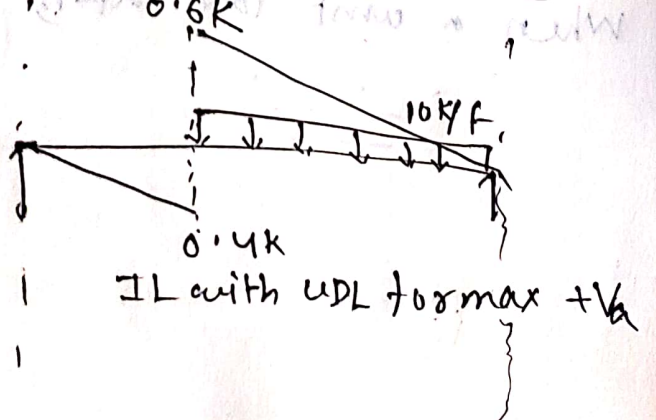
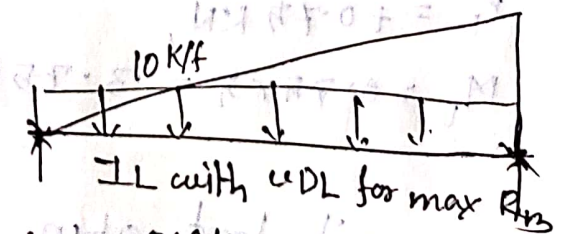
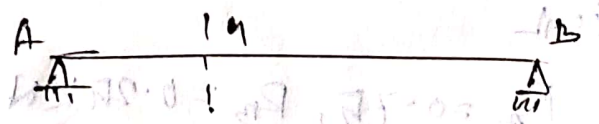
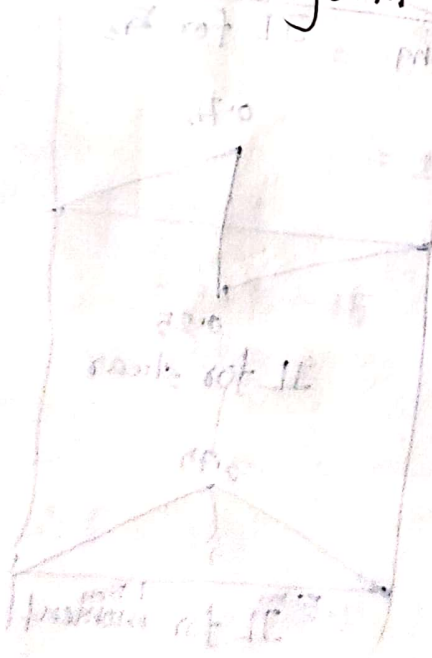
$$\int dR_A = \frac{\omega(1)}{L} \int_0^L x dx = \frac{\omega(1)L}{2}$$

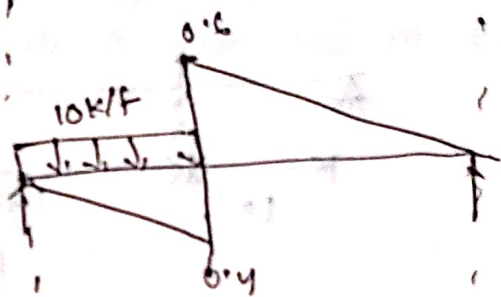
$$R_A = \frac{1}{2} (1) (25) (10) = 12.5 \text{ kips}$$

$$V_A = \frac{1}{2} ($$

Q.9

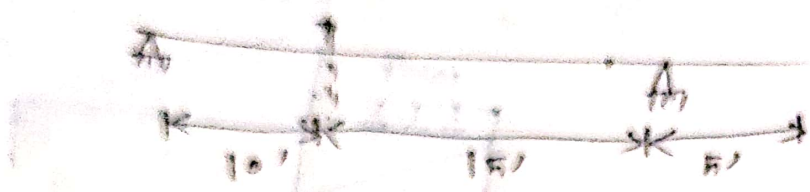
Draw IL diagram for R_A, R_B, V_A and M_A of the following





$$- \left(\frac{1}{2} \times 10 \times 0.4 \times 10 \right) + \left(\frac{1}{2} \times 15 \times 0.6 \times 10 \right)$$

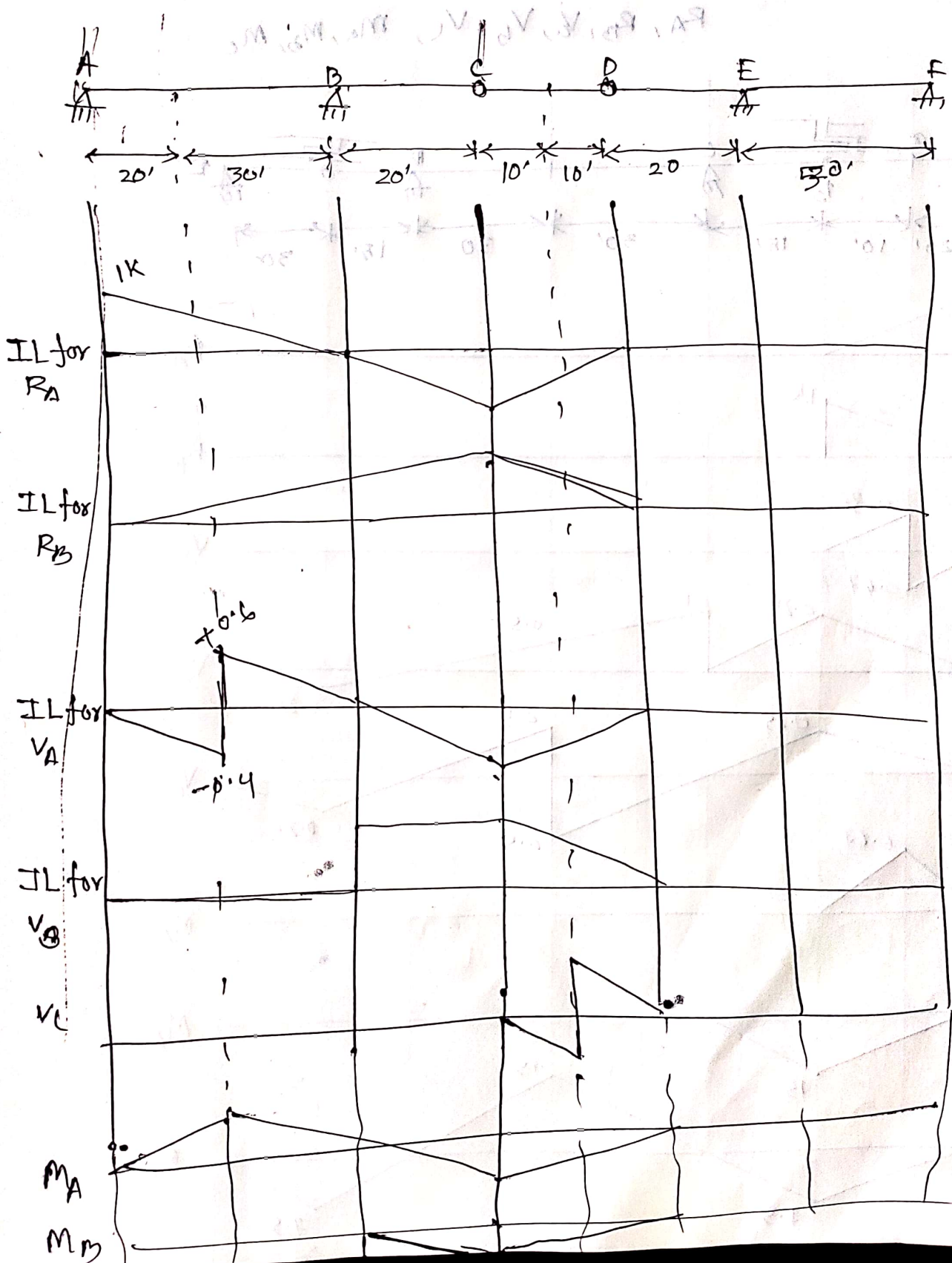
$$= 25$$



$$\left(\frac{1}{2} \times 10 \times 0.8 \times 10\right) + (0.8 \times 10 \times 0.8 \times \frac{1}{2})$$

