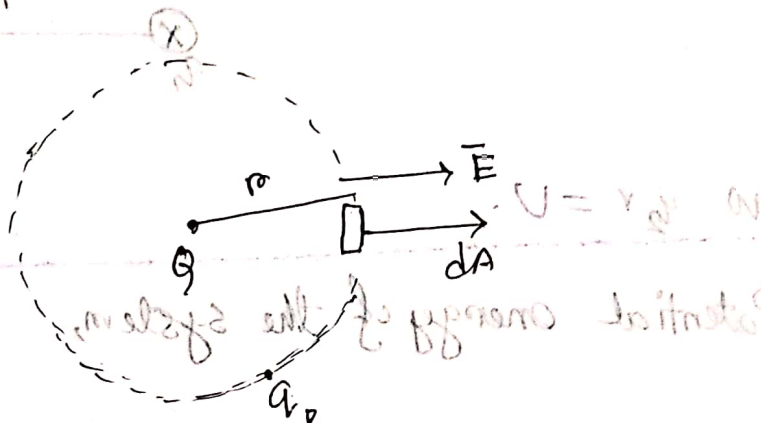


~~Electric field~~
Electric potential Energy

Relation or equating between Gauss law and Coulomb's law:

law:



$$\text{flux} = \oint \vec{E} \cdot d\vec{A}$$

$$= \oint E dA$$

$$= E \oint dA$$

$$= E \cdot 4\pi r^2$$

$$Q_{enc} = Q$$

Applying Gauss law

$$\epsilon_0 \oint E dA = Q_{enc}$$

$$E = \frac{Q}{4\pi \epsilon_0 r^2}$$

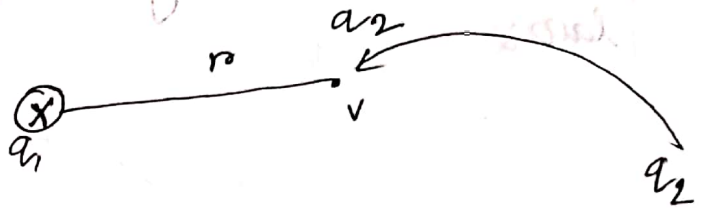
Force on charge q_0

$$F = q_0 E$$

$$F = q_0 \frac{Q}{4\pi \epsilon_0 r^2}$$

mirrored

$$V = \frac{q_1}{4\pi\epsilon_0 r^2}$$



$$W = q_2 V = U$$

Potential energy of the system,

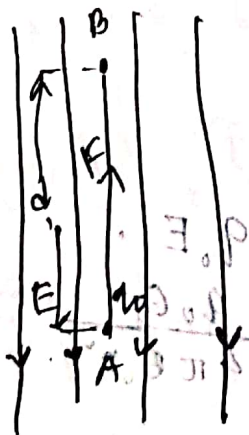
$$U = Vq_2$$

$$U = \frac{q_1 q_2}{4\pi\epsilon_0 r}$$

Unit, $U \rightarrow J$.

$V \rightarrow \text{volt} / J C^{-1}$.

Electric field and Electric potential:



uniform

$$F = q_0 E$$

work done, to move q_0 from A to B

$$W = F \cdot d = q_0 E \cdot d$$

Work done per unit charge,

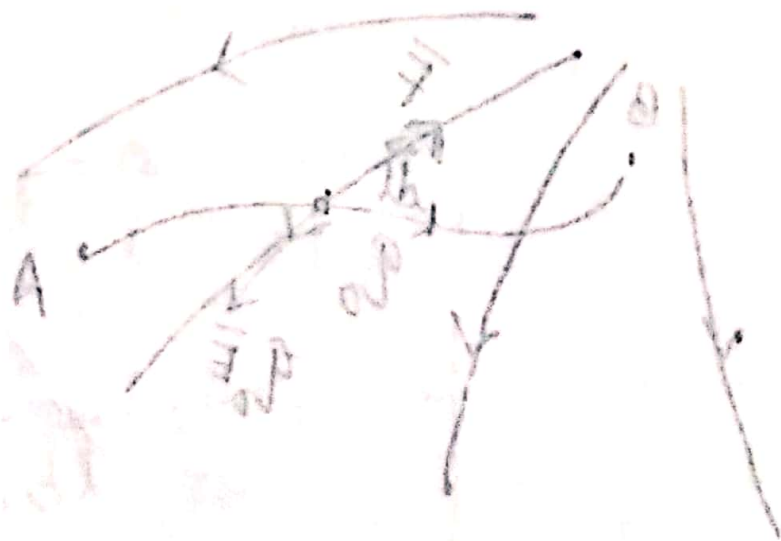
$$\frac{W}{q_0} = Ed.$$

$$\Rightarrow V_B - V_A = Ed.$$

$$\Rightarrow V = Ed.$$

relationship between E and V (non uniform field)

$$E = -\nabla V$$



CT-1

cycle - 5/10 - Day

02:00

Electric flux } 2 chapters.
Electric field }

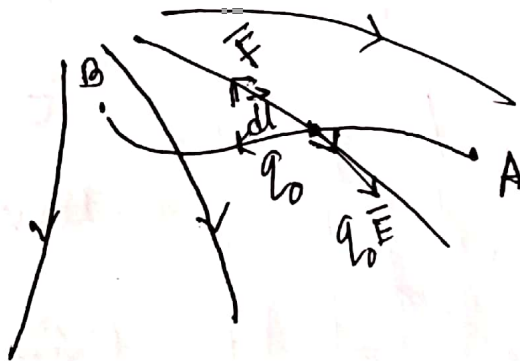
Work done per unit charge

$$W = \frac{qV}{J}$$

$$W = \int_A^B \vec{F} \cdot d\vec{l}$$

$$W = \int_A^B V \cdot C$$

Relation between E and V (non-uniform field):



