

Heaven's Light is Our Guide

Rajshahi University of Engineering & Technology
Rajshahi

**DEPARTMENT OF
CIVIL ENGINEERING**

Expt. No.01.....

Name of Expt *Introduction to Bridges*

<p>SUBJECT : <i>Reinforced Concrete</i></p> <p><i>Sessional - II</i></p> <p>COURSE NO. : <i>CE - 321B</i></p> <p>DATE OF EXPT.:.....</p> <p>DATE OF SUB. :.....</p>	<p>SUBMITTED BY :</p> <p>NAME : <i>Abu-Shah</i></p> <p>CLASS : <i>3rd year even semester</i></p> <p>GROUP :..... ROLL NO <i>1800144</i></p> <p>SESSION : <i>2018-10</i></p>
---	--

Chapter No : 01

Chapter Name : Introduction to Bridges.

Definition of Bridge :

A bridge is a structure built to span a physical structure obstacle (such as a body of water, valley, road or rail) without blocking the way underneath.

It is constructed for the purpose of providing passage over the obstacle, which is usually something that is otherwise difficult or impossible to cross.

There are many different designs of bridges, each serving a particular purpose and applicable to different situation.

Designs of bridges vary depending on factors such as :

- 1/ The function of the bridge.
- 2/ The nature of the terrain where the bridge is constructed & anchored &
- 3/ The material used to make it, &
- 4/ The funds available to build it.

Heaven's Light is Our Guide

Department of Civil Engineering

Rajshahi University of Engineering & Technology

Page

Parts of a bridge:

There are different types of bridge. Different bridge types contain different parts. Following are the main parts of a bridge:

- a) Guard rail.
- b) Deck.
- c) Abutment.
- d) Pile.
- e) Pier.
- f) Girder.
- g) Rail Track.

Heaven's Light is Our Guide

Department of Civil Engineering
Rajshahi University of Engineering & Technology

Page

Guard Rail:

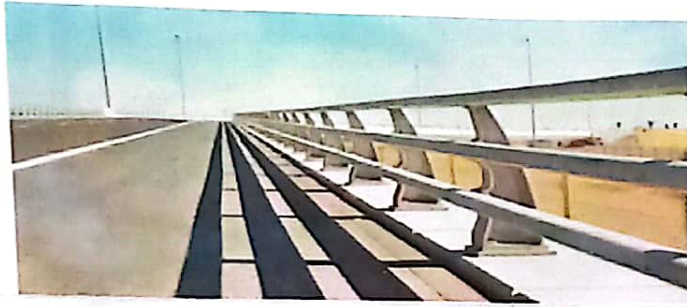


Fig: Guard Rail of a bridge

Curb:



Fig : Curb of a bridge

Heaven's Light is Our Guide

Department of Civil Engineering

Rajshahi University of Engineering & Technology

Page

Abutment:

The support provided at the two ends of a bridge is known as an abutment.

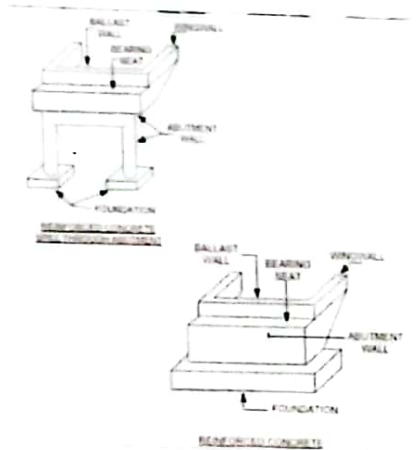


Fig : Abutment of bridges

Heaven's Light is Our Guide

Department of Civil Engineering

Rajshahi University of Engineering & Technology

Page

Deck:

A deck is a fundamental part of any bridge to pass vehicle, goods, people etc, from one side to another.

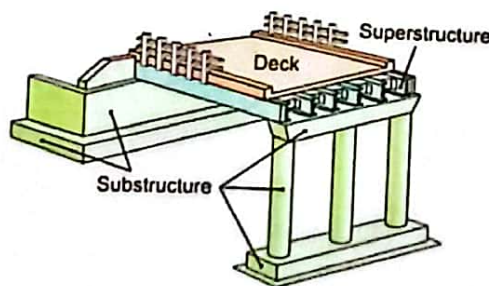
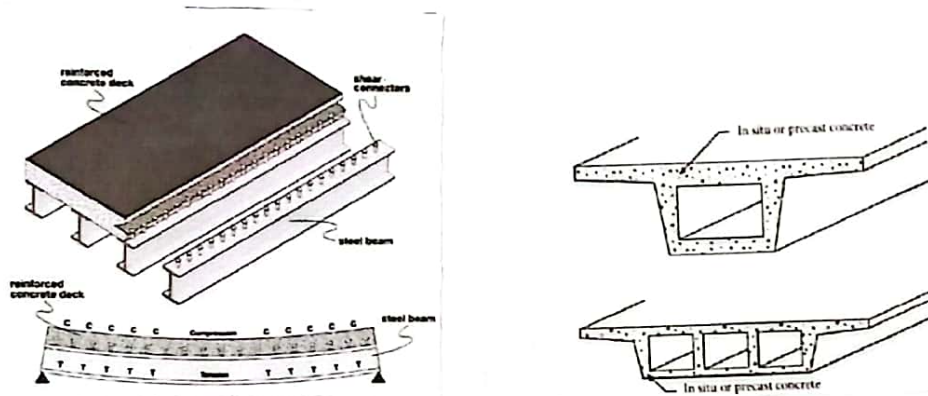


Fig : Deck of a bridge

Heaven's Light is Our Guide

Department of Civil Engineering

Rajshahi University of Engineering & Technology

Page

Girders:

Just like the beam, girder is used in the bridge. It can be two types I-joint and Box. This name has been given because of their shape. I-joint girder type is commonly used in bridges. Box girder can be precast or cast in place and it is generally existing in prestressed condition.

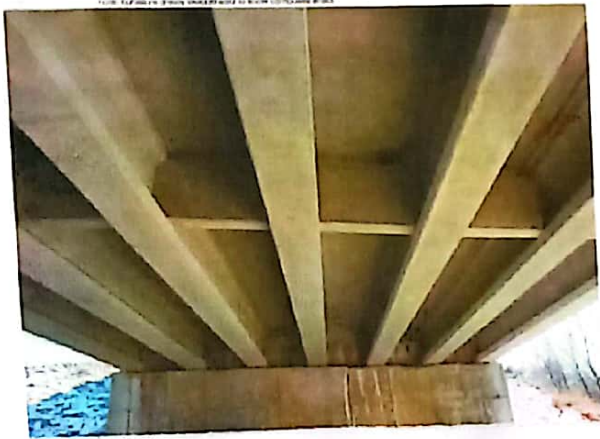


Fig : Girders of bridges.

Heaven's Light is Our Guide

Department of Civil Engineering
Rajshahi University of Engineering & Technology

Page

Pier:

Pier is the compression member which stay above the pile and make the structure stable. Pier generally provides for span at intermediate points.

Piers perform two main function:

- i) Transferring superstructure vertical loads to the foundation.
- ii) Resisting to the horizontal forces acting on the bridges.

For bridge pier to pier, distance is the span. Water pressure is the extra pressure which acts on to the pier laterally.



Fig : Pier of Padma bridge.

Heaven's Light is Our Guide

Department of Civil Engineering

Rajshahi University of Engineering & Technology

Page

Pile :

For the bridge with pier, the pile is a fundamental component. Pile type foundation is generally needed when the upper soil layer is loose. Pile depth depends on the soil layer. To find the hard soil layer which will make the structure stable, the pile is usually extended to some depth into the hard soil layer.

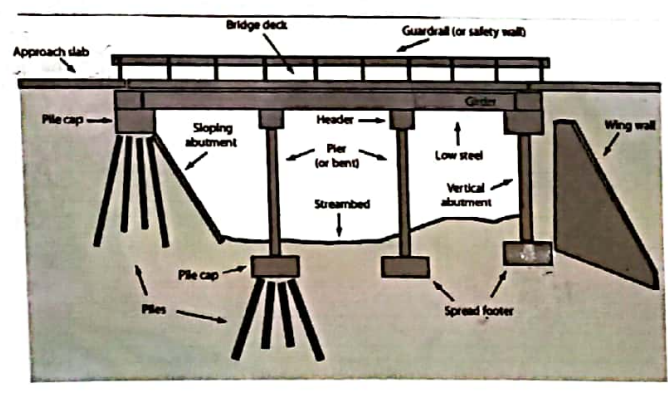


Fig : Pile of a bridge

Heaven's Light is Our Guide

Department of Civil Engineering

Rajshahi University of Engineering & Technology

Page

Rail Track:

Normally Road traffic is the main vehicle onto the bridge but if the train needs to be passed through that bridge rail track is the extra component.



Fig : Rail track of Padma bridge

Types of Bridges:

Following are the main types of bridges,

- 1) Truss Bridge.
- 2) Arch Bridge.
- 3) Suspension Bridge.
- 4) Cable - Stayed Bridge.
- 5) Slab Bridges.
- 6) Box Girders Bridge.
- 7) Fixed Bridges.
- 8) Movable Bridges.

Heaven's Light is Our Guide

Department of Civil Engineering
Rajshahi University of Engineering & Technology

Page

Truss Bridge :

Bridges with truss are made by steel force members with only tension & compression. No bending moment is allowed in this structure. Most stable structural shape for truss is triangular.

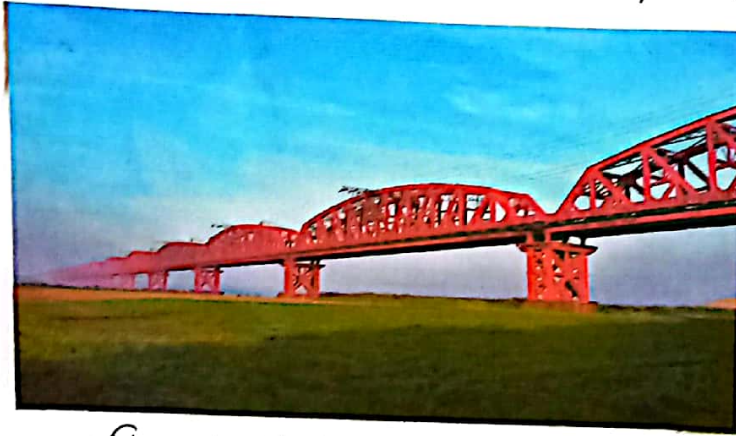


Fig : Hardne Bridge

Arch Bridges :

Arch bridge mainly exists in compression. Utilizes an aerodynamic system with torsional rigidity.

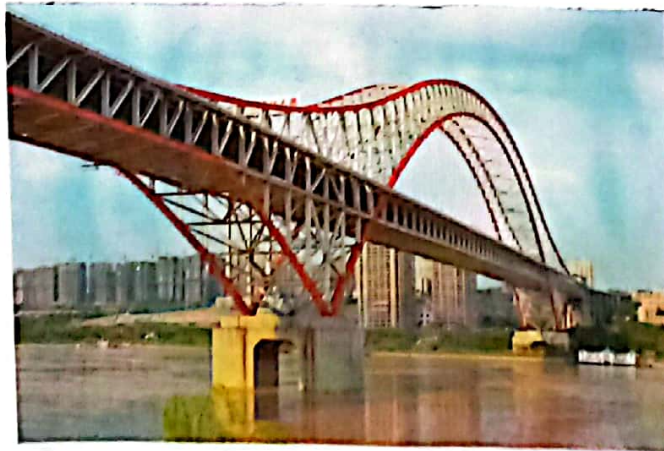


Fig : Arch bridge

Heaven's Light is Our Guide

Department of Civil Engineering

Rajshahi University of Engineering & Technology

Page

Suspension Bridges:

In suspension bridges long spans can be provided which is essential in many situations. It gives freedom to the engineers to provide a long span with the help of a cable.

Following are the basic components of a suspension bridge structural system:

Stiffening Girders / Trusses: Longitudinal structures support and distribute moving vehicle loads. Secure aerodynamic stability of the structure.

Main Cables: Main cables are connected to girders through hanger rope. These hanger ropes transfer the loads from girders to the main cables. The main function of these main cables is to carry these loads to the main towers.

Main Towers: Main cables are supported by these intermediate vertical structures and transfer the total load of the bridge to the foundation.

Heaven's Light is Our Guide

Department of Civil Engineering

Rajshahi University of Engineering & Technology

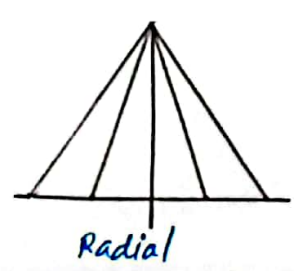
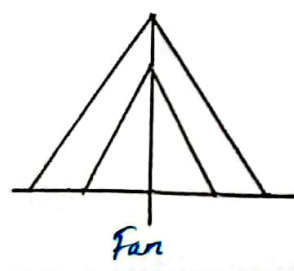
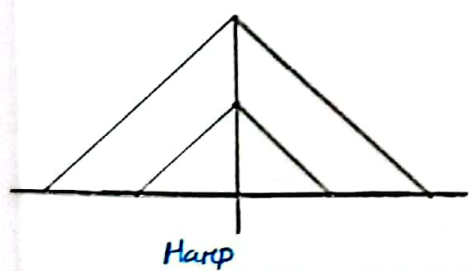
Page



Figure: Hanging Bridge - Rangamati

Cable - stayed bridges:

It has a lot of similarities to the suspension bridge. But there are few differences between a suspension bridge & cable stayed bridge. In this case, bridge mainly carries the vertical loads acting on the girders. The purpose of the stay cables is to provide intermediate support for the girders and it helps to span a long distance.