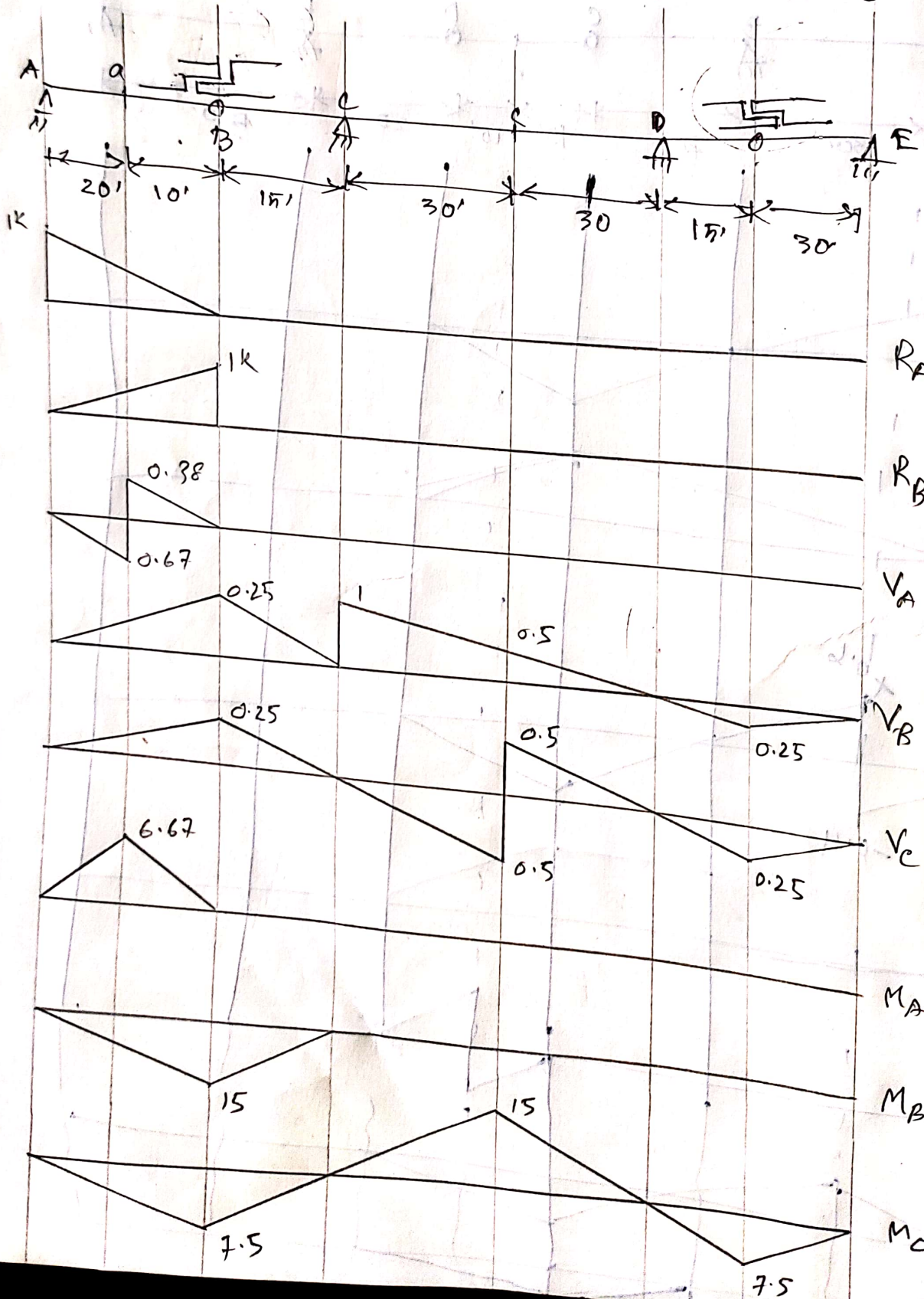
32 =

2. Draw IL diagram for R_A , R_B , V_A , V_B , M_A , M_B and M_C of the following balance cantilever bridge as a unit load moves from A to F



$\sum M_b = 0$
 $M_b - 1 \times 20 = 0$
 $M_b = 20$

$R_A, R_B, V_a, V_b, V_c, M_a, M_b, M_c$



Let $\mu_1, \mu_2, \dots, \mu_n$ be the means of n independent random variables X_1, X_2, \dots, X_n .

Let $\sigma_1^2, \sigma_2^2, \dots, \sigma_n^2$ be the variances of X_1, X_2, \dots, X_n .

Let $\mu = \mu_1 + \mu_2 + \dots + \mu_n$ be the mean of $X = X_1 + X_2 + \dots + X_n$.

Let $\sigma^2 = \sigma_1^2 + \sigma_2^2 + \dots + \sigma_n^2$ be the variance of X .

Let $Z = \frac{X - \mu}{\sigma}$ be the standardized random variable.

Let $\phi(z)$ be the probability density function of Z .

Let $\Phi(z)$ be the cumulative distribution function of Z .

Let $\phi'(z)$ be the derivative of $\phi(z)$.

Let $\Phi'(z)$ be the derivative of $\Phi(z)$.

Let $\phi''(z)$ be the second derivative of $\phi(z)$.

Let $\Phi''(z)$ be the second derivative of $\Phi(z)$.

Let $\phi'''(z)$ be the third derivative of $\phi(z)$.

Let $\Phi'''(z)$ be the third derivative of $\Phi(z)$.

Let $\phi^{(4)}(z)$ be the fourth derivative of $\phi(z)$.

Let $\Phi^{(4)}(z)$ be the fourth derivative of $\Phi(z)$.

Let $\phi^{(5)}(z)$ be the fifth derivative of $\phi(z)$.

Let $\Phi^{(5)}(z)$ be the fifth derivative of $\Phi(z)$.

Let $\phi^{(6)}(z)$ be the sixth derivative of $\phi(z)$.

Let $\Phi^{(6)}(z)$ be the sixth derivative of $\Phi(z)$.

Let $\phi^{(7)}(z)$ be the seventh derivative of $\phi(z)$.

Let $\Phi^{(7)}(z)$ be the seventh derivative of $\Phi(z)$.

Let $\phi^{(8)}(z)$ be the eighth derivative of $\phi(z)$.

Let $\Phi^{(8)}(z)$ be the eighth derivative of $\Phi(z)$.

Let $\mu_1, \mu_2, \dots, \mu_n$ be the means of n independent random variables X_1, X_2, \dots, X_n .