$$\vec{F} = -q_0 \vec{E}$$

Work done to move q_0 charge from A to B

$$W_{AB} = \int_A^B \vec{F} \cdot d\vec{l}$$

$$W_{AB} = - \int_A^B q_0 \vec{E} \cdot d\vec{l}$$

$$W_{AB} = -q_0 \int_A^B \vec{E} \cdot d\vec{l}$$

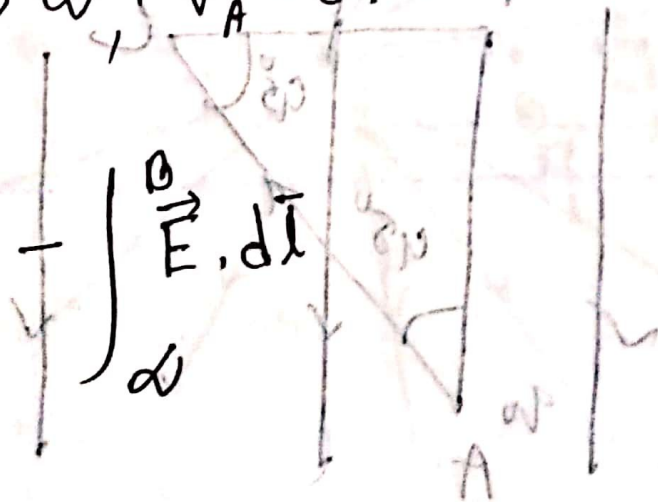
Work done per unit charge,

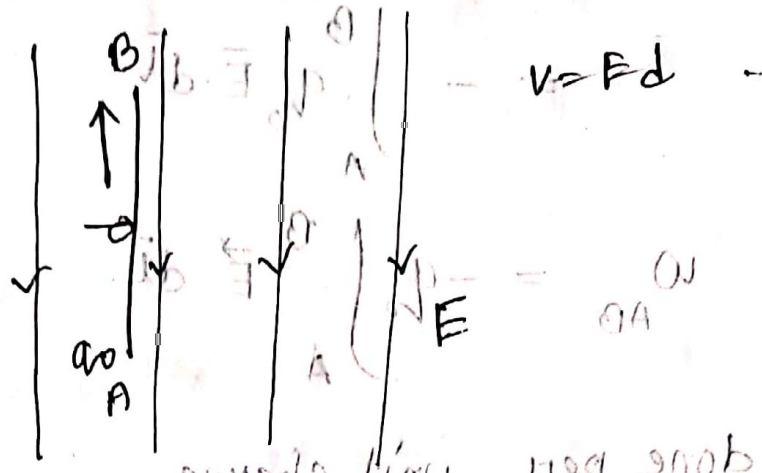
$$\frac{W_{AB}}{q_0} = - \int_A^B \vec{E} \cdot d\vec{l}$$

$$W_B - W_A = V_B - V_A = - \int_A^B \vec{E} \cdot d\vec{l}$$

If $A \rightarrow \infty$, $V_A = 0$.

$$V = - \int_{\infty}^B \vec{E} \cdot d\vec{l}$$

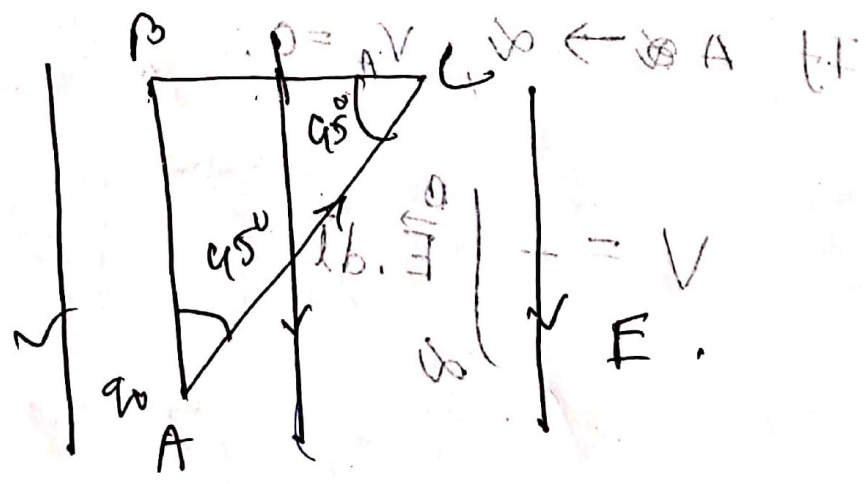




$$V_B - V_A = - \int_A^B \vec{E} \cdot d\vec{l}$$

$$= - E \int_A^B \cos 0^\circ dl$$

$$= E d$$



$$V_C - V_A = - \int_A^C \vec{E} \cdot d\vec{l}$$

$$= - \int_A^C E dl \cos 135^\circ$$

$$= - E \int_A^C dl (-1/\sqrt{2})$$

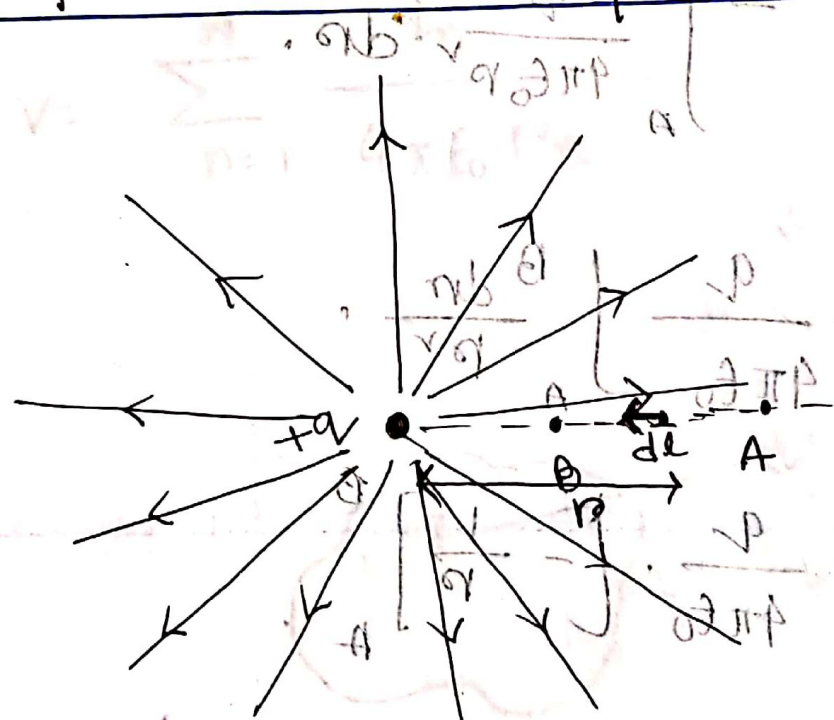
$$= \frac{E}{\sqrt{2}} \int_A^C dl = \frac{E}{\sqrt{2}} d\sqrt{2} = -Ed \cdot \frac{1}{\sqrt{2}}$$

$$V_C - V_B = 0 \quad [\because \theta = 90^\circ.]$$

$$\therefore V_B - V_A = 0 + Ed \cdot \frac{1}{\sqrt{2}}$$

$$= Ed \cdot \frac{1}{\sqrt{2}}$$

Electric potential due to a point charge:



$$V_B - V_A = ?$$

$$V_B - V_A = \int_A^B \vec{E} \cdot d\vec{l}$$

$$= E \cdot dl \cos 180^\circ$$

$$= -Edl = -E dr$$

And $dl = -dr$

$$V_B - V_A = - \int_A^B E dr$$

We know, for point charge

$$E = \frac{q}{4\pi\epsilon_0 r^2}$$

$$\therefore V_B - V_A = - \int_A^B \frac{q}{4\pi\epsilon_0 r^2} dr$$

$$= - \frac{q}{4\pi\epsilon_0} \int_A^B \frac{dr}{r^2}$$

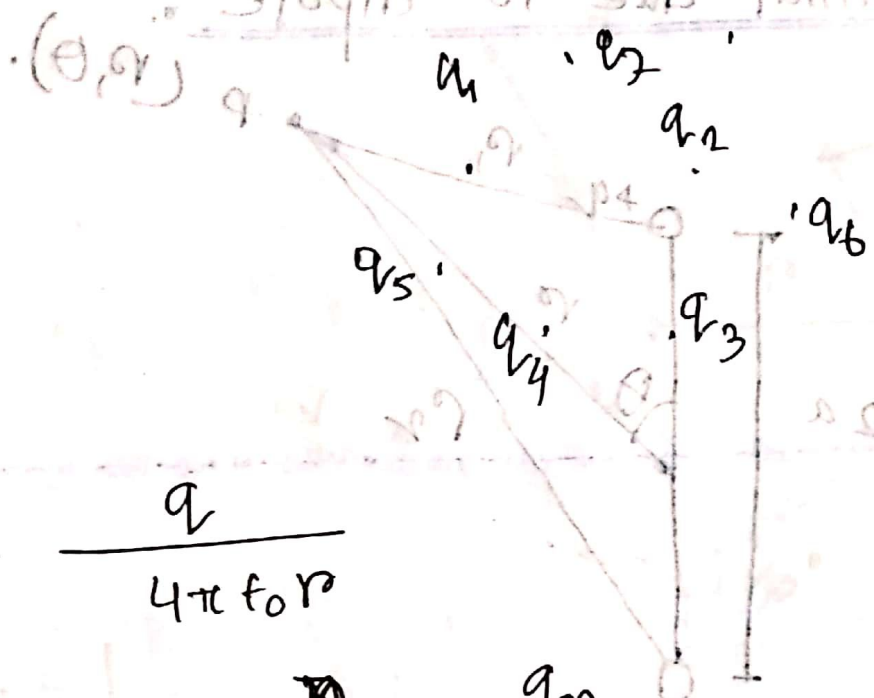
$$= - \frac{q}{4\pi\epsilon_0} \left[-\frac{1}{r} \right]_A^B$$

$$V_B - V_A = - \frac{q}{4\pi\epsilon_0} \left(\frac{1}{r_B} - \frac{1}{r_A} \right)$$

when, $A \rightarrow \infty$, $V_A = 0$

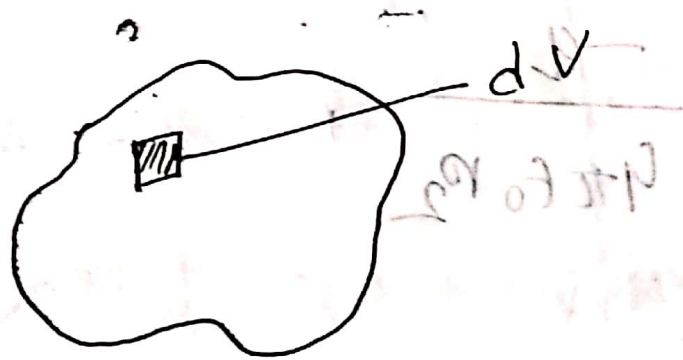
$$V = \frac{q}{4\pi\epsilon_0 r}$$

Electric potential due to dipole:



$$V = \frac{q}{4\pi\epsilon_0 r}$$

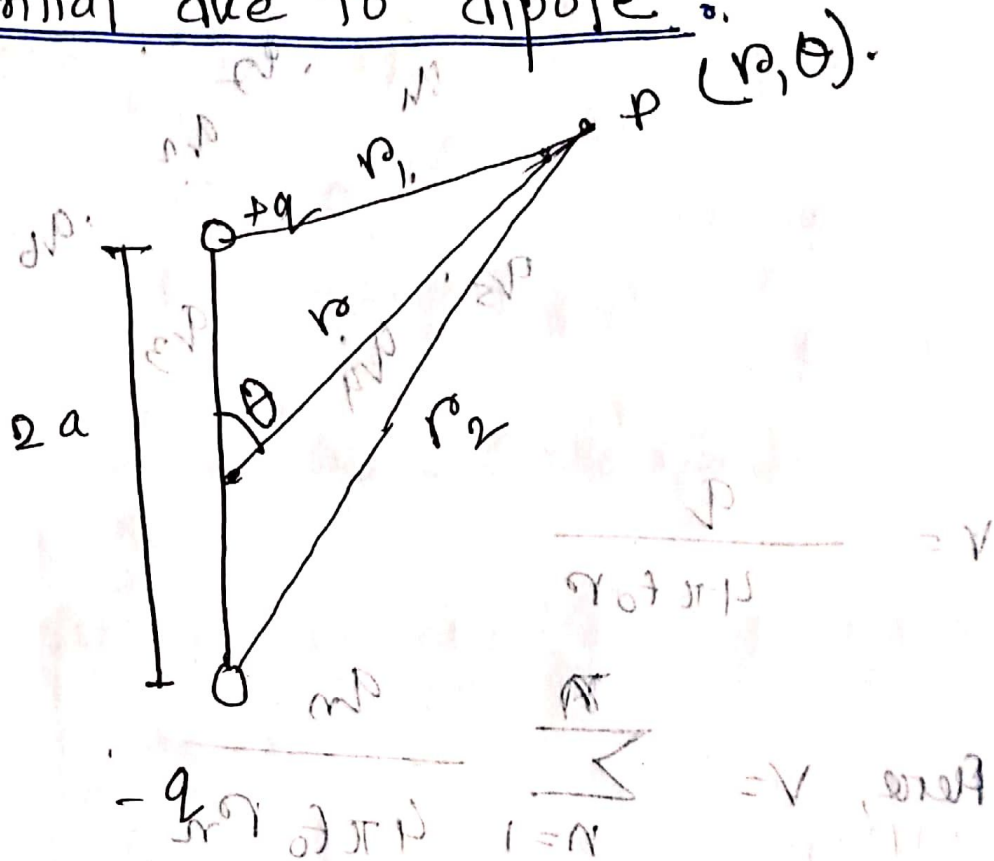
Here, $V = \sum_{n=1}^N \frac{q_n}{4\pi\epsilon_0 r_n}$



$$V = \int dV$$

$$\frac{q \cos \theta}{4\pi\epsilon_0 r^2} = V$$

Electric potential due to dipole:



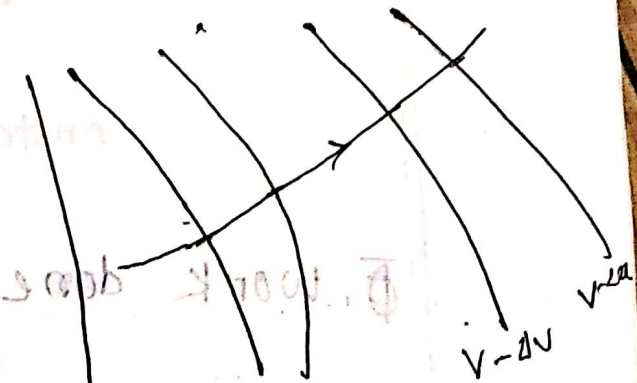
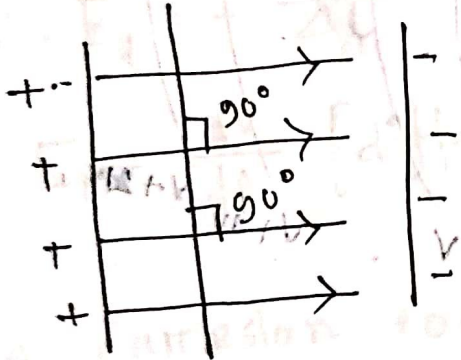
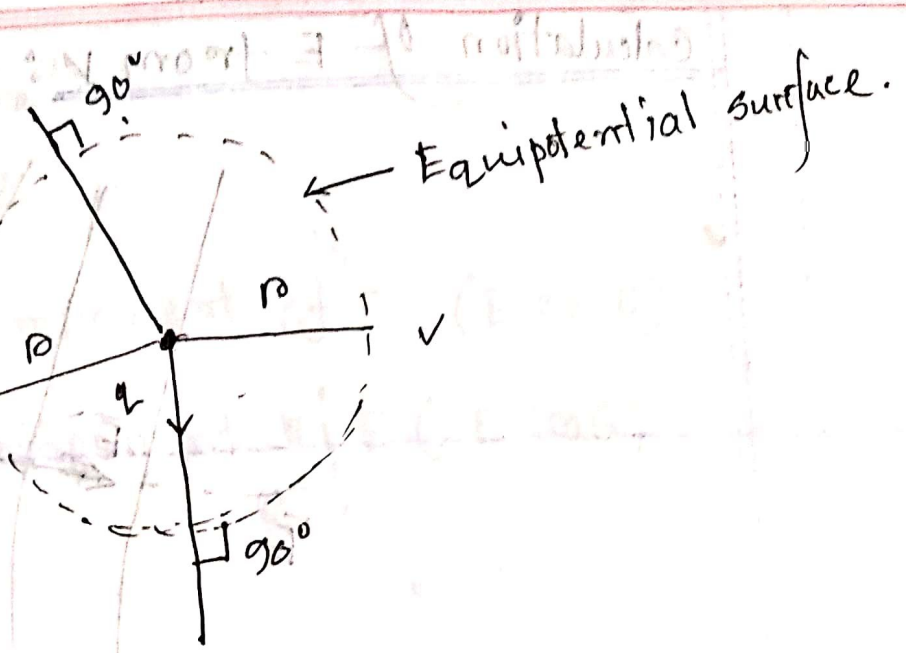
$$V_1 = \frac{q}{4\pi\epsilon_0 r_1}$$

$$V_2 = \frac{-q}{4\pi\epsilon_0 r_2}$$

$$V = \frac{p \cos \theta}{4\pi\epsilon_0 r^2}$$

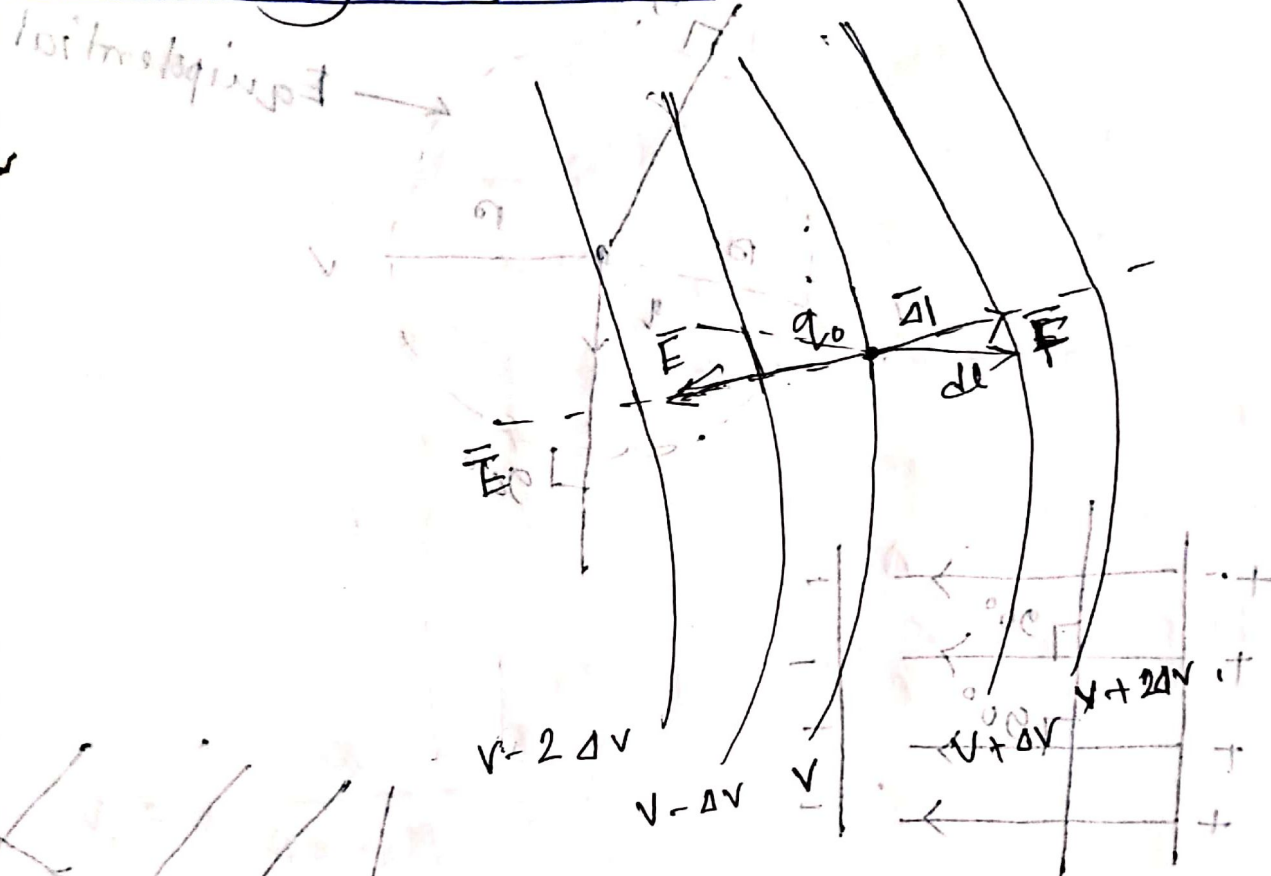
$$V_b = V$$

Q.19



Handwritten notes:
 Equipotential surfaces are perpendicular to the electric field lines.
 The potential difference between two equipotential surfaces is ΔV .
 The electric field is the negative gradient of the potential: $E = -\nabla V$.

Calculation of E from V:



∴ work done to move charge q_0 through potential difference $= q_0 \Delta V$.