Heaven's Light is Our Guide

Department of Civil Engineering

Rajshahi University of Engineering & Technology

Page



Figure: Shah Amanat Bridge - Chattogram.

Heaven's Light is Our Guide

Department of Civil Engineering

Rajshahi University of Engineering & Technology

Page

Slab Bridges:

It is the most common type of bridges. Use in every place where the span is not so long.



Box Girder Bridges:

It's a box type girder different from normal I girder and it can easily resist more amount of torsion. This type of bridge contains top deck, vertical web, bottom slab. Box girder bridge can be subdivided into three basic categories:

1) Single cell box.

2) Multicell box.

3) Box with struts supporting a cantilever deck.

Heaven's Light is Our Guide

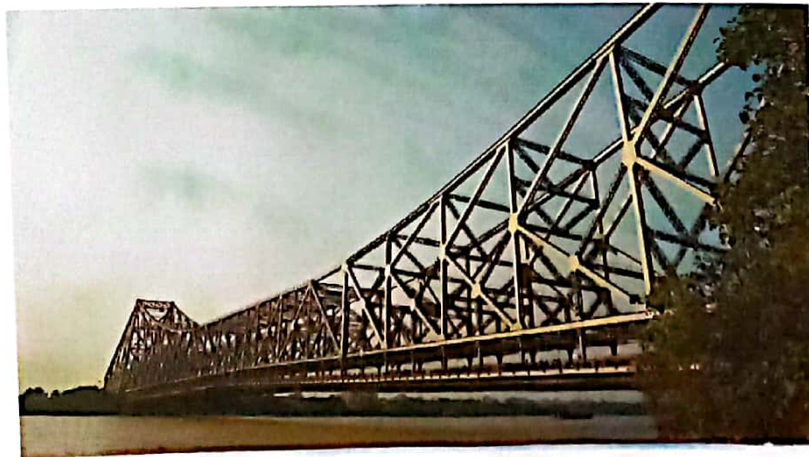
Department of Civil Engineering
Rajshahi University of Engineering & Technology

Page



Fixed Bridges:

Majority of bridges are fixed, with no moveable parts to provide higher clearance for river/sea transport that is following below them. They are designed to stay where they are deemed unusable or demolished.



Heaven's Light is Our Guide

Department of Civil Engineering
Rajshahi University of Engineering & Technology

Page

Movable Bridges:

A movable bridge is a bridge that has dynamic moving parts used to change the form of the bridge usually to allow passage for boats. There are many types of movable bridges, and they differ in the way they transform.

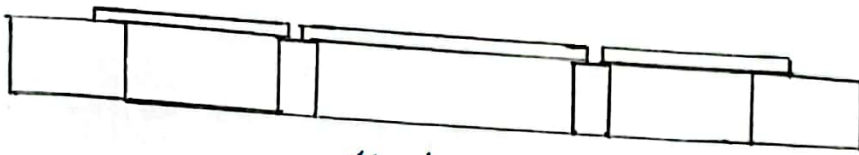


Heaven's Light is Our Guide

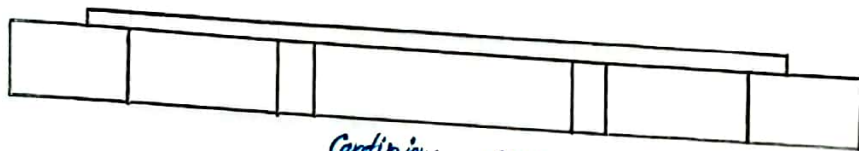
Department of Civil Engineering
Rajshahi University of Engineering & Technology

Page

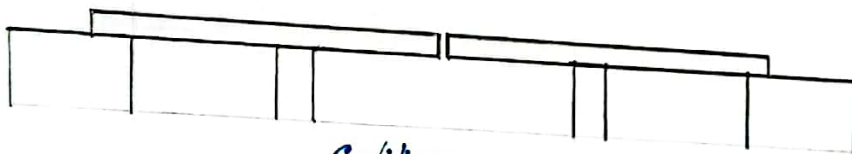
Span Type:



Simple span



Continuous span



Cantilever span

Site selection for bridge:

The characteristics of an ideal site for a bridge across a river are

- a) A straight reach of the river.
- b) Steady river flow without cross currents.
- c) A narrow channel with firm banks.
- d) Suitable high banks above high flood level on each side.
- e) Rock or other hard in erodible strata close to the river bed level.
- f) Absence of sharp curves in the approaches.
- g) Absence of expensive river training works.
- h) Avoidance of excessive underwater construction.

Heaven's Light is Our Guide

Rajshahi University of Engineering & Technology
Rajshahi

**DEPARTMENT OF
CIVIL ENGINEERING**

Expt. No. 02

Name of Expt Design of Slab Bridge

<p>SUBJECT : <u>Reinforced Concrete Sessional-21</u></p> <p>COURSE NO. : <u>CE- 3218</u></p> <p>DATE OF EXPT.:.....</p> <p>DATE OF SUB. :.....</p>	<p>SUBMITTED BY :</p> <p>NAME : <u>Abu-Shad</u></p> <p>CLASS : <u>3rd year 2 even semester</u></p> <p>GROUP :..... ROLL NO <u>1800144</u></p> <p>SESSION : <u>2018-19</u></p>
--	--

Heaven's Light is Our Guide

Department of Civil Engineering
Rajshahi University of Engineering & Technology

Page

Chapter No : 02

Name of the chapter: Design of slab Bridge . (Design of railing & rail post)

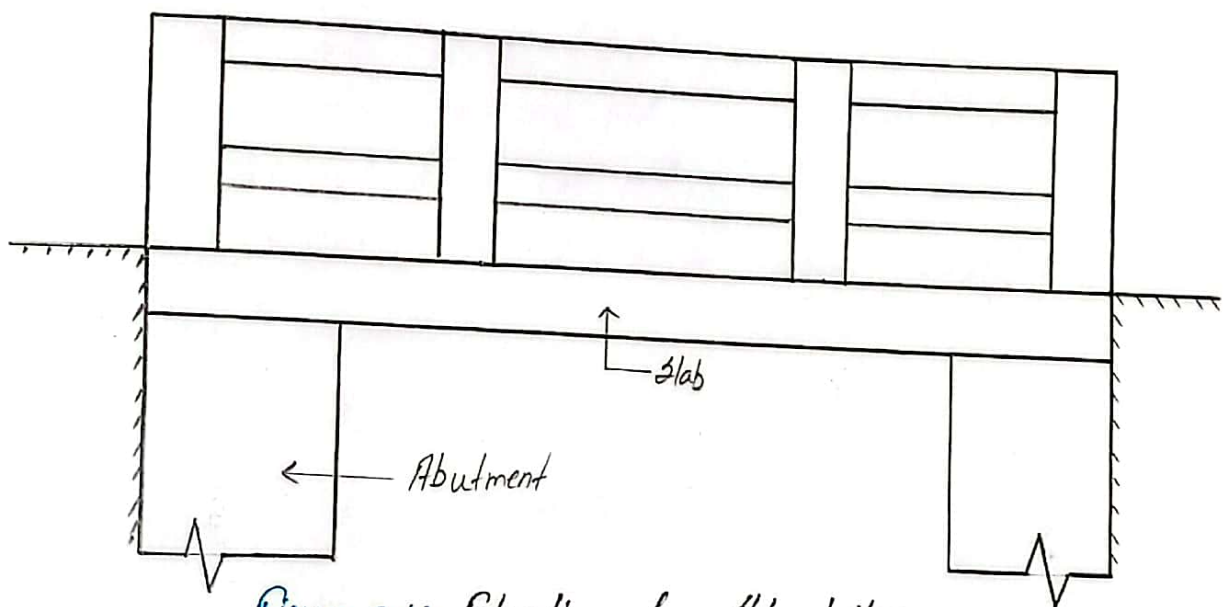


Figure 2.1: Elevation of slab bridge

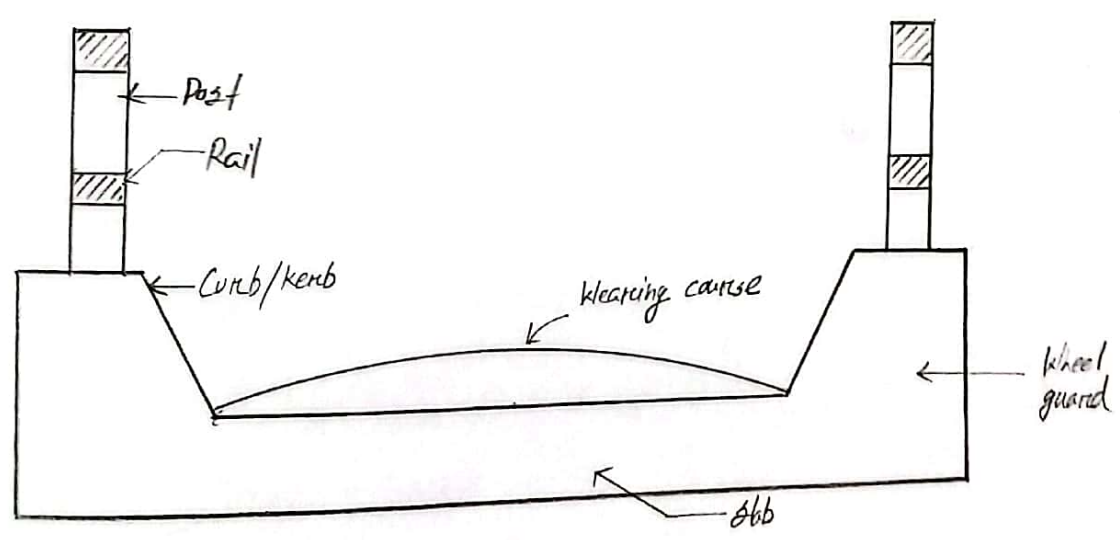


Figure: 2.2: Gross-section of slab bridge.

Heaven's Light is Our Guide

Department of Civil Engineering
Rajshahi University of Engineering & Technology

Page

Design specification:

- 1) Length of clear span = $8' + \frac{\text{last 2 digit of roll}}{4}$
 $= 8' + \frac{44}{4} = 19'$
- 2) Width of the span = $30'$
- 3) Horizontal load = 200 plf
- 4) Vertical live load = 150 plf
- 5) Horizontal thrust due to wheel = 500 plf
- 6) Material properties :-
 $f_c' = 3500 \text{ psi}$
 $f_y = 60000 \text{ psi}$
- 7) Loading system = H20S16 Truck load.

Design of Rail & Post:

Relevant properties:

- 1) $n = E_s / E_c = \frac{29 \times 10^6}{57000 \sqrt{3500}} = 8.6 \approx 9$
- 2) $\pi = f_s / f_c = \frac{0.4 \times 60,000}{0.45 \times 3500} = 15.24$
- 3) $k = \frac{n}{n + \pi} = \frac{9}{9 + 15.24} = 0.37$
- 4) $j = 1 - k/3 = 1 - \frac{0.37}{3} = 0.88$
- 5) $R = \frac{1}{2} f_c j k = \frac{1}{2} \times 3500 \times 0.45 \times 0.88 \times 0.37 = 256.41$

Heaven's Light is Our Guide

Department of Civil Engineering
Rajshahi University of Engineering & Technology

Page

Railing Post:

- (i) Let the spacing of rail post, $s = 6.5'$
- (ii) Number of rail post $= \frac{19'}{6.5'} + 1 = 3.92 \approx 4$
- (iii) Actual spacing of rail post $s_a = \frac{19}{4-1} = 6.34'$

Assume the section of railing = $6" \times 6"$

Load calculation

- (1) Self weight $= \frac{6" \times 6"}{12' \times 12'} \times 150 = 37.5 \text{ plf}$
- (2) Vertical load $= 150 \text{ plf}$

$$\therefore \text{Total load } W_v = 187.5 \text{ plf}$$

$$\begin{aligned} \text{So, vertical moment, } M_v &= \frac{W_v \times s_a^2}{8} \\ &= \frac{187.5 \times 6.3}{8} \\ &= 942.08 \text{ lb-ft} \end{aligned}$$

Depth check:

We know,

$$\begin{aligned} d &= \sqrt{\frac{M}{R_b}} = \sqrt{\frac{942.08 \times 12}{25.41 \times 6}} \\ &= 2.71" \end{aligned}$$

$$\text{Deductive} = t - LL - \frac{V}{2} = 6 - 2 - 0.5 = 3.5$$

$\therefore \text{dreq} < \text{dett} \therefore \text{OK design}$

Heaven's Light is Our Guide

Department of Civil Engineering
Rajshahi University of Engineering & Technology

Page

Steel calculation:

$$\begin{aligned} \text{Steel area, } A_s &= \frac{M}{f_s j d} \\ &= \frac{942.08 \times 12}{24000 \times 0.88 \times 30.5} \\ &= 0.15 \text{ in}^2 \end{aligned}$$

Minimum reinforcement required

$$\begin{aligned} A_{s(\min)} &= \frac{3 \sqrt{f_c'}}{f_y} b d = \frac{3 \times \sqrt{3500} \times 12 \times 30.5}{60,000} \\ &= 0.124 \text{ in}^2 \end{aligned}$$

$$\begin{aligned} A_s (\min) &= \frac{200}{f_y} b d = \frac{200 \times 12 \times 30.5}{60,000} \\ &= 0.14 \text{ in}^2 \end{aligned}$$