Let $\sigma_1^2, \sigma_2^2, \dots, \sigma_n^2$ be the variances of X_1, X_2, \dots, X_n .

Let $\mu = \mu_1 + \mu_2 + \dots + \mu_n$ be the mean of $X = X_1 + X_2 + \dots + X_n$.

Let $\sigma^2 = \sigma_1^2 + \sigma_2^2 + \dots + \sigma_n^2$ be the variance of X .

Let $Z = \frac{X - \mu}{\sigma}$ be the standardized random variable.

Let $\phi(z)$ be the probability density function of Z .

Let $\Phi(z)$ be the cumulative distribution function of Z .

Let $\phi'(z)$ be the derivative of $\phi(z)$.

Let $\Phi'(z)$ be the derivative of $\Phi(z)$.

Let $\phi''(z)$ be the second derivative of $\phi(z)$.

Let $\Phi''(z)$ be the second derivative of $\Phi(z)$.

Let $\phi'''(z)$ be the third derivative of $\phi(z)$.

Let $\Phi'''(z)$ be the third derivative of $\Phi(z)$.

Let $\phi^{(4)}(z)$ be the fourth derivative of $\phi(z)$.

Let $\Phi^{(4)}(z)$ be the fourth derivative of $\Phi(z)$.

Let $\phi^{(5)}(z)$ be the fifth derivative of $\phi(z)$.

Let $\Phi^{(5)}(z)$ be the fifth derivative of $\Phi(z)$.

Let $\phi^{(6)}(z)$ be the sixth derivative of $\phi(z)$.

Let $\Phi^{(6)}(z)$ be the sixth derivative of $\Phi(z)$.

Let $\phi^{(7)}(z)$ be the seventh derivative of $\phi(z)$.

Let $\Phi^{(7)}(z)$ be the seventh derivative of $\Phi(z)$.

Let $\phi^{(8)}(z)$ be the eighth derivative of $\phi(z)$.

Let $\Phi^{(8)}(z)$ be the eighth derivative of $\Phi(z)$.

Influence line for Reaction:

Draw IL for R_A and R_B

When 1K at A:

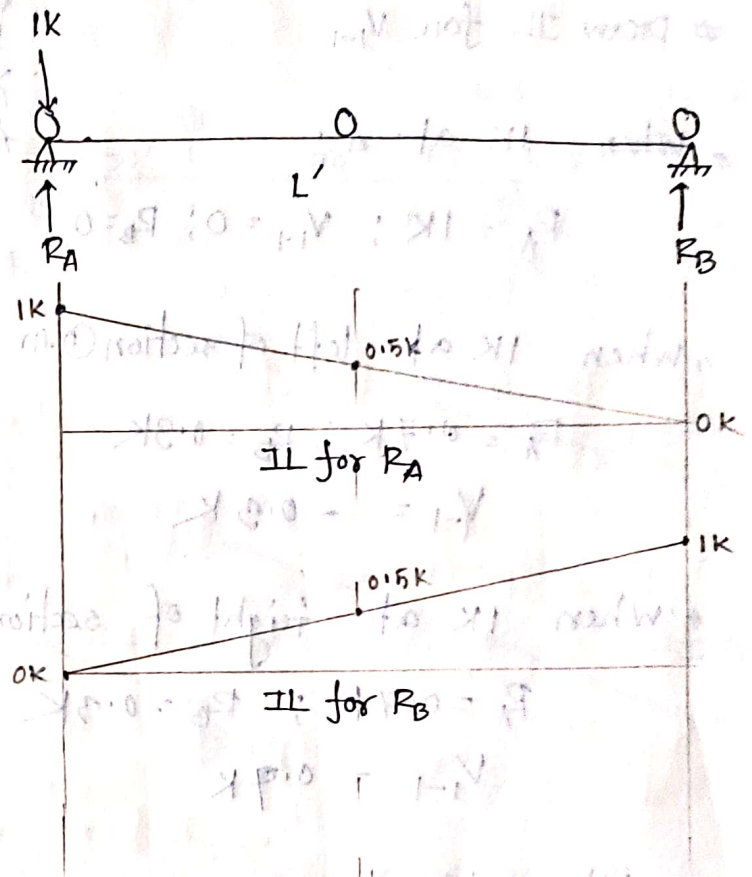
$$R_A = 1K; R_B = 0K$$

When 1K at $L/2$ from A:

$$R_A = 0.5K; R_B = 0.5K$$

When 1K at B:

$$R_A = 0K; R_B = 1K$$



In case of distribution load

$$\frac{1}{L} = \frac{i}{x} \quad [\text{From similar Triangle}]$$

$$i = \frac{x}{L}$$

Now,

$$\int_0^L dR_A = \int_0^L i \times w \times dx$$

$$\Rightarrow R_A = \int_0^L \frac{x}{L} w dx$$

$$R_A = \left[\frac{w}{2} \frac{x^2}{L} \right]_0^L$$

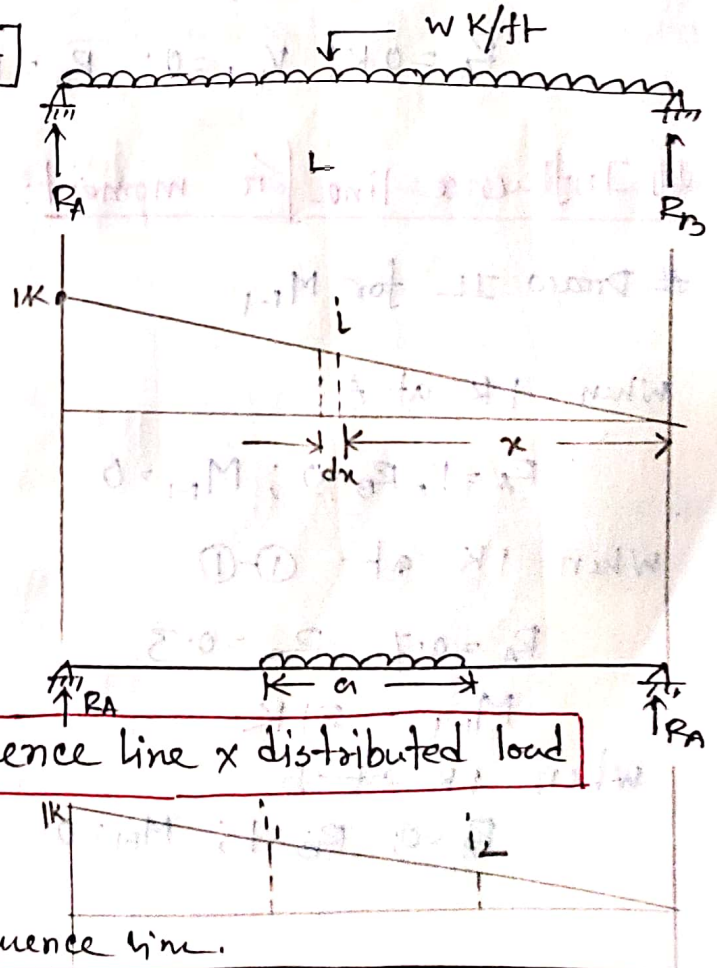
$$R_A = \frac{wL}{2}$$

$$\therefore R_A = \frac{1}{2} \times (1 \times L) \times w$$

$$\therefore R_A = \text{Area of the influence line} \times \text{distributed load}$$

$$\therefore R_A = \left[\frac{i_1 + i_2}{2} \times a \right] \times w$$

↪ area of the influence line.