In other definition, this work $= \vec{F} \cdot \Delta l$.

$$\begin{aligned}
 &= -q_0 \vec{E} \cdot d\vec{l} \\
 &= -q_0 E dl \cos(\pi - \theta) \\
 &= q_0 E \Delta l \cos \theta.
 \end{aligned}$$

$$\therefore q_0 E \Delta l \cos \theta = q_0 \Delta V.$$

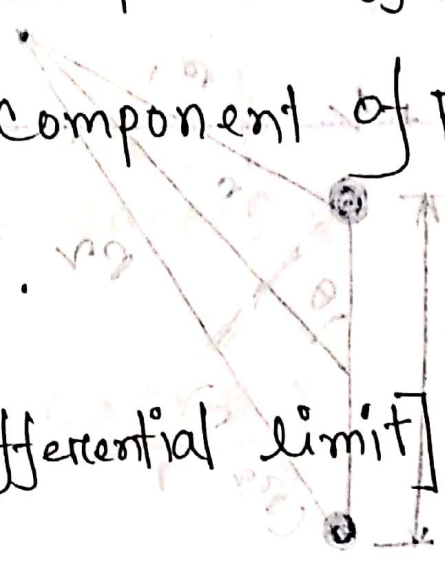
$$\Rightarrow E \cos \theta = \frac{\Delta V}{\Delta l}$$

-l direction \Rightarrow component of E ($E \cos \theta$).

+l direction \Rightarrow component of E ($-E \cos \theta$)

$$\therefore E_l = - \frac{\Delta V}{\Delta l}$$

$$E_l = - \frac{dV}{dl} \text{ [differential limit]}$$



In cartesian coordinate system,

$$E_x = - \frac{\partial V}{\partial x}$$

$$E_y = - \frac{\partial V}{\partial y}$$

$$E_z = - \frac{\partial V}{\partial z}$$

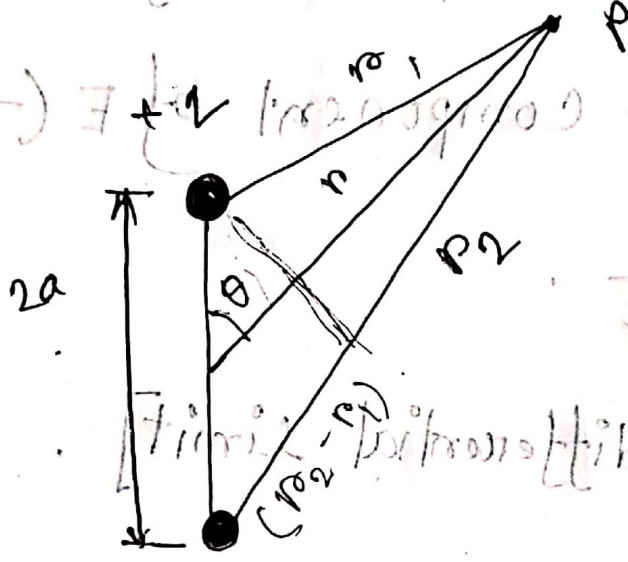
In polar coordinate system,

$$E_r = - \frac{\partial V}{\partial r}$$

$$E_\theta = - \frac{1}{r} \cdot \frac{\partial V}{\partial \theta}$$

$$E = \sqrt{E_p^2 + E_\theta^2}$$

Electric potential due to dipole



for +q,

$$V_1 = \frac{q}{4\pi\epsilon_0 r_1}$$

for -q,

$$V_2 = \frac{-q}{4\pi\epsilon_0 r_2}$$

Net potential

$$V = V_1 + V_2$$

$$= \frac{q}{4\pi\epsilon_0} \left(\frac{1}{r_1} - \frac{1}{r_2} \right)$$

$$= \frac{q}{4\pi\epsilon_0} \left(\frac{r_2 - r_1}{r_1 r_2} \right)$$

$$r \gg 2a \Rightarrow r_1 r_2 = r^2$$

$$r_2 - r_1 = 2a \cos \theta$$

$$\therefore V = \frac{q}{4\pi\epsilon_0} \left(\frac{2a \cos \theta}{r^2} \right)$$

$$= \frac{p \cos \theta}{4\pi\epsilon_0 r^2}$$

When, $\theta = 0^\circ$;

$$V = \frac{p}{4\pi\epsilon_0 r^2}$$

$$\theta = 180^\circ, \quad V = -\frac{p}{4\pi\epsilon_0 r^2}$$

$$\theta = 90^\circ, \quad V = 0$$



For two parallel plate's electric field:

$$E = \frac{\sigma}{\epsilon_0}$$

Electric field for conducting plate:

left cap $\Rightarrow \phi = 0$.

curved $\Rightarrow \phi = 0$.

right cap $\Rightarrow \phi = \int \vec{E} \cdot d\vec{A}$

$$= E \int dA$$

$$= E \cdot A$$

$\sigma = \text{charge per unit area}$

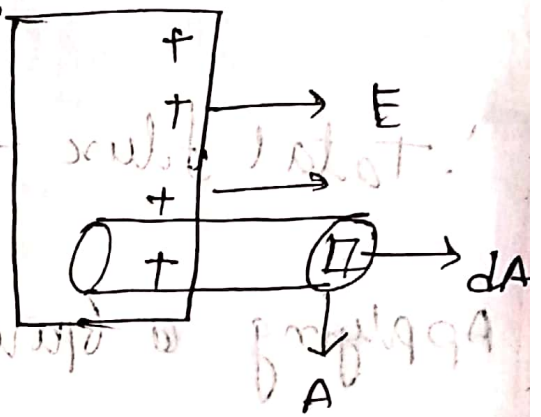
\therefore Total flux = $EA + 0 + 0$
 $= EA$

Charged enclosed, $Q_{enc} = \sigma A$

Applying Gauss law. $\epsilon_0 \oint \vec{E} \cdot d\vec{A} = Q_{enc}$

$$\Rightarrow \epsilon_0 EA = \sigma A$$

$$\Rightarrow E = \frac{\sigma}{\epsilon_0}$$



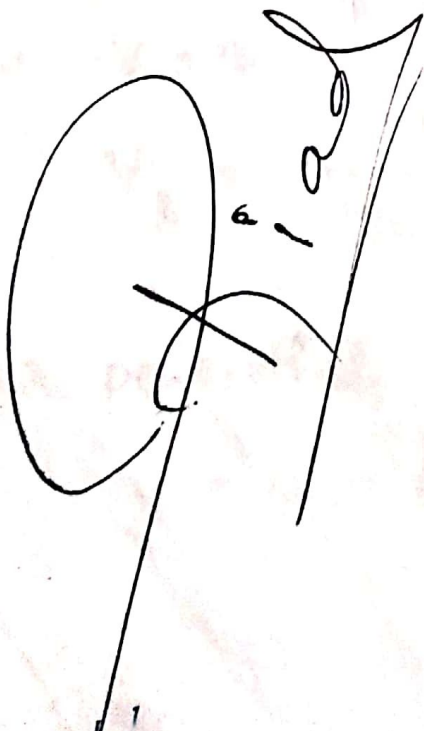
$$E_r = - \frac{\partial v}{\partial r} = \frac{1}{4\pi\epsilon_0} \frac{2P \cos \theta}{r^3}$$

$$E_\theta = - \frac{1}{r} \frac{\partial v}{\partial \theta} = \frac{P \sin \theta}{4\pi\epsilon_0 r^3}$$

