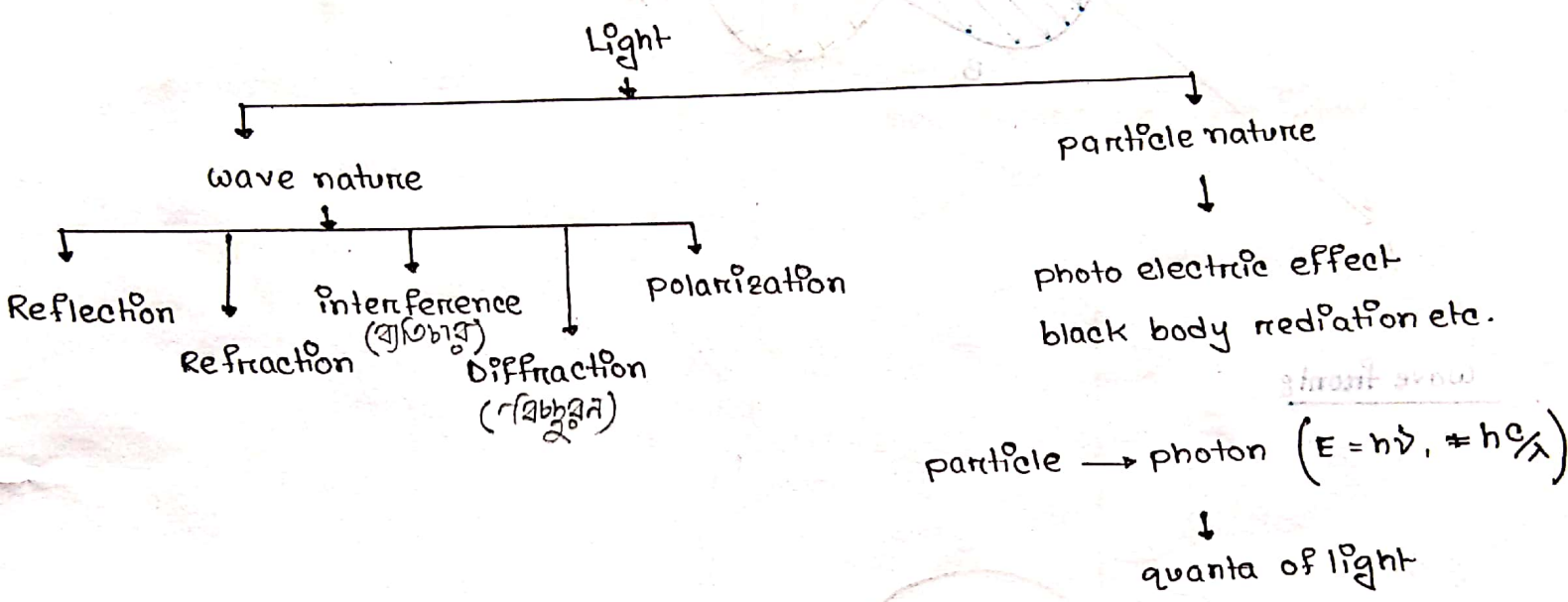
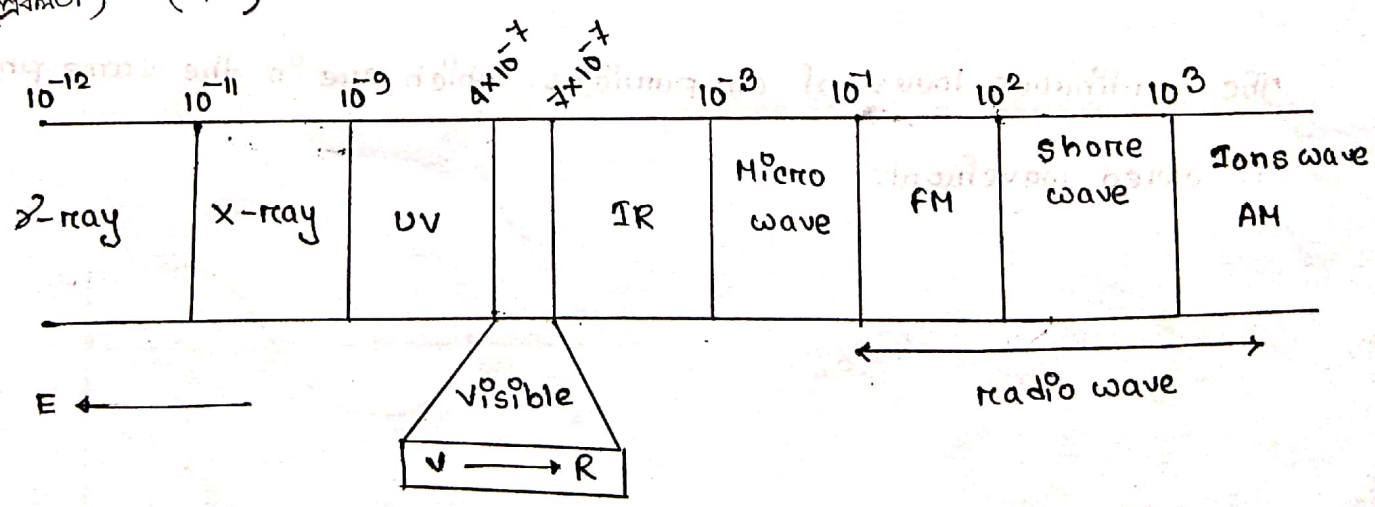
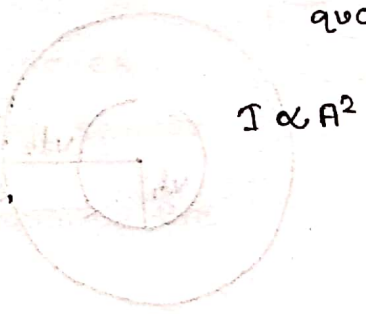


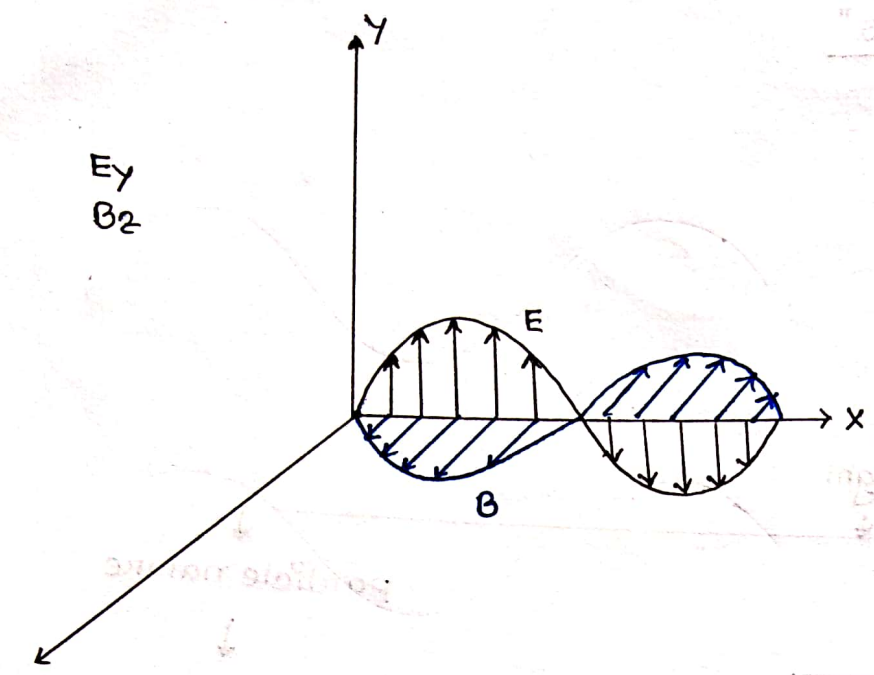
PHYSICS
"Optics"

light → wave-particle duality
→ electromagnetic wave

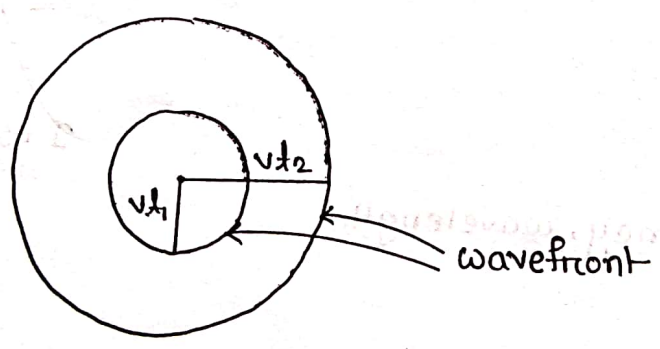


wave → amplitude, frequency, wavelength, (বৈশিষ্ট্য)
Intensity, phase. (প্রবলতা) (মাত্রা)



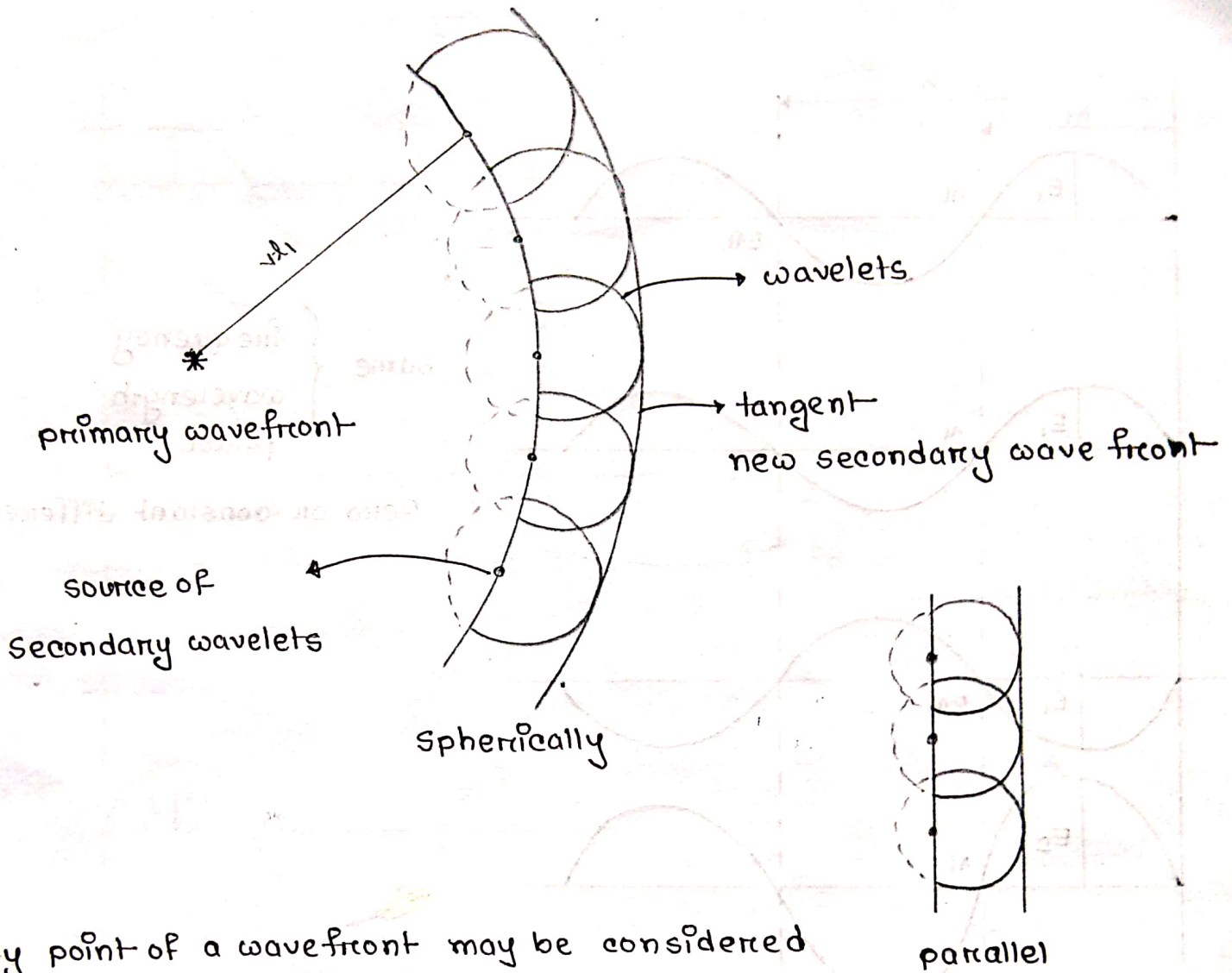


Wave fronts



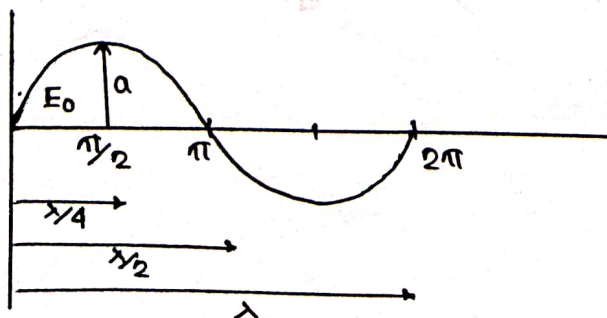
The continuous locus of all particles, which are in the same phase, is called wavefront.

Huygen's principle:



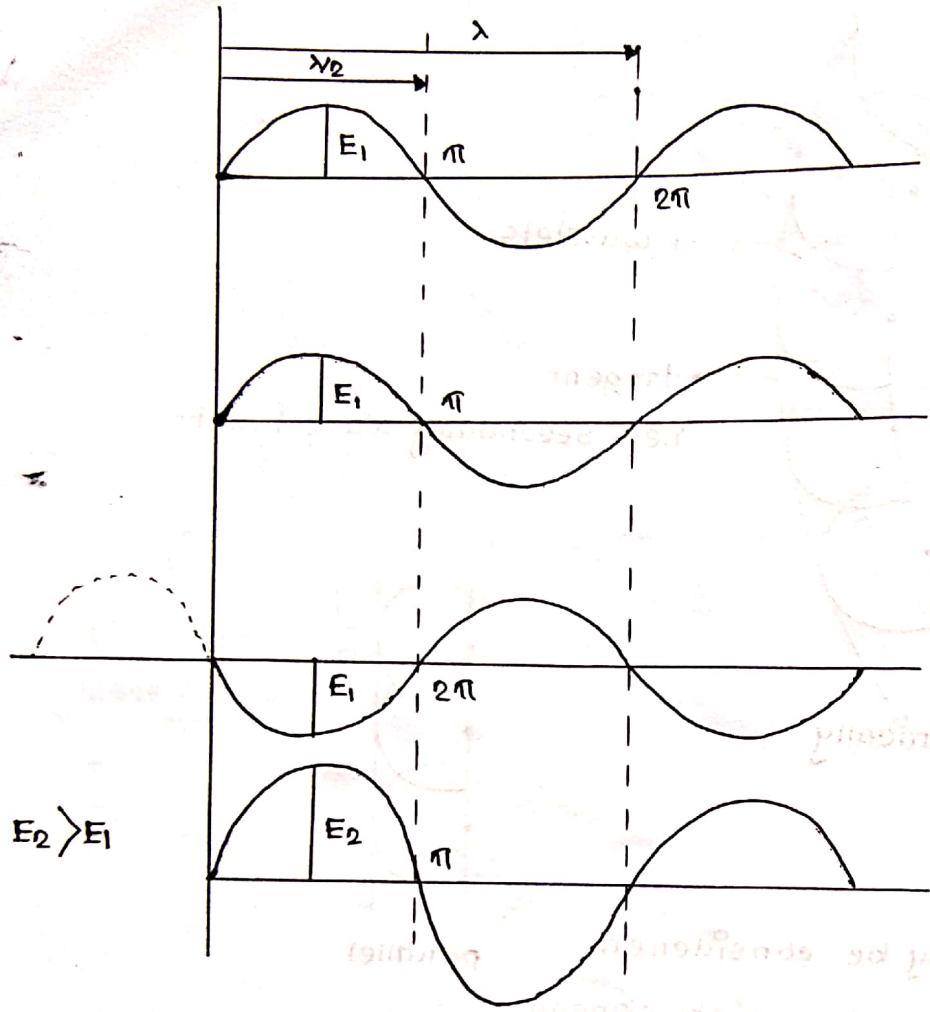
Every point of a wavefront may be considered as a source of secondary wavelets which spread out in forward direction with a speed equal to the speed of propagation of the wave.

The new wavefront is the tangential surface to all of these secondary wavelets.



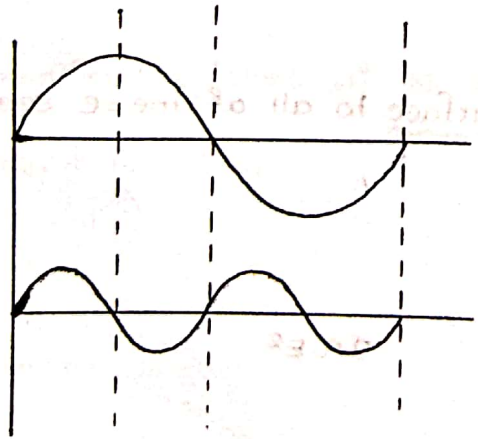
$\Delta \propto E^2$

① Cohesent source: (ସ୍ୱାସ୍ୱାମ୍ୟତ ଓଡ଼େଇ)

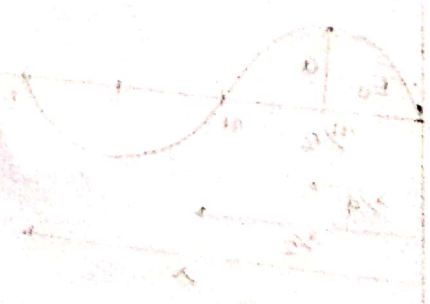


same { frequency
wavelength
phase
Zero or constant difference

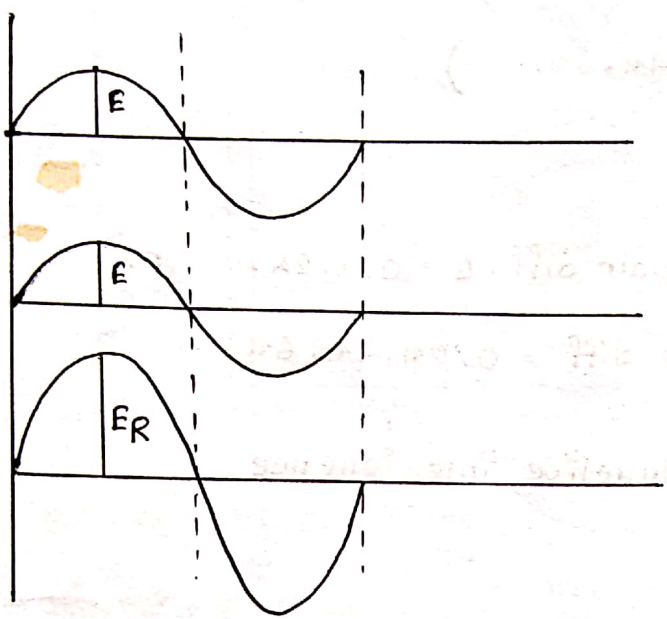
② Incohesent source:



f -> different
change in the phase



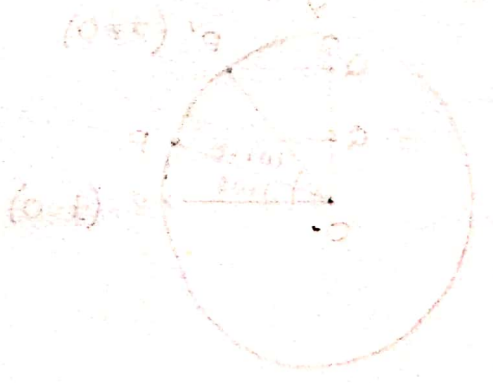
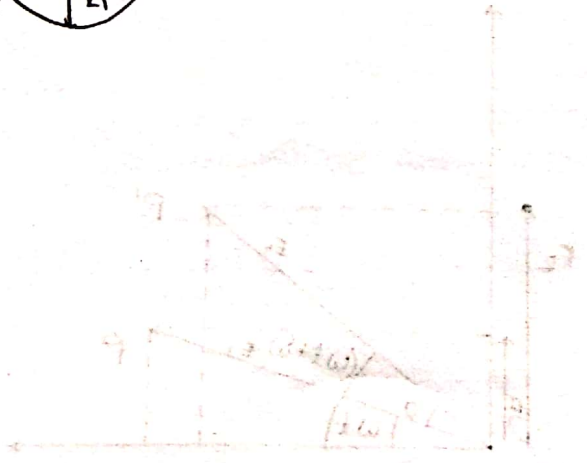
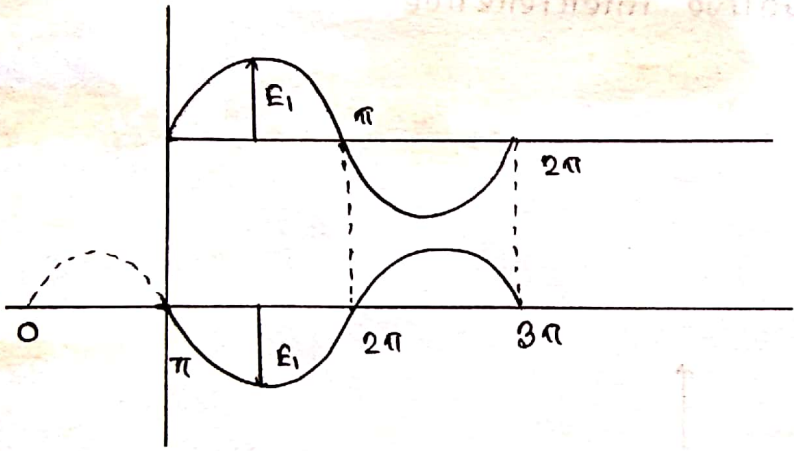
Super position of light waves:

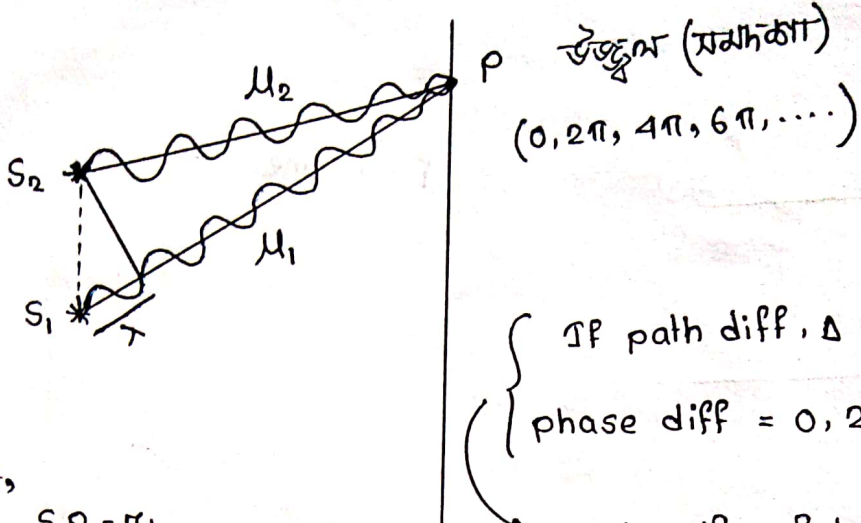


$f \rightarrow$ same

$$I \propto \frac{1}{2} c \epsilon_0 E_R^2$$

$$I \propto E_R^2$$





IF path diff, $\Delta = 0, \lambda, 2\lambda, \dots, n\lambda$
 phase diff = $0, 2\pi, 4\pi, 6\pi, \dots$
 constructive interference

let,
 $S_1P = \mu_1$
 $S_2P = \mu_2$

Path difference.