Influence Line for shear force:

Draw IL for V_{1-1}

When 1K at A:

$$R_A = 1K; V_{1-1} = 0; R_B = 0$$

When 1K at left of section ①-①

$$R_A = 0.7K; R_B = 0.3K$$

$$V_{1-1} = -0.3K$$

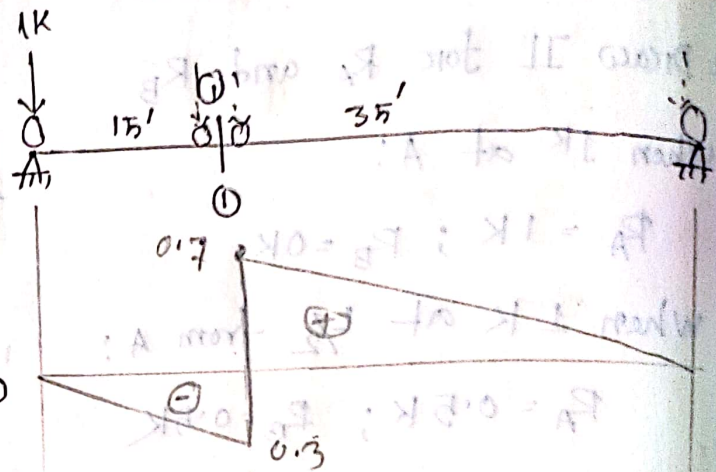
When 1K at right of section ①-①

$$R_A = 0.7K; R_B = 0.3K$$

$$V_{1-1} = 0.7K$$

When 1K at B:

$$R_A = 0K; V_{1-1} = 0; R_B = 1$$



Influence line for moment:

Draw IL for M_{1-1}

When 1K at A:

$$R_A = 1, R_B = 0; M_{1-1} = 0$$

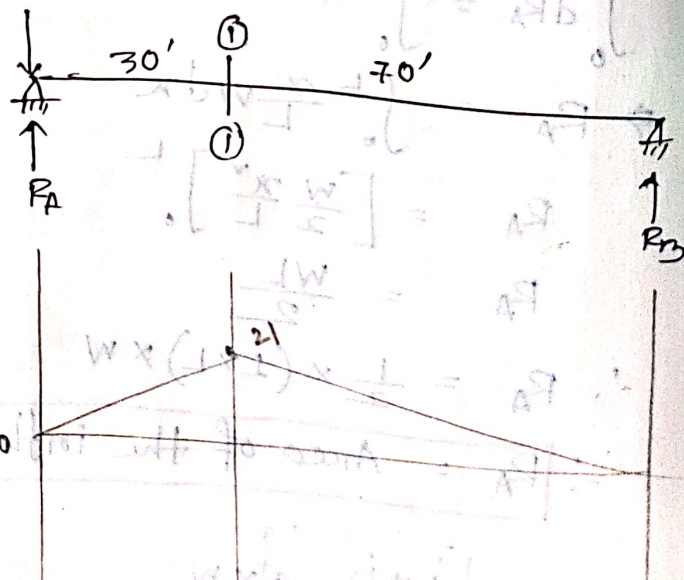
When 1K at ①-①

$$R_A = 0.7 \quad R_B = 0.3$$

$$M_{1-1} = 21K$$

When 1K at B

$$R_A = 0; R_B = 1; M_{1-1} = 0$$



Problem-01

Draw IL for R_A, V_{1-1}, M_{1-1}

When 1K at A

$$R_A = 1; R_B = 0$$

$$V_{1-1} = 0; M_{1-1} = 0$$

When 1K at just left from section (1-1)

$$R_A = 0.7K; R_B = 0.3K$$

$$V_{1-1} = -0.3; M_{1-1} = 21K'$$

When 1K at just to right from section (1-1)

$$R_A = 0.3K; R_B = 0.7K$$

$$V_{1-1} = 0.7; M_{1-1} = 21K'$$

When 1K at B

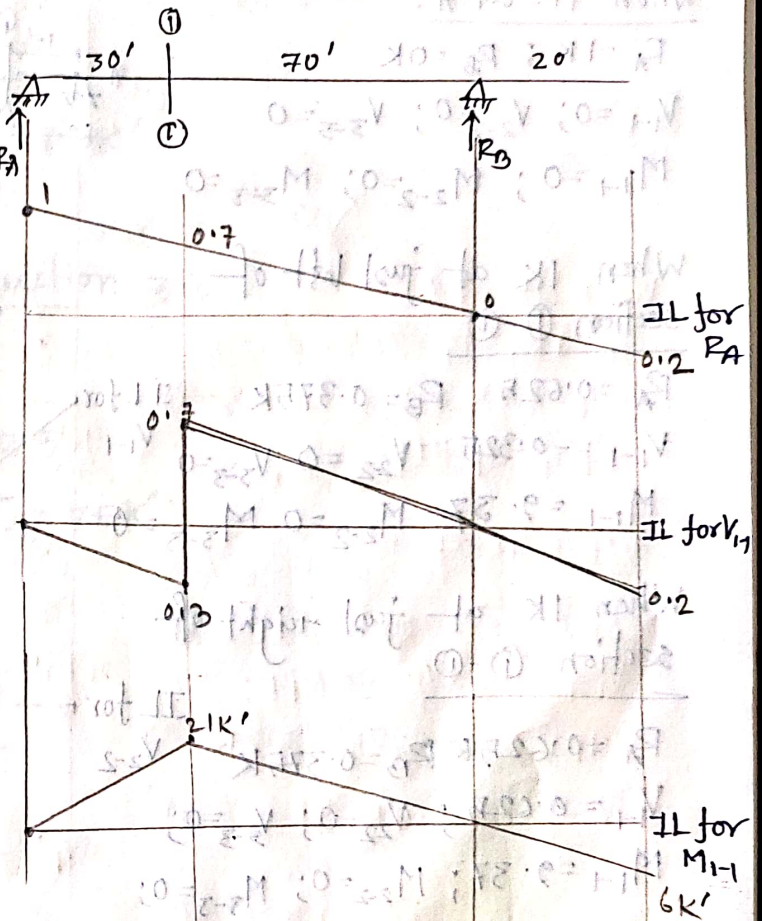
$$R_A = 0; R_B = 1K$$

$$V_{1-1} = 0; M_{1-1} = 0$$

When 1K at C

$$R_A = -0.2K; R_B = 1.2K$$

$$V_{1-1} = -0.2K; M_{1-1} = -6K'$$

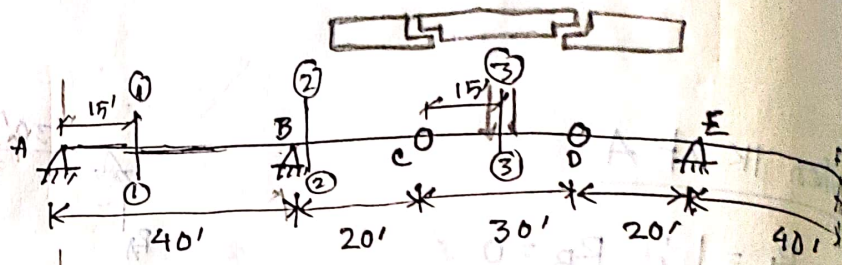


Problem-02

Draw IL for $V_{1-1}, V_{2-2}, V_{3-3}, M_{1-1}, M_{2-2}, M_{3-3}$

When 1K at A:

$R_A = 1K; R_B = 0K$
 $V_{1-1} = 0; V_{2-2} = 0; V_{3-3} = 0$
 $M_{1-1} = 0; M_{2-2} = 0; M_{3-3} = 0$



When 1K at just left of section ①-①

$R_A = 0.625; R_B = 0.375K$
 $V_{1-1} = -0.325; V_{2-2} = 0; V_{3-3} = 0$
 $M_{1-1} = 9.37; M_{2-2} = 0; M_{3-3} = 0$

When 1K at just right of section ①-①

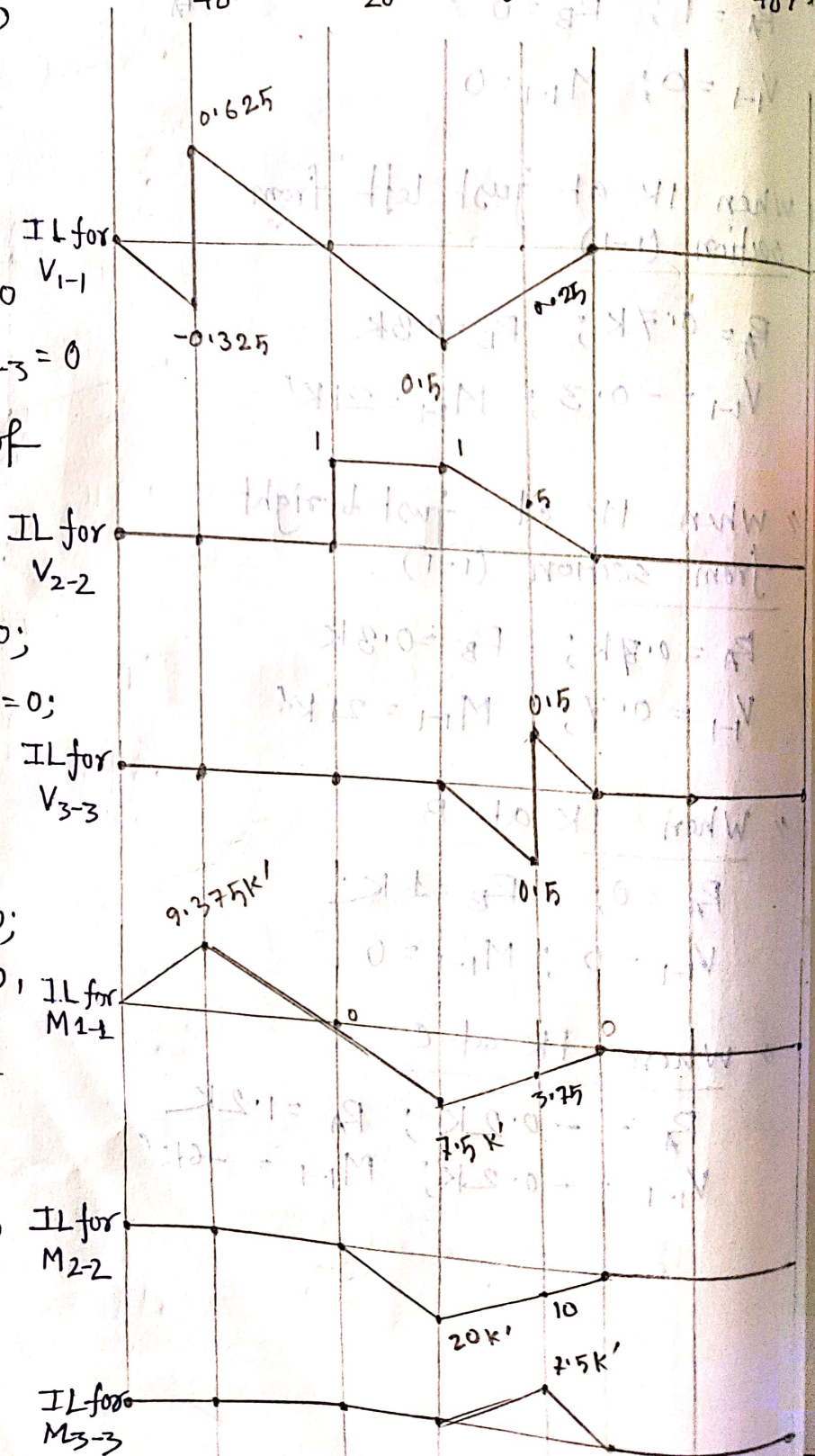
$R_A = 0.625K; R_B = 0.375K$
 $V_{1-1} = 0.625; V_{2-2} = 0; V_{3-3} = 0;$
 $M_{1-1} = 9.37; M_{2-2} = 0; M_{3-3} = 0;$

When 1K at B

$R_A = 0; R_B = 1K$
 $V_{1-1} = 0; V_{2-2} = 0; V_{3-3} = 0;$
 $M_{1-1} = 0; M_{2-2} = 0; M_{3-3} = 0;$

When 1K at just left of section ②-②

$R_A = -0.5K; R_B = 1.5K$
 $V_{1-1} = 0.5; V_{2-2} = 1; V_{3-3} = 0$
 $M_{1-1} = 7.5; M_{2-2} = 20K$
 $M_{3-3} = 0$



When 1K at just left of section 3-3

$$R_A = -0.25K; R_B = 0.75K$$

$$V_{1-1} = 0.25; V_{2-2} = 1; V_{3-3} = -0.5$$

$$M_{1-1} = -3.75; M_{2-2} = -10K'; M_{3-3} = 7.5K'$$

When 1K at just right of section 3-3

$$R_A = -0.25K; R_B = 0.75K$$

$$V_{1-1} = 0.25; V_{2-2} = 1; V_{3-3} = 0.5$$

$$M_{1-1} = -3.75; M_{2-2} = 10; M_{3-3} = 7.5K';$$

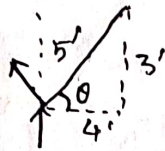
When 1K at point D

$$V_{1-1} = 0; V_{2-2} = 0; V_{3-3} = 0$$

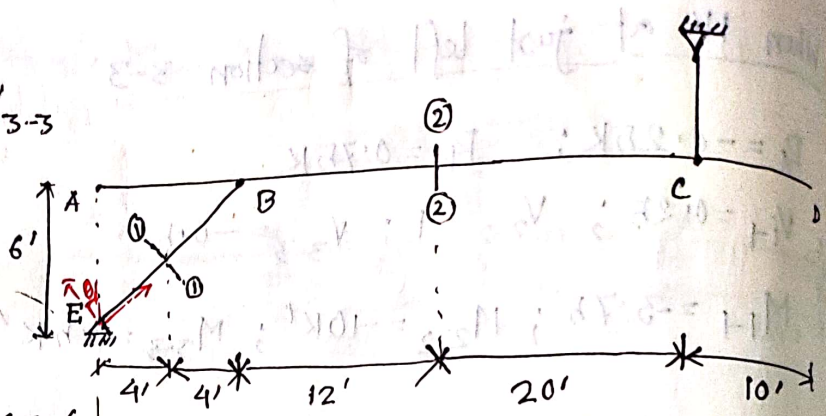
$$M_{1-1} = 0; M_{2-2} = 0; M_{3-3} = 0$$