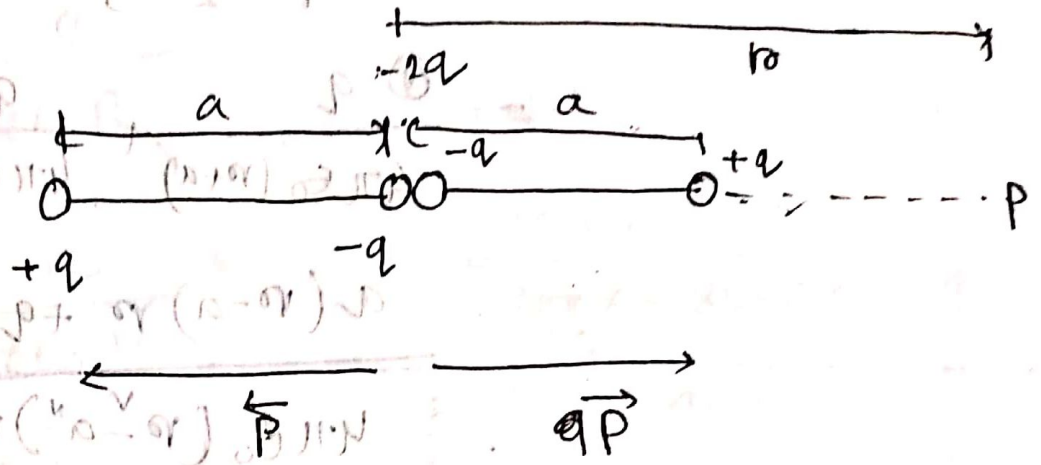
$$E = \frac{1}{4\pi\epsilon_0} \frac{P}{r^3} \sqrt{(4 \cos^2 \theta + \sin^2 \theta)}$$

$$\frac{P}{4\pi\epsilon_0} \cos \theta = \left(\frac{P \cos \theta}{r} \right) \frac{r}{4\pi\epsilon_0} = V$$

$$\theta = \pi/2 \rightarrow E = \frac{P}{4\pi\epsilon_0 r^3}$$



Electric potential due to electric quadrupole:



Electric quadrupole

$$Q = 2qa^2$$

For +q (left).

$$\text{Potential, } V_1 = \frac{q}{4\pi\epsilon_0(r+a)}$$

For +q charge (right)

$$\text{Potential, } V_2 = \frac{q}{4\pi\epsilon_0(r-a)}$$

For -2q charge

$$\text{Potential, } V_3 = \frac{-2q}{4\pi\epsilon_0 r}$$

① we know,

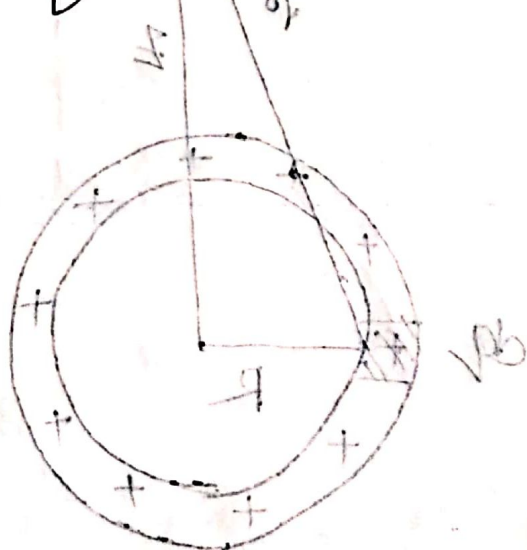
$$V = \frac{q}{4\pi\epsilon_0 R}$$

$$R = \frac{q}{4\pi\epsilon_0 V} = \frac{1.5 \times 10^{-8}}{4\pi \times 8.854 \times 10^{-12} \times 30}$$

$$= 4.5 \text{ m}$$

② For the segments of sub potential differential
 $dv = \frac{q}{4\pi\epsilon_0 R^2} \cdot \left(-\frac{1}{R^2} \cdot dR\right)$

$$\Rightarrow dR = \frac{4\pi\epsilon_0 R^2 \cdot q}{-q} dv$$



Potential due to charge element

$$\frac{q}{4\pi\epsilon_0 R} = V_p$$

∴ net potential, $V = V_1 + V_2 + V_3$

$$= \frac{q}{4\pi\epsilon_0(r+a)} + \frac{q}{4\pi\epsilon_0(r-a)} + \frac{-2a}{4\pi\epsilon_0 r}$$

$$= \frac{a(r-a)r + q(r+a)r + 2q(r^2-a^2)}{4\pi\epsilon_0(r^2-a^2)r}$$

$$= \frac{a(r^2-a^2) + q(r+a)r + 2q(r^2-a^2)}{4\pi\epsilon_0 r (r^2-a^2)}$$

$$V = \frac{2qa^2}{4\pi\epsilon_0 r (r^2-a^2)}$$

Consider a point charge with $q = 1.5 \times 10^{-8} \text{ C}$

1) what is the radius of the equipotential surface having a potential of 30 volts?

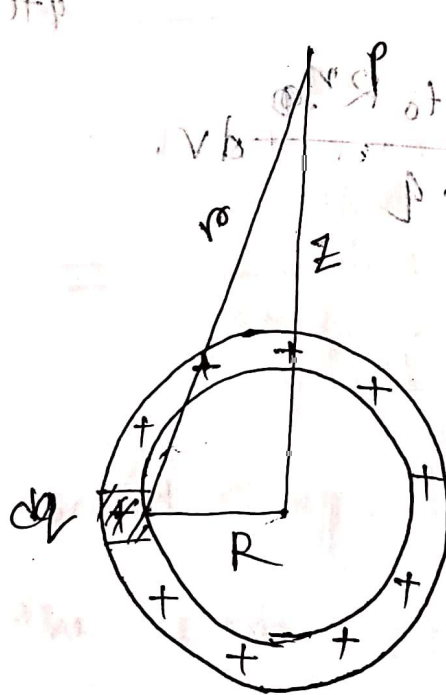
2) Are surfaces whose potentials differ by a constant amount equally spaced in radii?

$$V \propto \frac{1}{r} \text{ (monopole).}$$

$$V \propto \frac{1}{r^2} \text{ (dipole).}$$

$$V \propto \frac{1}{r^3} \text{ (quadrupole).}$$

□ Electric potential due to charged ring:



$Q = \text{total charge on the ring.}$

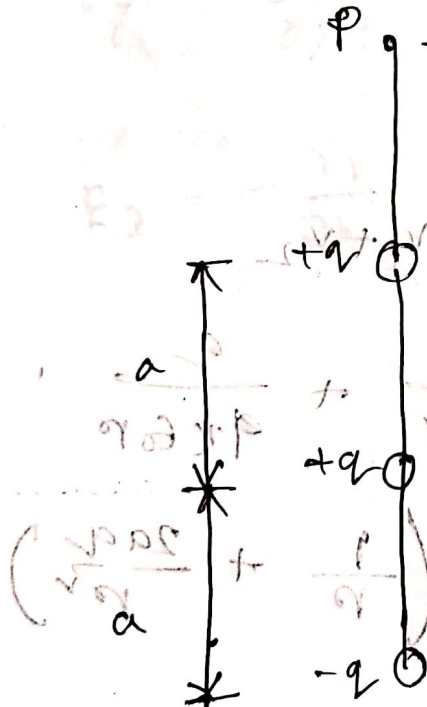
Potential due to charge element dq ,

$$dV = \frac{dq}{4\pi\epsilon_0 r}$$

$$\therefore \text{Total potential, } V = \int \frac{dq}{4\pi\epsilon_0 r^2}$$

$$= \frac{q}{4\pi\epsilon_0 r}$$

$$\therefore V = \frac{q}{4\pi\epsilon_0 \sqrt{r^2 + 2^2}}$$



Prove that $V = \frac{1}{4\pi\epsilon_0} \left(\frac{q}{r} + \frac{2qa}{r^2} \right)$ for $r \gg a$.