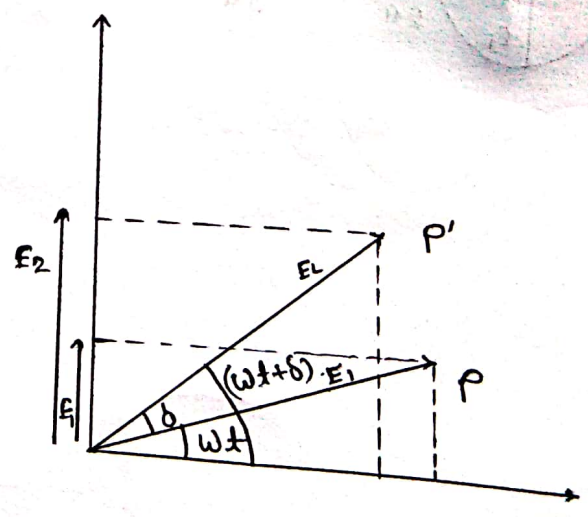
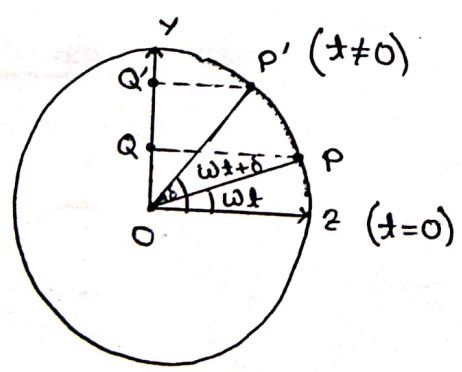
$$\Delta = \mu_1 - \mu_2$$

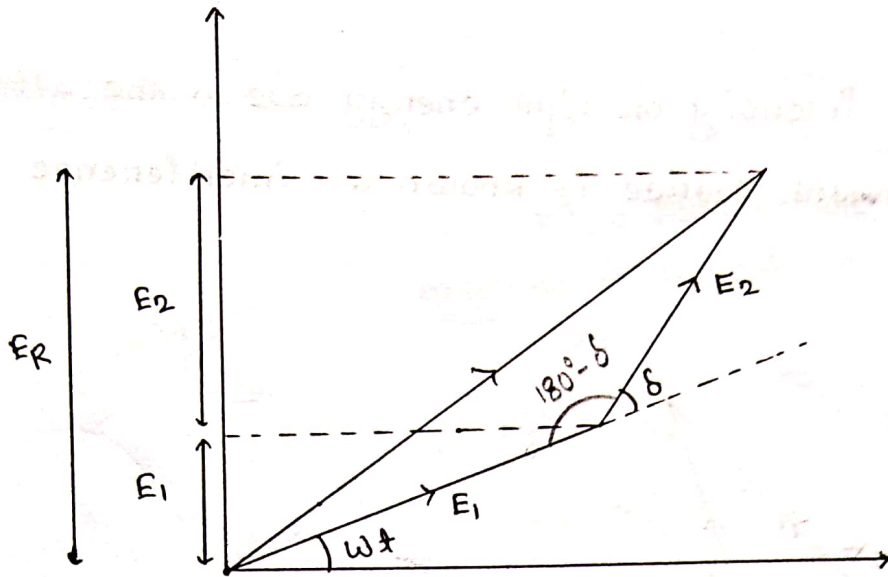
IF path diff, $\Delta = \lambda/2, 3\lambda/2, \dots, (2n+1)\lambda/2$
 destructive interference.

① side wave view $\rightarrow \lambda, 2\pi$

② End wave view

$$\theta = \omega t$$

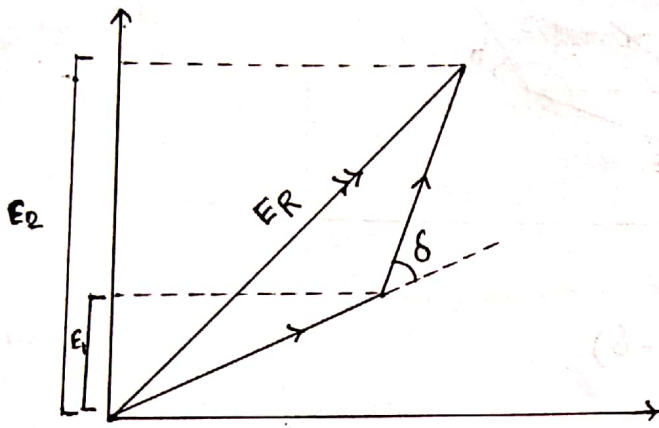




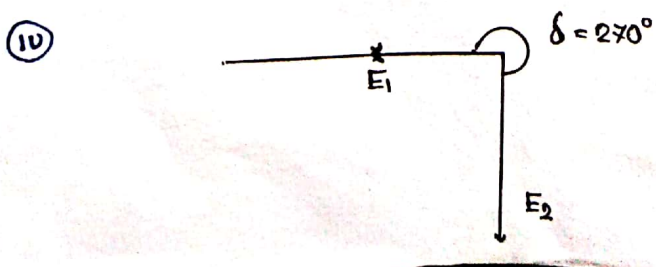
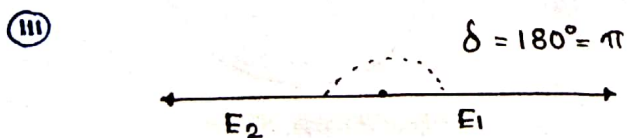
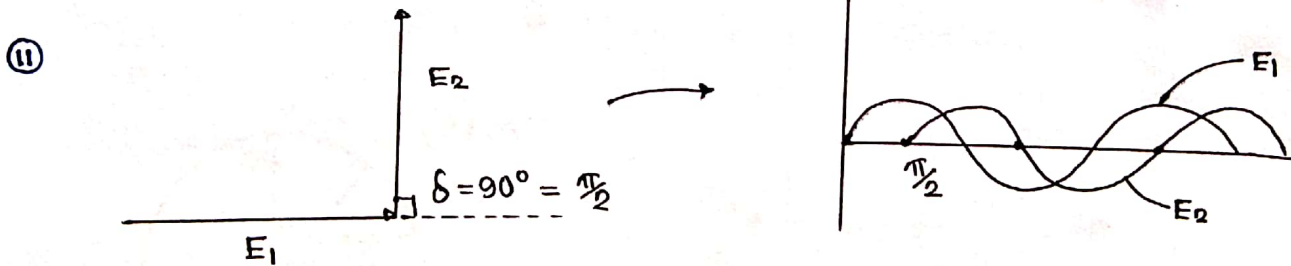
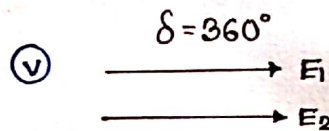
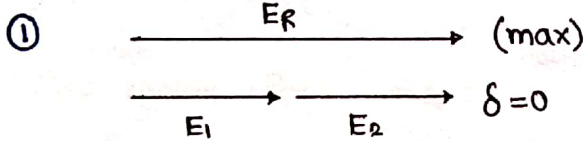
$$E_R^2 = E_1^2 + E_2^2 - 2E_1E_2 \cos(180^\circ - \delta)$$

$$= E_1^2 + E_2^2 + 2E_1E_2 \cos \delta$$

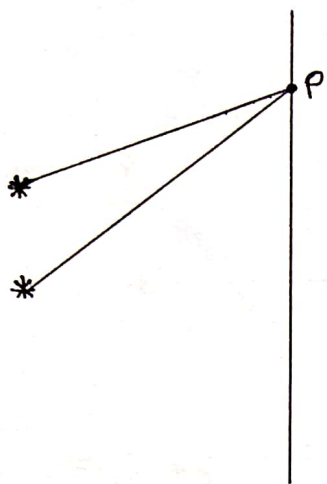
The redistribution of intensity of light energy due to the superposition of two or more coherent source is known as interference.



$$E_R^2 = E_1^2 + E_2^2 + 2E_1E_2 \cos \delta$$



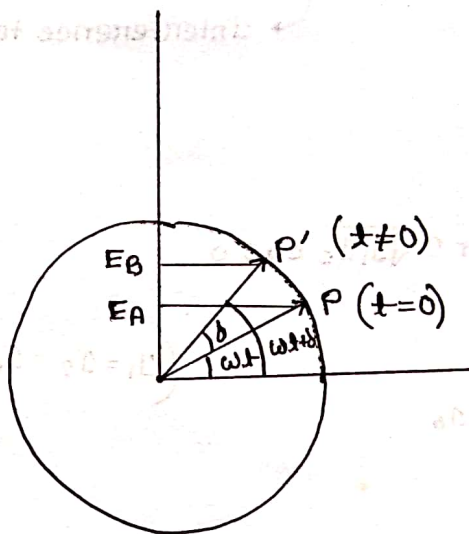
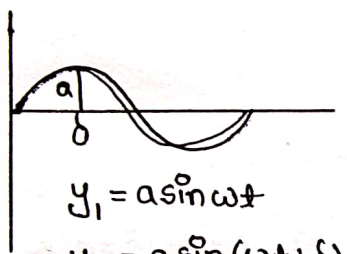
Theory of interference:



The electric field vector components of two waves arriving at the point P.

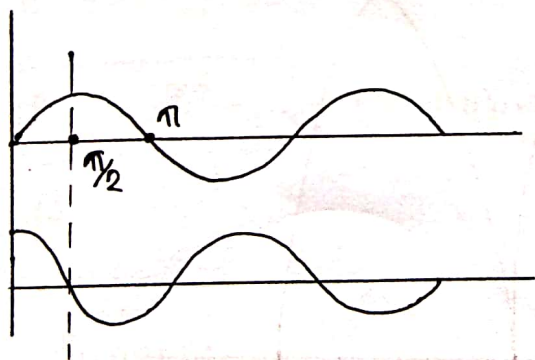
$$E_A = E_1 \sin \omega t$$

$$E_B = E_2 \sin (\omega t + \delta)$$



$$E_R = E_A + E_B$$

$$= (E_1 + E_2 \cos \delta) \sin \omega t + E_2 \sin \delta \cdot \cos \omega t$$



let,

$$E_1 + E_2 \cos \delta = E \cos \phi \quad \text{--- (i)}$$

$$E_2 \sin \delta = E \sin \phi \quad \text{--- (ii)}$$

$$\text{(i)}^2 + \text{(ii)}^2 \Rightarrow$$

$$(E_1 + E_2 \cos \delta)^2 + E_2^2 \sin^2 \delta = E^2 (\cos^2 \phi + \sin^2 \phi)$$

$$\therefore E^2 = E_1^2 + E_2^2 + \frac{2E_1 E_2 \cos \delta}{}$$

Interference term

$$I \propto E^2$$

$$I = I_1 + I_2 + 2\sqrt{I_1 I_2} \cos \delta$$

IF $\delta = 0$

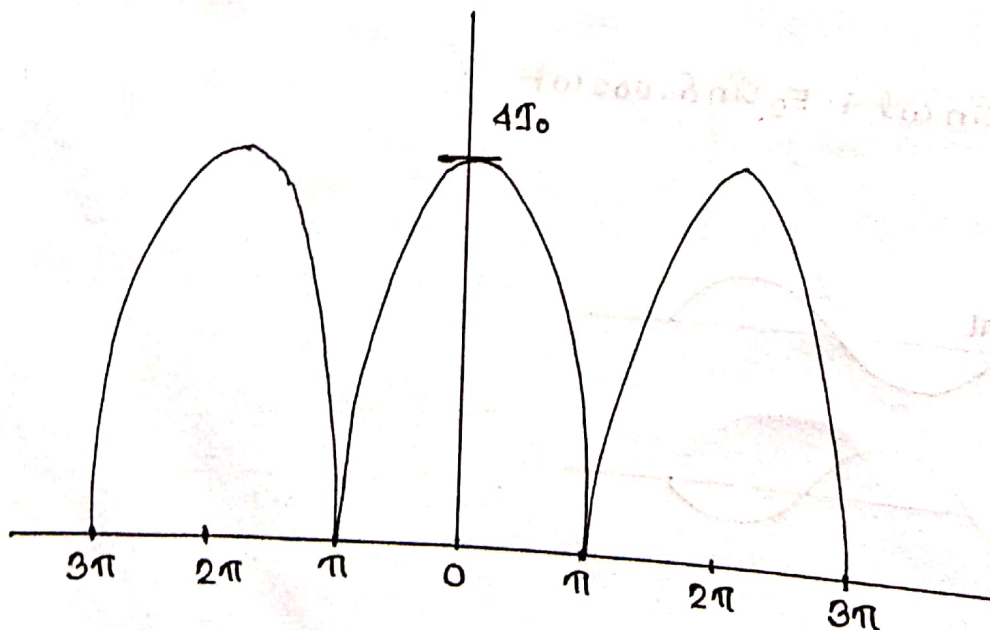
$$I = 4I_0$$

max

$$(I_1 = I_2 = I_0 \text{ इकाई})$$

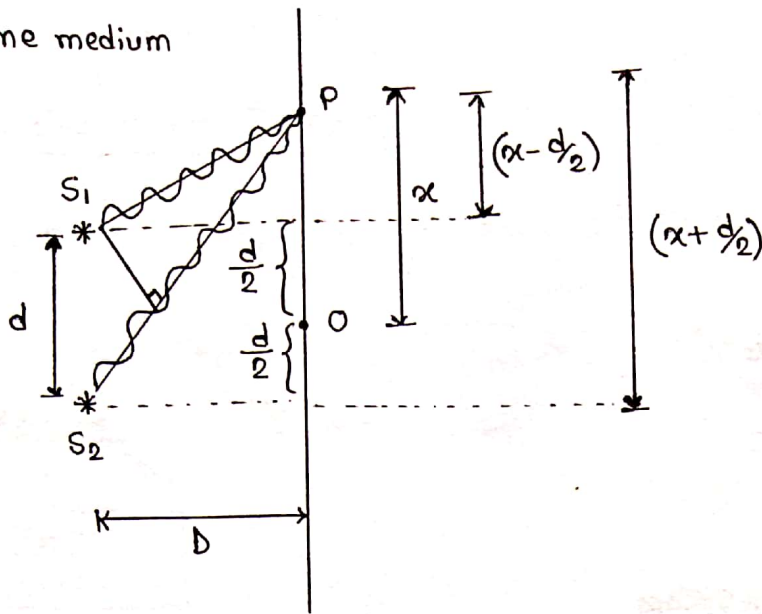
IF $\delta = 180^\circ$ or π

$$I_{\min} = 0$$

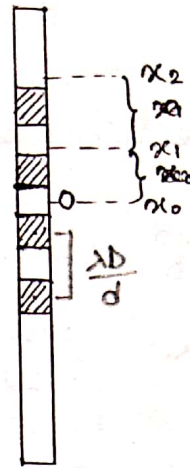


Same medium

#



$$I \propto A^2$$



path difference, $\Delta = \mu (S_2P - S_1P)$

$$\Delta \approx S_2P - S_1P$$

$$\Rightarrow S_2P^2 = D^2 + \left(x + \frac{d}{2}\right)^2$$

$$\Rightarrow S_1P^2 = D^2 + \left(x - \frac{d}{2}\right)^2$$

$$\therefore S_2P^2 - S_1P^2 = 2xd$$

$$\Rightarrow S_2P - S_1P = \frac{2xd}{S_2P + S_1P}$$

$$S_1P = S_2P = D \quad [\text{খুব বহুদূর হলে অবস্থান}]$$

$$\Rightarrow \Delta = \frac{2xd}{2D}$$

$$\therefore \Delta = \frac{\alpha d}{D} \rightarrow \text{পথ পার্থক্য}$$

$$\therefore \beta = \frac{\alpha d}{D}$$

Bright fringes:

$$\frac{\alpha d}{D} = n\lambda$$

$$\therefore \alpha_n = \frac{n\lambda D}{d}$$

$$\alpha_0 = 0$$

$$\alpha_2 - \alpha_1 = \frac{\lambda D}{d}$$

কোনদিক উজ্জ্বল থেকে n তম উজ্জ্বল ভোগার প্রতিফলিত তরঙ্গ

For dark,

destructive interference:

$$\frac{\alpha d}{\lambda} = (2n+1) \frac{\lambda}{2}$$

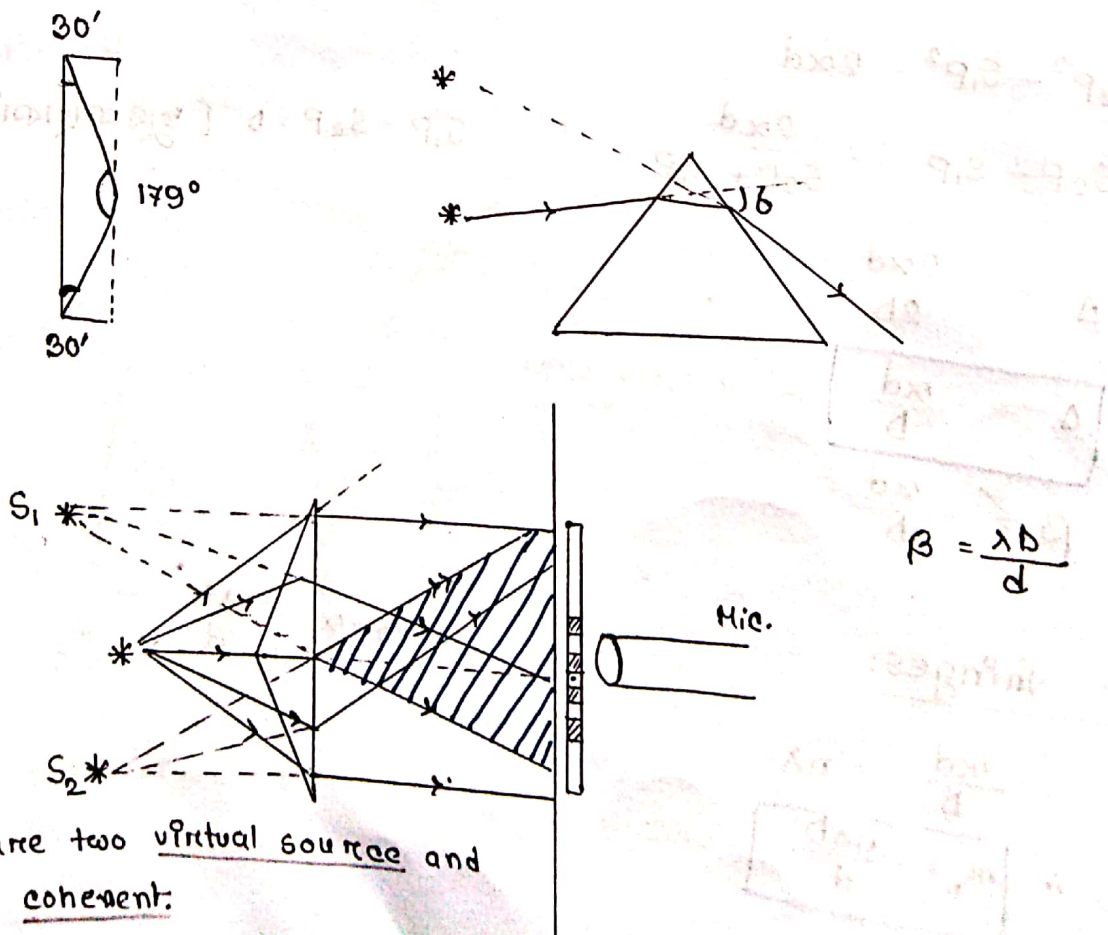
$$\therefore \alpha_n = \frac{(2n+1) \lambda}{2d}$$

$$\therefore \alpha_2 - \alpha_1 = \frac{\lambda}{d} \rightarrow \text{জোড়া স্রষ্টা}$$

$$\therefore \beta = \frac{\lambda}{d}$$

Fresnel's biprism:

Two prisms are very small refracting angles joined base to base.



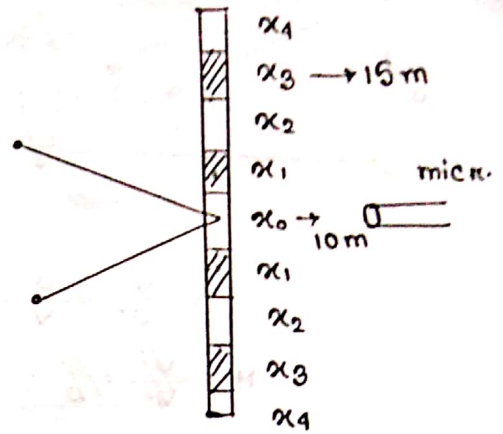
S₁ and S₂ are two virtual source and they produce coherent.

Determination of wave length:

① Fringes width: $\beta = \frac{\lambda D}{d}$

$$\beta = \frac{\alpha_3 - \alpha_0}{3} = \frac{15 - 10}{3}$$

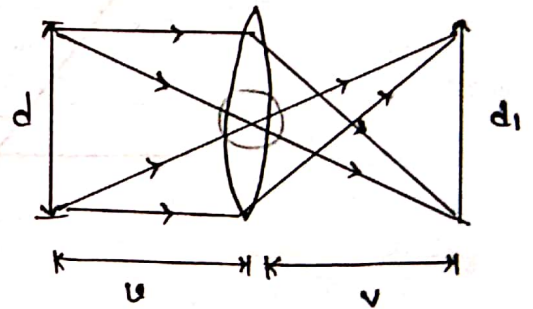
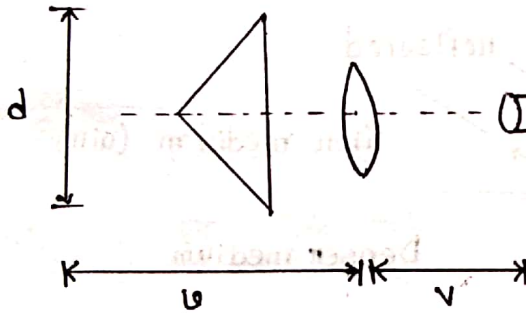
$$\beta = \frac{\alpha_N - \alpha_0}{N}$$



$$\alpha = \frac{n\lambda D}{d}$$

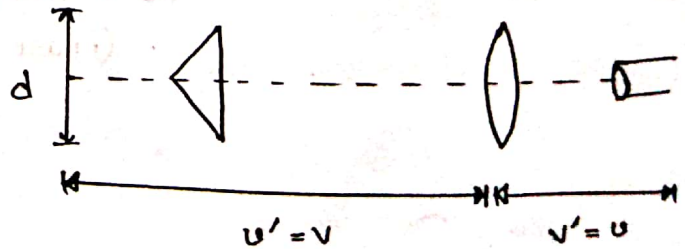
$n \rightarrow 0$ $\alpha \rightarrow 0$

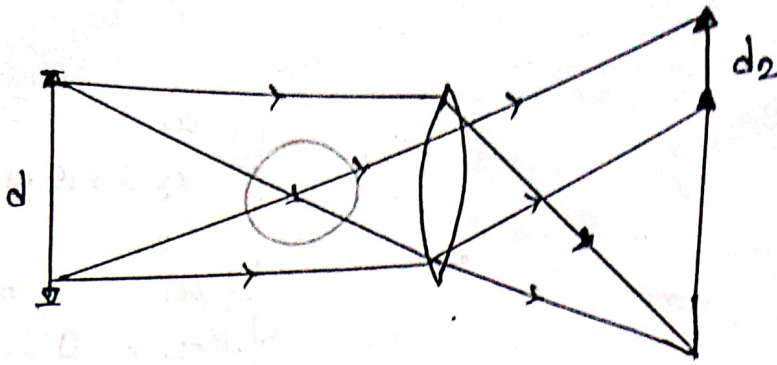
② Determination of d :



Sharp image, same size, are seen

Magnification, $M = \frac{v}{u} = \frac{d_1}{d}$ ①





$$= \frac{v'}{u'} = \frac{u}{v}$$

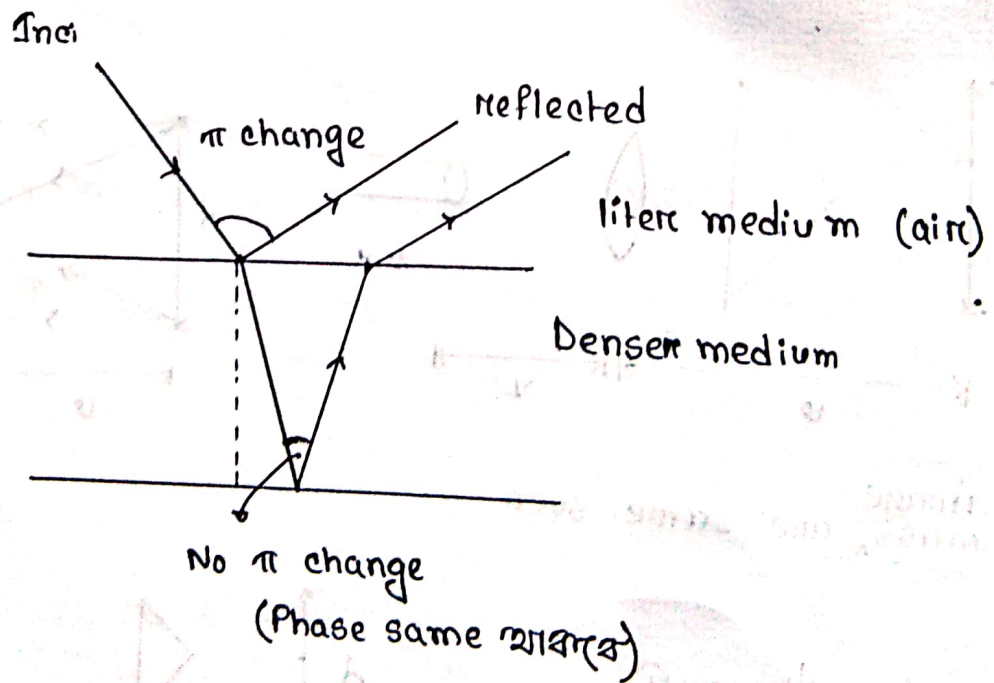
$$M = \frac{v'}{u'} = \frac{v}{u} = \frac{d_2}{d} \quad \text{--- (ii)}$$

(i) x (ii) \Rightarrow

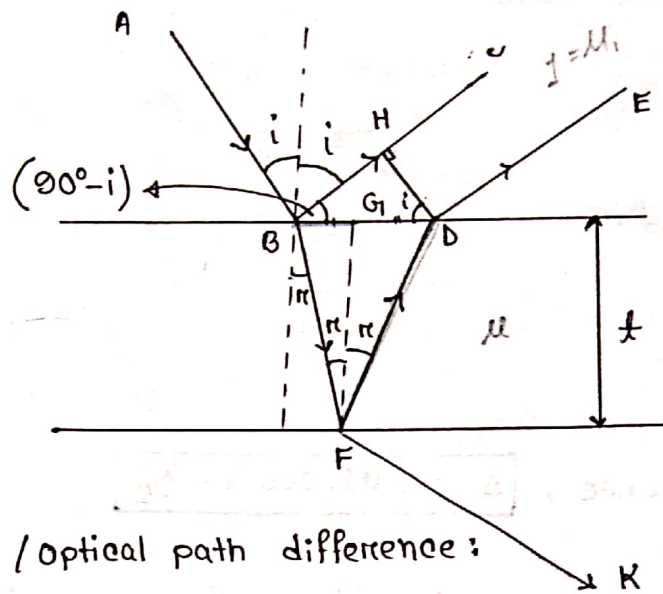
$$\frac{d_1 d_2}{d^2} = 1$$

$$\Rightarrow d^2 = d_1 d_2$$

$$\Rightarrow \boxed{d = \sqrt{d_1 d_2}}$$



Interference due to reflected Light :



Geometrical / Optical path difference :

$$\Delta = \mu (BF + FD) - BH \cdot \mu$$

$\Delta BGF \Rightarrow$

$$\cos \pi = \frac{BF}{BG}$$

$$\therefore BF = \frac{FG}{\cos \pi} = \frac{t}{\cos \pi}$$

$$\therefore FD = \frac{t}{\cos \pi}$$

$$BG = GD, \quad BD = BG + GD$$

$$\tan \pi = \frac{BG}{FG}$$

$$\Rightarrow BG = FG \cdot \tan \pi$$

$$= t \tan \pi$$

$$\therefore BD = 2t \tan \pi$$

$\Delta BDH \Rightarrow$

$$\sin i = \frac{BH}{BD}$$

$$\Rightarrow BH = 2t \tan \pi \cdot \sin i = 2\mu t \tan \pi \cdot \sin \pi$$

From Snell's law,

$$\mu = \frac{\sin i}{\sin \pi} \Rightarrow \sin i = \mu \sin \pi$$

$$\Delta = \frac{2\mu t}{\cos r} - 2\mu t \frac{\sin^2 r}{\cos r}$$

$$= \frac{2\mu t}{\cos r} (1 - \sin^2 r)$$

$$= \frac{2\mu t}{\cos r} \cdot \cos^2 r$$

$$\Delta = 2\mu t \cdot \cos r$$

corrected path difference, $\Delta = 2\mu t \cdot \cos r - \frac{\lambda}{2}$

When a ray is reflected at a boundary of a rarer denser medium a path change of $\frac{\lambda}{2}$ or π (phase change) occurs for BC.