Problem-03

Draw IL for V_{1-1} , V_{2-2} , V_{3-3}
 M_{1-1} , M_{2-2}



$\theta = 36.86^\circ$



When 1K at A

$R_E = 1K$; $R_F = 0$

$V_{1-1} = 0.8K$; $V_{2-2} = 0$; $F_{3-3} = 0$

$M_{1-1} = 4$; $M_{2-2} = 0$

When 1K at B

$R_E = \frac{32}{40} = 0.8K$; $R_F = 0.2K$

$V_{1-1} = 0.8 \times \frac{4}{8} = 0.4K$

$M_{1-1} = (0.4 \times 8) = 3.2K'$

$V_{2-2} = -0.2K$ $M_{2-2} = 4K'$

When 1K at just left of section 2-2

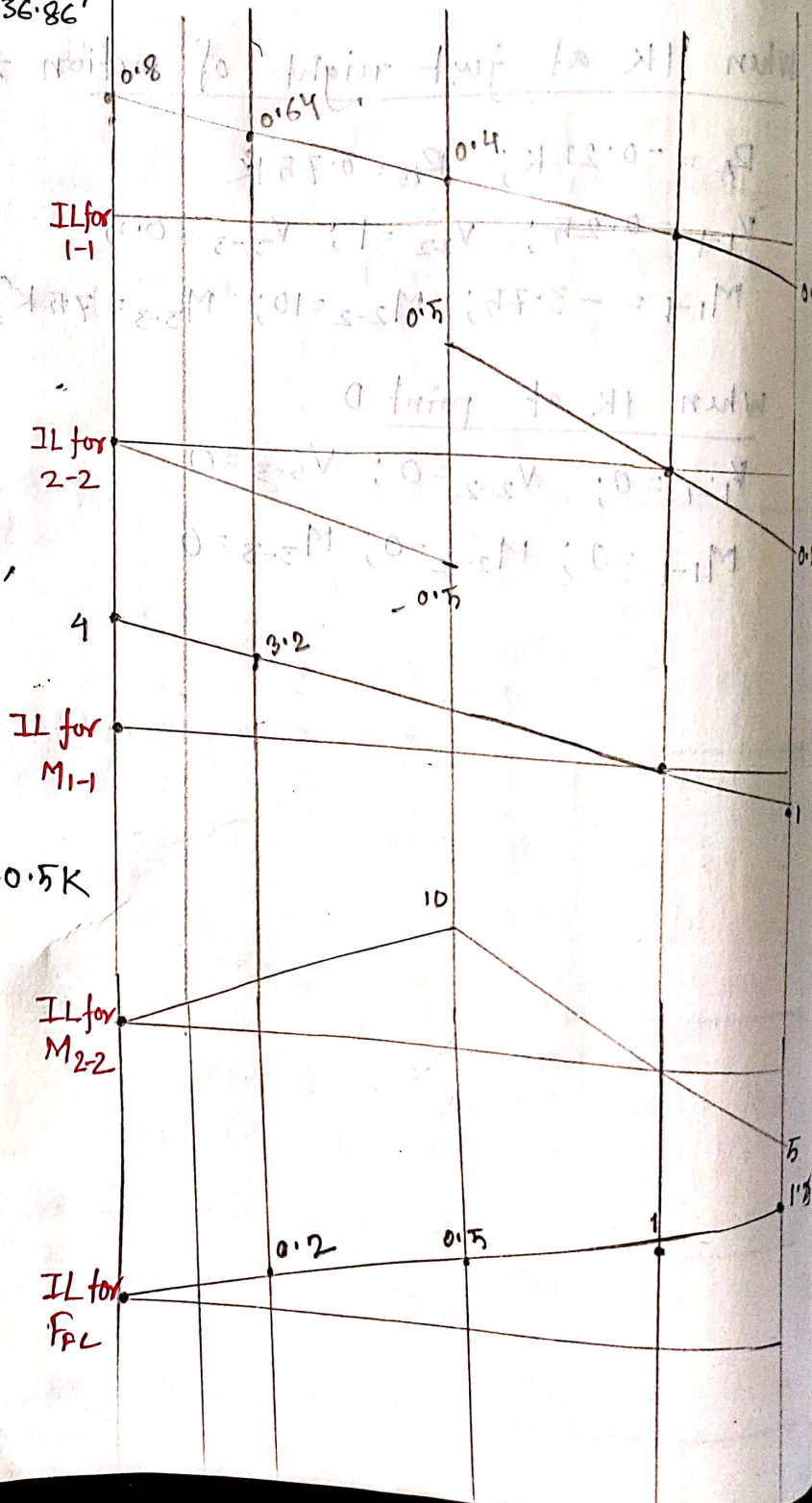
$R_E = 0.5K$; $R_F = 0.5K$

$V_{1-1} = -0.5 \times \frac{8}{10} = -0.4K$

$F_{3-3} = 0.5K$

$M_{1-1} = (0.4 \times 8) = 3.2K'$

$M_{2-2} = 10K'$



When 1K at just right of section 2-2

$$R_E = 0.5K; R_F = 0.5K$$

$$V_{1-1} = 0.4K; V_{2-2} = 0.5K; F_{FL} = 0.5K$$

$$M_{1-1} = 2K; M_{2-2} = 10K;$$

When 1K at c:

$$R_E = 0; R_F = 1K;$$

$$V_{1-1} = 0; M_{1-1} = 0; F_{FL} = 1K$$

$$V_{2-2} = 0; M_{2-2} = 0$$

When 1K at D:

$$R_E = -0.25K; R_F = 1.25K$$

$$V_{1-1} = (-0.25 \times \frac{8}{10}) = -0.2K;$$

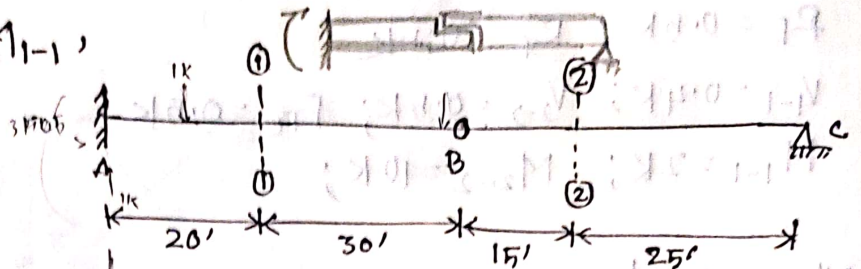
$$M_{1-1} = (-0.2 \times 5) = 1K$$

$$V_{2-2} = -0.25K; M_{2-2} = (-0.25 \times 20) = -0.5K'$$

$$F_{FL} = 1.25K$$

Problem-04:

Draw IL for V_{1-1} , V_{2-2} , M_{1-1} , M_{2-2} , M_A :