\therefore Steel required = 0.15 in²

Heaven's Light is Our Guide

Department of Civil Engineering

Rajshahi University of Engineering & Technology

Page

So we will provide 4#5 bars

Reinforcing Diagram :

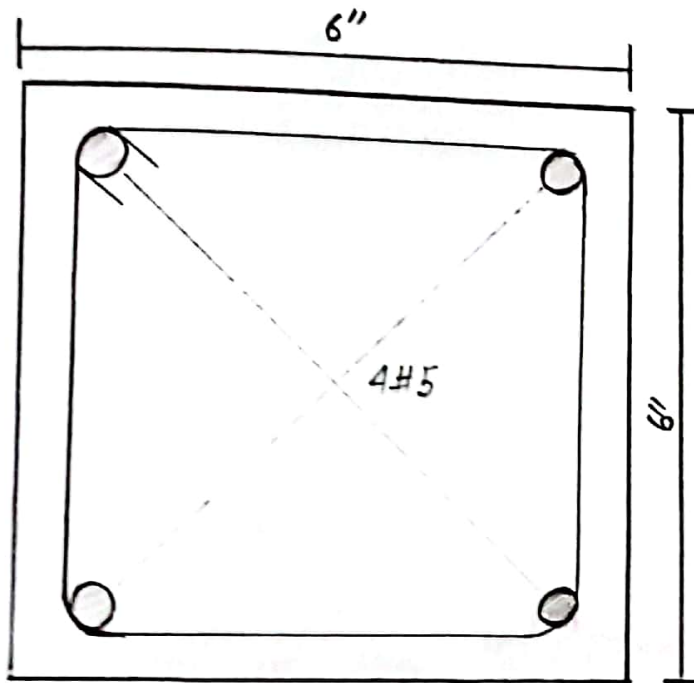
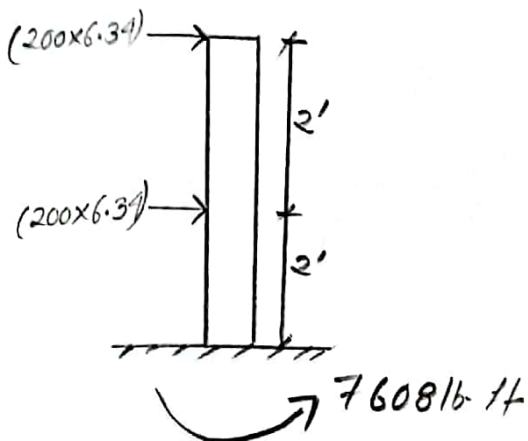


Figure 3: Cross section of footing

Design of post:



Assume, the section of rail post = $8'' \times 8''$

Height of the rail post = $4'$

Maximum Horizontal moment at base, $M_H = (200 \times 6.34 \times 4) + (200 \times 6.34 \times 2)$
 $= 7608 \text{ lb-ft}$

Depth check:

Moment, $M_H = 7608 \text{ lb-ft}$

Now, $d_{req} = \sqrt{\frac{7608 \times 12}{256.41 \times 8}}$
 $= 6.66''$

Heaven's Light is Our Guide

Department of Civil Engineering

Rajshahi University of Engineering & Technology

Page

$$\text{So } t_{\text{eff}} = 6.66 + 1.5 = 8.16''$$

Our assumed section $t = 8''$

So it is relatively closed $t_{\text{eff}} \approx t$

So our assumed section for rail post $(8'' \times 8'')$
is ok.

Steel calculation:

$$A_s = \frac{M}{f_s j d} = \frac{7608 \times 12}{24000 \times 0.88 \times 6.5} = 0.66 \text{ in}^2$$

Minimum reinforcement required,

$$A_{s(\text{min})} = \frac{3 \sqrt{f_c'}}{f_y} b d = \frac{3 \sqrt{3500}}{60,000} \times 12 \times 6.5 = 0 \text{ in}^2$$

$$\text{again } A_{s(\text{min})} = \frac{200}{f_y} b d = \frac{200}{60,000} \times 12 \times 6.5 = 0.26 \text{ in}^2$$

So we will choose steel area 0.66 in^2

we can provide 4#5 bars

Reinforcing Diagram:

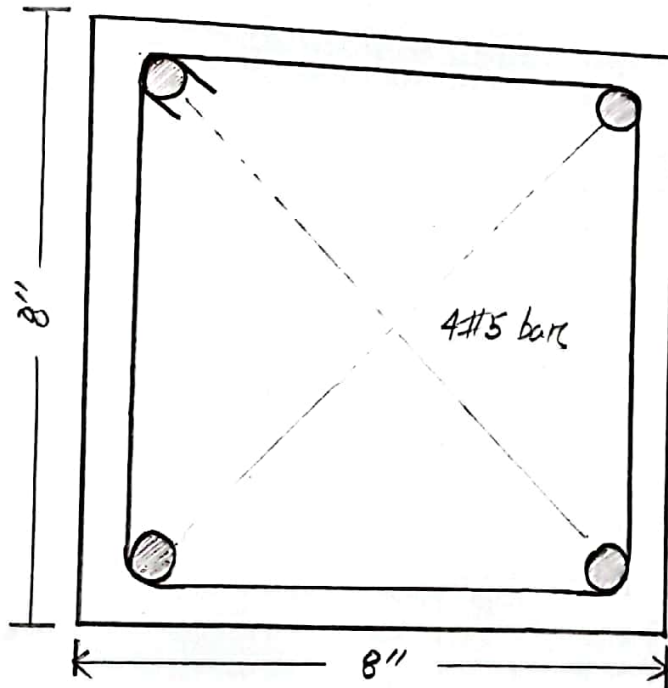
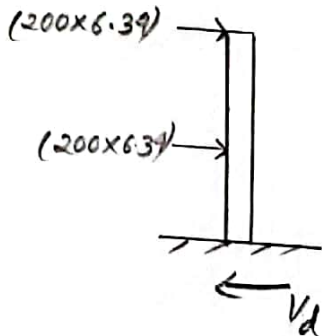


Figure 4: Cross section of rail post.

Shear Check:



Developed shear, $V_d = (200 \times 6.39) + (200 \times 6.39)$
 $= 2536 \text{ lb}$

Allowable shear, $V_{all} = 1.1 \sqrt{f_c'} b d = 1.1 \sqrt{3500} \times \times 6.5$
 $= 3384 \text{ lb}$

$\therefore V_{all} > V_{dev}$, so no stirrup need. But we should provide.

Web reinforcement

spacing, $s = 3t = 3 \times 8 = 24''$

and $s_{rp} = \frac{AV}{0.0015b} = \frac{2 \times 11}{0.0015 \times 8} = 18.33''$

So, #3 bar will be provided at rail post for stirrup at 18.33" spacing

Heaven's Light is Our Guide

Rajshahi University of Engineering & Technology
Rajshahi

**DEPARTMENT OF
CIVIL ENGINEERING**

Expt. No. 2.2

Name of Expt *Edge Beam Design*

SUBJECT : <i>Reinforced Concrete Sessional-II</i>	SUBMITTED BY :
COURSE NO. : <i>CE - 3218</i>	NAME : <i>Abu-shad</i>
DATE OF EXPT.:	CLASS : <i>3rd year even semester</i>
DATE OF SUB. :	GROUP : <i>01</i> ROLL NO <i>1800144</i>
	SESSION : <i>2018-19</i>

Chapter No : 2.2

Chapter Name : Edge Beam Design:

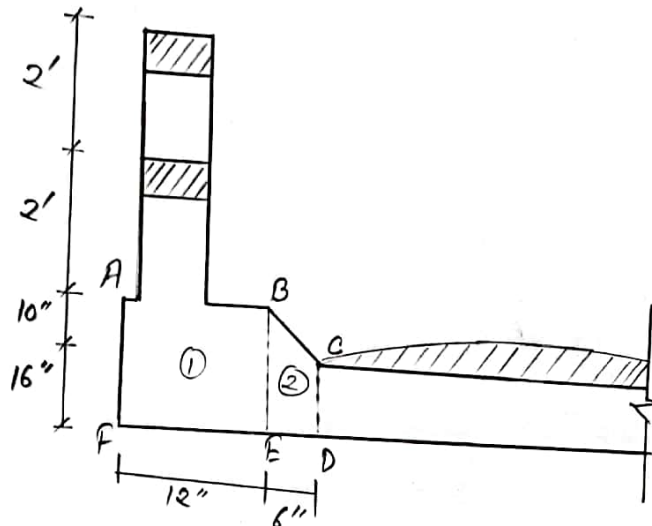


Figure : Edge Beam

Dead load of kerb:

$$\begin{aligned}
 \text{i) Dead load of section (18ft)} &= \left[\frac{(10+16) \times 1}{144} + \frac{(0.5 \times 6 \times 10)}{144} + \right. \\
 &\quad \left. \frac{6 \times 16}{144} \right] \times 150 \\
 &= 456.25 \text{ plf}
 \end{aligned}$$

Heaven's Light is Our Guide
 Department of Civil Engineering
 Rajshahi University of Engineering & Technology

Page

1) Load coming from railing & rail post:

$$= \frac{\left[\frac{2 \times 6 \times 6}{199} \times 19 \right] + \left[\frac{8 \times 8}{199} \times 4 \times 4 \right]}{19} \times 150$$

$$= 131.14 \text{ plf}$$

∴ Total dead load $w_d = 587.4 \text{ plf}$

Dead load moment $M_D = \frac{w_d \times L^2}{8} = \frac{587.4 \times 19^2}{8}$

$$= 26505.97 \text{ lb-ft}$$

Live load moment $M_L = 0.1 \times H_{20516} \times L = 0.1 \times 16000 \times 19$

$$= 30,400 \text{ lb-ft}$$

∴ Total moment = $M_D + M_L = 56905.97 \text{ lb-ft}$

Depth check:

$$d_{req} = \sqrt{\frac{M}{R_b}} = \sqrt{\frac{56905.97 \times 12}{256.41 \times 12}}$$

$$= 14.9''$$

Effective Depth = $26 - CC - \frac{\phi}{2} - \frac{\phi'}{4}$

$$= 26 - 1.5 - \frac{4}{8} - \frac{6}{8} \times 2$$

$$= 23.63'' > d_{req} \quad \therefore \text{OK}$$

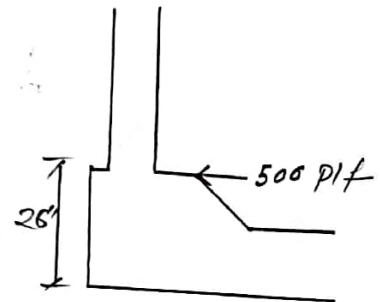
Reinforcement Calculation:

$$A_s = \frac{M}{f_s j d} = \frac{56905.94 \times 12}{24,000 \times 0.88 \times 23.63}$$
$$= 1.37 \text{ in}^2$$

Use 4# bars

Moment of critical section:

$$M_c = (W_{thrust} \times \frac{26}{12}) + W_{HL} \times (2 + \frac{26}{12} + 4)$$
$$= 2633.33 \text{ lb-ft}$$



Depth check:

$$d_{req} = \sqrt{\frac{2633.33 \times 12}{256.4 \times 12}}$$
$$= 3.2 \text{ inches}$$

$$d_{eff} = 16 \text{ inches} - 1.5 \text{ inches} - \frac{3}{8} \text{ inches} - \frac{6}{2 \times 8} \text{ inches} = 13.75 \text{ inches} > d_{req}$$

∴ Depth is ok.

1

Reinforcement Calculation:

$$A_s = \frac{2633.39 \times 12}{24,000 \times 0.98 \times 13.75} = 0.1 \text{ in}^2$$

Use #3 bar $a_f = \frac{12 \times 0.11}{0.1} = 14. \dots \text{ c to c}$

Web reinforcement:

$$s = 3t = 3 \times 26 = 78 \text{ ''}$$

$$s = \frac{A_v}{0.0015b} = \frac{2 \times 0.11}{0.0015 \times 18} = 8.15 \text{ ''} \approx 8 \text{ '' c/c}$$

Reinforcement Details:

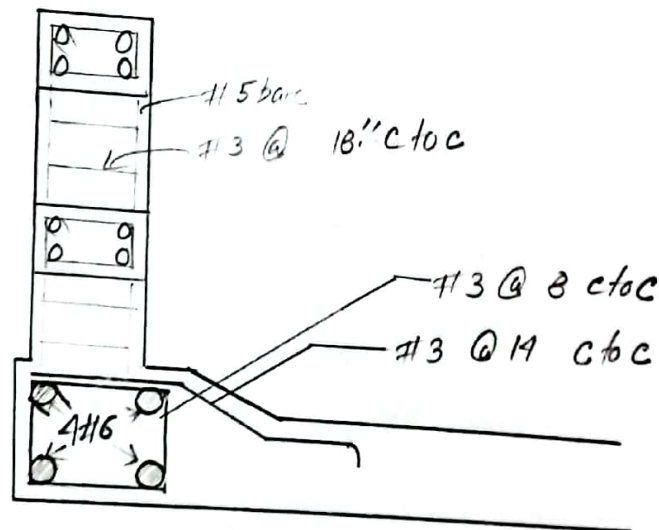


Figure: Reinforcement detail of edge beam.