For constructive interference,

$$2\mu t \cos r - \frac{\lambda}{2} = n\lambda$$

$$\therefore 2\mu t \cos r = (2n+1) \frac{\lambda}{2} \longrightarrow \text{condition for brightness.}$$

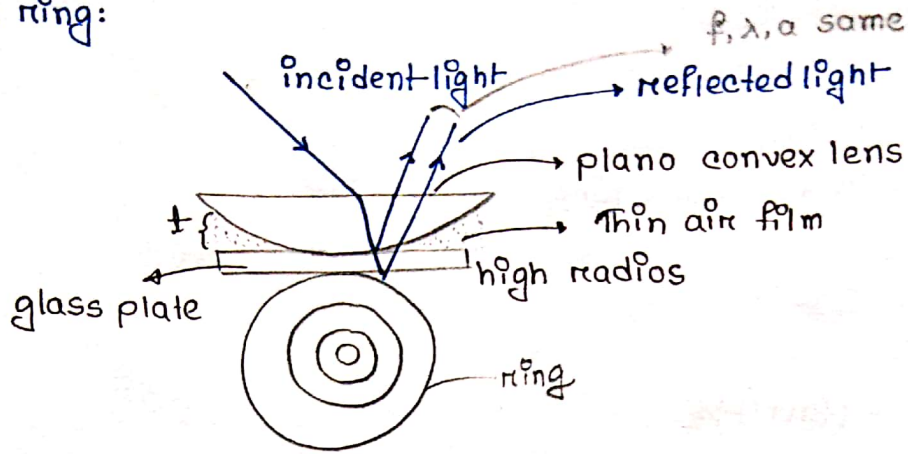
For destructive interference,

$$2\mu t \cos r - \frac{\lambda}{2} = (2n+1) \frac{\lambda}{2}$$

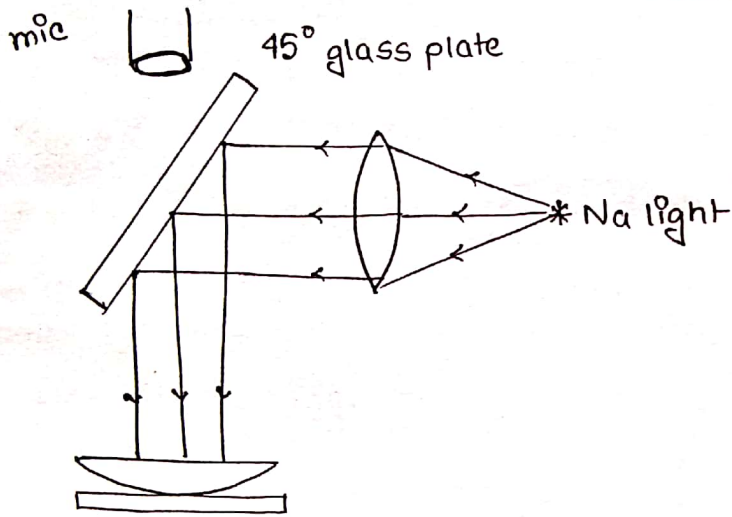
$$\therefore 2\mu t \cos r = n\lambda \longrightarrow \text{condition for dark.}$$

Interference due to transmitted light.

Newton's ring:



* Na light (Monochromatic colour) - 5890-5896 Å
 → 5893 Å



Newton's ring is found when a plano convex lens is placed on the glass plate. The part of the incident light is reflected from the lower portion of the plano convex lens.

glass to air boundary.

Remainder of the is transmitted to the and reflected from the upper portion of the glass plate. or air to glass boundary.

$$\Delta = 2\mu t \cos \pi - \frac{\lambda}{2}$$

\nearrow (-for air) \searrow = 0

$$\Rightarrow \Delta = 2t - \frac{\lambda}{2} \longrightarrow (2n+1) - \text{dark ring}$$

For Dark ring,

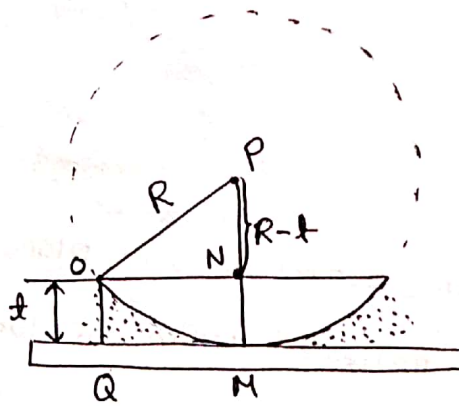
$$2t - \frac{\lambda}{2} = (2n+1)\frac{\lambda}{2}$$

$$\Rightarrow 2t = n\lambda$$

For bright ring,

$$2t - \frac{\lambda}{2} = n\lambda$$

$$\Rightarrow 2t = (2n+1)\frac{\lambda}{2}$$



$\Delta PON \Rightarrow$

$$R^2 = (R-t)^2 + t_m^2$$

$$t_m = t \quad \text{⊖}$$

$$\therefore t_m^2 = 2Rt - t^2$$

$$R \gg t \rightarrow 2Rt \gg t^2$$

$$\therefore t_m^2 = 2Rt$$

$$\therefore t = \frac{t_m^2}{2R}$$

For dark ring:

$$2\mu t \cos \pi - \lambda/2 = (2n+1)\lambda/2$$

\downarrow \downarrow

$$\Rightarrow 2t - \lambda/2 = (2n+1)\lambda/2$$

$$\Rightarrow 2t = n\lambda$$

$$\Rightarrow \frac{v_m^2}{R} = n\lambda$$

$$\Rightarrow v_m^2 = n\lambda R$$

$$\Rightarrow \boxed{v_m = \sqrt{n\lambda R}}$$

$$r_m \propto \sqrt{n}$$

$r_m \propto \sqrt{1} \rightarrow$ center ring is dark

Diameter of the ring:

$$D_m^2 = 2r_m$$

$$\therefore \boxed{D_m^2 = 4nR\lambda}$$

Central dark spot:

$$\Delta = 2t - \lambda/2$$

No air film
contact point

$$t = 0$$

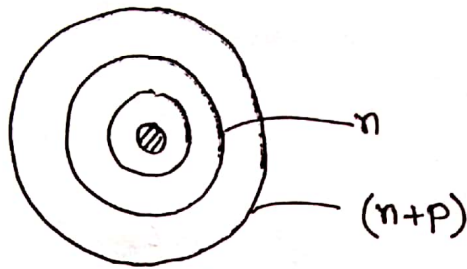
$$\Delta = \lambda/2$$

Determination of wavelength (λ) of light

center a dark (কেন্দ্রমাঝখানে)

$$D_n^2 = 4\lambda nR$$

↪ Diameter of the dark ring



For $(n+p)^{\text{th}}$ ring:

$$D_{(n+p)}^2 = 4(n+p)\lambda R$$

$$\therefore D_{(n+p)}^2 - D_n^2 = 4Rp\lambda$$

let,

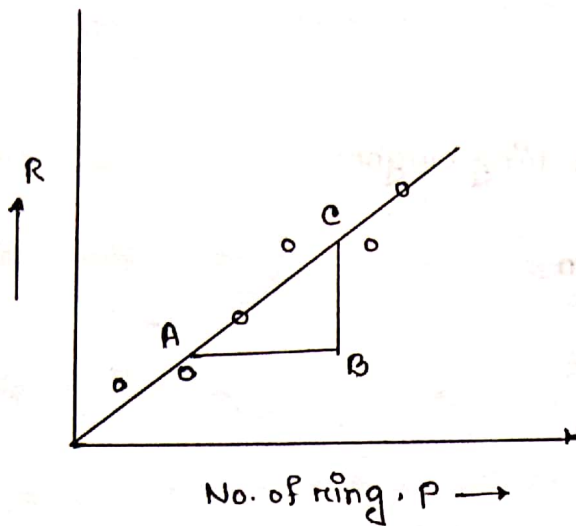
$$n = 3$$

$$n+p = 5$$

$$\therefore p = 2$$

$$\therefore \lambda = \frac{D_{(n+p)}^2 - D_n^2}{4PR}$$

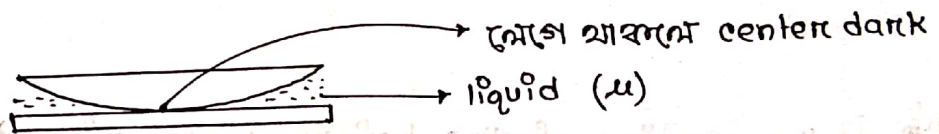
$$\Rightarrow \begin{array}{ccc} D_{(n+p)}^2 - D_n^2 & = & \frac{4R\lambda P}{\downarrow \quad \downarrow} \\ \downarrow y & & m \quad x \end{array}$$



$$\text{slope} = \frac{BC}{AB} = 4R\lambda$$

$$\therefore \lambda = \frac{\text{slope}}{4R}$$

Determination of μ of liquid:



path difference,

$$\Delta = 2\mu t \cos \pi - \frac{\lambda}{2}$$

For dark,

$$2\mu t \cos \pi - \frac{\lambda}{2} = (2n+1) \frac{\lambda}{2}$$

$$\Rightarrow 2\mu t \cos \pi = n\lambda$$

$$\cos \pi = -1 \text{ (২নং), } 2\mu t = n\lambda \text{ — (1)}$$

$$R^2 = 2tR$$

অর্থাৎ,

$$D^2 = \frac{4n\lambda R}{\mu}$$

$$\Rightarrow (D_n)_{\text{liquid}}^2 = \frac{4n\lambda R}{\mu}$$

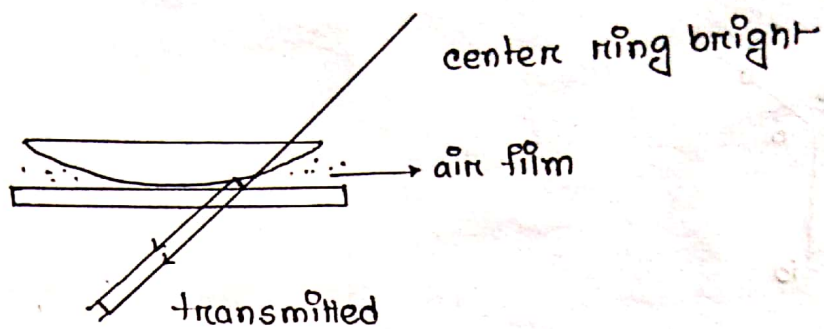
$$\therefore (D_{n+p})_{\text{liq}}^2 = \frac{4(n+p)\lambda R}{\mu}$$

$$(D_n)_{\text{air}}^2 = 4n\lambda R$$

$$(D_{n+p})_{\text{air}}^2 = 4(n+p)\lambda R$$

$$\therefore \mu = \frac{(D_{n+p})_{\text{air}}^2 (D_n)_{\text{air}}^2}{(D_{n+p})_{\text{liq}}^2 - (D_n)_{\text{liq}}^2}$$

Newton's ring in transmitted light:



For dark \Rightarrow

$$2\mu t \cos r = (2n+1) \lambda/2$$

$$\downarrow \qquad \downarrow$$

$$2t = (2n+1) \lambda/2$$

For bright \Rightarrow

$$2t = n\lambda$$

$\therefore t = \frac{r_n^2}{2R}$, the radius of the bright ring, $r_n^2 = n\lambda R$.

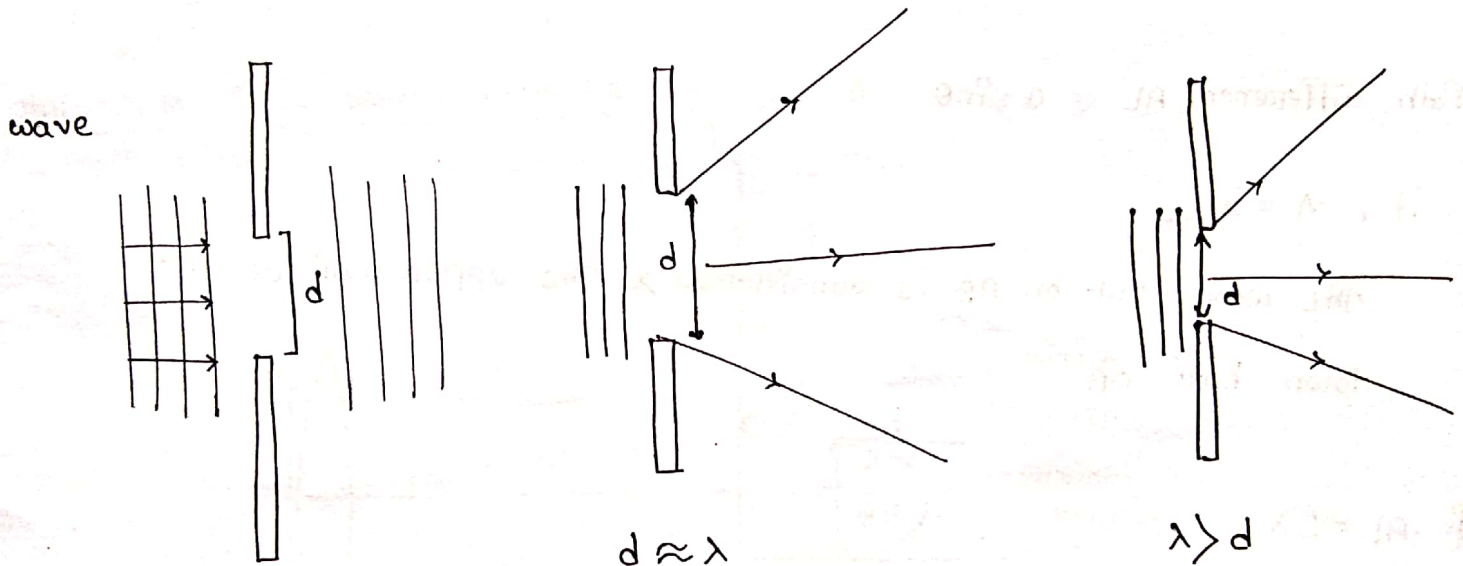
The radius of the dark ring, $r_n^2 = (2n+1) \lambda R/2$.

Math

Diffraction: (wave property)

The bending of waves around the sharp edges of an obstacle is called diffraction.

The diffraction is occurred the dimension of the obstacles are comparable to the wavelength of the waves.



$$d \gg \lambda$$

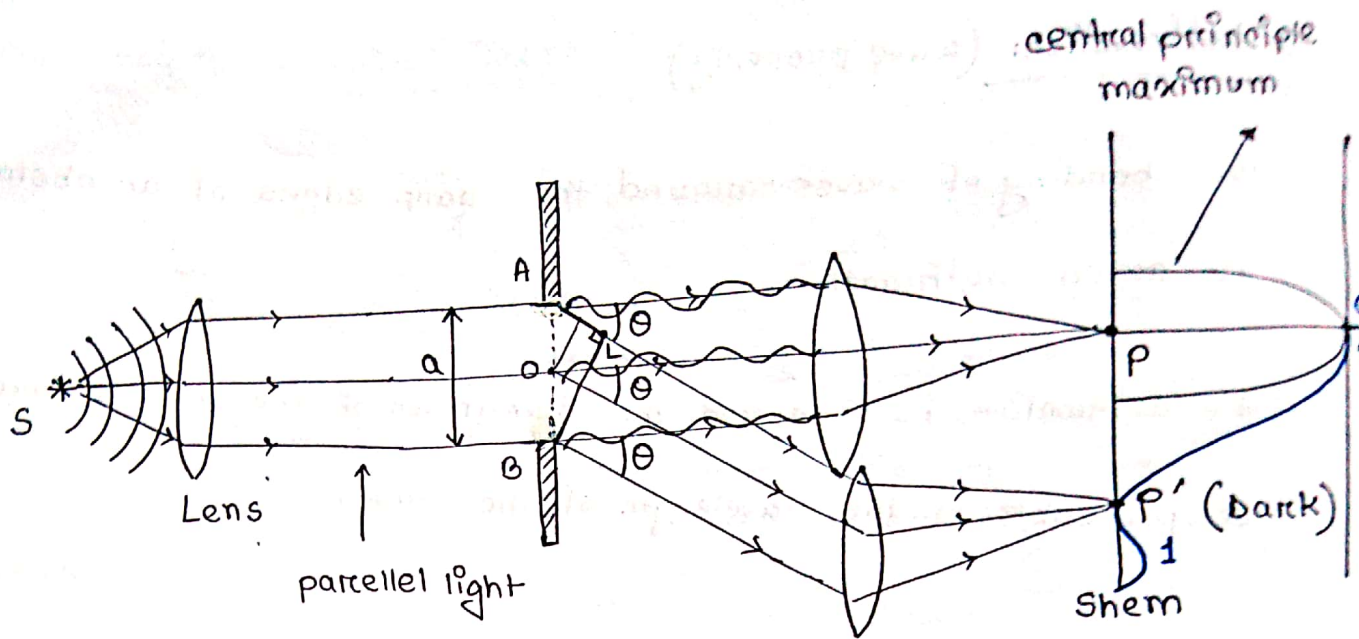
① No bending

② The diffraction effect is observable.

③ The diffraction effect is observed at large distance from the slit.

④ Fraunhofer diffraction \rightarrow source and slit are at finite distance.

⑤ Fresnel diffraction \rightarrow source and slit are at infinite distance.



• Path difference, $AL = a \sin \theta = \Delta$

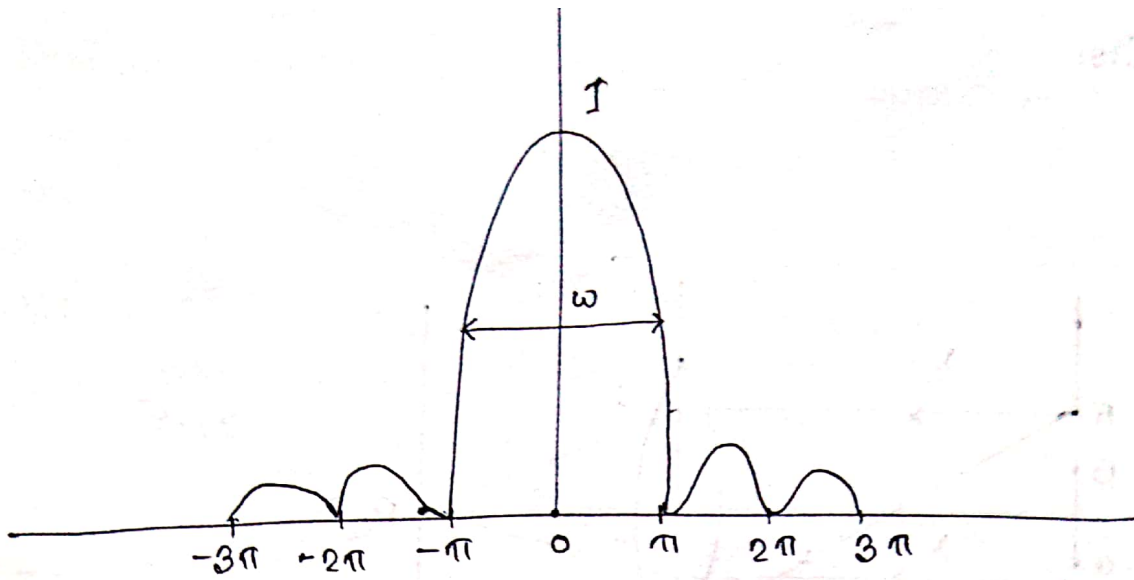
if, $\Delta = \lambda \dots$

The wavefront on AB is considered λ . The upper half OA and lower half OB.

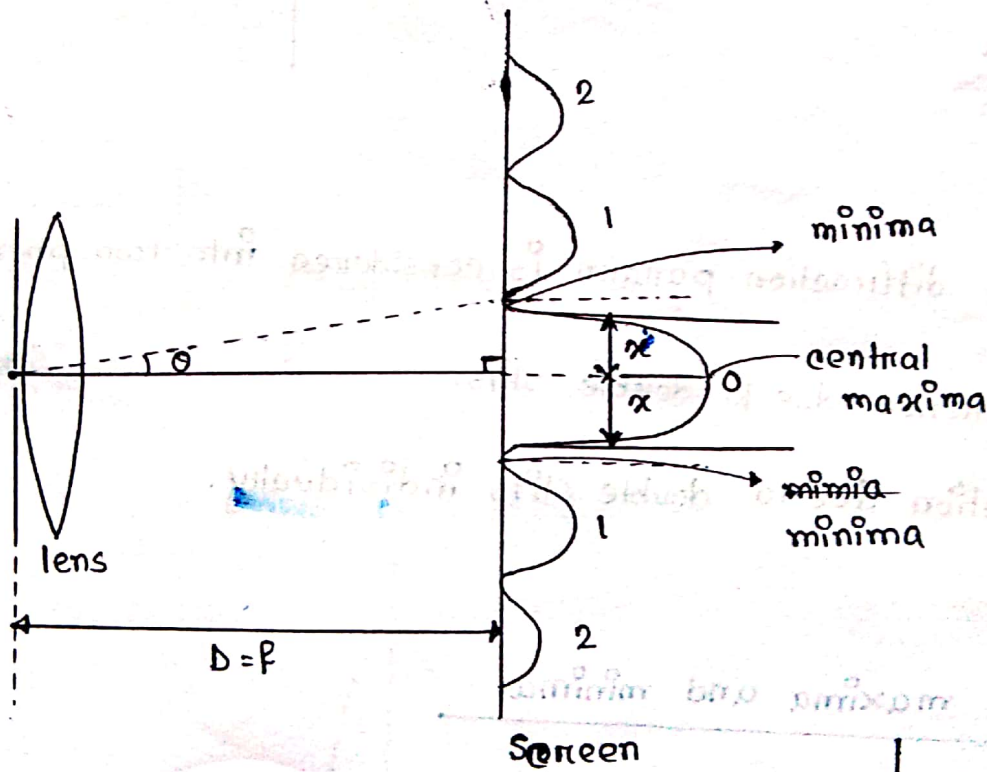
if $AL = 2\lambda$

The wave front 2λ

The lower and upper half are differ by $\lambda/2$.