When 1K at A

$$R_A = 1K; R_C = 0$$

$$V_{1-1} = 0; V_{2-2} = 0; M_A = 0;$$

When 1K at just left of the section (1-1)

$$R_A = 1K; R_C = 0K$$

$$V_{1-1} = 0; V_{2-2} = 0$$

$$M_{1-1} = 0; M_{2-2} = 0$$

$$M_A = 20K'$$

When 1K at just right of the section (1-1):

$$R_A = 1K; R_C = 0K$$

$$V_{1-1} = 1K; V_{2-2} = 1K$$

$$M_{1-1} = 0K'; M_{2-2} = 0K'$$

$$M_A = -20K';$$

When 1K at B

$$R_A = 1K; R_C = 0K$$

$$V_{1-1} = 1K; V_{2-2} = 0K$$

$$M_{1-1} = 30K'; M_{2-2} = 0K'$$

$$M_A = -50K';$$

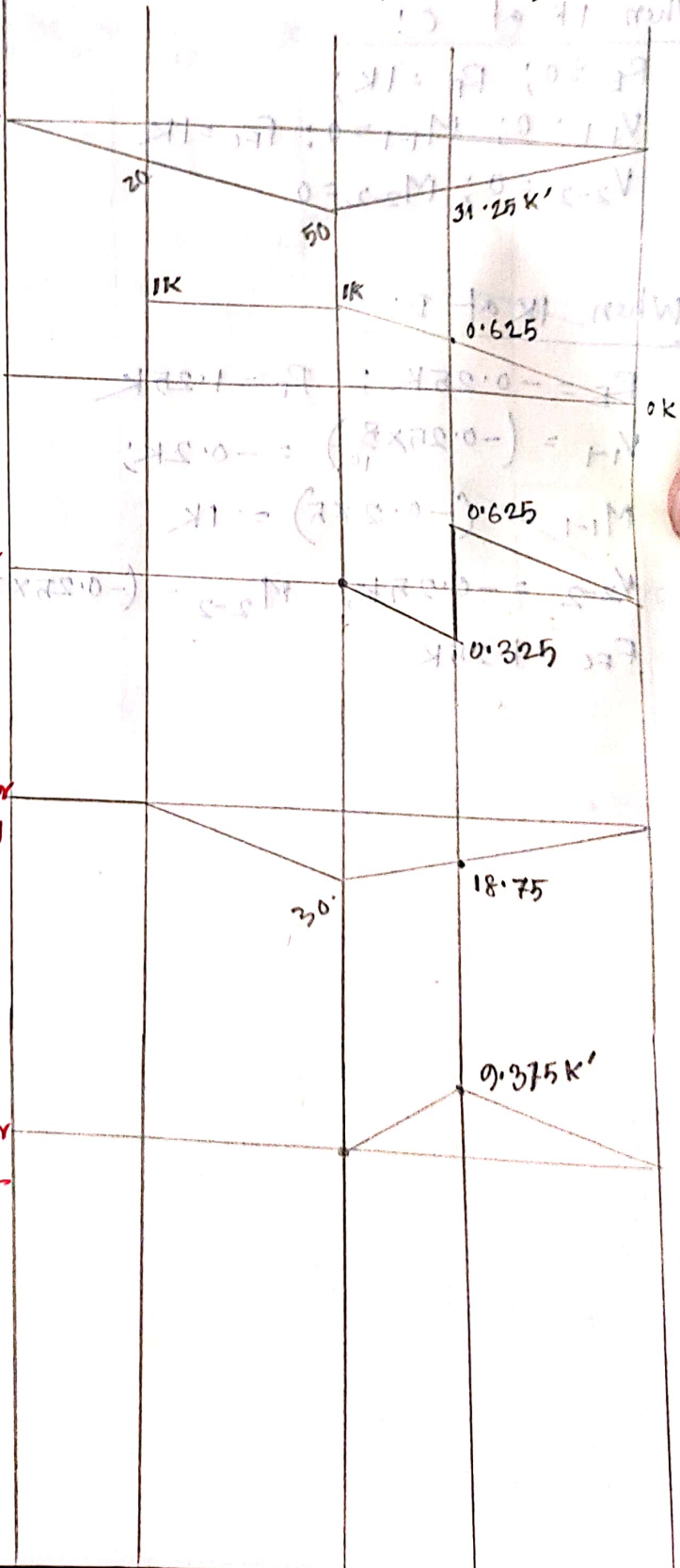
IL for M_A

IL for V_{1-1}

IL for V_{2-2}

IL for M_{1-1}

IL for M_{2-2}



When 1K at just left of the section (2-2)

$$R_B = 0.625K; R_C = 0.375K \quad \left(R_C = \frac{15}{40} \right)$$

$$V_{1-1} = 0.625K \quad V_{2-2} = 0.325K$$

$$M_{1-1} = 18.75K' \quad M_{2-2} = 9.375K'$$

$$M_A = -31.25K'$$

When 1K at just right of the section (2-2)

$$R_C = 0.375K \quad R_B = 0.625K$$

$$V_{1-1} = 0.625K \quad V_{2-2} = 0.625K$$

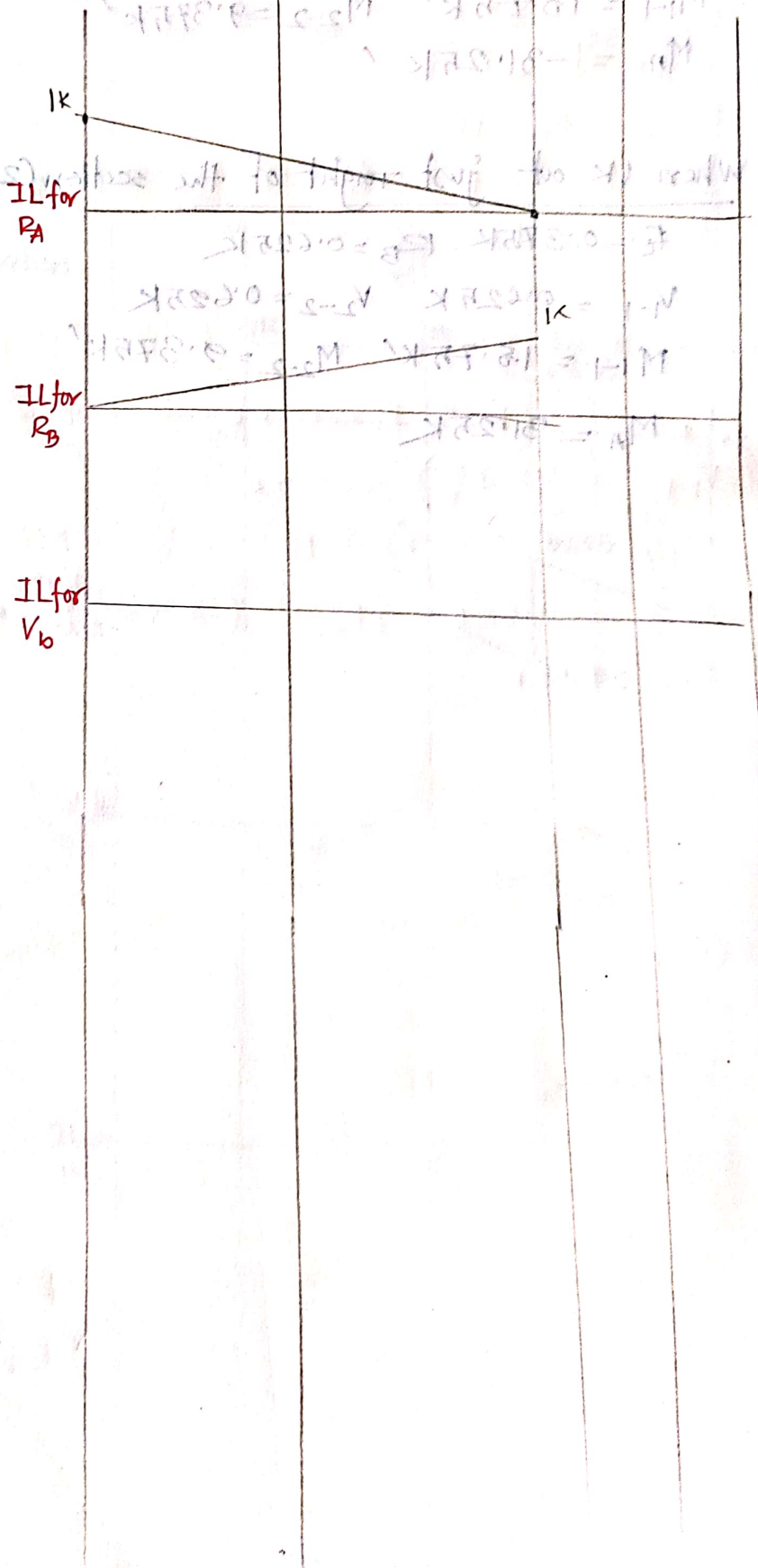
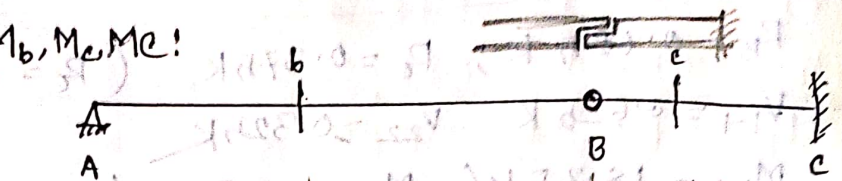
$$M_{1-1} = 18.75K' \quad M_{2-2} = 9.375K'$$