Soln: Pure dipole,

$$V_1 = \frac{2qa}{4\pi\epsilon_0 r^2}$$

$$[\theta = 0^\circ]$$

Potential

For point charge

$$V_2 = \frac{q}{4\pi\epsilon_0 r}$$

∴ Total potential at P = $V_1 + V_2$

$$= \frac{2qa}{4\pi\epsilon_0 r^2} + \frac{q}{4\pi\epsilon_0 r}$$

$$V = \frac{1}{4\pi\epsilon_0} \left(\frac{1}{r} + \frac{2aq}{r^2} \right)$$

∴ Total potential at P = $\frac{1}{4\pi\epsilon_0} \left(\frac{1}{r} + \frac{2aq}{r^2} \right)$

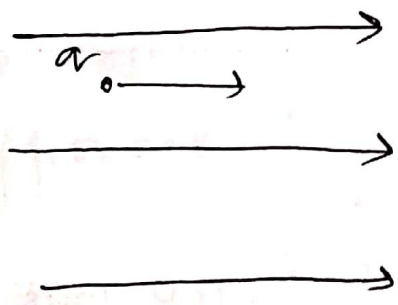
The potential at $(-2, 4, 6)$. ϕ is $V = 80x^2 + 60y^2$. then

find E_x, E_y, E_z .

Soln.
 $E_x = -\frac{\partial V}{\partial x} = -160(-2) = 320 \text{ Nc}^{-1} \text{ or } \text{V/m}$

$E_y = -\frac{\partial V}{\partial y} = -60 \cdot 2 \cdot (4) = 480 \text{ Nc}^{-1} \text{ or } \text{V/m}$

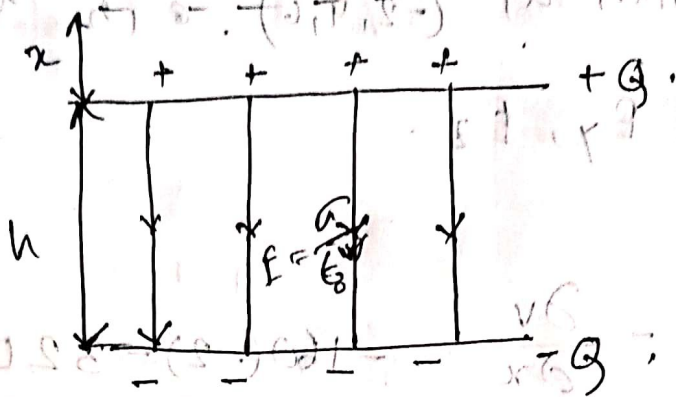
$E_z = -\frac{\partial V}{\partial z} = 0$



$qE = ma$
 $a = \frac{qE}{m}$

acceleration $a = v \cdot \frac{dv}{dr}$

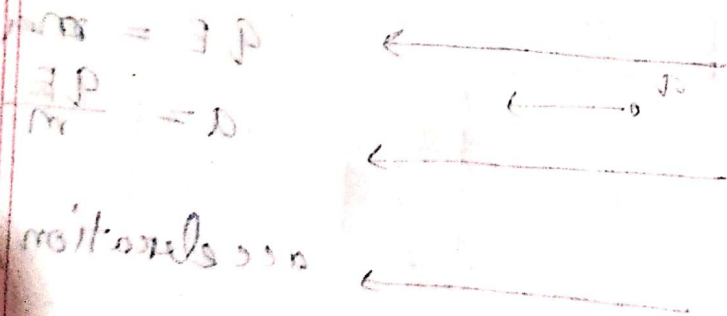
0.09.19.
G.H.D. Day



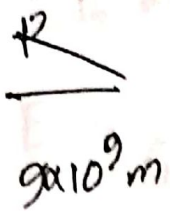
energy per unit volume $\rightarrow \frac{1}{2} \epsilon_0 E^2$

$$\int \frac{1}{2} \epsilon_0 E^2 dV$$

Total energy

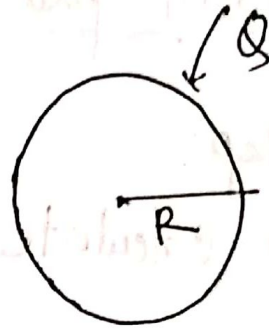


Capacitors and Capacitance.



Capacitance

1 F.



6400 km

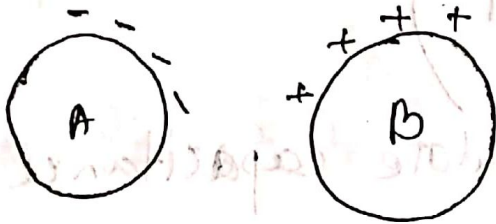
700 μF .

1 cm

1 pF.

$$V = \frac{Q}{4\pi\epsilon_0 R}$$

$$C = \frac{Q}{V} = \frac{4\pi\epsilon_0 R}{\text{constant}}$$



$$C_B = \frac{Q}{V_B}$$

$C = \frac{\text{charge on the object}}{\text{potential difference}}$

V_B goes down C_B goes on!

Parallel plate capacitor:

Step:

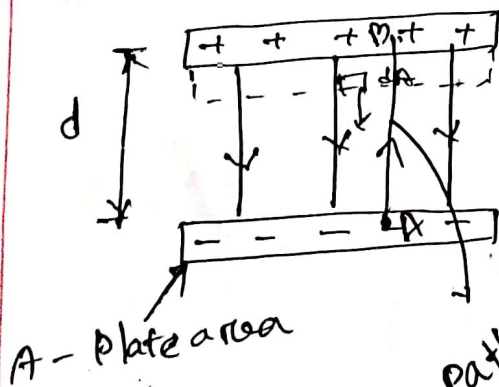
i) Calculate charge on each plate.

ii) Calculate electric field between two plates.
(using Gauss law)

iii) Calculate potential difference between two plates.

$$(V_B - V_A) = - \int_A^B E \cdot dl$$

iv) $C = \frac{Q}{V} \rightarrow$ calculate capacitance.