The width of the central maxima:



$$\tan \theta = \frac{\alpha}{f}$$

$$\Rightarrow \frac{\sin \theta}{\cos \theta} = \frac{\alpha}{f}$$

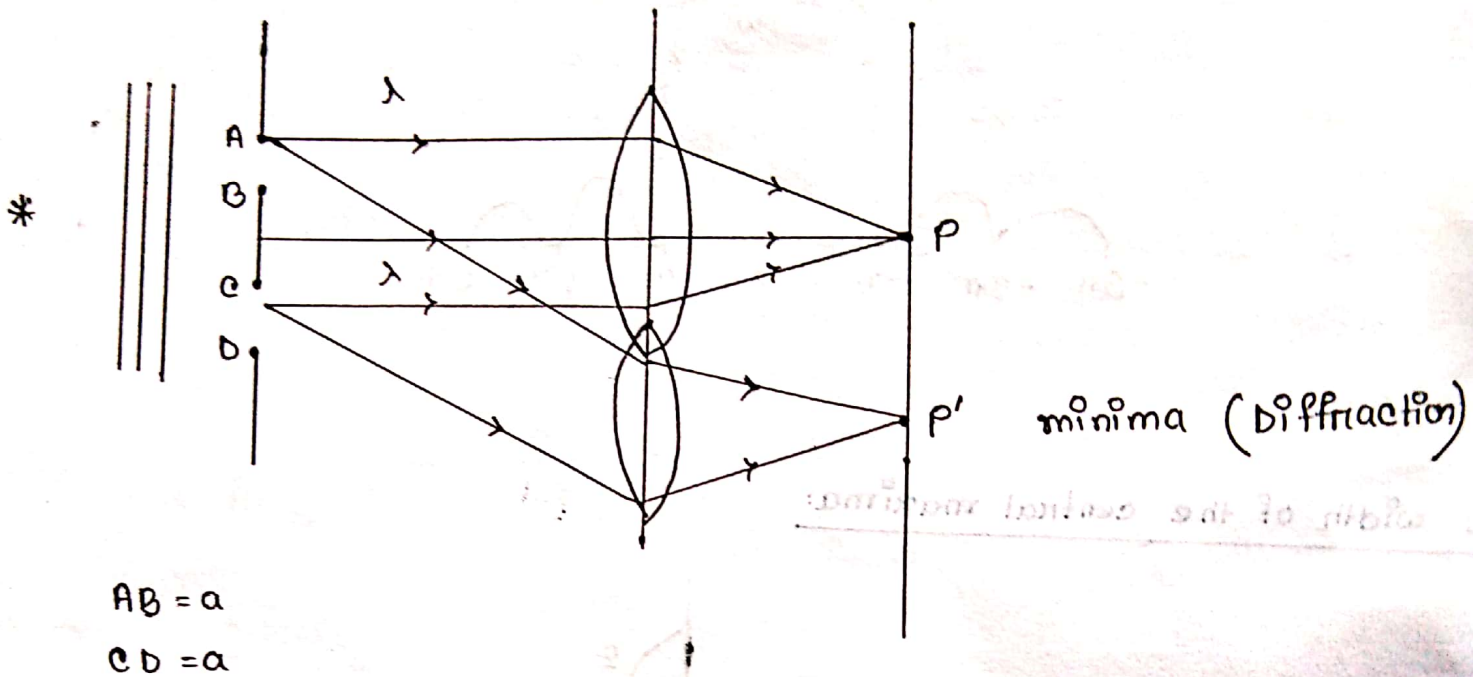
$$\Rightarrow \sin \theta = \frac{\alpha}{f} \quad [\theta \approx 0^\circ]$$

$$\begin{aligned} \neq a \sin \theta &= \lambda \\ \Rightarrow \sin \theta &= \lambda/a \end{aligned}$$

$$\alpha = \frac{f\lambda}{a}$$

$$\begin{aligned} \text{width, } w &= 2\alpha \\ w &= \frac{2f\lambda}{a} \end{aligned}$$

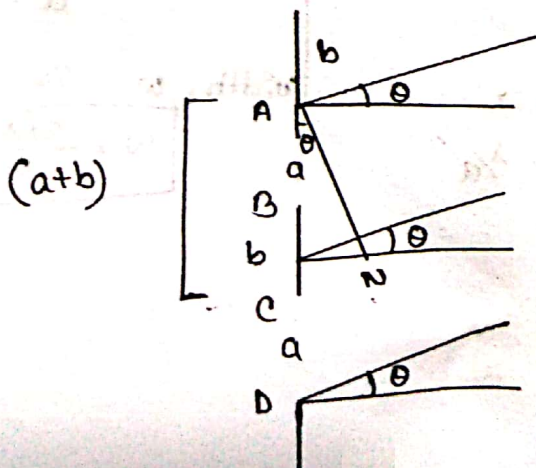
Double slits:



Double slit diffraction pattern is considered into two phenomenon

- ① Interference due to double slits.
- ② Diffraction due to double slits individually.

① Interference maxima and minima:



path difference, $eN = (a+b)\sin\theta$

For maxima,

$$(a+b)\sin\theta_n = n\lambda$$

$$\Rightarrow \sin\theta_n = \frac{n\lambda}{(a+b)}$$

For minima,

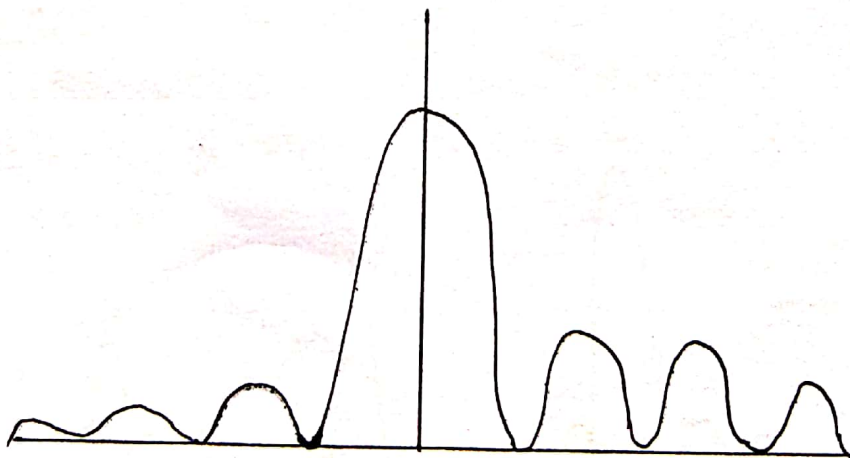
$$(a+b)\sin\theta'_n = (2n+1)\frac{\lambda}{2}$$

$$\Rightarrow \sin\theta'_n = \frac{(2n+1)\lambda}{2(a+b)}$$

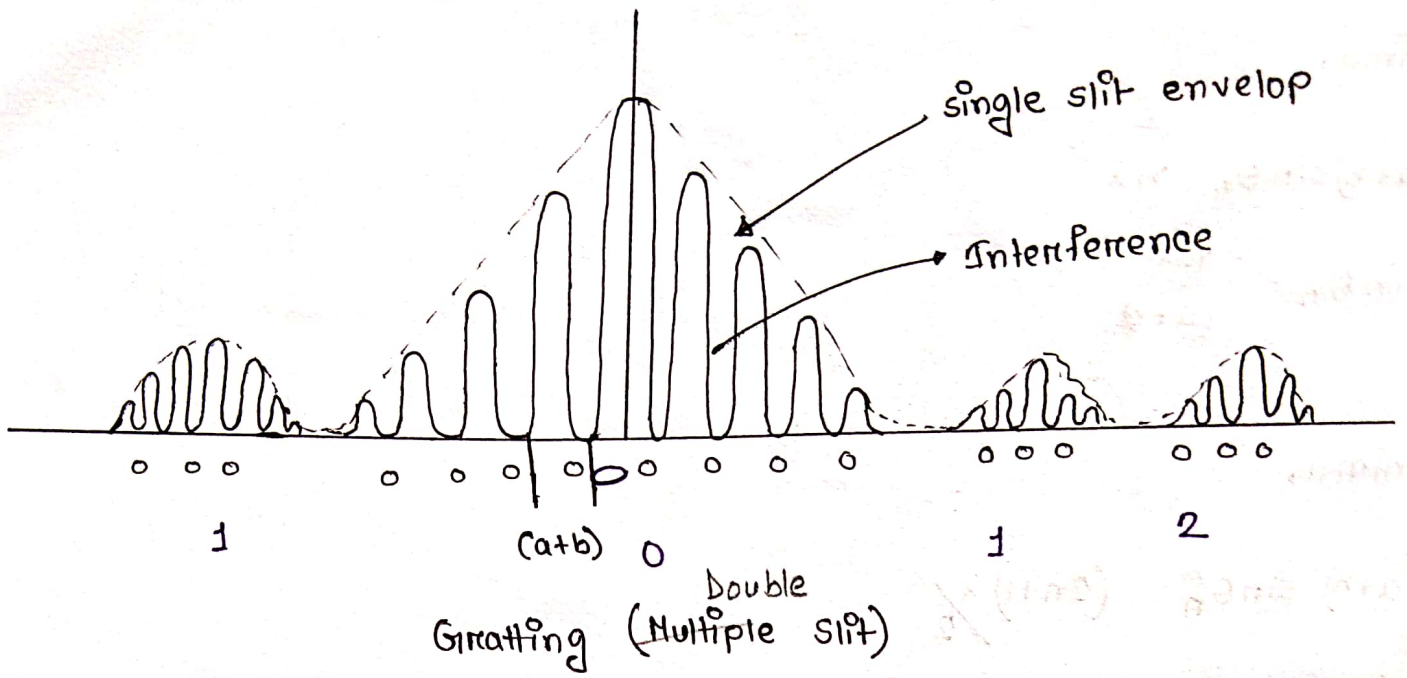
$$\sin\theta_1 = \frac{3\lambda}{2(a+b)}$$

$$\sin\theta_2 = \frac{5\lambda}{2(a+b)}$$

$$\left. \begin{array}{l} \sin\theta_1 = \frac{3\lambda}{2(a+b)} \\ \sin\theta_2 = \frac{5\lambda}{2(a+b)} \end{array} \right\} \therefore \sin\theta_2 - \sin\theta_1 = \frac{\lambda}{a+b}$$



① single



② Diffraction maxima and minima:

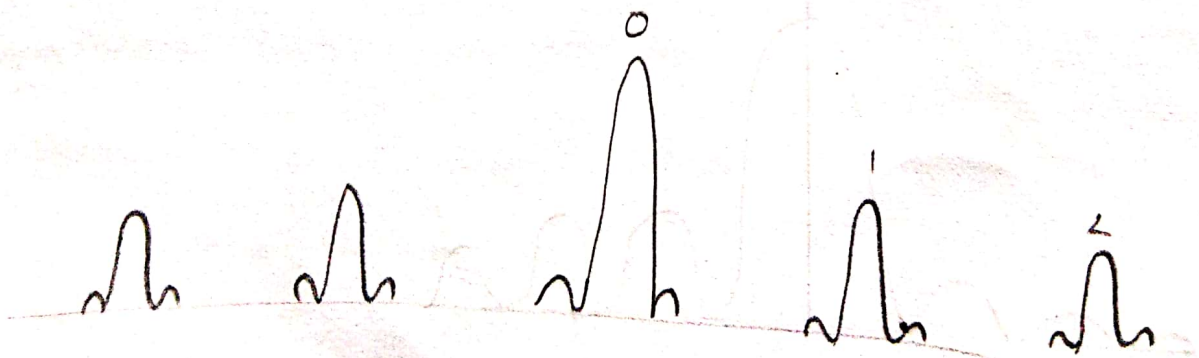
path difference, = $a \sin \theta$

For minima,

$a \sin \theta = n \lambda$

Diffraction grating:

optical device.



Grating (multiple slit)

multiple slits

The gratings are prepared by ruling equal distance parallel lines on the glass surface. The lines are drawn with a fine diamond point.

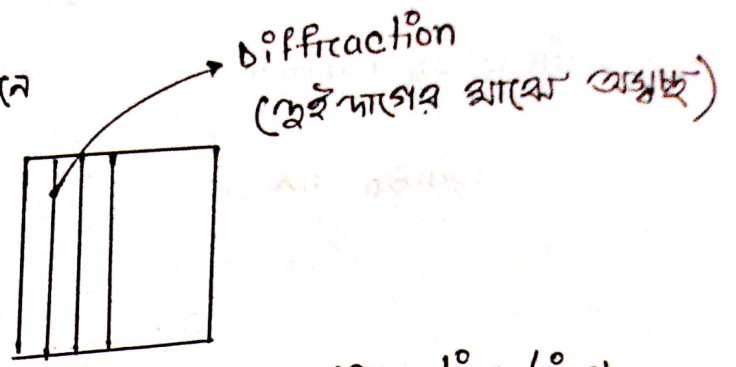
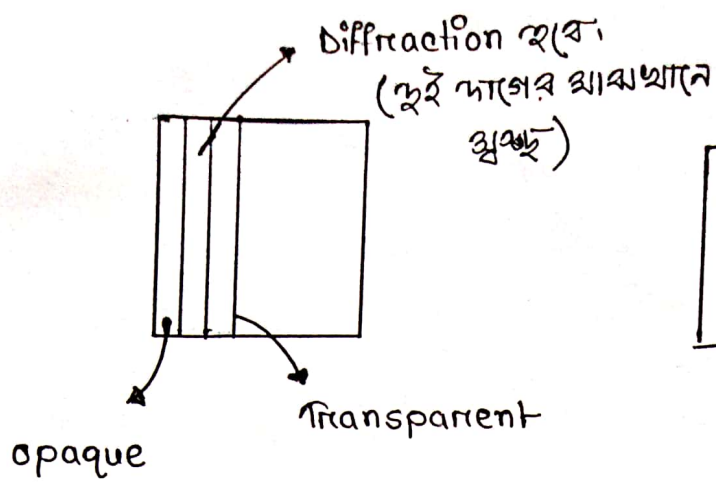
→ Transmission grating

→ Reflection grating

The space in between the new two lines is transparent and the line portion is such transmission such grating act as...

On the other hand,

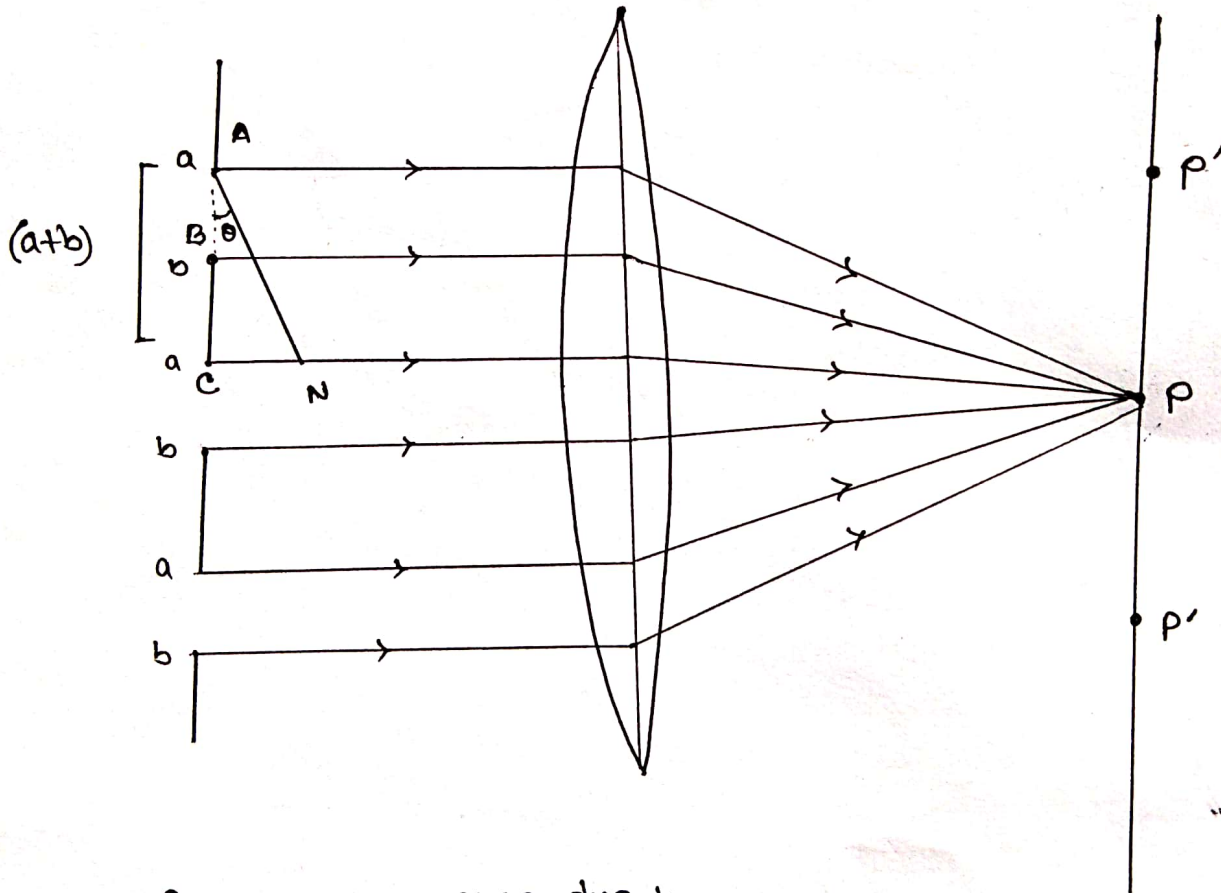
The lines are drawn on a silver surface, the light is reflected between any two lines. such ...



15000 line / inch
 $(a+b) = \frac{254}{15000} \text{ line/cm.}$

① Transmission Grating

② Reflected Grating



① Interference phenomenon due to more than one slits.
 path difference,

$$CN = (a+b) \sin \theta$$

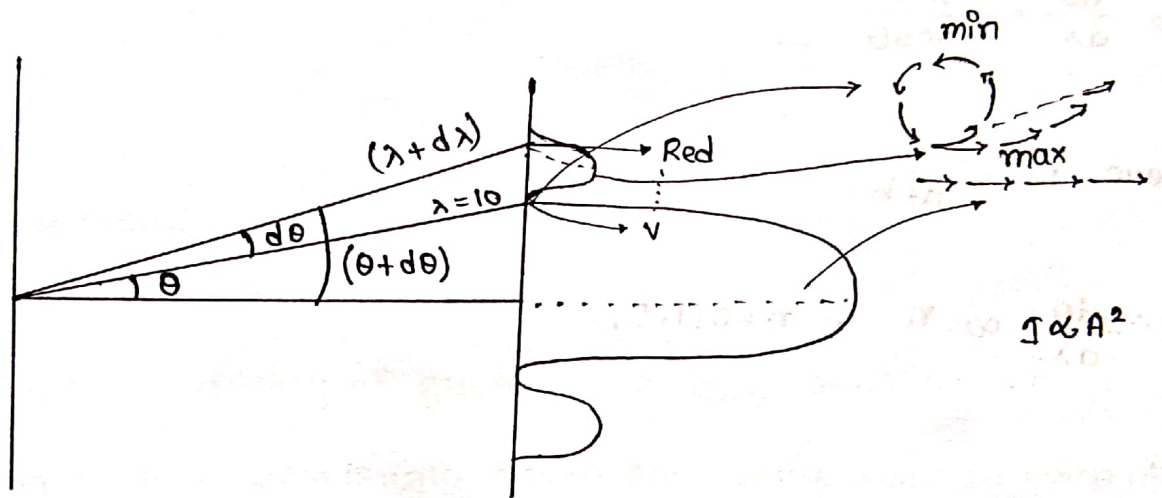
$$\therefore (a+b) \sin \theta = n \lambda \quad [\text{For interference max}]$$

$$(a+b) \sin \theta = (2n+1) \lambda / 2 \quad [\text{for interference min}]$$

ii) Diffraction minima,

$$a \sin \theta = n \lambda$$

Mixed Wavelength:



$$(a+b) \sin \theta = n \lambda$$

↓
|

$$(a+b) \sin(\theta + d\theta) = n (\lambda + d\lambda)$$

Dispersive power:

$$\frac{d\theta}{d\lambda}$$

... of grating is a ratio of the difference in the angle of diffraction of any two neighbouring spectrum lines to the difference the wavelength of the two spectrum lines.

$$(a+b) \sin \theta = n \lambda$$

$$(a+b) \cos \theta d\theta = n d\lambda$$

$$\therefore \frac{d\theta}{d\lambda} = \frac{n}{(a+b) \cos \theta}$$

$$\Rightarrow \frac{d\theta}{d\lambda} = \frac{n N'}{a \cos \theta}$$

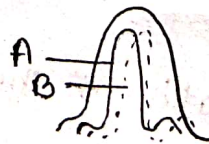
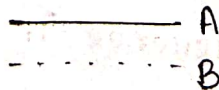
where $N' = \frac{1}{a+b}$

$$\therefore \frac{d\theta}{d\lambda} \propto n, \quad n=0, 1, 2, \dots$$

Distinguish between dispersive power

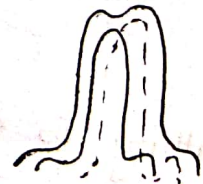
Resolving power:

The ability of an optical instrument to produce distinctly separate images of two objects located very close to each other is called resolving power.



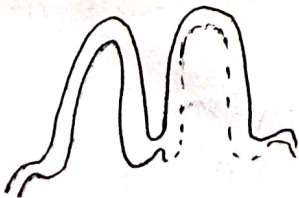
(i)

unresolved



(ii)

Rayleigh criterion



(iii) Resolved

Rayleigh Criterion: with the central maximum of one falls ^{falls} of the first minimum of

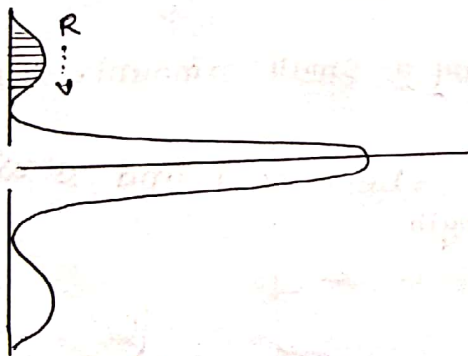
the other, in other words. When the central bright images of one falls on the first dark of the other. Then the two images are said to be just resolved. This called Rayleigh criterion of resolution.

Resolving power of grating:

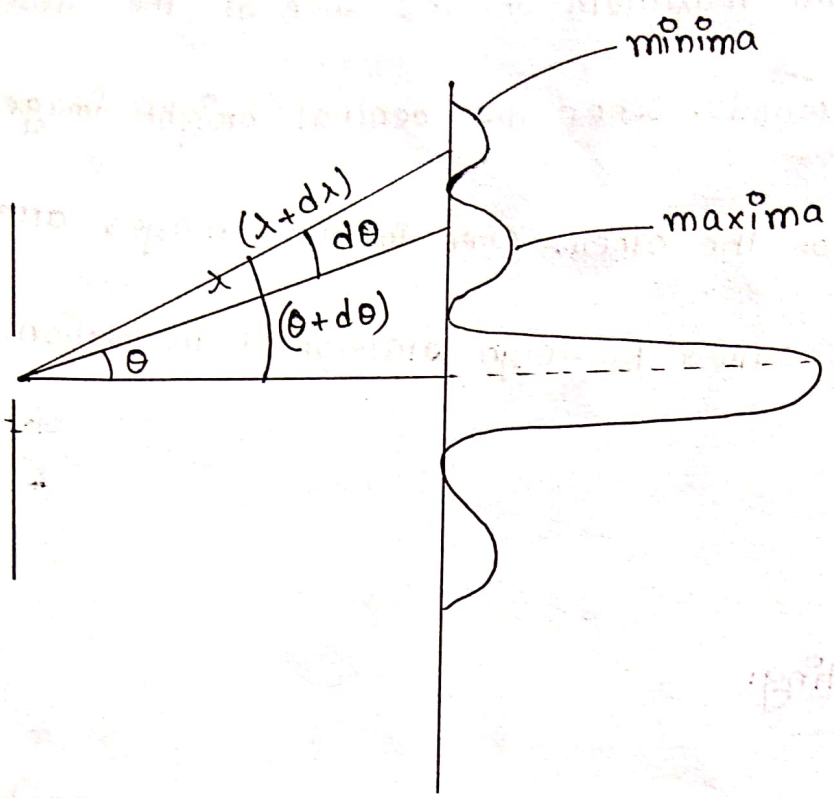
It is defined as the capacity of grating to form separate of diffraction maxima of two wavelength which are very close to each other.

$$(a+b)\sin\theta = n\lambda$$

$$\theta \propto \lambda$$



$\lambda, \lambda + d\lambda$



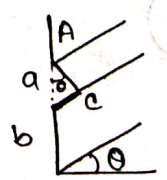
$$(a+b) \sin \theta_n = n\lambda$$

$$(a+b) \sin(\theta_n + d\theta) = n(\lambda + d\lambda)$$

If diffraction angle is increased by a small amount, then $(d\theta)$

the path difference of secondary wave-length between A and c will

increased $\frac{\lambda}{N}$.



$$\therefore (a+b) \sin(\theta_n + d\theta) = n\lambda + \frac{\lambda}{N}$$

$$n(\lambda + d\lambda) = n\lambda + \frac{\lambda}{N}$$

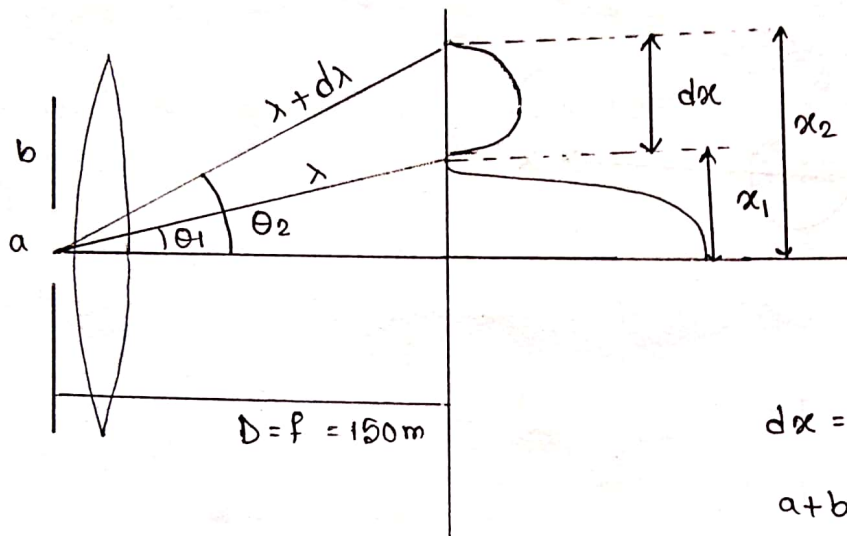
$$\therefore \frac{\lambda}{d\lambda} = nN$$

↓
resolving power.