Heaven's Light is Our Guide

Rajshahi University of Engineering & Technology
Rajshahi

**DEPARTMENT OF
CIVIL ENGINEERING**

Expt. No. *2.3*

Name of Expt *Design of slab*

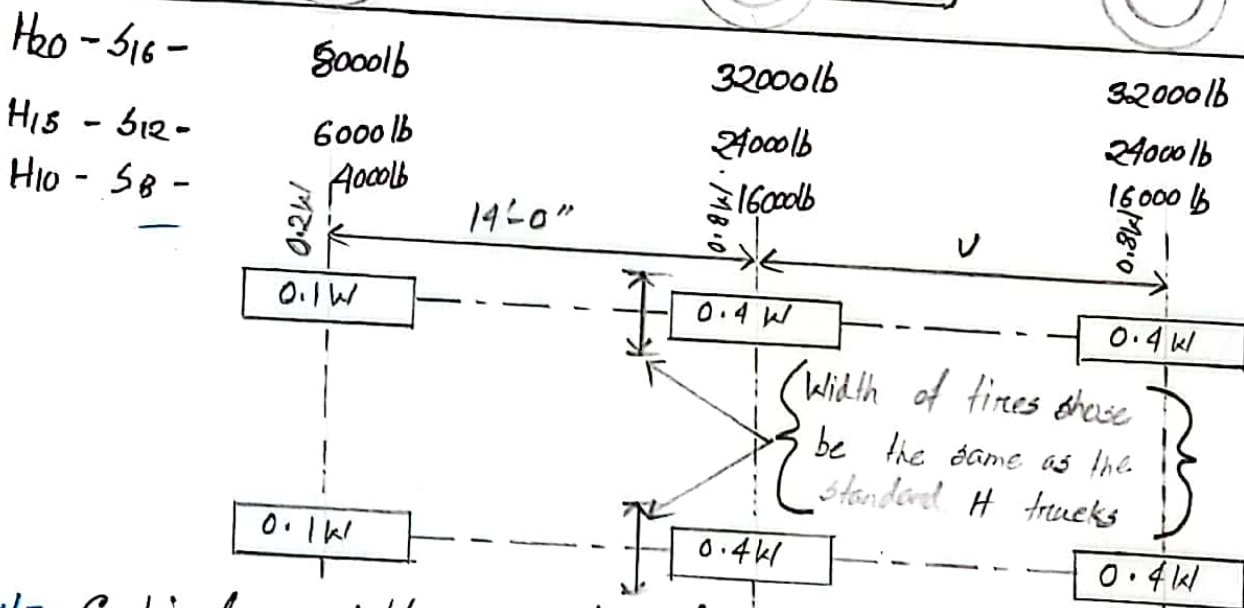
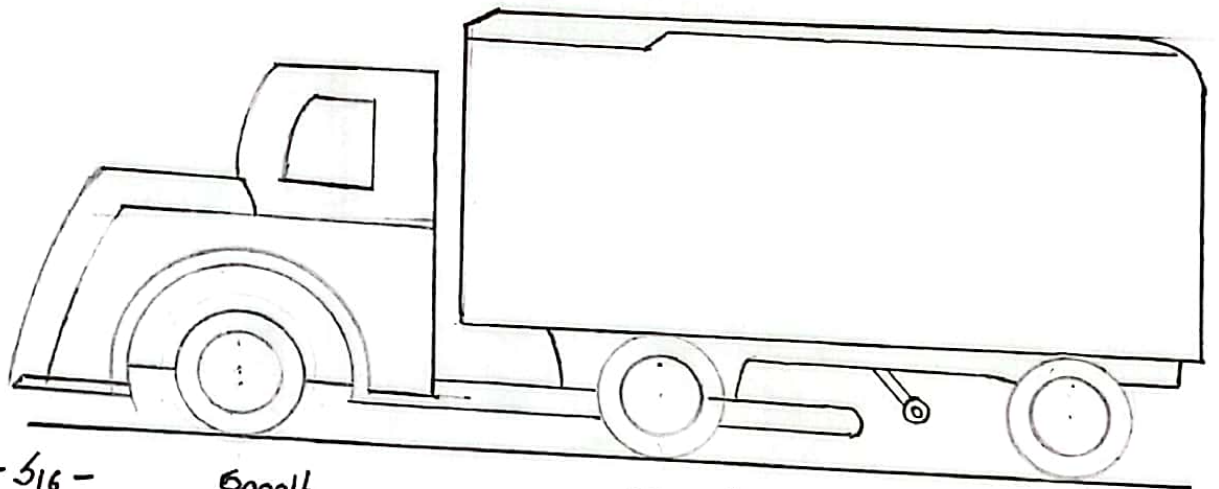
SUBJECT : <i>Reinforced Concrete Slab and T</i>	SUBMITTED BY :
COURSE NO. : <i>CE-3218</i>	NAME : <i>Abu-Shad</i>
DATE OF EXPT. :	CLASS : <i>3rd year even semester</i>
DATE OF SUB. :	GROUP : ROLL NO <i>1800199</i>
	SESSION : <i>2018-19</i>

Heaven's Light is Our Guide
 Department of Civil Engineering
 Rajshahi University of Engineering & Technology

Page

Chapter No: 2.3

Chapter Name: Design of slab.



W = Combined weight on the first two axis which is the same as for the corresponding H truck.

V = V-variable spacing - 14 feet to 30 feet inclusive spacing to be used in that which produces maximum stress.

Figure : Standard H-5 truck.

Heaven's Light is Our Guide
 Department of Civil Engineering
 Rajshahi University of Engineering & Technology

Page

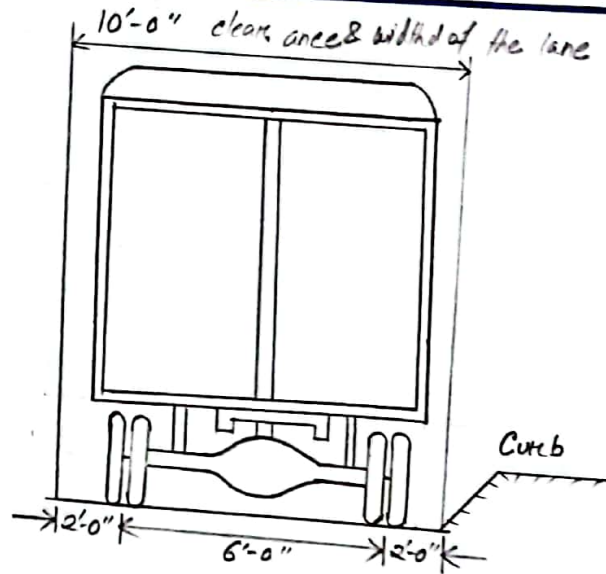
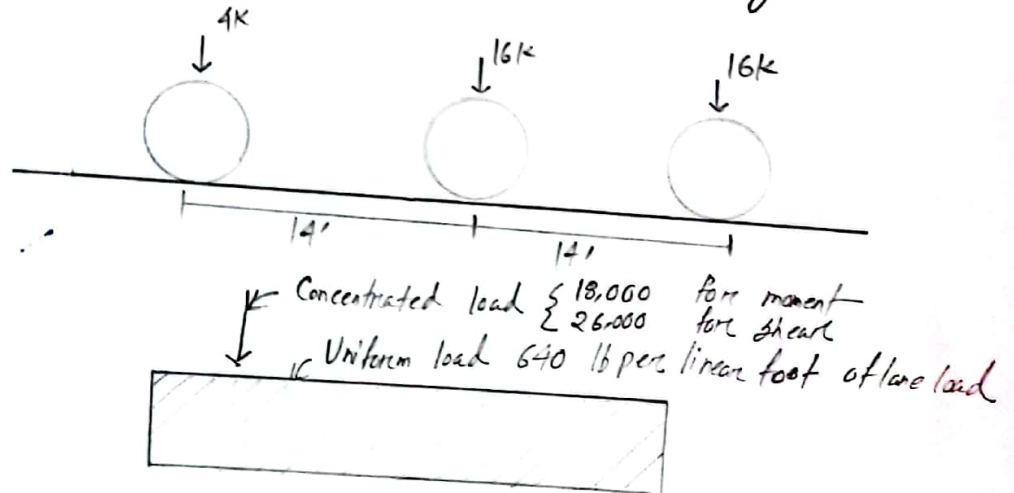


Figure : Standard H-3 truck loading



H₂₀-S₁₆ - 44 Loading

For H₁₅-S₁₂-44 & H₁₀-S₈-44 loading value is 75% & 50% of the H₂₀-S₁₆-44 Loading.

Design of slab:

Design consideration

① Span length:

For simple span, $s = c$ to c distance of support

$$s_{max} = \text{clear distance} + \text{thickness of slab.}$$

② Bending moment:

Case-I: Main reinforcement perpendicular to traffic,

$$\begin{aligned} \text{Live load moment} &= \frac{s+2}{32} P_{20}; \text{ for } H_{20} \\ &= \frac{s+2}{32} P_{15}; \text{ for } H_{15} \end{aligned}$$

Case-II: Main reinforcement parallel to traffic

Distribution of wheel load, $E = 4 + 0.06s$ (ft) $\leq 7.0'$

Maximum live load moment per foot width of slab without impact,

① Span up to including 50; $s \leq 50'$

$$\text{Live load moment} = 900s \text{ lb-ft}$$

Heaven's Light is Our Guide

Department of Civil Engineering
Rajshahi University of Engineering & Technology

Page

(ii) span 50 to 100 ft; $50 < l < 100$

$$\text{live load moment} = 1000 (1.355 - 20) \text{ lb-ft}$$

(3) Distribution reinforcement:

For main reinforcement parallel to traffic,

$$\text{percentage} = \frac{100}{\sqrt{5}} ; \text{maximum} = 50\%$$

For main reinforcement perpendicular to traffic,

$$\text{percentage} = \frac{220}{\sqrt{5}} \quad \text{maximum} = 67\%$$

Span:

Effective span = 19 ft

Thickness of slab = 16" (assume)

Load calculation:

Dead load:

(i) Self weight of slab = $1\frac{1}{2} \times 150 = 200 \text{ psf}$.

(ii) Wearing course = 20 psf

\therefore Total dead load = 220 psf

Analysis of bending moment and shear force:

Dead load moment: $M_D = \frac{wL^2}{8} = \frac{220 \times 19^2}{8} = 9927.5 \text{ lb-ft}$

Reaction = $\frac{wL}{2} = 2090 \text{ K}$

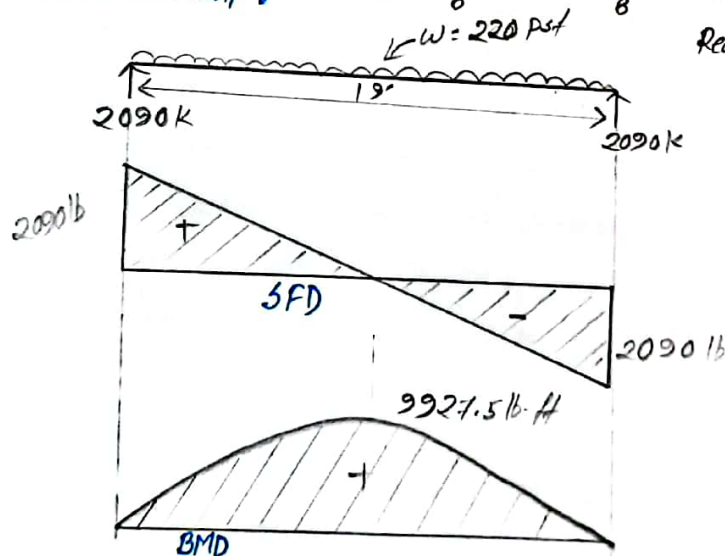


Figure: SFD & BMD

Heaven's Light is Our Guide
Department of Civil Engineering
Rajshahi University of Engineering & Technology

Page

Live load moment :

Load on each rear wheel = 16k

Distribution of wheel loads, $F = 4 + 0.065 \leq 70'$
 $= 5.14' \leq 7'$

Load on per unit width of slab = $P/E = 16/5.14 = 3.11 \text{ k/ft}$

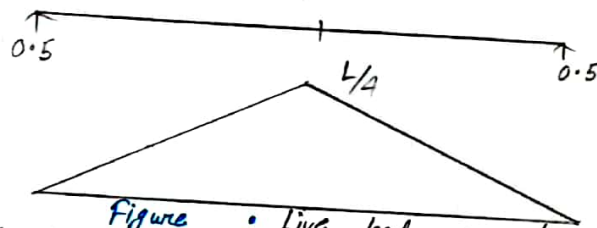


Figure : Live load moment
Live load moment = $P/E \times L/4 = 3.11 \times 10/4 = 14.79 \text{ k-ft}$

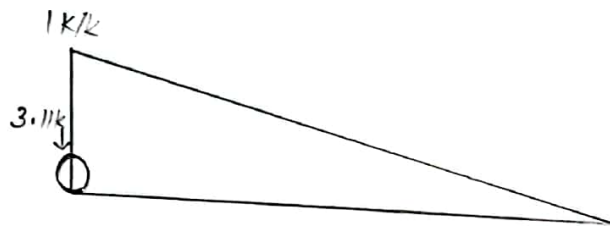


Figure : Live load shear

Live load shear = $3.11 \times 1 = 3.11 \text{ k}$

Impact analysis:

Impact co-efficient for shear, $I_c = \frac{50}{L+25} \leq 0.3$
 $= \frac{50}{19+25} \leq 0.3$

Impact analysis:

= 0.3

$$\begin{aligned}\text{Impact shear force} &= \text{live load shear force} \times I_c \\ &= 3.11 \times 0.3 = 0.933 \text{ K}\end{aligned}$$

$$\begin{aligned}\text{Impact moment} &= \text{Live load moment} \times I_c \\ &= 14.79 \times 0.3 \\ &= 4.437 \text{ K-ft}\end{aligned}$$

Design Value for shear & moment:

$$\begin{aligned}\text{Design shear} &= \text{Dead load shear} + \text{Live load shear} + \text{Impact load shear} \\ &= 2.09 + 3.11 + 0.933 \\ &= 6.13 \text{ K}\end{aligned}$$

$$\begin{aligned}\text{Design moment} &= \text{Dead load moment} + \text{Live load moment} + \text{Impact load moment} \\ &= 9.93 + 14.79 + 4.43 \\ &= 29.15 \text{ K-ft}\end{aligned}$$

Heaven's Light is Our Guide
Department of Civil Engineering
Rajshahi University of Engineering & Technology

Page

Depth check :

$$d_{req} = \sqrt{\frac{M}{R_b}} = \sqrt{\frac{29.15 \times 12000}{256.14 \times 12}} = 10.67''$$

$$d_{eff} = 16'' - 1'' = 15'' > d_{req}$$

∴ OK design

Reinforcement calculation:

$$A_b = \frac{M}{f_s d} = \frac{29.15 \times 12000 \times 1}{24000 \times 0.98 \times 15} = 1.1 \text{ in}^2$$

Use #5 bar @ 3.25" c to c

Distribution reinforcement:

Main reinforcement is parallel to the traffic,

$$\text{percentage} = \frac{100}{\sqrt{3}} = \frac{100}{\sqrt{19}} = 22.94\%$$

$$\therefore \text{Distribution reinforcement} = 0.2294 \times 1.11 = 0.25 \text{ in}^2$$

Use #4 @ 9.5" c to c

Heaven's Light is Our Guide

Department of Civil Engineering
Rajshahi University of Engineering & Technology

Page

Shear check:

$$\text{Allowable shear } V_{all} = 1.1 \sqrt{f_c'} b d = 1.1 \sqrt{3500} \times 12 \times 15$$

$$= 11713.84 \text{ lb}$$

$$= 11.71 \text{ K}$$

$$V_d = \quad = \text{Design shear} = 6.13 \text{ K}$$

\therefore No need of stirrup.

Bond check:

$$U_{dev} = \frac{V}{\sum_o j d} = \frac{6.13 \times 10^3}{\pi \times \frac{4}{8} \times \frac{12}{3.25} \times 0.88 \times 15} = 80 \text{ psi}$$

$$\text{Allowable bond stress, } U_{all} = \frac{6.7 \sqrt{f_c'}}{D} = \frac{6.7 \sqrt{3500}}{4/8} \leq 560$$

$$= 792.75 \leq 560$$

$$= 560$$

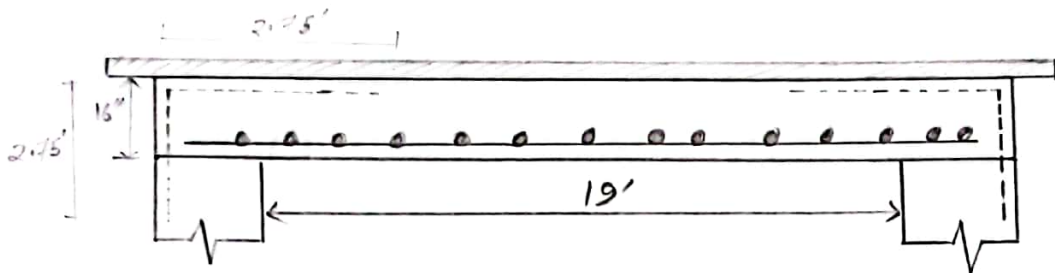
$\therefore U_{dev} < U_{all} \quad \therefore$ Design is OK.

Heaven's Light is Our Guide

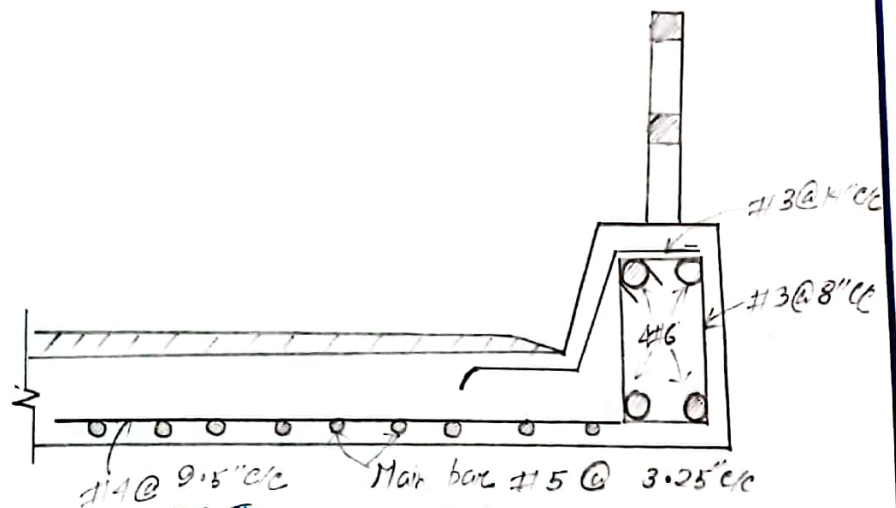
Department of Civil Engineering
Rajshahi University of Engineering & Technology

Page

Working Diagram:



(a) Longitudinal section.



(b) Transverse section.

Figure : Details of slab bridge

Heaven's Light is Our Guide

Rajshahi University of Engineering & Technology
Rajshahi

**DEPARTMENT OF
CIVIL ENGINEERING**

Expt. No. *2.4*

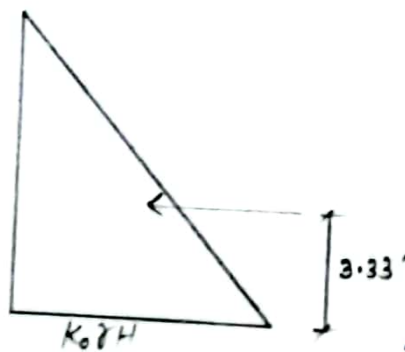
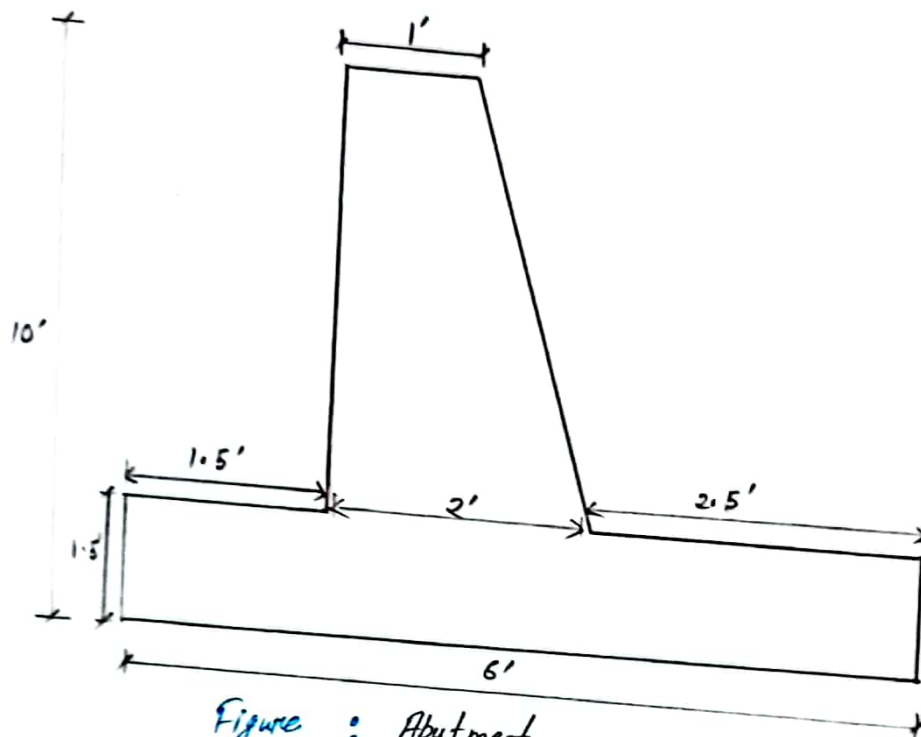
Name of Expt *Design of Abutment Wall*

SUBJECT : <i>Reinforced Concrete Sessional-II</i>	SUBMITTED BY :
COURSE NO. : <i>CE-3218</i>	NAME : <i>Abu-Hasd</i>
DATE OF EXPT.:	CLASS : <i>3rd year even semester</i>
DATE OF SUB. :	GROUP : ROLL NO <i>1800144</i>
	SESSION : <i>2018-19</i>

Heaven's Light is Our Guide
Department of Civil Engineering
Rajshahi University of Engineering & Technology

Page

Chapter No: 2.4
Name of the chapters: Design of Abutment Wall



Forces acting on structure of abutment:

- i) Lateral earth pressure.
- ii) surcharge pressure.
- iii) wheel load.

Failure modes:

- i) External stability.
- ii) Internal stability.

(i) External stability:

(a) Sliding Failure:

Sliding force = Total active pressure acting on abutment

Resistance force = Total friction force acting between concrete and soil at the base of abutment,

$$\text{Factor of abutment} = \frac{\text{Resisting force}}{\text{Sliding force}}$$

[must be > 1.5]

Heaven's Light is Our Guide

Department of Civil Engineering
Rajshahi University of Engineering & Technology

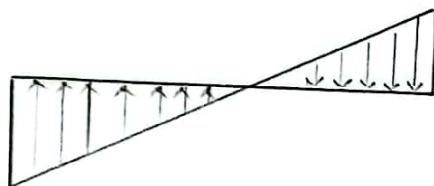
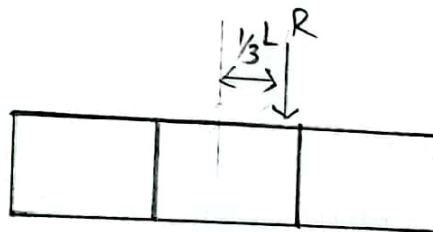
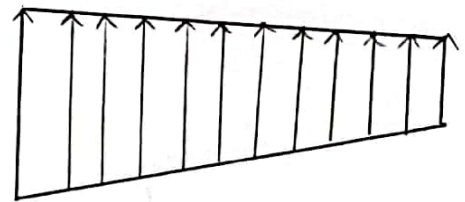
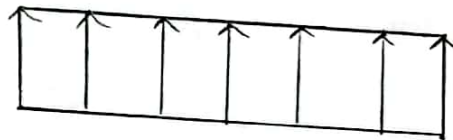
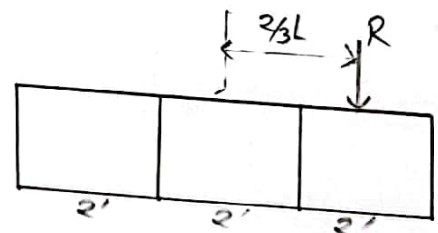
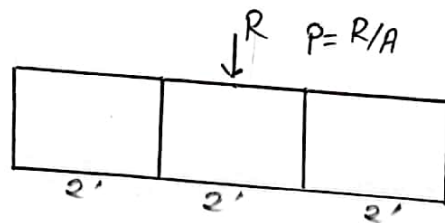
Page

(b) Overturning failure :

Overturning failure = overturning moment.

$$\text{Factor of safety} = \frac{\text{Resisting force}}{\text{Sliding force}}$$

(c) Bearing failure (Inadequacy in soil bearing capacity)
We have to consider a strip \rightarrow



Heaven's Light is Our Guide

Department of Civil Engineering
Rajshahi University of Engineering & Technology

Page

Retaining wall :

Types of retaining wall \rightarrow

- (i) Gravity retaining wall.
- (ii) Cantilever retaining wall.

Factors controlling height of abutment :

- i) Height of flood level.
- ii) Free board.
- iii) Scour depth.

Specification :

- (i) Height of the abutment = 10'.
- (ii) Allowable soil pressure = 3 ksf.
- (iii) Unit weight of soil = 120 pcf.
- (iv) Angle of internal friction, $\phi = 30^\circ$.
- (v) Minimum factor of safety = 1.5.
- (vi) Friction co-efficient $f = 0.5$.