$$M_A = 31.25K'$$

Problem-05

Draw IL for R_A , R_B , V_b , V_c , M_b , M_c , M_C !

(s-s) reaction at left end of beam



Problem - 06

Draw IL for V_c, V_D, M_c, M_D and R_B

$$\theta = \tan^{-1} \frac{5}{10} = 26.565^\circ$$

When 1K at A:

$$\sum M_E = 0$$

$$-1 \times 10 + R_B \cos \theta \times 12 - R_B \sin \theta \times 20 = 0$$

$$R_B = 5.59 \text{ K}$$

$$R_{Bx} = 5.59 \cos 26.565^\circ = 5 \text{ K}$$

$$R_{By} = 5.59 \sin 26.565^\circ = 2.5 \text{ K}$$

$$\sum F_x = 0$$

$$R_{Bx} = R_{Ex} = 5 \text{ K}$$

$$\sum F_y = 0$$

$$R_{Ey} + 1 = R_{By}$$

$$R_{Ey} = 1.5 \text{ K}$$

$$V_c = 5 \text{ K} ; V_D = -(1 + 1.5) \text{ K} = -2.5 \text{ K}$$

$$M_c = +20 \text{ K}' \quad M_D = -1 \times 18 + 1.5 \times 8 = -30 \text{ K}'$$

When 1K at F:

All values are zero

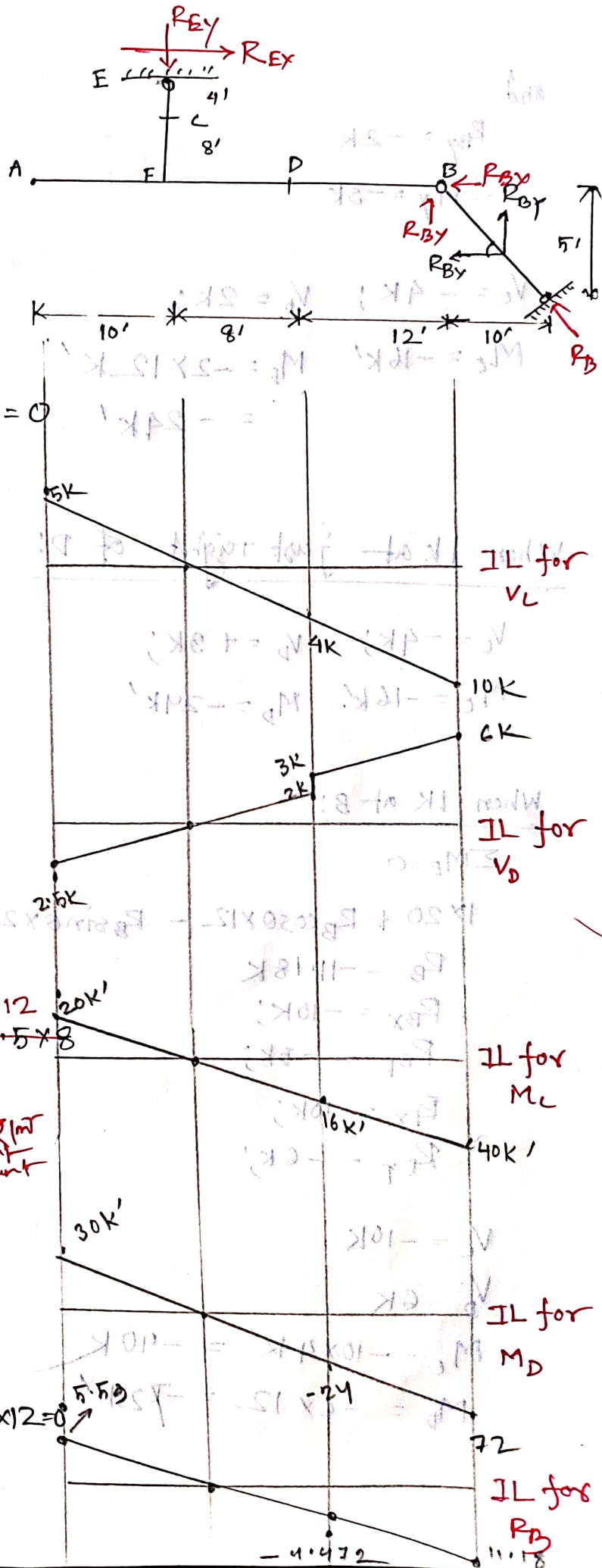
When 1K at just left of D:

$$\sum M_E = 0$$

$$1 \times 8 - R_B \sin \theta \times 20 + R_B \cos \theta \times 12 = 0$$

$$R_B = -4.472 \text{ K}$$

$$R_{Bx} = -4 \text{ K} = R_{Ex}$$



Extra moment
E point of count
20'

and

$$R_{By} = -2k$$

$$\therefore R_{By} = -3k$$

$$V_c = -4k; \quad V_D = 2k;$$

$$M_c = -16k' \quad M_D = -2 \times 12 k' \\ = -24k'$$

When 1k at just right of D:

$$V_c = -4k; \quad V_D = +3k;$$

$$M_c = -16k' \quad M_D = -24k'$$

When 1k at B:

$$\sum M_E = 0$$

$$1 \times 20 + R_B \cos 30^\circ \times 12 - R_B \sin 30^\circ \times 20 = 0$$

$$R_B = -11.18k$$

$$R_{Bx} = -10k';$$

$$R_{By} = -5k';$$

$$R_{Ex} = -10k';$$

$$R_{Ey} = -6k';$$

$$V_c = -10k$$

$$V_D = 6k$$

$$M_c = -10 \times 4 k = -40k$$

$$M_D = -6 \times 12 = -72k'$$

When 1k at F

$$R_F = 1k;$$

all values are 0