Diffraction

18.1 - 18.7

Ex: 18.7



$$d x = x_2 - x_1$$

$$a + b = 1000 \text{ lines/cm}$$

$$(a+b) \sin \theta_n = n \lambda$$

$$(a+b) \sin \theta_1 = \lambda_1$$

$$\Rightarrow \theta_1 = 30^\circ$$

similarly,

$$(a+b) \sin \theta_2 = \lambda_2$$

$$\Rightarrow \theta_2 = 31.3^\circ$$

$$\tan \theta_1 = \frac{x_1}{f}$$

$$\Rightarrow x_1 =$$

$$\tan \theta_2 = \frac{x_2}{f}$$

$$\Rightarrow x_2 =$$

$$\therefore x_2 - x_1 = f (\tan \theta_2 - \tan \theta_1)$$

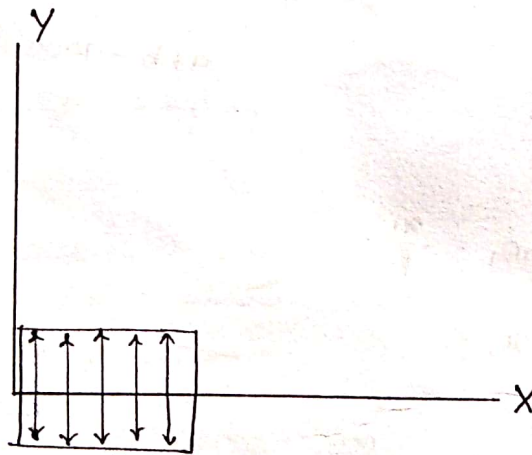
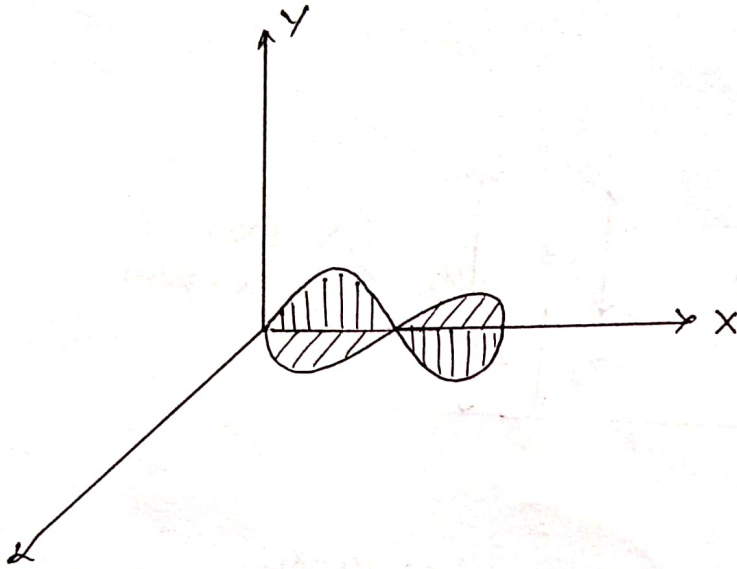
$$= 4.7 \text{ cm}$$

(Ans)

Ex: 19.1, 19.6

Polarization:

$$c = f\lambda$$

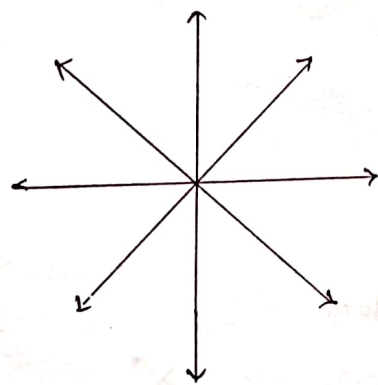


The vibrating electric field vector and the direction of propagation of the wave constitute a plane. There is an infinite number of such planes around the direction of propagation. In an ideal light wave the vibration of electric field vectors ^{are} confined to a single plane.

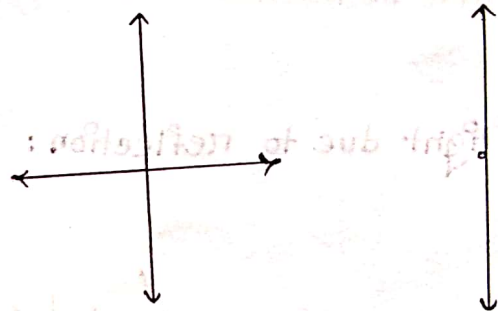
Unpolarised light: A light wave in which \vec{E} -vector oscillates in more than one plane, is referred to as unpolarized light. Ex - sun, candle, Na light

polarized light: Polarized light is the light wave that only fluctuate in one specific plane.

The plane created by the direction of propagation oscillation of \vec{E} -vector and the direction of propagation, this is known as plane of polarization.



unpolarized light

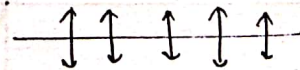


• → polarization to the plane of paper

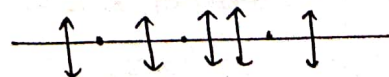
↕ → parallel " " "

• → s-component

↕ → p-component



polarized light



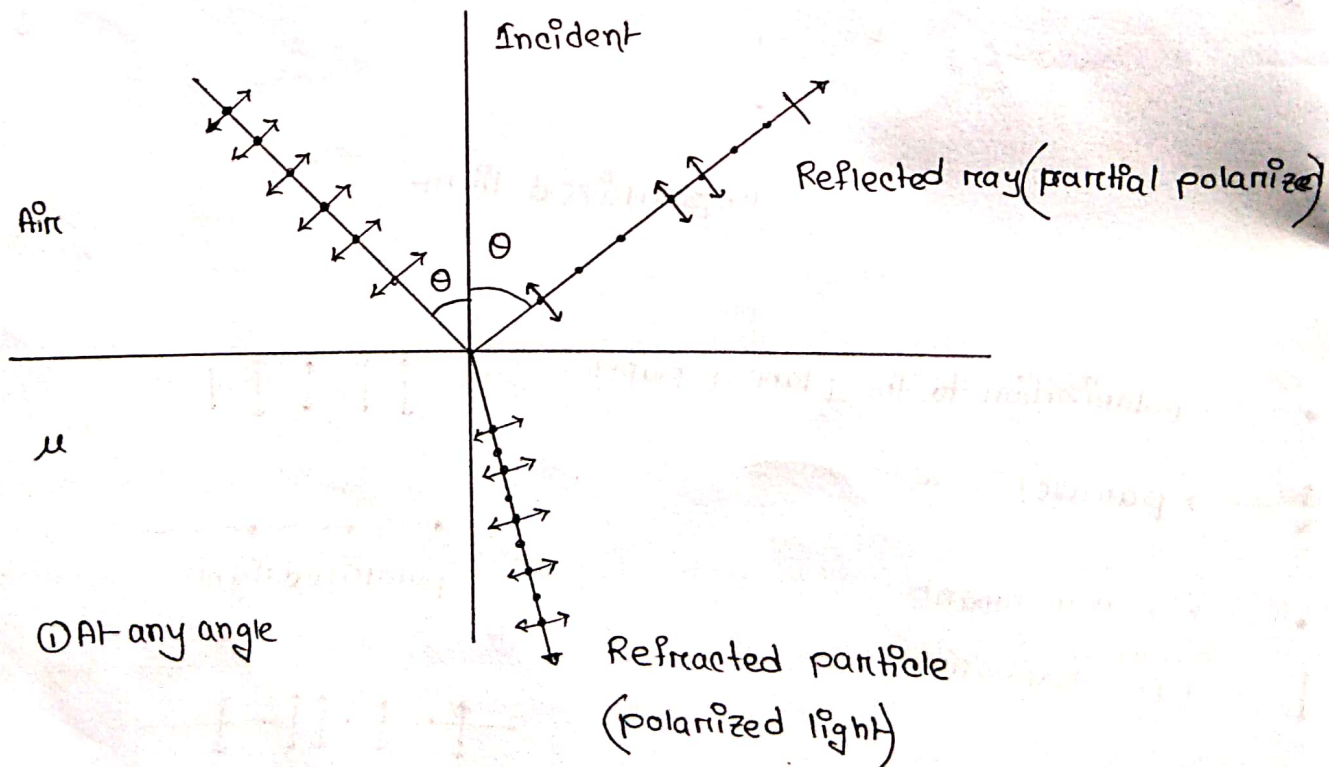
partial polarized light

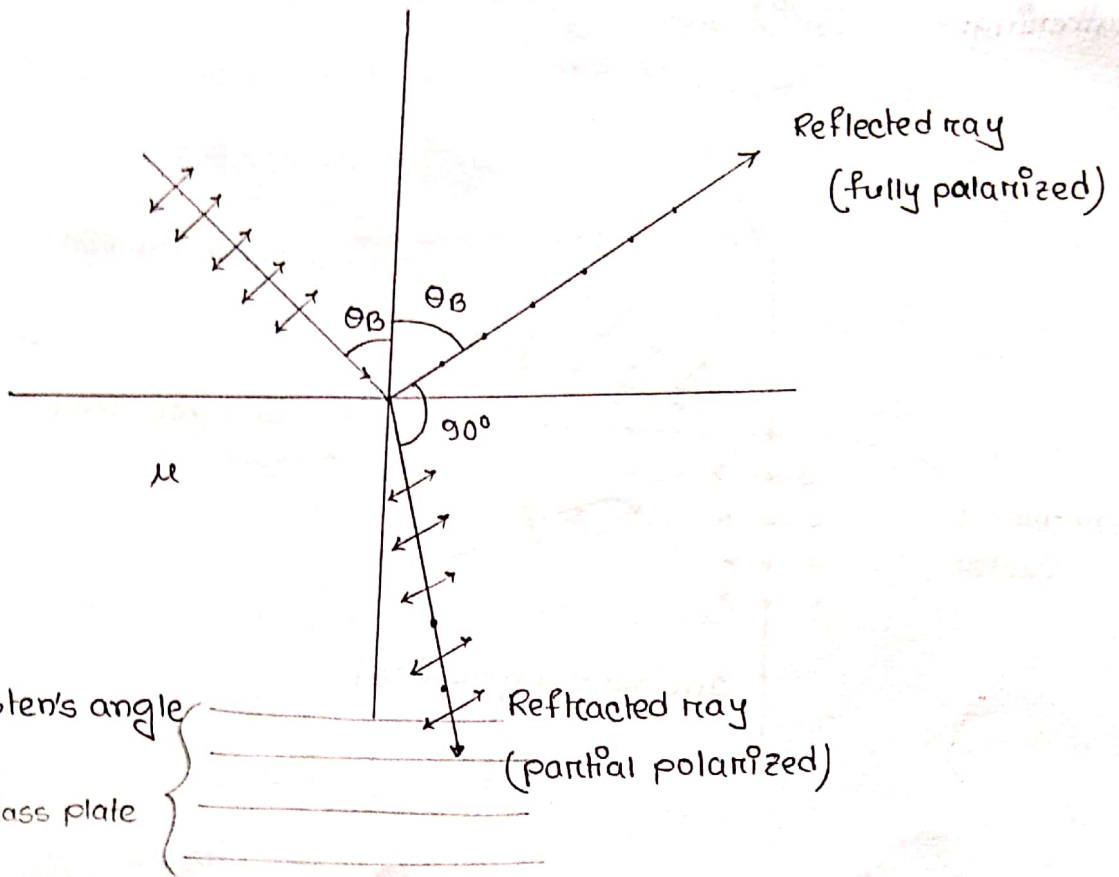
plane polarized light: Oscillation occur in a single frame plane.
the oscillation of \vec{E} vector are strictly confined to a single plane.

production of plane polarized light:

- (i) Reflection
- (ii) Refraction
- (iii) Scattering
- (iv) Selective absorption
- (v) Double refraction.

polarized light due to reflection:





① At Brewster's angle
pile of glass plate

Refracted ray
(partial polarized)

Reflected ray
(fully polarized)

Brewster's law:

$$\mu = \tan \theta_B = \frac{\sin \theta_B}{\cos \theta_B} \quad \text{--- (i)}$$

From Snell's eqn

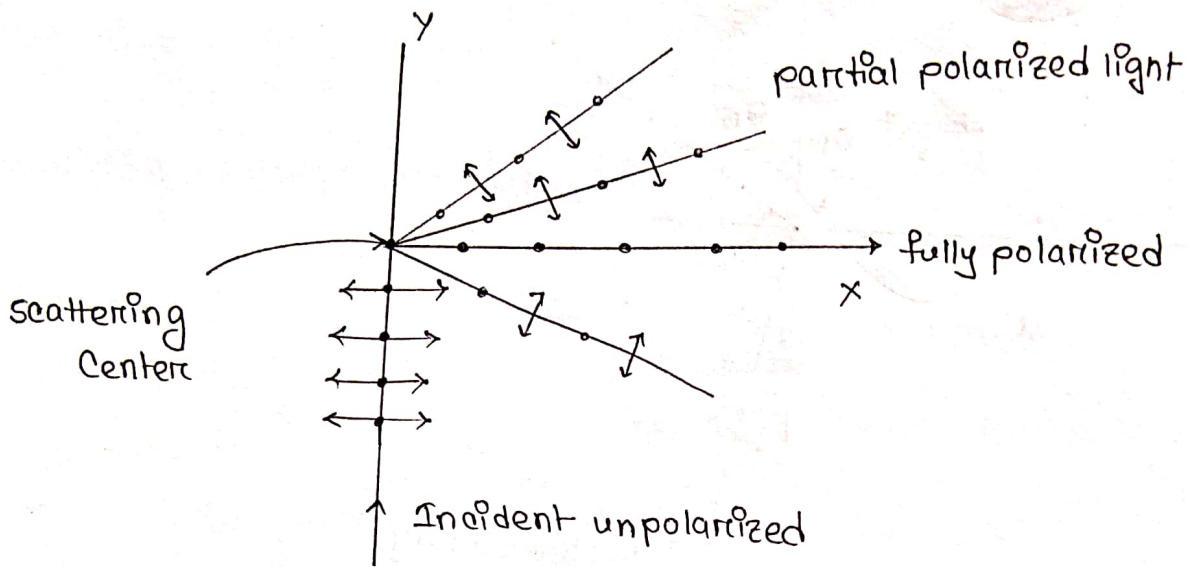
$$\mu = \frac{\sin i}{\sin r} = \frac{\sin \theta_B}{\sin \pi} \quad \text{--- (ii)}$$

$$\therefore \cos \theta_B = \sin \pi = \cos \left(\frac{\pi}{2} - \pi \right)$$

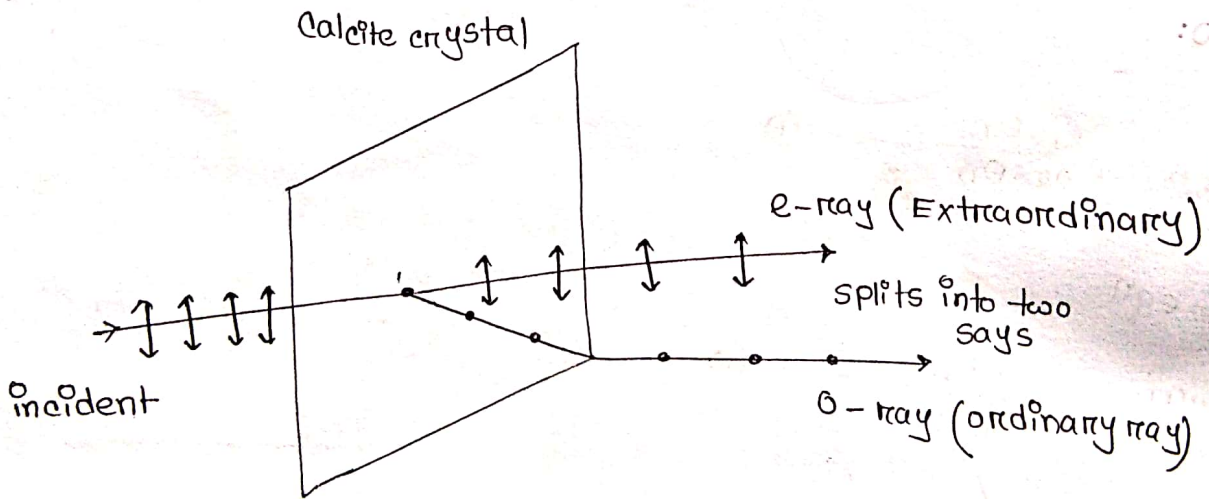
$$\Rightarrow \theta_B + \pi = \frac{\pi}{2}$$

At an Brewster's angle a reflected and a refracted ray are perpendicular to each other.

Scattering: (বিচ্ছিন্ন)



Double refractive:

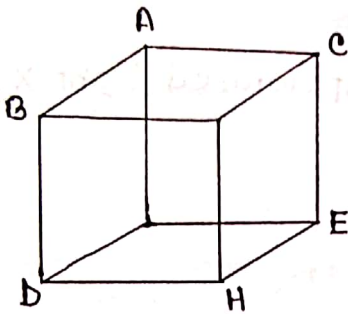


It is also known as bi-refringes

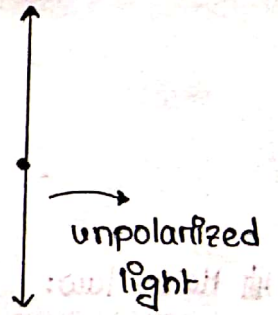
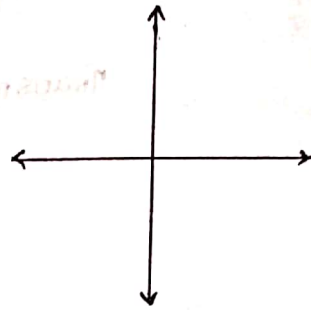
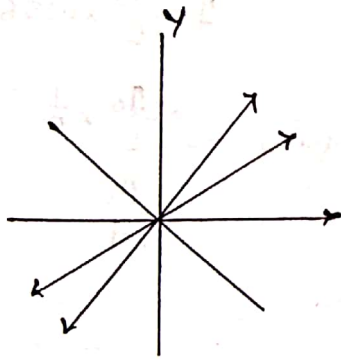
↳ different refractive angle of different polarization.

Polarizer: A polarizer is an optical element which utilize the phenomenon of selective absorption or double refraction and transform unpolarized light into polarized light. Plane polarized light is obtained by eliminating one of the two components in the unpolarized light.

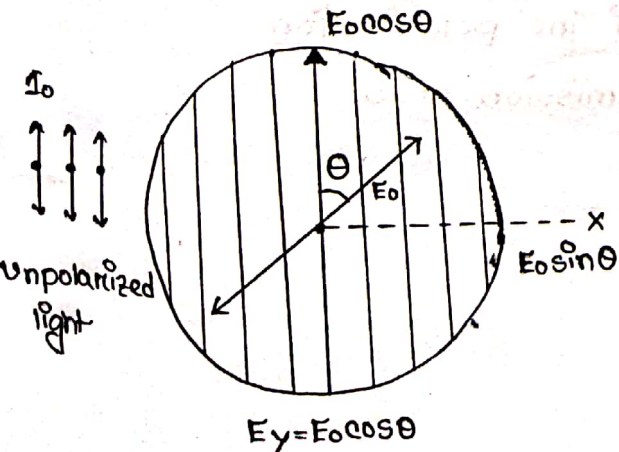
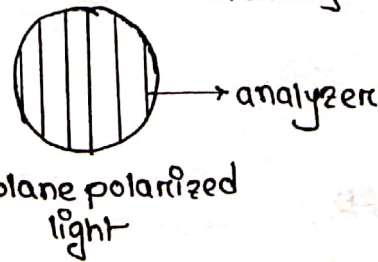
Optic axis:



Calcite crystal (CaCO_3)



$I = \frac{1}{2} I_0 \rightarrow$ unpolarized intensity



[polarized light is a light with one component and plane, and light is plane and axis, and sin component is not.]

$$I \propto E_y^2$$

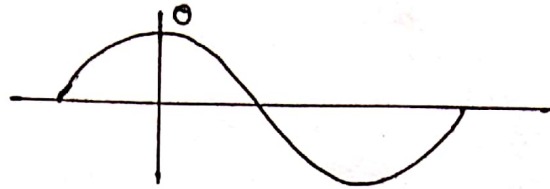
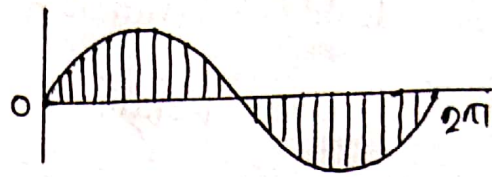
$$I = E_0^2 \cos^2 \theta$$

$$I = I_0 \cos^2 \theta$$

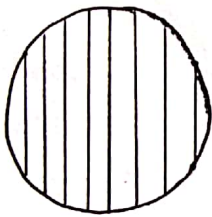
$$I = \frac{I_0}{2\pi} \int_0^{2\pi} \cos^2 \theta$$

$$= \frac{1}{2} I_0$$

I = polarized light intensity



Intensity of polarized light = Intensity of unpolarized light $\times \frac{1}{2}$



I



Transmission 60° axis

$$I = \frac{I_0}{2} \times \cos 60^\circ$$

$$= \frac{I_0}{2} \times \frac{1}{2}$$

$$= \frac{I_0}{4}$$

Malus law:

The intensity of polarized light is the square cosine angle between the plane of the polarization and transmission axis.

$$I = \frac{1}{2} I_0 \cos^2 \theta$$

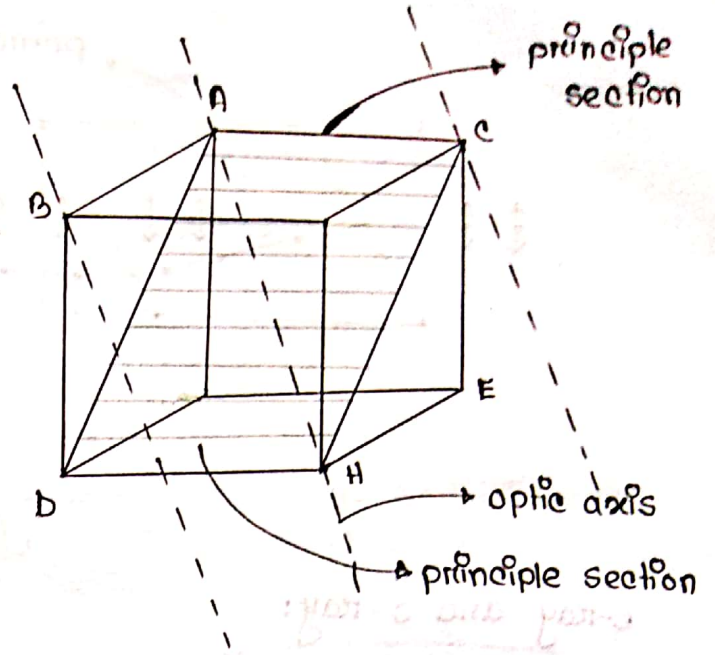
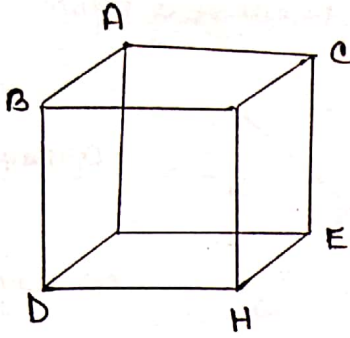
If $\theta = 0^\circ, \quad I = \frac{1}{2} I_0$