Heaven's Light is Our Guide

Department of Civil Engineering
Rajshahi University of Engineering & Technology

Page

$$K_a = \frac{1 - \sin \phi}{1 + \sin \phi} = \frac{1 - \sin 30^\circ}{1 + \sin 30^\circ} = 0.33$$

$$K_p = \frac{1 + \sin \phi}{1 - \sin \phi} = 3$$

$$K_a \times H = 0.33 \times 120 \times 10 = 396 \text{ psf.}$$

$$\text{Total active pressure} = \frac{1}{2} \times 396 \times 10 = 1980 \text{ lb.}$$

$$\text{Overturning moment} = P_o \times H/3 = 1980 \times 10/3 = 6600 \text{ lb-ft.}$$

Considering 1' strip \rightarrow

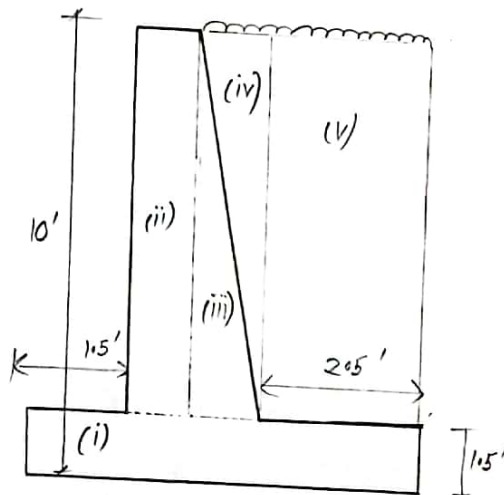


Figure : section for calculating resisting moment...

Heaven's Light is Our Guide
 Department of Civil Engineering
 Rajshahi University of Engineering & Technology

Page

Total weight and resisting moment

Case-I

Section	Weight (lb)	Moment arm (lb-ft)	Resisting moment (lb-ft)
i	1.5 x 6 x 150	3	4050
ii	8.5 x 150 x 1	1.5 + 0.5	2550
iii	1/2 x 1 x 8.5 x 150	2.5 + (1 x 1/2)	1804.125
iv	1/2 x 1 x 8.5 x 120	1.5 + 1 + 2/3	1615
v	2.5 x 8.5 x 120	3.5 + (2.5 x 1/2)	12,112.5
Total	= 63220.5		22,131.62

Case-II

Dead Load	Load = 2420 lb Total weight = 87425 lb	Live arm = 2'	moment = 4840 lb-ft Total moment = 26971.6 lb-ft
-----------	---	---------------	---

Case-III

Live Load	Load = 3000 Total weight = 117425	Live arm = 2'	moment = 6000 Total moment = 329716 lb-ft
-----------	--------------------------------------	---------------	--

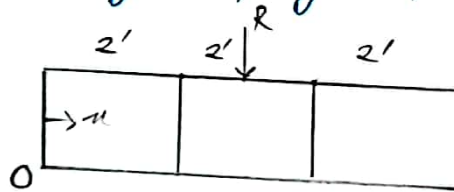
Stability Check:

Case - I: Case structure is dead,

$$\begin{aligned} \text{Factor of safety against sliding} &= \frac{W \times f}{P_u} \\ &= \frac{6322.5 \times 0.5}{1980} \\ &= 1.6 > 1.5 \quad (\text{OK}) \end{aligned}$$

$$\begin{aligned} \text{Factor of safety against sliding of overturning} \\ &= \frac{22131.62}{6600} = 3.3 > 1.5 \quad (\text{OK}) \end{aligned}$$

Check for bearing capacity of soil:



location of resultant from O,

$$\bar{X} = \frac{M_R - M_0}{W} = \frac{22131.6 - 66000}{6322.5} = 2.96'$$

$$e = h/2 = 6/2 = 3'$$

$$e = h/2 - \bar{x}$$

$$= 3 - 2.96$$

$$= 0.04$$

$$M = W \times e$$

$$= 6322.5 \times 0.04$$

$$= 3414.15 \text{ lb-ft}$$

Heaven's Light is Our Guide

Department of Civil Engineering
Rajshahi University of Engineering & Technology

Page

$$\sigma = P/A + MC/I$$

$$= \frac{6322.5}{6 \times 1} + \frac{3414 \cdot 15 \times 3}{18}$$

$$= 1622.78 \text{ psf} < 3000 \text{ psf (allowable)}$$

$$I = \frac{bh^3}{12} = \frac{6 \times 6^3}{12}$$
$$= 18$$

or $\sigma = P/A - MC/I$

$$= \frac{6322.5}{6 \times 1} - \frac{3414 \cdot 15 \times 3}{18}$$

$$= 489.72 \text{ psf} < 3000 \text{ psf (allowable)}$$

Case-II

super structure is present but no live load, on
super structure -

$$\text{Factor of safety against overturning} = M_R/M_o = \frac{26971.6}{6600}$$
$$= 4.01 > 1.5 \text{ (OK)}$$

$$\text{Factor of safety against sliding} = \frac{W_f \times 0.5}{1980}$$
$$= \frac{8742.5 \times 0.5}{1980}$$
$$= 2.2 > 1.5$$

(OK)

Heaven's Light is Our Guide
Department of Civil Engineering
Rajshahi University of Engineering & Technology

Page

Case -111

Superstructure is present with live load on the
superstructure -

$$\begin{aligned}\text{Factor of safety against overturning} &= M_F/M_o \\ &= \frac{32971.6}{6600} = 5 > 1.5 \\ &\quad \text{(ok)}\end{aligned}$$

$$\begin{aligned}\text{Factor of safety against sliding} &= \frac{W_F \times 0.5}{1980} \\ &= 2.97 > 1.5 \\ &\quad \text{(ok)}\end{aligned}$$

Heaven's Light is Our Guide

Department of Civil Engineering
Rajshahi University of Engineering & Technology

Page

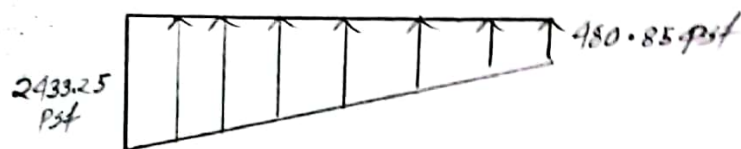
Case-II :

$$\bar{x} = \frac{M_R - M_0}{W} = \frac{26971.6 - 6600}{8742.5} = 2.33'$$

$$\therefore e = \frac{h}{2} - \bar{x} = \frac{6}{2} - 2.33 = 0.67'$$

$$\therefore M = We = 5857.5 \text{ lb-ft}$$

$$\therefore \sigma = \frac{8742.6}{6 \times 1} \pm \frac{5857.5 \times 3}{18} = (2433.25 \text{ \& } 980.85) \text{ psf}$$



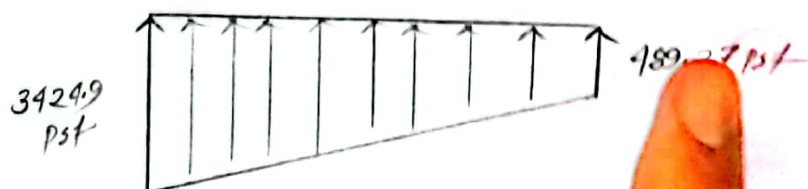
Case-III :

$$\bar{x} = \frac{M_R - M_0}{kI} = \frac{32971.6 - 6600}{11742.5} = 2.25'$$

$$\therefore e = \frac{h}{2} - \bar{x} = \frac{6}{2} - 2.25 = 0.75'$$

$$\therefore M = we = 8806.87 \text{ lb-ft}$$

$$\therefore \sigma = \frac{11742.05}{6 \times 1} \pm \frac{8806.87 \times 3}{18} = (3124.9 \text{ \& } 189.27) \text{ psf}$$



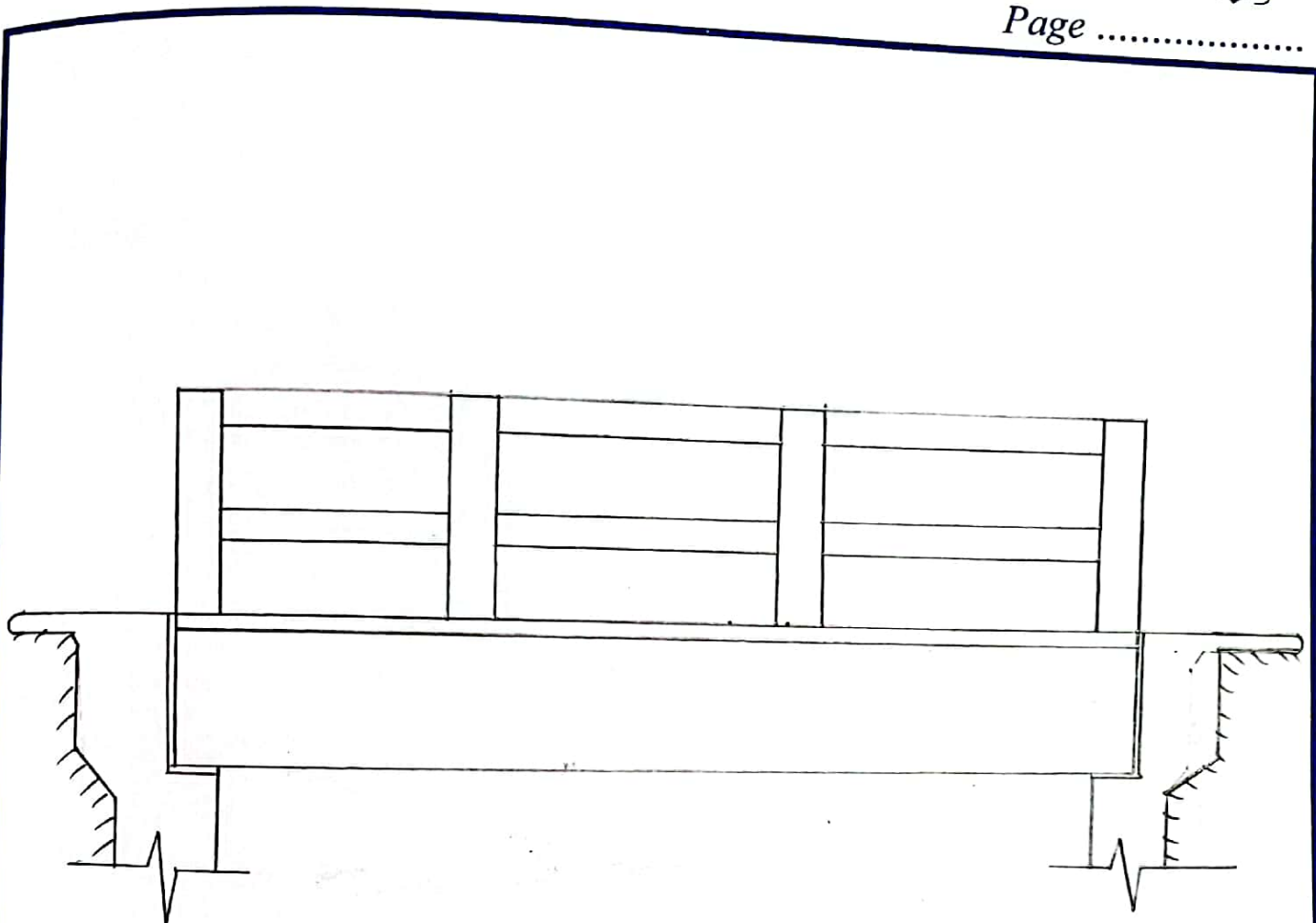


Figure: Bridge Profile

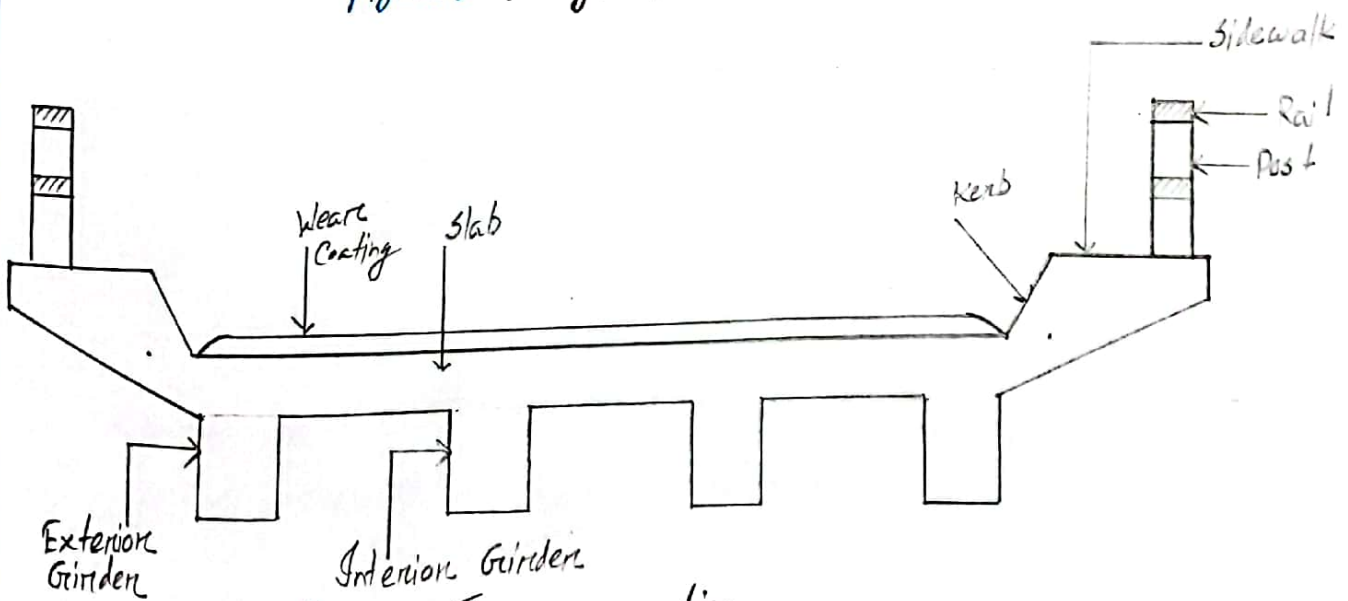


Figure: Transverse section
Plate Girder Bridge

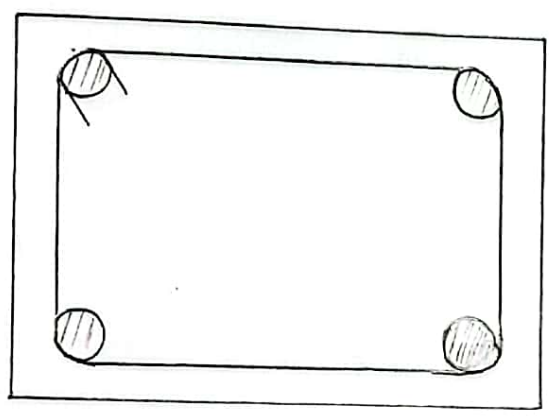
Heaven's Light is Our Guide

Department of Civil Engineering
Rajshahi University of Engineering & Technology

Page

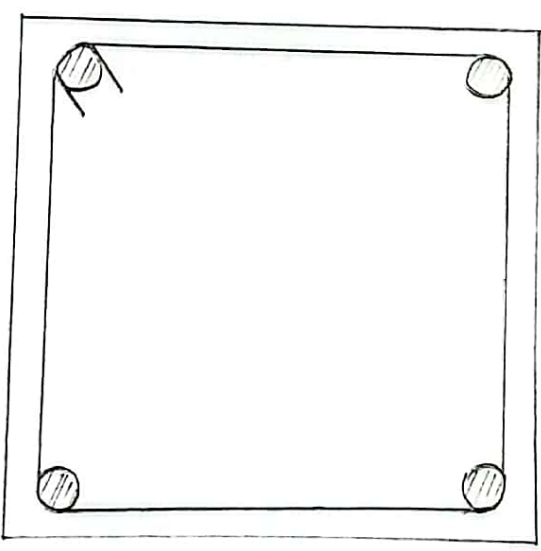
Reinforcement detail of Rail & Post:

Rail:



Description: (6x6)" with 4#5 bar

Post:



Description: (8x8)" with 4#5 bar

Heaven's Light is Our Guide

Department of Civil Engineering
Rajshahi University of Engineering & Technology

Page

Design specification:

- (i) Clear span length = last 2 digit of roll + $50/3$
 $= 44 + 50/3$
 $= 60.67'$
- (ii) Width of the bridge = equivalent two lanes = $20'$
- (iii) No of girders = 4
- (iv) Loading \rightarrow HS 20 truck load.
- (v) Material properties, $f_c' = 3000$ psi, $f_y = 50,000$ psi.
- (vi) Width of girder = $15''$
- (vii) Height of wearing course = 20 psf

Design Calculations:

$$\text{Center to center spacing of girders} = \frac{20}{4-1} = 6.67'$$

$$\text{Clear spacing between two girders} = (6.67 - 15/12) = 5.92'$$

Relevant Properties:

$$n = 9, \quad r = 14.81,$$

$$k = 0.38, \quad j = 0.87$$

$$R = 223.16 \text{ psi}$$

Heaven's Light is Our Guide

Department of Civil Engineering
Rajshahi University of Engineering & Technology

Page

Design for slab:

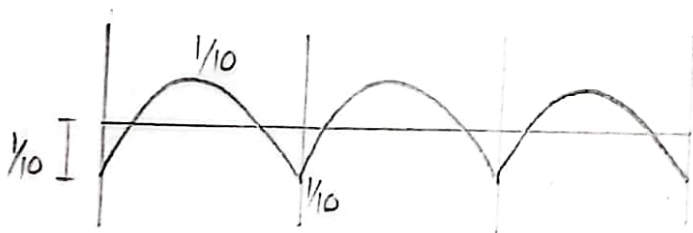
Assume the thickness of slab $t = 6''$

Dead load moment:

$$\text{Self weight} = \frac{1}{12} \times 150 = 75 \text{ psf}$$

$$\text{weight of wearing course coat} = 20 \text{ psf}$$

$$\therefore \text{Total dead load } w = (75 + 20) = 95 \text{ psf}$$



$$\text{Dead load moment } M_0 = \frac{wL^2}{10} = \frac{1}{10} \times 95 \times 5.42^2 = 279.07 \text{ lb-ft}$$

Live Load Moment:

For main reinforcement perpendicular to traffic:

$$M_{LL} = \frac{5+2}{32} \times 1.5 = \frac{5.42+2}{32} \times 2000 = 278.25 \text{ lb-ft}$$

Heaven's Light is Our Guide

Department of Civil Engineering
Rajshahi University of Engineering & Technology

Page

Impact Moment:

$$I = \frac{50}{L + 125} \leq 0.3$$

$$= \frac{50}{5.42 + 125} = 0.38 \leq 0.3$$

\therefore 30% of Live moment

$$\therefore M_I = 0.3 \times M_{LL} = (0.3 \times 2782.5) = 834.75 \text{ lb-ft}$$

\therefore Design moment:

$$\begin{aligned} M_D &= M_D + M_{LL} + M_I \\ &= 279.07 + 2782.5 + 834.75 \\ &= 3896.32 \text{ lb-ft} \end{aligned}$$

Depth check:

$$d_{req} = \sqrt{\frac{M}{R_b}} = \sqrt{\frac{3896.32 \times 12}{223.16 \times 12}} = 4.18''$$

$$d_{act} = 6'' - 1'' = 5''$$

$$d_{act} > d_{req}$$

So, that design is ok

Heaven's Light is Our Guide

Department of Civil Engineering
Rajshahi University of Engineering & Technology

Page

Main reinforcement calculation:

$$A_s = \frac{M}{f_s j d} = \frac{3896.32 \times 12}{20,000 \times 0.875} = 0.53 \text{ in}^2$$

$$\begin{aligned} \text{spacing} &= \frac{0.31 \times 12}{0.53} \\ &= 7.02 \approx 7'' \text{ c/c} \end{aligned}$$

Use #5 bars @ 7" c/c

Distribution reinforcement calculation:

For main reinforcement perpendicular to traffic,

$$\begin{aligned} A_{st} &= \frac{220}{\sqrt{S}} \leq 67\% \text{ of main reinforcement,} \\ &= \frac{220}{15.92} = 94.49 \leq 67\% \end{aligned}$$

$$\therefore A_{st} = 0.67 \times 0.53 = 0.36 \text{ in}^2$$

$$\text{Use \# 4 @ } \frac{0.2 \times 12}{0.36} = 6.63 \approx 6.5'' \text{ c/c}$$

Shear check:

$$\text{Dead load shear } V_{\max} = \frac{wL}{2} = 257.45 \text{ lb/ft}$$

$$\begin{aligned} \text{Live load on per unit width of slab} &= \frac{P}{L} = \frac{12000}{4 + 0.06 \times L} \\ &= \frac{12000}{4 + 0.06 \times 60.67} \end{aligned}$$

$$\begin{aligned} \therefore \text{Impact shear} &= 1570.69 \frac{\text{lb}}{\text{ft}} \\ &= 471.2 \text{ lb/ft} \end{aligned}$$

Heaven's Light is Our Guide

Department of Civil Engineering
Rajshahi University of Engineering & Technology

Page

$$\therefore V_d = \frac{257.45 + 1570.64 + 47.12}{bd \times (1 \times 12)} = \frac{2299.28}{12 \times 12 \times 5}$$

cause in 1H strip $= 3.19 \text{ psi}$

$$V_{all} = 1.1 \sqrt{f_{e'}} = 1.1 \sqrt{3000} = 60.2 \text{ psi}$$

$$\therefore V_d < V_{all}$$

No need stirrup.

Band check:

$$V_d = \frac{V_{max}}{\phi_o J D} = \frac{V_{max}}{\pi \times \frac{12}{\text{spacing}} \times d_b \times 0.87 \times 5}$$
$$= \frac{257.45}{\pi \times \frac{12}{7} \times \frac{5}{8} \times 0.87 \times 5}$$
$$= 17.58 \text{ psi}$$

$$V_{all} = \frac{1.7 \sqrt{f_{e'}}}{D} = \frac{1.7 \sqrt{3000}}{5/8} = 148.98$$

$\therefore V_{all} > V_d$ The design is ok

Heaven's Light is Our Guide

Department of Civil Engineering
Rajshahi University of Engineering & Technology

Page

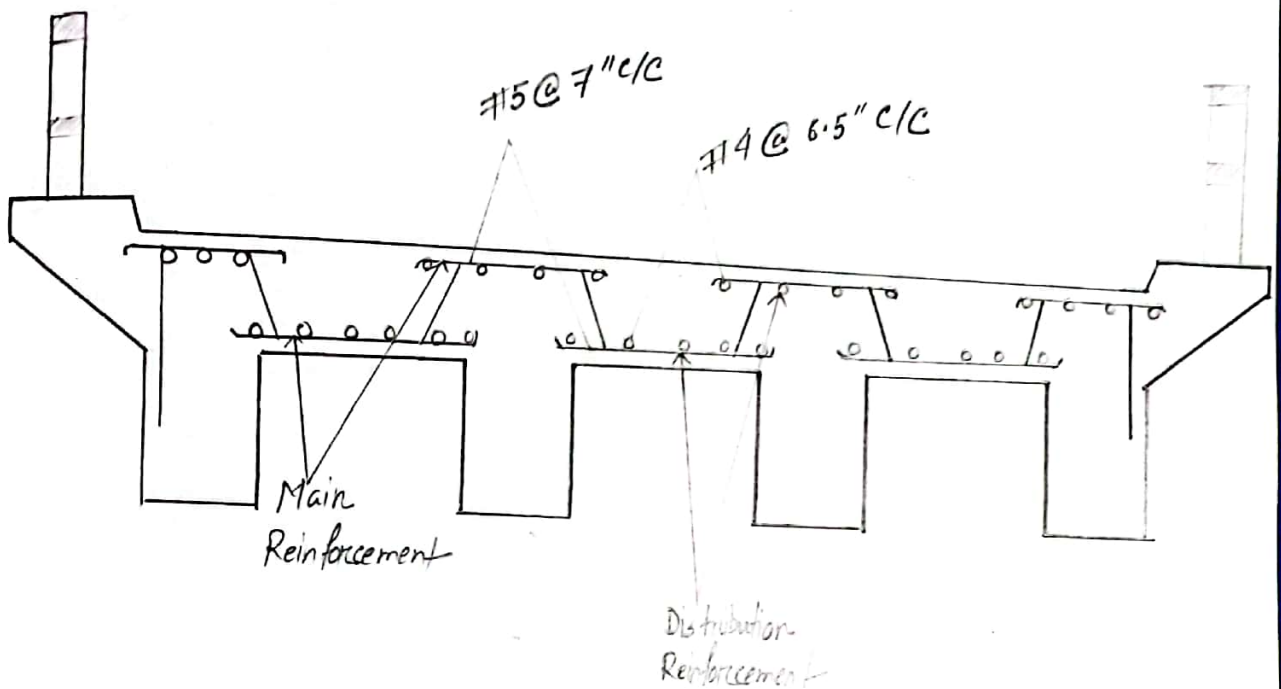
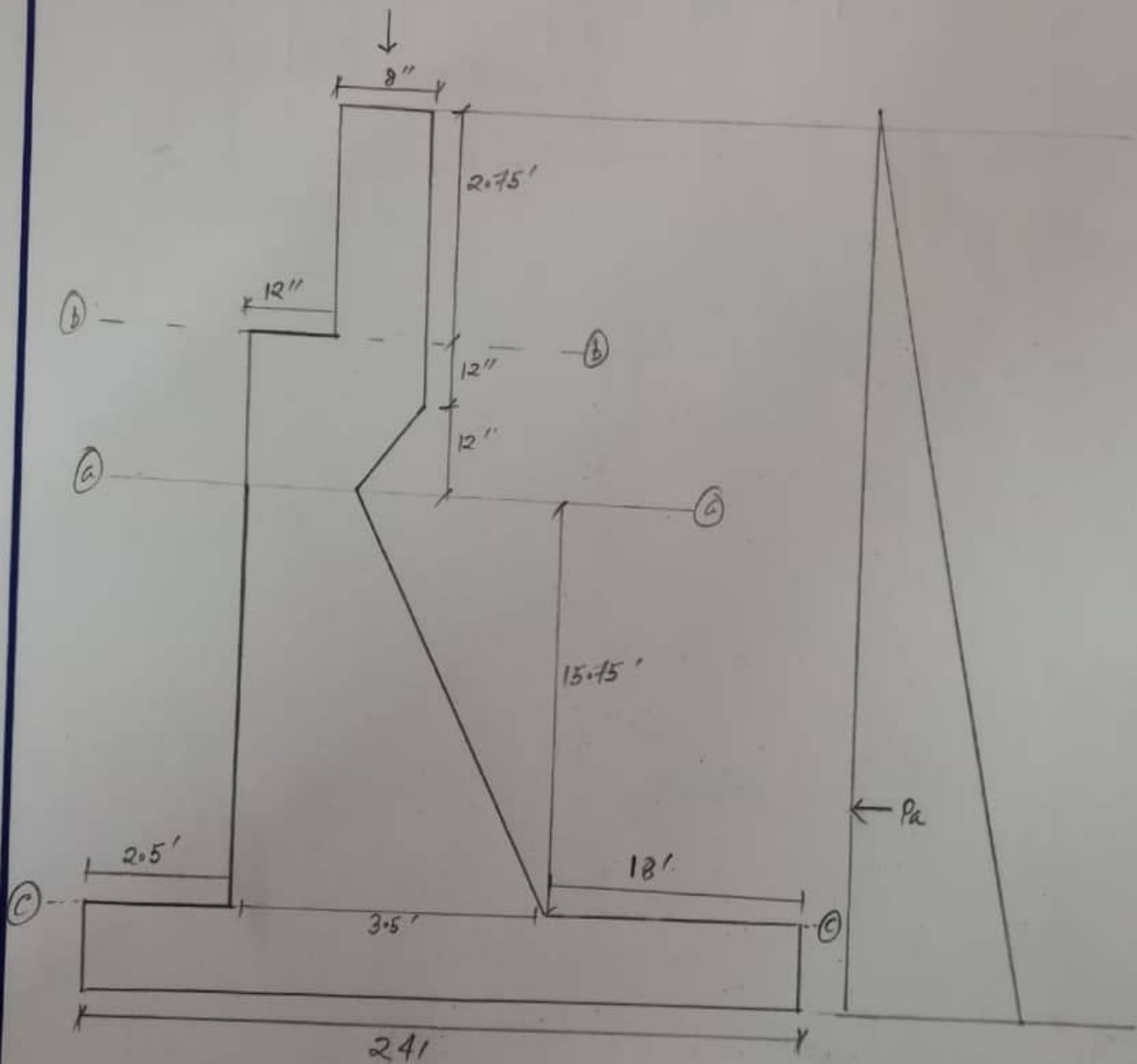


Figure: Typical reinforcement details of deck slab.