$\theta = 90^\circ, \quad I = 0$

$\theta = 180^\circ, \quad I = \frac{1}{2} I_0$

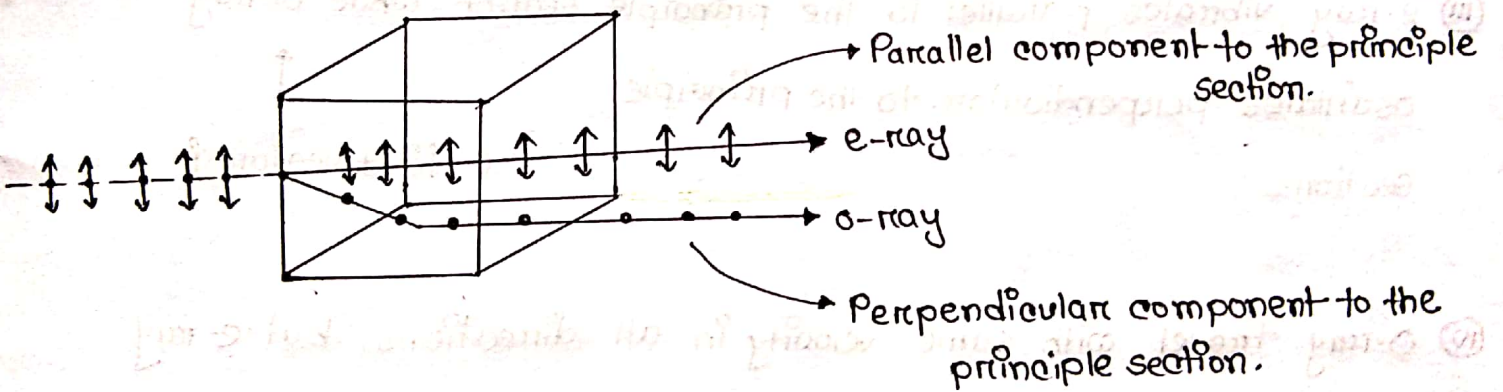
$\theta = 270^\circ, \quad I = 0$

Optic axis:



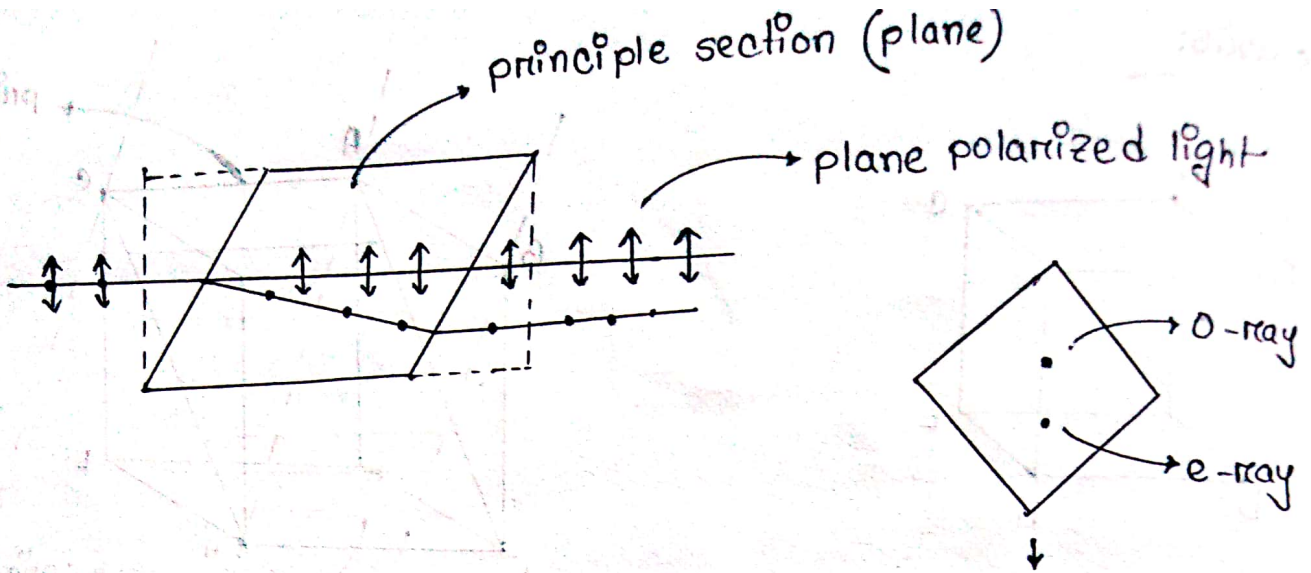
[plane of optic axis is parallel]

Double refraction:

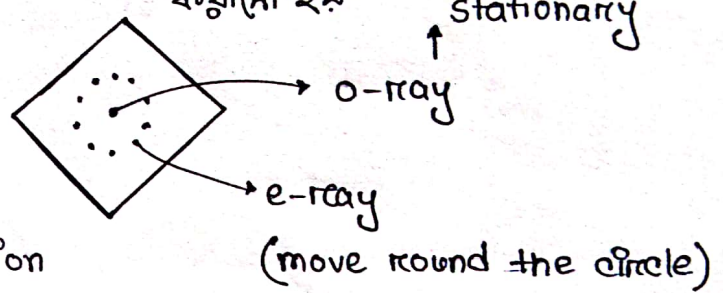


Anisotropic \rightarrow Different Physical Values.
Different direction/axis.

Physical value \rightarrow Heat, conductance, resistance
পরিবর্তন হবে না



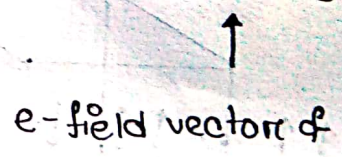
যদি plane টাকে move
করা মোহর



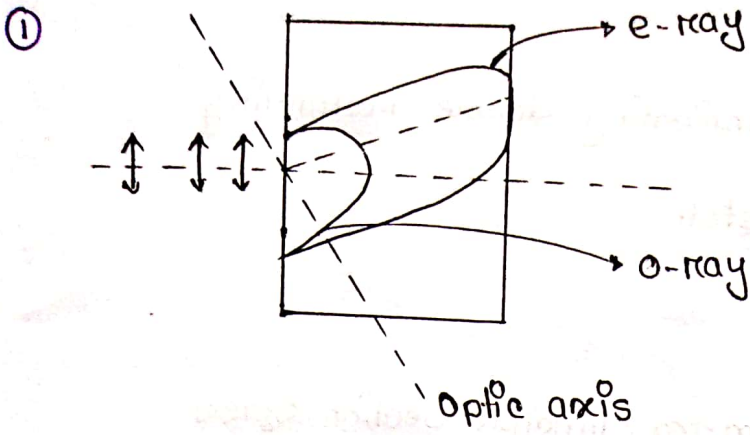
e-ray and o-ray:

- ① Both rays are plane polarized.
- ② O-ray follow the law of refraction but e-ray doesn't follow the law of refraction.

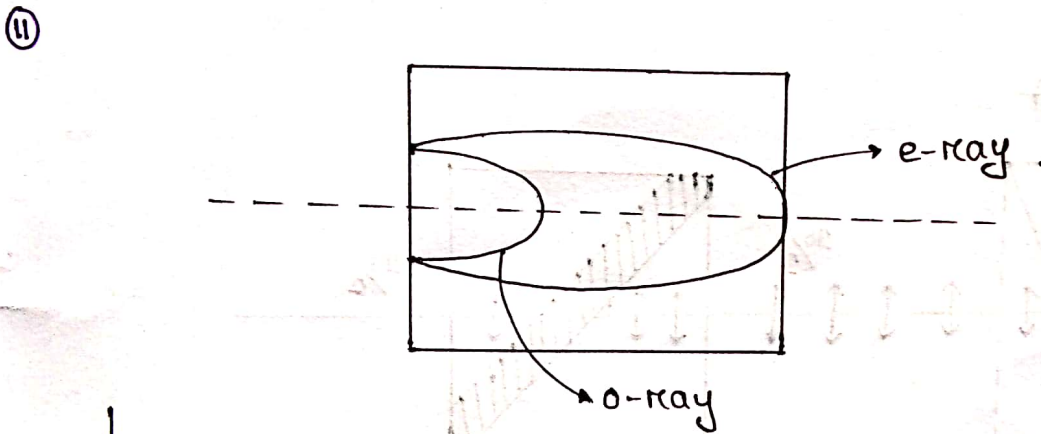
③ e-ray vibrates parallel to the principle section while o-ray oscillates perpendicular to the principle section.



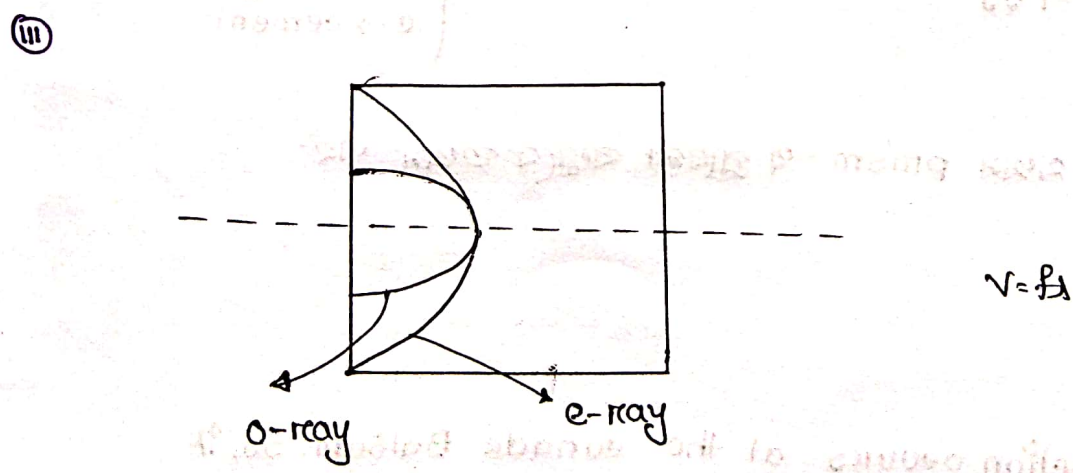
④ O-ray travel with same velocity in all directions, but e-ray travel with different velocity in different directions.



At any angle θ , o-ray and e-ray have different velocity and different direction.



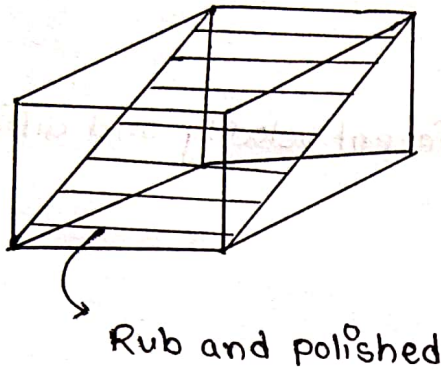
⊥
different velocity same direction.



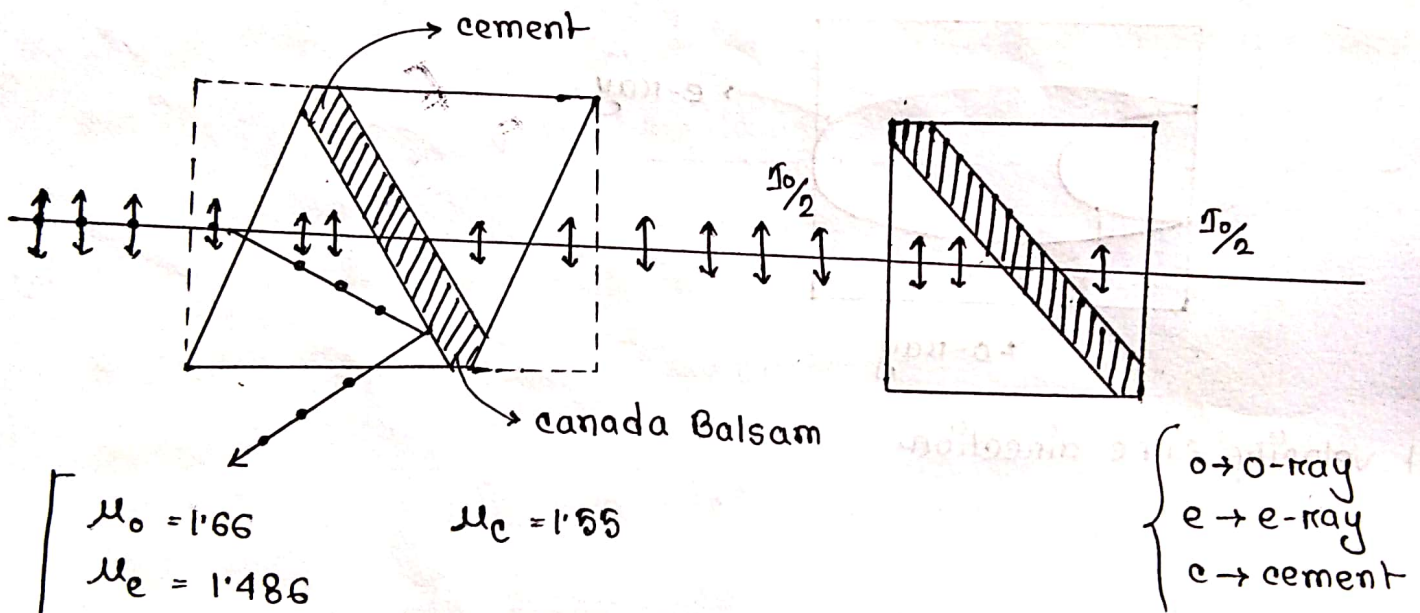
same velocity
same directions

Nicol Prism:

Nicol prism is a polarizing device fabricating double refracting crystal. It is made for calcite crystal.



→ prism কে principle section বঙ্গাবর
কর্তন করলে ২টি prism পাওয়া থাকে।
যাদের তলকে rub and polished করা হয়।



$$\mu_o = 1.66$$

$$\mu_c = 1.55$$

$$\mu_e = 1.486$$

$\left\{ \begin{array}{l} o \rightarrow o\text{-ray} \\ e \rightarrow e\text{-ray} \\ c \rightarrow \text{ciment} \end{array} \right.$

o-ray and e-ray যখন prism-এ প্রবেশ করবে তখন এই index show করবে।

$$\text{As, } \mu_o > \mu_c$$

The total internal reflection occurs at the Canada Balsam, so, it reflects at Canada Balsam. Hence Nicol prism acts as a polarizer and an analyzer.

Specific rotation:

Rotation of plane polarized light:

$$\begin{aligned} R &\propto l \\ R &\propto \frac{1}{A} \\ R_i &\propto \frac{l}{A} \\ R &= \rho \frac{l}{A} \end{aligned}$$

1) $\theta \propto l$ [Thickness of the substance or length of solution.]

$\theta \propto c$ [Concentration of solution or density of substance.]

$\theta \propto$ depends on λ

$\theta \propto$ Temperature T

At a given λ and T [constant]

$$\theta \propto lc$$

$$\theta = slc$$

\rightarrow rotation constant (specific rotation)

$$S = \frac{\theta}{lc}$$

\rightarrow dm

$$S = \frac{100\theta}{lc}$$

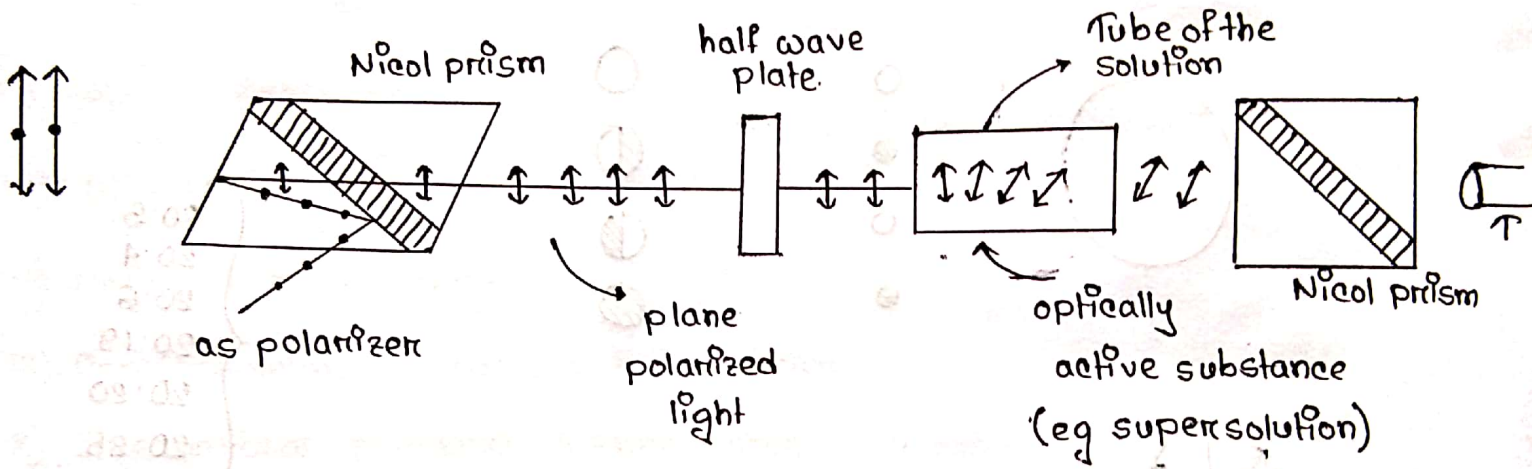
\rightarrow cm

$l \rightarrow$ dm

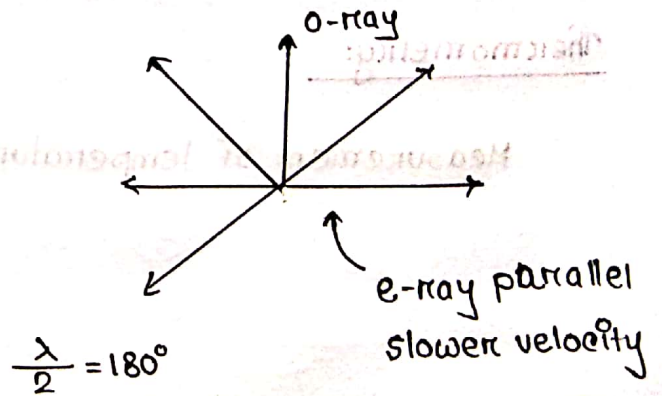
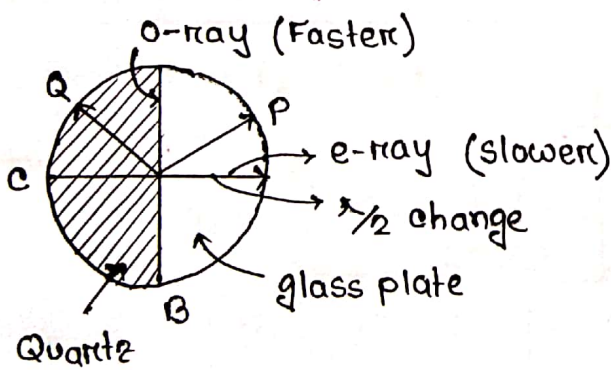
$c \rightarrow$ gm/cc

A specific rotation for a given wavelength or given temperature is defined as the rotation produced by 1 dm length of the solution containing 1 g of optically active material per cc solution.

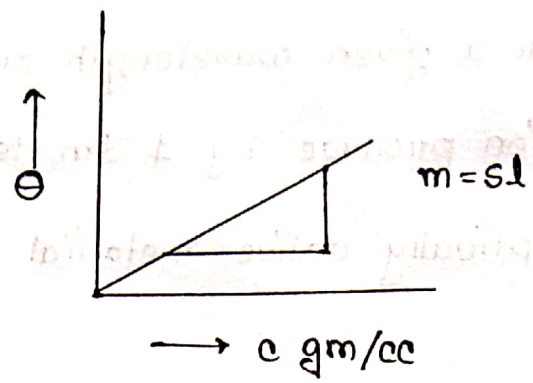
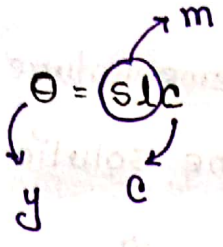
Laurent's half shade polarimeter:



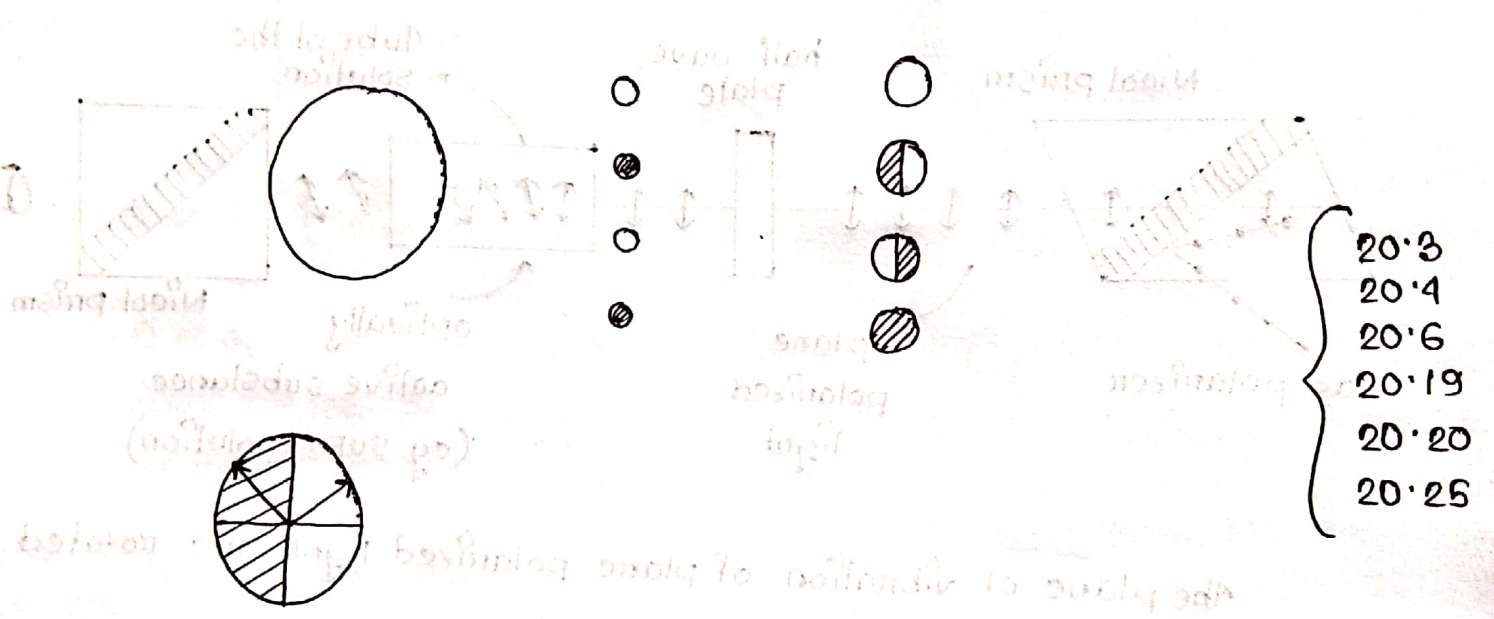
The plane of vibration of plane polarized light are rotated by solution.



- (i) If parallel to OP
- (ii) parallel to the OQ
- (iii) Parallel to AB
- (iv) Parallel to CB

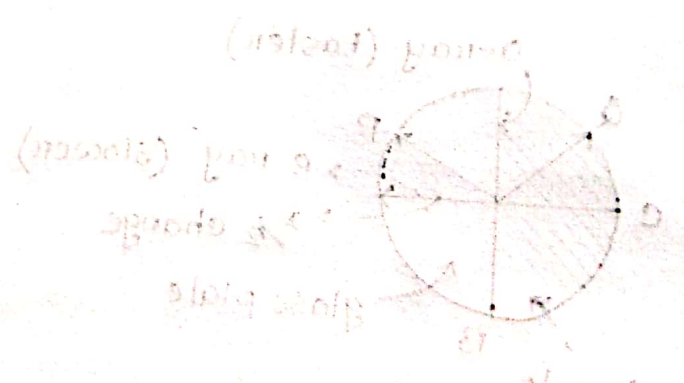


half shade device क्या use क्यों ?