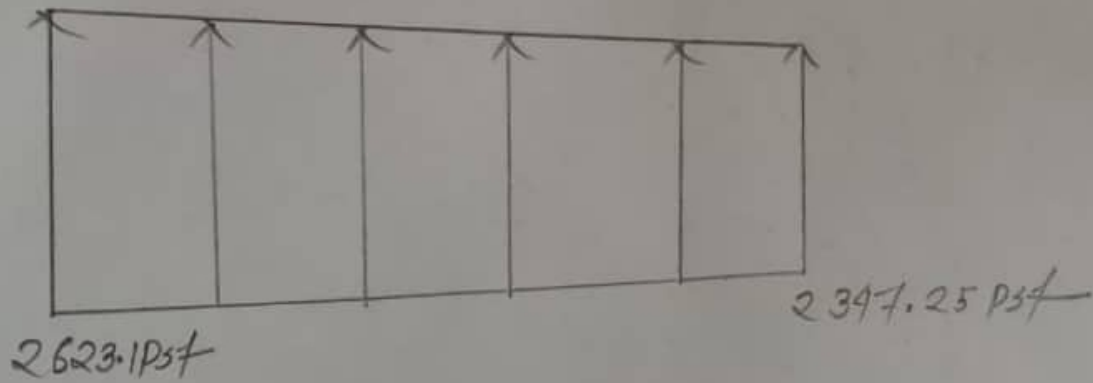
Design of Back fill:



Heaven's Light is Our Guide

Department of Civil Engineering
Rajshahi University of Engineering & Technology

Page



Design of abutment for Deck Girder Bridge:

Design specification:

- 1/ Overall height of the abutment = 22'
- 2/ Bearing capacity of soil = 4 ksf
- 3/ Unit weight of soil = 120 pcf
- 4/ Angle of internal friction, $\phi = 30^\circ$
- 5/ Co-efficient of friction, $f = 0.5$
- 6/ $f_c' = 3,000$ psi, $f_y = 50,000$ psi

Active earth pressure co-efficient, $K_a = \frac{1 - \sin \phi}{1 + \sin \phi} = \frac{1 - \sin(30^\circ)}{1 + \sin(30^\circ)}$
 $= \frac{1}{3}$

Passive earth pressure co-efficient, $K_p = \frac{1}{K_a} = 3$

Now, $P_a = \frac{1}{2} \times K_a \gamma_s H \times H = \frac{1}{2} \times \frac{1}{3} \times 120 \times (22)^2 = 9670.32 \text{ lb}$

\therefore Active earth pressure, $P_a = 9670.32 \text{ lb}$

\therefore Overturning moment, $M_o = P_a \times H/3 = 9670.32 \times \frac{22}{3}$
 $= 70915.68 \text{ lb-ft}$

Table: Calculation for total load, weight & resisting moment.

Section	Weight (lb)	Moment-arm (ft)	Moment (lb-ft)
1.	$24 \times 2 \times 150 = 7200$	$24/2 = 12$	86400
2.	$15.25 \times 1 \times 150 = 2287.5$	$2.5 + 0.5 = 3$	6862.5
3.	$1 \times 29/2 \times 150 = 250$	$2.5 + 0.833 = 3.33$	833.33
4.	$1 \times 1 \times 150 = 150$	$2.5 + 0.5 = 3$	450
5.	$2.75 \times 8/2 \times 150 = 275$	$2.5 + 1 + 0.33 = 3.833$	1054.075
6.	$1/2 \times 8/2 \times 1 \times 120 = 90$	$2.5 + 1 + 2/3 \times 8/2 = 3.99$	157.77
7.	$1/2 \times 8/2 \times 1 \times 150 = 50$	$2.5 + 1 + 1/3 \times 8/2 = 3.72$	186.11
8.	$1/2 \times 2.5 \times 15.25 \times 120 = 2287.5$	$2.5 + 1 + 2/3 \times 0.5 = 3.17$	11818.75
9.	$18 \times 15.25 \times 120 = 32940$	15	494100
10.	$4.75 \times 19.833 \times 120 = 11304.8$	14.08	159171.72
11.	$1/2 \times 2.5 \times 15.25 \times 150 = 2859.375$	4.333	12390.625
Total	$\text{klf} = 59644.175$	EMR	773424.88

Condition - 1: When superstructure is absent

$$M_{a-a} = \frac{1}{2} K_a \times \gamma \times h_a \times h_a \times \frac{h_a}{3}$$

$$= \frac{1}{2} \times 0.333 \times 120 \times \frac{(4.75)^3}{3} = 713.76 \text{ lb-ft}$$

$$M_{b-b} = \frac{1}{2} \times K_a \times \gamma \times h_b \times h_b \times \frac{h_b}{3} = \frac{1}{3} \times 0.333 \times 120 \times \frac{2.75^3}{3}$$

$$= 138.50 \text{ lb-ft}$$

Depth check:

For section a-a; $d = \sqrt{\frac{M_{a-a} \times 12}{R \times b}}$

$$= \sqrt{\frac{713.76 \times 12}{223.16 \times 12}}$$

$$= 1.8''$$

$$d_{eff} = 1 - 1 - \frac{5}{8} \times 2 = 12'' - 1'' - \frac{5''}{8 \times 2} = 10.69'' > d$$

$\therefore d_{eff} > d$

\therefore Check is okay.

For section (b-b)

$$d = \sqrt{\frac{M_{b-b}}{R \times b}} = \sqrt{\frac{138.50 \times 12}{223.16 \times 12}} = 0.8''$$

$$\therefore d_{eff} = 18 - 1 - \frac{5}{8} \times 2 = 16.69'' > d$$

\therefore Design is okay.

Stability Check:

Factor of safety (Fs) against sliding = $\frac{W_f \times f}{P_a}$

$$= \frac{59644.175 \times 0.5}{9670.32}$$

$$= 3.1 > 1.5$$

(okay)

Factor of safety against overturning = $\frac{M_R}{M_o} = \frac{773424.88}{76915.68}$

$$= 10.9 > 1.5$$

(okay)

Check for soil pressure:

We know, $\sigma = W_f/A \pm Mc/I$

Here, $A = 24 \times 1 = 24 \text{ ft}^2$; $I = \frac{1 \times 24^3}{12} = 1152 \text{ ft}^4$; $c = B/2 = 24/2 = 12'$

$$e = c - a = c - \frac{M_R - M_o}{W_f} = 0.222$$

$$\therefore M = W_f \times e = 59644.175 \times 0.222 = 13241 \text{ lb-ft}$$

$$\therefore \sigma_1 = \frac{59644.175}{24} + \frac{13241 \times 12}{1152} = 2623.1 \text{ psf} < 4000 \text{ psf}$$

$$\sigma_2 = \frac{59644.175}{24} - \frac{13241 \times 12}{1152} = 2347.25 \text{ psf} < 4000 \text{ psf}$$

Bond check:

$$V_d = \frac{V}{\sum j d} = \frac{66.37 \times 1000}{\pi \times \frac{9}{8} \times \frac{12}{16} \times 87 \times 90} = 3.37 \text{ K si}$$

$$V_{all} = 0.1 f_c' = 300 \text{ ksi} > V_d$$

\therefore Bond check OK.

Design of base:

Moment with respect to base,

$$M = 1/2 \times K_e \times \gamma_s \times \frac{H^3}{3} = 1/2 \times 0.333 \times 120 \times \frac{20^3}{3} = 52800 \text{ lb-ft}$$

Depth check:

$$d = \sqrt{\frac{M}{R_b}} = \sqrt{\frac{52800 \times 12}{223 \times 12}} = 15.4''$$

$$d_{\text{act}} = 168'' = 1.5' = 166.5'' > d$$

Reinforcement calculation:

$$A_s = \frac{52800 \times 12}{20,000 \times 0.87 \times 166.5} = 2.18 \text{ in}^2$$

$$\text{but } A_s(\text{min}) = 0.002bt = 0.002 \times 12 \times 168 = 4.032 \text{ in}^2$$

$$\therefore A_s = 4.032 \text{ in}^2$$

(i) Spacing, $s = \frac{12 \times 0.6}{4.032} = 1.78''$

(ii) s_{max} , $s = 3t = 3 \times 168 = 504''$

(iii) $s_{\text{max}} = 18''$

\therefore Using #7 bars @ 1.5" C/C

Department of Civil Engineering
Rajshahi University of Engineering & Technology

Page

Reinforcement Calculation:

$$\text{At section @ -@, } A_{s(a-a)} = \frac{M_{a-a}}{f_{st}d} = \frac{713.76 \times 12}{20,000 \times 0.87 \times 10.69} = 0.65 \text{ in}^2$$

Minimum reinforcement, $A_{smin} = 0.002bt$
 $= 0.002 \times 12 \times 12$
 $= 0.288 \text{ in}^2$

Spacing, $s = \frac{12 \times 0.2}{0.288} = 8.33 \approx 8" \text{ c/c}$

$s_{max} = 3t = 3 \times 8 = 24"$

$s_{max} = 18"$

∴ Using # 4 bar @ 8" c/c

For distribution reinforcement,

$$A_{st} = 0.002bt = 0.288 \text{ in}^2$$

∴ Using # 4 bar @ 8" c/c

At section b-b,

$$A_{s(b-b)} = \frac{M_{b-b}}{f_{st}d} = \frac{138.50 \times 12}{20,000 \times 0.87 \times 16.69} = 0.006 \text{ in}^2$$

but, minimum steel $A_s = 0.002 \times bt = 0.002 \times 12 \times 18 = 0.432 \text{ in}^2$

∴ Using # 4 bar @ spacing, $s = \frac{12 \times 0.2}{0.432} = 5.55 \approx 5" \text{ c/c}$

Distribution, $A_{st} = 0.432 \text{ in}^2$
 Use # 4 @ 5" c/c

Design of stem:

$$M_{c-c} = \frac{1}{2} \times k_a \times \gamma \times h_c \times h_c \times h_c^2$$

$$= \frac{1}{2} \times 0.933 \times 120 \times (18)^3 / 3 = 38841.12 \text{ lb-ft}$$

$$V_{c-c} = \frac{1}{2} \times 0.933 \times 120 \times (18)^2 = 6473.52 \text{ lb}$$

Depth Check:

$$d_{c-c} = \sqrt{\frac{M_{c-c}}{R \times b}} = \sqrt{\frac{38841.12 \times 12}{220.16 \times 12}} = 13.93''$$

$$\therefore d_{eff} = 42'' - 1.5'' = 40.5'' > d_{c-c}$$

\therefore Check is okay.

Reinforcement Calculation:

$$\text{At section c-c, } A_{s(c-c)} = \frac{M_{c-c}}{f_s d} = \frac{38841.12 \times 12}{20,000 \times 0.87 \times 40.5} = 0.66 \text{ in}^2$$

$$A_s \text{ min} = 0.0018 \text{ bf} = 0.0018 \times 12 \times 42 = 1.008$$

$$(i) \text{ spacing, } s = \frac{12 \times 0.44}{1.008} = 5.5''$$

Use #6 bar.

$$(ii) s_{max}, \text{ bf} = 3 \times 42 = 126''$$

$$(iii) s_{max} = 18''$$

\therefore Using #6 bar @ 5" c/c.

Shear check:

$$V_{all} = 1.1 \sqrt{f_c'} b d = 1.1 \sqrt{3000} \times 12 \times 40.5$$
$$= 29281.24 > V_{c-e}$$

∴ Check is okay.

Development length: Here,

$$u_d = \frac{V}{\phi_s f_A}$$
$$= \frac{6473.52}{\pi \times \frac{6}{8} \times 12/5 \times 0.87 \times 40.5}$$
$$= 32.5 \text{ psi}$$

$$\therefore L_d = \frac{f_s D}{4 u_d} = \frac{20,000 \times 6/8}{4 \times 32.5} = 115.38$$

∴ Minimum development length $L_{dmin} = 12D = 12 \times 6/8$
 $= 9"$

∴ Design is okay.