Thermometry:

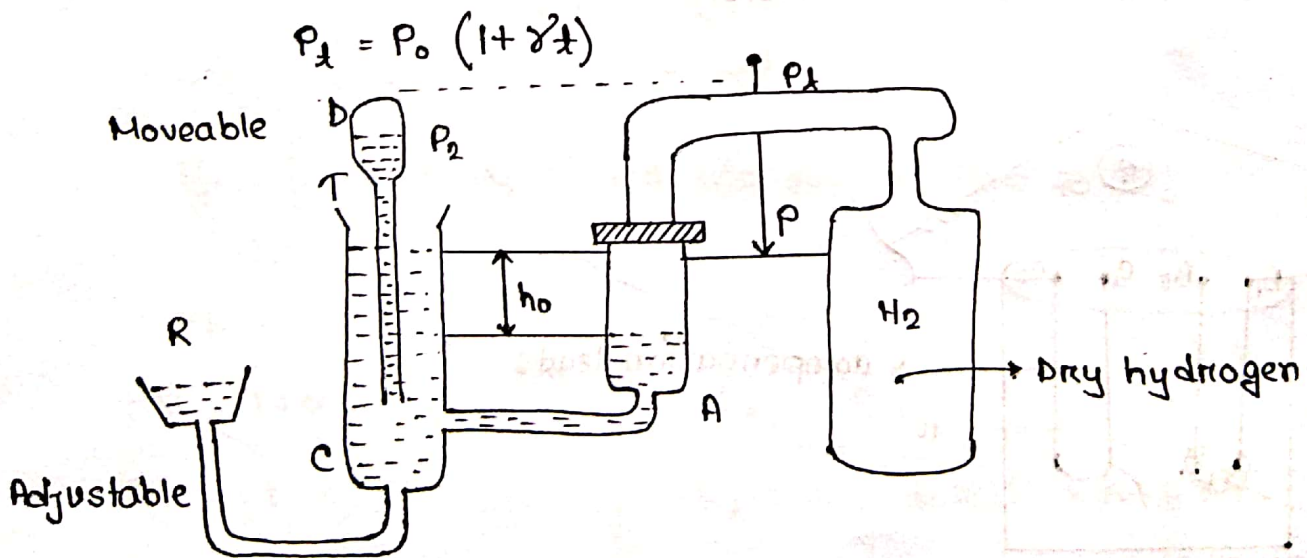
Measurement of temperature:



Types of thermometry:

- i) Liquid thermometer.
- ii) Gas thermometer.
- iii) Resistance "
- iv) Thermo-electric "
- v) Radiation "
- vi) Vapour pressure
- vii) Bimetallic "
- viii) Magnetic susceptibility
- ix) Constant volume hydrogen thermometer.
- x) International standard thermometer.
- xi) Volume constant "

Change in pressure with temperature:



$$1) P_0 = h_0 + P$$

↳ atmospheric pressure

$P_0 = 0^\circ$ temperature & pressure

$$ii) P_{100} = P_0 (1 + 100\gamma)$$

$$P_t = P_0 (1 + \gamma t)$$

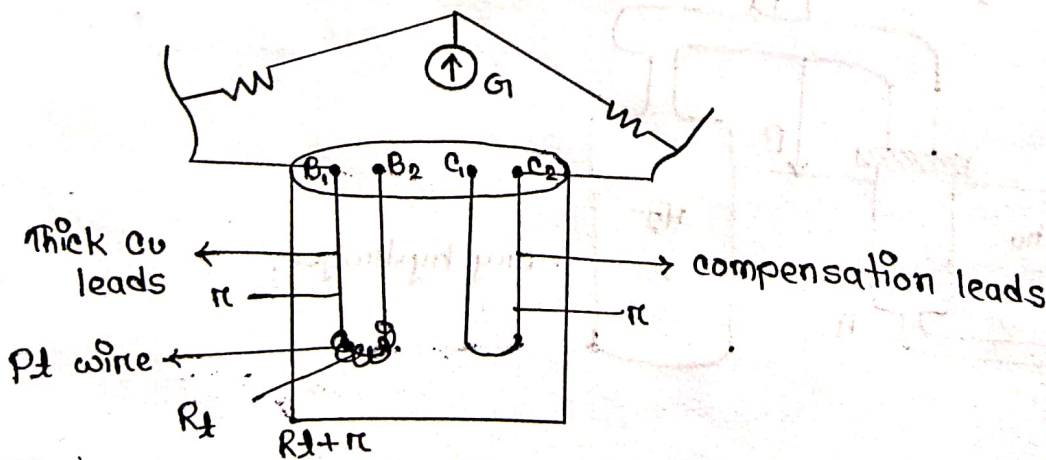
$$P_t - P_0 = P_0 \gamma t$$

$$P_{100} - P_0 = P_0 \gamma 100$$

$$t = \frac{P_t - P_0}{P_{100} - P_0} \times 100$$

Pt Resistance thermometer:

Change in resistance with temperature:



$$R_t = R_0 (1 + \alpha t + \beta t^2)$$

$$R_t = R_0 (1 + \alpha t)$$

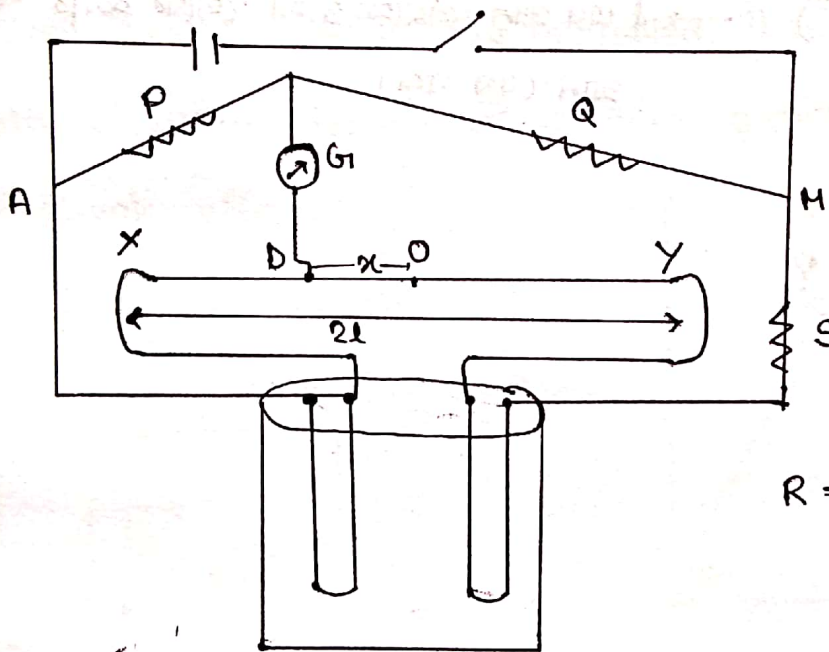
$$R_{100} = R_0 (1 + 100\alpha)$$

$$R_t = R_0 (1 + \alpha t)$$

$$\rightarrow t = \frac{R_t - R_0}{R_{100} - R_0} \times 100$$

Callender and Griffith bridge:

Wheatstone's bridge used to measure resistance.



$R = A$ (যেখানে D)

$$\frac{P}{Q} = \frac{R}{S} \quad [\text{যদি } G_1 \text{ এর মধ্যে current flow না হয়}]$$

$$XD = l - x$$

$$DY = l + x$$

$$R_{XD} = (l - x)p$$

$$R_{DY} = (l + x)p$$

$$P = Q$$

$$R_{AD} = R_{ND}$$

$$R_t + r + (l - x)p = r + s + (l + x)p$$

$$R_t = s + 2xp$$

Advantage and disadvantage of platinum resistance thermometer:

$$R_t = R_0 + \alpha R_0 \rho$$

The resistance of Pt wire of $0^\circ\text{C} \rightarrow R_0 = 5.5 \Omega$

" " " " at $100^\circ\text{C} \rightarrow R_{100} = 7.5 \Omega$

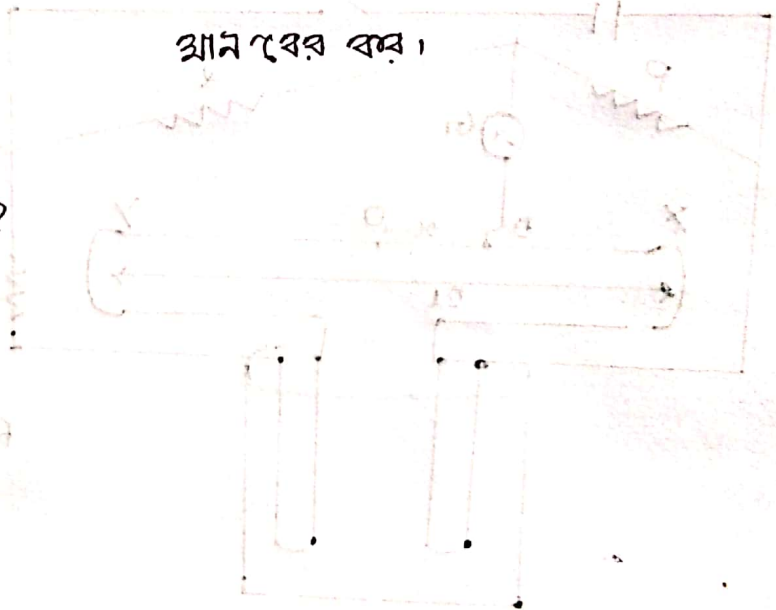
" " " " at $444.6^\circ\text{C} \rightarrow R_{444.6} = 14.5 \Omega$

$$R_t = R_0 (1 + \alpha t + \beta t^2) \rightarrow t \text{ এর মান বন্ধির অর্থাৎ } t \text{ হোক } \alpha, \beta \text{ এর}$$

$$3.62 \times 10^{-3} / ^\circ\text{C}$$

$$1.28 \times 10^{-7} / ^\circ\text{C}$$

$$\left. \begin{array}{l} \alpha = ? \\ \beta = ? \end{array} \right\}$$



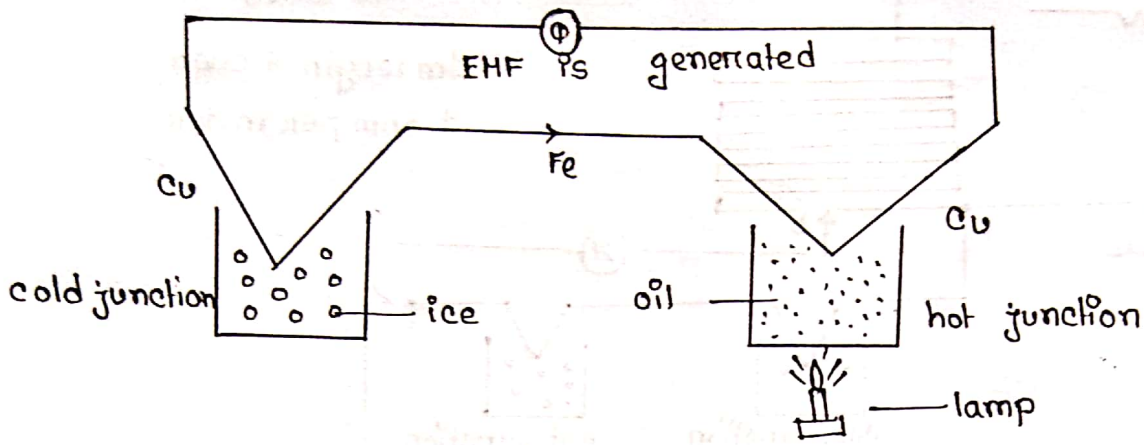
Thermocouple:

Two dissimilar metals

Two junctions

One junction is kept at cold and other junction is kept at hot.

Current flows

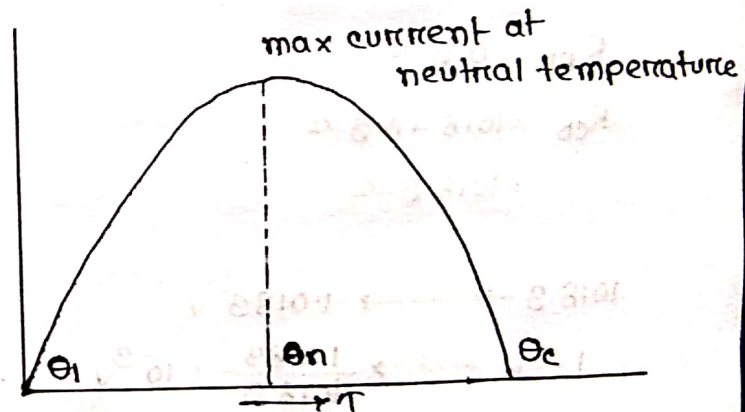
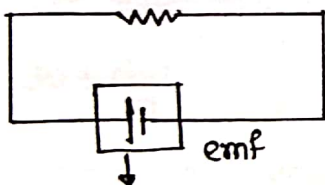


at cold junction current flows from Cu to Fe.

at hot " " " " Fe to Cu.

The current flows in this way is called thermo electricity.

Thermoelectromotive force - এই current generate করে। এই effect এর নাম Seebeck effect.

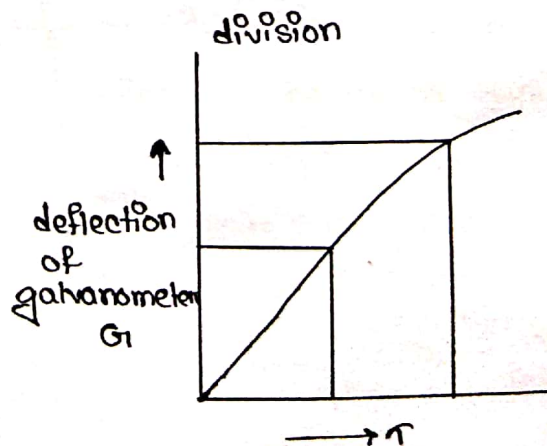


Higher voltage থেকে deflection or emf or current lower voltage এর চিহ্নে আসে।

+10 0 -10

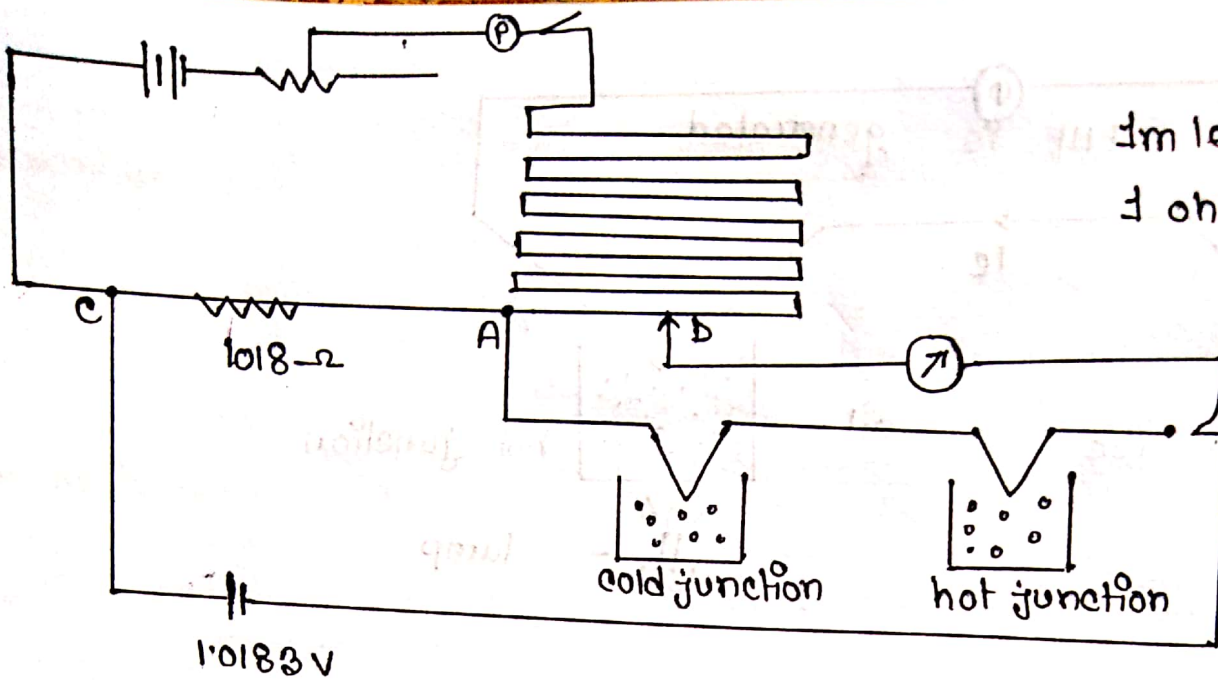
$$\text{Neutral temp. } \theta_n = \frac{\theta_c + \theta_e}{2}$$

- i) using galvanometer
- ii) using potentiometer.

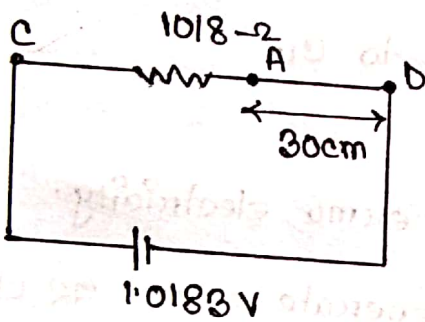


10 wires

1m length of each
1 ohm per meter.



1.0183 V



100 cm \rightarrow 1 Ω

30 cm \rightarrow 0.3 Ω

1.0183 V

$$R_{AB} = 0.3 \Omega$$

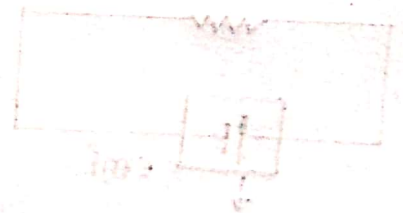
$$R_{CB} = 1018 + 0.3 \Omega$$

$$= 1018.3 \Omega$$

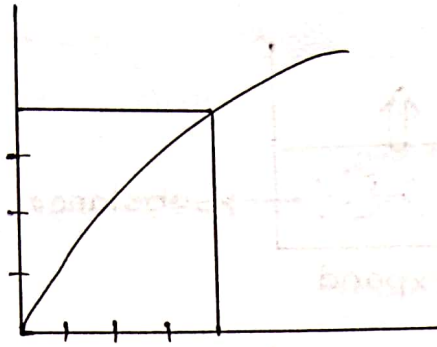
$$1018.3 \Omega \rightarrow 1.0183 \text{ V}$$

$$1 \Omega \rightarrow \frac{1.0183}{1018.3} = 10^{-3} \text{ V}$$

1m wire \rightarrow 1 volt 10^{-3} V
1mm \rightarrow 10^{-6} V



2nd Case:



Zeroth law of thermodynamics:

↳ Deals with transferring of heat from one place to another place.

equilibrium systems: A B C

A → B - equilibrium.

Joule law: First law of thermodynamics,

$$\Delta H = \Delta U + \Delta W$$

$$dH = dU + dW$$

↳ work

→ Increase the internal energy.

Applied heat

$$W = F \cdot dx$$

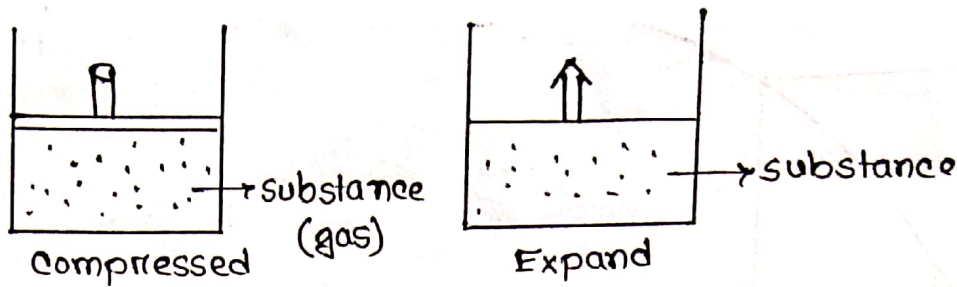
$$= P \cdot A \cdot dx$$

$$= P \cdot dV$$

$$dW = \int_{V_1}^{V_2} P \cdot dV$$

$$P = \frac{F}{A} \text{ Nm}^{-2}$$

↳ Area of the cross section.



Work done on the system.

Work done by the system.

Isothermal Process:

The system is perfectly conduction to the surroundings.

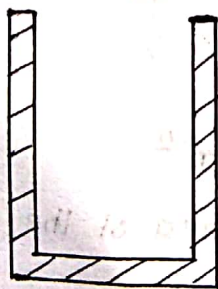
Temperature remain constant when pressure is increased.

When the pressure is increased, temperature increases.

Since the system is perfectly conducting to the surrounding, so the system rejects heat to the surrounding. So, the temperature remain constant through the process.

Adiabatic process:

No heat is transferred.



perfectly insulated.

$$dH = dU + dW$$

i) $PV^\gamma = \text{constant}$

$\gamma \rightarrow \text{constant}$

ii) $\tau V^{\gamma-1} = \text{constant}$

iii) $\frac{P^{\frac{1}{\gamma}}}{\tau^{\frac{1}{\gamma}}} = \text{constant}$

Slope of Isothermal and adiabatic:

$PV = \text{constant} = K$

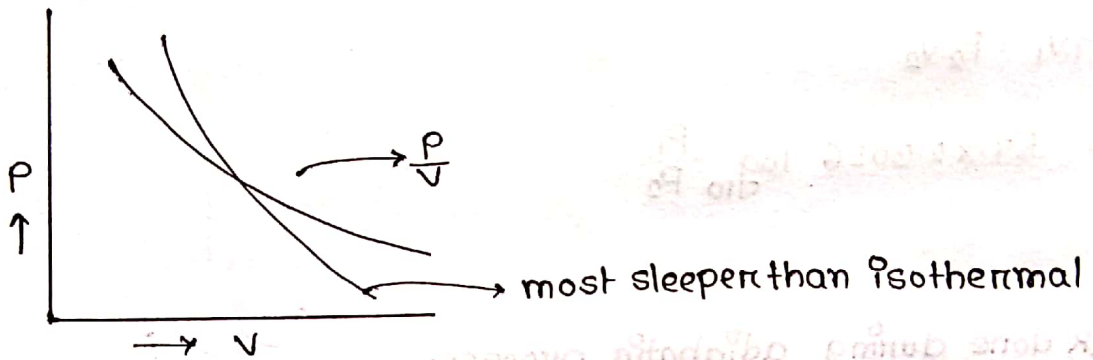
$PV^\gamma = K$

$Pdv + vdp = K$

$\gamma PV^{\gamma-1} dv + vdp = 0$

$\frac{dp}{dv} = -\frac{P}{V}$

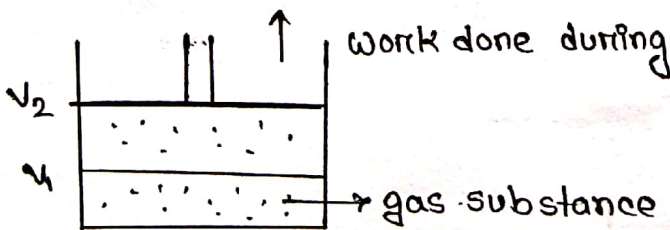
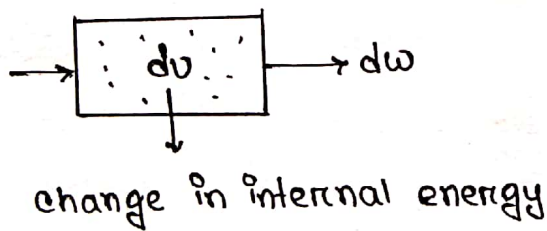
$\frac{dp}{dv} = -\gamma \frac{P}{V} \quad [\gamma > 1]$



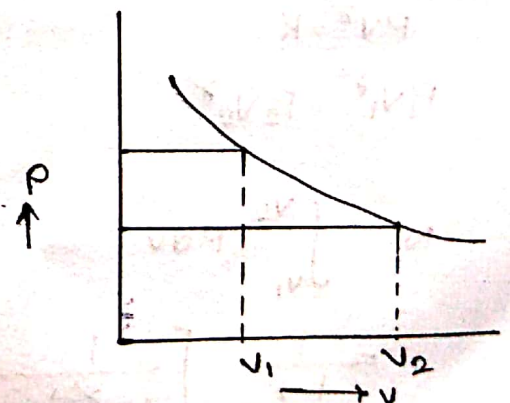
G.I. → assignment

1st law of Thermodynamics:

$dH = dU + \int_{V_1}^{V_2} Pdv$



$dH = dU + Pdv$
 $0 \leftarrow dU = -Pdv$
 $= -dW$



$W = \int_{V_1}^{V_2} Pdv$

$$\# PV = RT$$

$$\Rightarrow P = \frac{RT}{V}$$

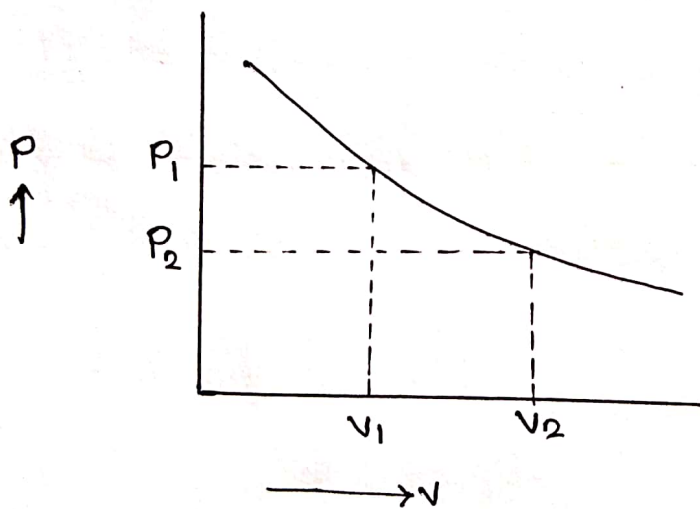
$$\# N = RT \ln \frac{V_2}{V_1}$$

$$= RT \times 2.303 \log_{10} \frac{V_2}{V_1}$$

$$\# P_1 V_1 = P_2 V_2$$

$$W = RT \times 2.3026 \log_{10} \frac{P_1}{P_2}$$

Work done during adiabatic process:



$$PV^\gamma = K$$

$$P_1 V_1^\gamma = P_2 V_2^\gamma$$

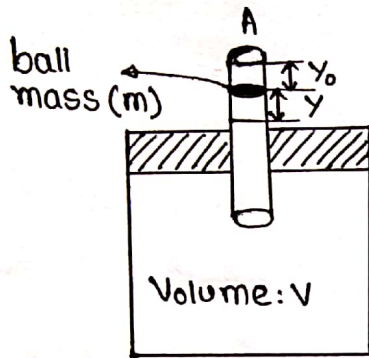
$$N = \int_{V_1}^{V_2} P dv$$

$$= \frac{1}{1-\gamma} \left[\frac{1}{V_2^{\gamma-1}} - \frac{1}{V_1^{\gamma-1}} \right]$$

$$= \frac{1}{1-\gamma} [P_2 V_2 - P_1 V_1]$$

$$= \frac{1}{1-\gamma} R (\tau_2 - \tau_1)$$

Rachhard's experiment:



$$PV^\gamma = K$$

$$\gamma V^{\gamma-1} P dV + V^\gamma dp = 0$$

$$\gamma P dV + V dp = 0$$

$$\gamma P \gamma A + \frac{V F}{A} = 0$$

$$F = \frac{\gamma P A^2}{V} y$$

$$F = m \frac{d^2 y}{dt^2}$$

to find γ

$$P = P_0 + \frac{mg}{A}$$

$$dV = \gamma A$$

$$dp = \frac{F}{A}$$

simple harmonic motion.

$$\frac{d^2 y}{dt^2} + \frac{\gamma P A^2}{V m} y = 0$$

here,

$$\omega^2 = \frac{\gamma P A^2}{V m}$$

$$\Rightarrow \frac{4\pi^2}{T^2} = \frac{\gamma P A^2}{V m}$$

$$\Rightarrow \gamma = \frac{4\pi^2 V m}{T^2 P A^2}$$

Second law of thermodynamics:

↳ heat transferred

Reversible process:

- There should not be any loss of heat due to friction or radiation.
- System may slow rate.
- The system retraced back.

Irreversible process:

- Heat loss due to friction or conductor.
- fast rates
- cannot retrace back.

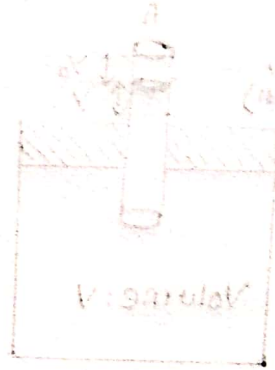
↳ high temp. — low temp.

Kelvin-planck:

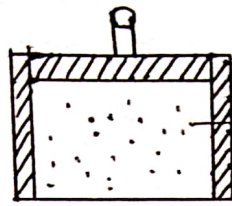
According to Kelvin-planck, It is impossible to continue supply of heat... (ଅର୍ଥ)

(heat supply ଅ(ଅର୍ଥ))

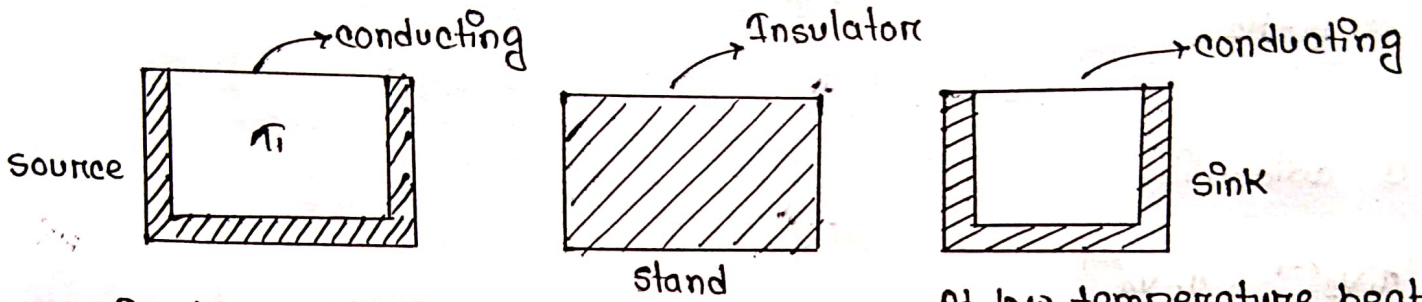
Consious:



Carnot's reversible engine:

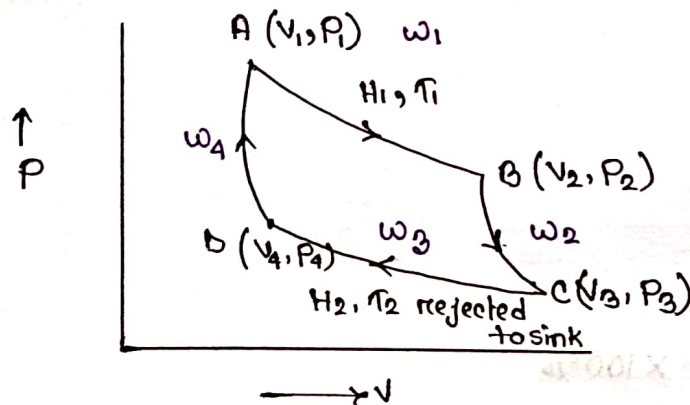


perfect gas as a working substance.



At high temperature engine absorbs heat

At low temperature heat rejects to the sink.



i) Work done during Isothermal (A to B) $\rightarrow w_1 = R\pi_1 \log \frac{V_2}{V_1}$

ii) " " " adiabatic (B to C) $\rightarrow w_2 = \frac{R[\pi_1 - \pi_2]}{1 - \gamma}$

$$N = \int_{V_1}^{V_2} P dv$$

iii) Work done during Isothermal (C to D) $\rightarrow w_3 = -R\pi_2 \log \frac{V_3}{V_4}$

iv) " " " adiabatic (D to A) $\rightarrow w_4 = -\frac{R(\pi_1 - \pi_2)}{1 - \gamma}$

The net work during cycle, $W = W_1 + W_2 + W_3 + W_4$

$$\therefore W = R\pi_1 \log \frac{V_2}{V_1} - R\pi_2 \log \frac{V_3}{V_4}$$

$$= R [\pi_1 - \pi_2] \log \frac{V_2}{V_1}$$

$$= H_1 - H_2$$

B to C adiabatic,

$$\pi_1 V_2^{\gamma-1} = \pi_2 V_3^{\gamma-1}$$

and A to D,

$$\pi_1 V_1^{\gamma-1} = \pi_2 V_4^{\gamma-1}$$

$$\therefore \frac{V_2}{V_1} = \frac{V_3}{V_4}$$

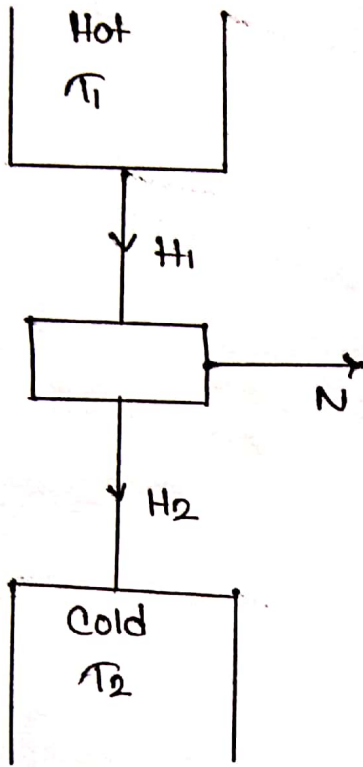
efficiency, $\eta = \frac{\text{Output}}{\text{Input}}$

$$= \frac{H_2 - H_1}{H_1} \times 100\%$$

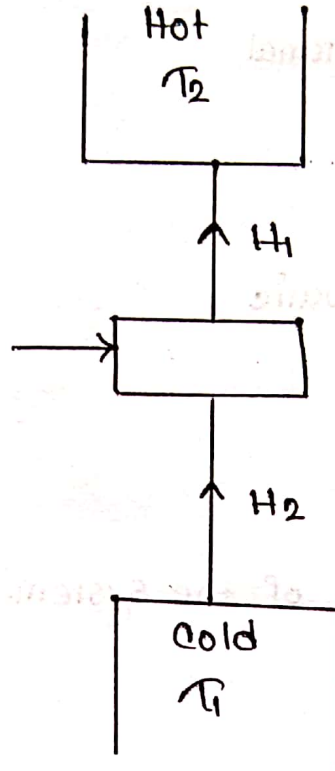
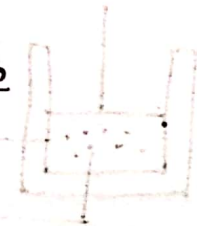
$$= \frac{R(\pi_1 - \pi_2) \log \frac{V_2}{V_1}}{R\pi_1 \log \frac{V_2}{V_1}}$$

$$= 1 - \frac{\pi_2}{\pi_1}$$

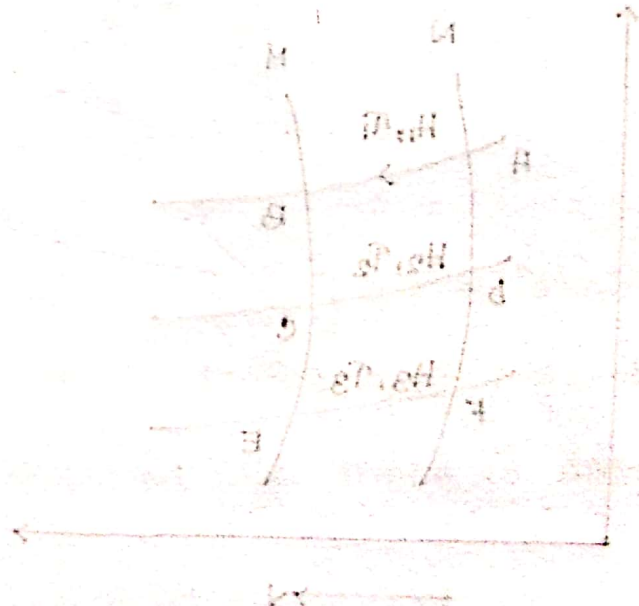
Carnot's engine and refrigerator:



Heat engine



refrigerator



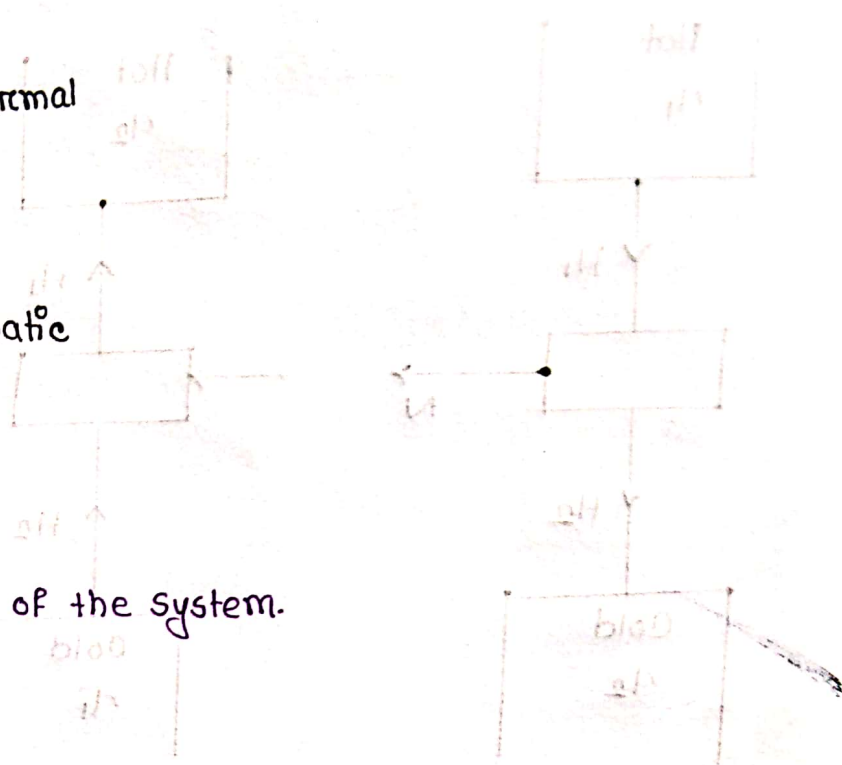
$$dW = \int_{V_1}^{V_2} \frac{PdV}{L} = 0$$

$dH = dW + dU \rightarrow$ Isothermal

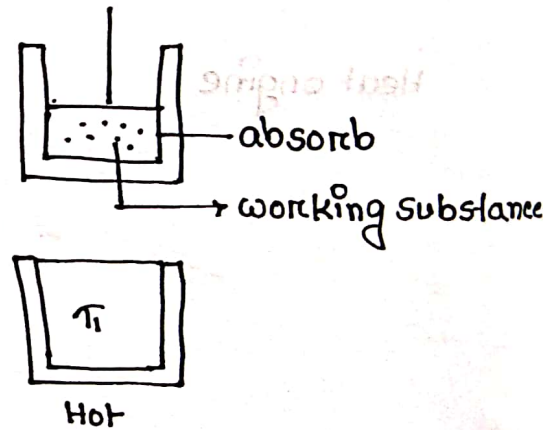
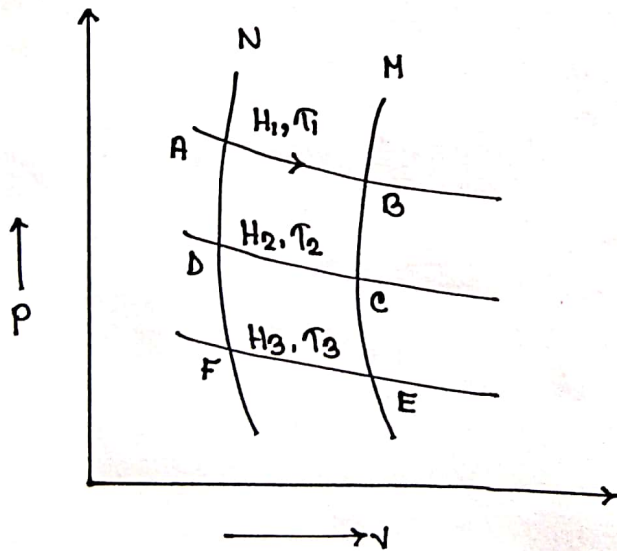
$PV = K$

$dH = dW + 0 \rightarrow$ Adiabatic

$PV^\gamma = K$



Entropy measuring disorder of the system.



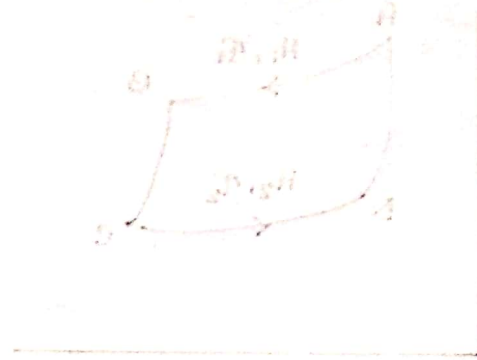
For ABCB

$$\frac{H_1}{T_1} = \frac{H_2}{T_2}$$

For CDEF

$$\frac{H_2}{T_2} = \frac{H_3}{T_3}$$

$$\therefore \frac{H_1}{T_1} = \frac{H_2}{T_2} = \frac{H_3}{T_3} = \text{constant}$$



(or) the loss in entropy of working substance (A to B)

The quantity H/T bet adiabatic process is constant and this is called the change in entropy.

$$S_2 - S_1 = \frac{\delta H}{T}$$

$$\text{change in entropy} \int ds = \frac{\delta H}{T} = \int_{T_1}^{T_2} \frac{\delta H}{T}$$

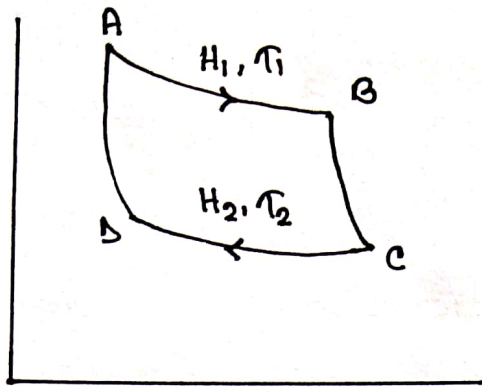
$$0 = \frac{dH}{dT} = \frac{\delta H}{dT} = \dots$$

Thus entropy remains constant is during an adiabatic reversible process. When heat is absorbed during a process, there is increase in entropy. when heat is rejected there is decrease in entropy.

(or) the loss in entropy in work body (A to B)

(or) the loss in entropy (A to B)

Changing entropy in a reverseable process:



The gain in entropy by working substance (A to B)

$$\frac{H_1}{T_1}$$

The lose in entropy (C to D) by working substance

$$\frac{H_2}{T_2}$$

$$\oint ds = \frac{H_2}{T_2} = \frac{H_1}{T_1} = 0$$

Changing entropy in a irreversible process:

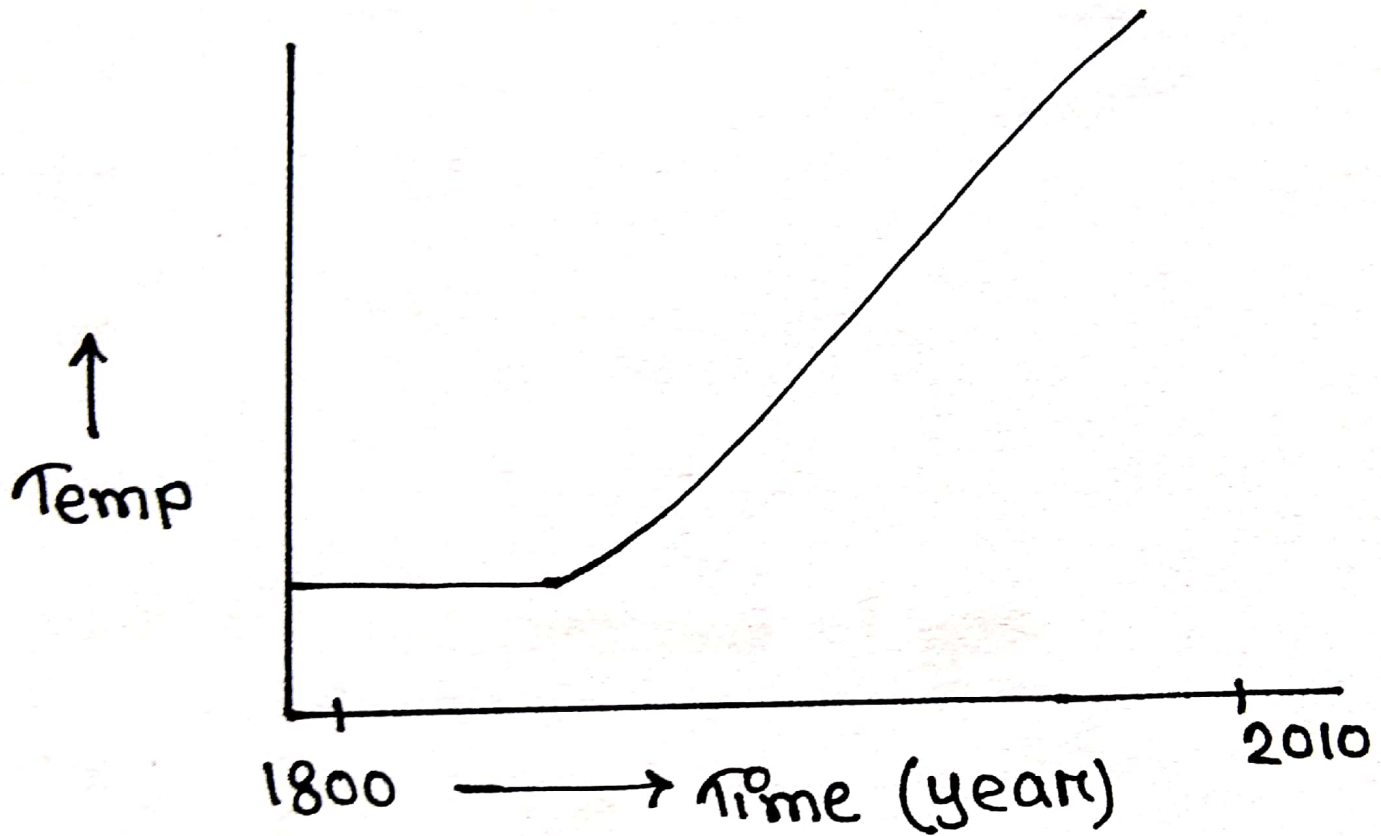
The lose in entropy in $\frac{\text{work}}{\text{hot}}$ body (A to B)

$$\frac{H}{T_1}$$

The gain in entropy (C to D)

$$\frac{H}{T_2}$$

$$ds = \frac{H}{T_2} - \frac{H}{T_1} = +ve$$



Third law of thermodynamics:

entropy \rightarrow disorder of the system

$$\frac{H_1}{T_1} \neq \frac{H_2}{T_2}$$

is not zero but +ve quantity

$$ds = \int_{T_1}^{T_2} \frac{\delta H}{T}$$

① $-10 \rightarrow 0$ $\delta H = ms \cdot \Delta T$

② $0 \rightarrow 0K$ $\delta H = 80$

③ $0 \rightarrow 100^\circ C$ $ds = \int_{T_1}^{T_2} \frac{\delta H}{T}$

④ $100 \rightarrow 100^\circ C$

$$ds_1 = \int_{T_1}^{T_2} \frac{ms \Delta T}{T}$$

change in entropy of the reservoir.

$$ds_2 = \frac{-\delta H}{T} = \frac{-ms \Delta T}{373}$$

$$ds_1 - ds_2 = 43.9 \text{ cal/K}$$

✓ # Kinetic theory of gas:

postulates:

(i)



(ii)



(iii)



Expressure for the pressure of gas.

$$p = \frac{1}{3} \rho c^2$$

$$p = \frac{M}{V}$$

$M \rightarrow$ Mass of gas of volume V .

$m \rightarrow$ mass of the each molecule.

$\rho \rightarrow$ density.

$$p = \frac{1}{3} \cdot \frac{M}{V} \cdot c^2$$

$$\Rightarrow pV = \frac{1}{3} Mc^2$$

$$pV = RT$$

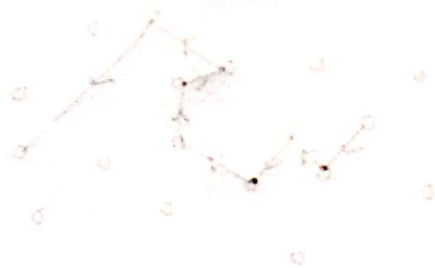
$$\Rightarrow \frac{1}{3} Mc^2 = RT$$

$$\Rightarrow \frac{1}{2} Mc^2 = \frac{3}{2} RT$$

let,

$$M = m \times N \quad (\text{For 1 mole gas})$$

$$\therefore \frac{1}{2} mNc^2 = \frac{3}{2} RT$$



$$\Rightarrow \frac{1}{2} mc^2 = \frac{3}{2} \left(\frac{R}{N}\right) T$$

$$\Rightarrow \frac{1}{2} mc^2 = \frac{3}{2} kT$$

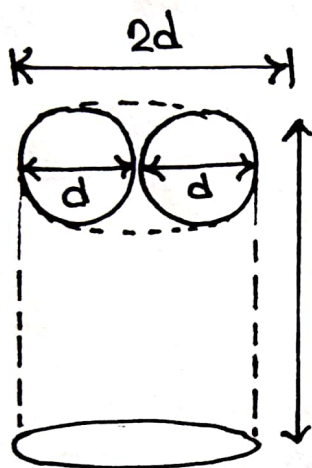
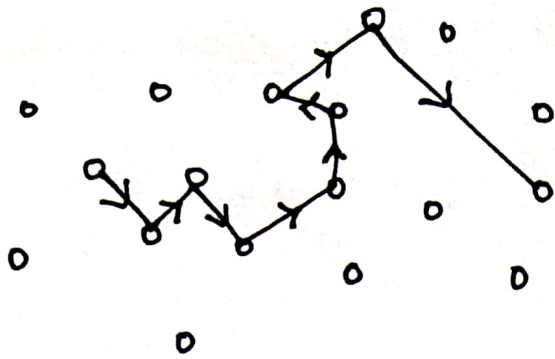
$$\therefore E_K = \frac{3}{2} kT$$

At $T=0$, $E_K=0$

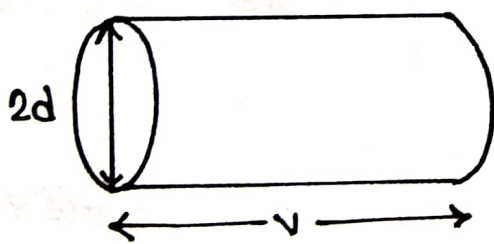
\hookrightarrow molecules or atoms are stable.

$$E_K \propto T$$

Mean Free path:



The effective collision area, πd^2



$$\lambda = \frac{S}{N} \begin{matrix} \longrightarrow \text{average distance} \\ \longrightarrow \text{number of collision.} \end{matrix}$$