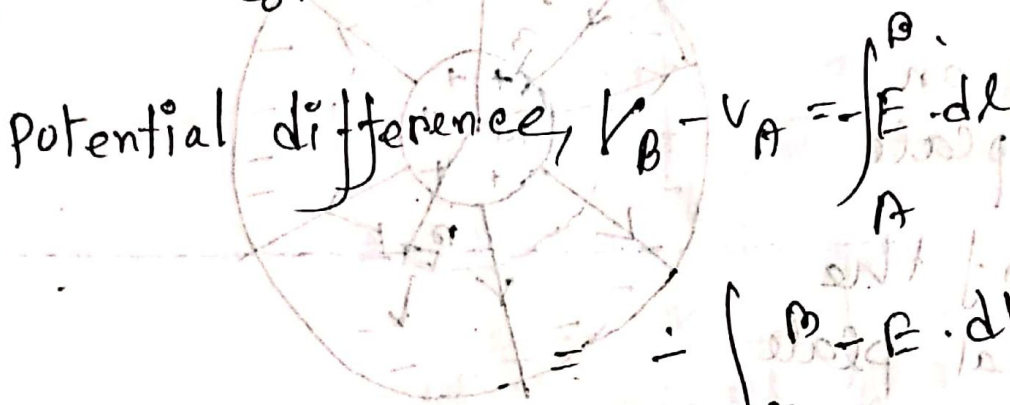
Applying Gauss law,

$$\epsilon_0 \oint \vec{E} \cdot d\vec{A} = Q_{enc}$$

$$\vec{E} \oint dA = \frac{Q}{\epsilon_0}$$

$$\Rightarrow \epsilon_0 E A = q$$

$$\Rightarrow E = \frac{q}{\epsilon_0 A}$$



$$V_B - V_A = \int_A^B E \cdot dl$$

$$V_B - V_A = E \int_A^B dl$$

$$V = E d$$

Capacitance, $C = \frac{q}{V}$

$$= \frac{\epsilon_0 E A}{E d}$$

$$C = \frac{\epsilon_0 A}{d}$$

74

Cylindrical capacitor:

q = charge on each plate

l = length of the cylindrical plate

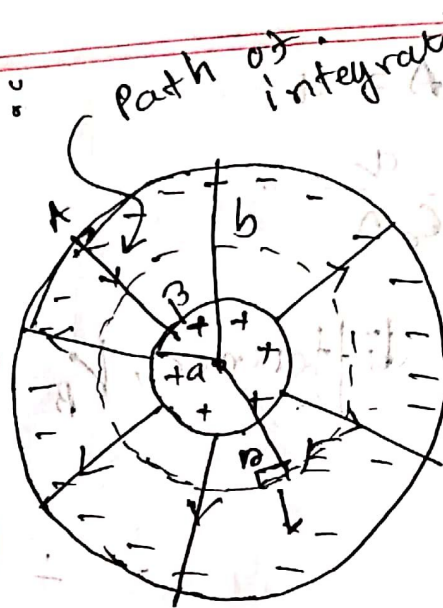
Applying Gauss' law

$$\epsilon_0 \oint E \cdot d\vec{A} = Q_{enc}$$

$$\Rightarrow \epsilon_0 E \oint dA = q$$

$$\Rightarrow \epsilon_0 E 2\pi r l = q$$

$$\Rightarrow E = \frac{q}{2\pi \epsilon_0 r l}$$



Potential difference,

$$V_B - V_A = - \int_A^B \vec{E} \cdot d\vec{l}$$

$$= - \int_A^B (-\vec{E} \cdot d\vec{l})$$

$$= \int_A^B E dr$$

$$= - \int_b^a E \cdot dr$$

$$= - \int_b^a \frac{q}{2\pi \epsilon_0 r l} \cdot dr$$

$$= \frac{q}{2\pi \epsilon_0 l} \int_b^a \frac{dr}{r}$$

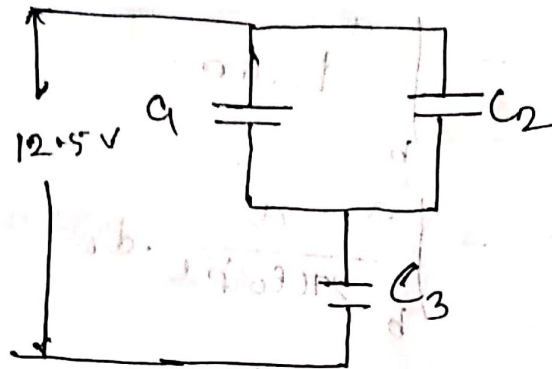
$$= \frac{q}{2\pi \epsilon_0 l} \ln \frac{a}{b}$$

$$\therefore V = \frac{q}{2\pi \epsilon_0 l} \ln \frac{b}{a}$$

$$\therefore \text{Capacitance, } C = \frac{q}{V} = \frac{q}{\frac{q}{2\pi \epsilon_0 l \ln \frac{b}{a}}} = \frac{2\pi \epsilon_0 l \ln \frac{b}{a}}{1}$$

$$C = 2\pi \epsilon_0 l \ln \frac{b}{a}$$

Problems



$C_1 = 12 \mu F$

$C_2 = 5.3 \mu F$

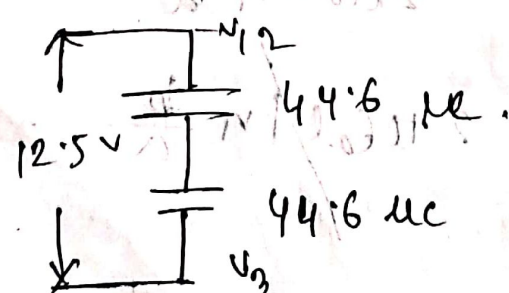
$C_3 = 4.5 \mu F$

① Equivalent capacitance for the combination.

② what is the charge on C_1, C_2, C_3 .

① $C_{eq} = 3.57 \mu F$

② Total charge, $C_{eq} = \frac{Q}{V} \Rightarrow Q = C_{eq} V = 44.6 \mu C$



$V_3 = \frac{Q_3}{C_3} = \frac{44.6}{4.5} = 9.91 V$

$$V_{12} = \frac{q_{12}}{C_{12}}$$

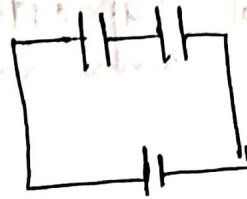
$$= 2.58 \text{ V.}$$

$$q_1 = C_1 V_{12} = 12 \times 2.58$$

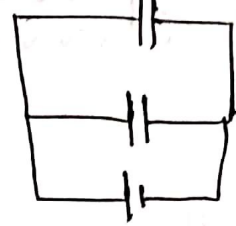
$$= 31 \mu\text{C.}$$

$$q_2 = C_2 V_{12} = 5.3 \times 2.58$$

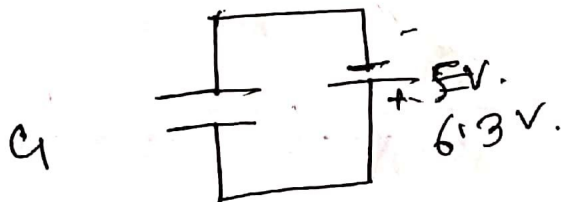
$$= 13.7 \mu\text{C.}$$



(Seri-q)

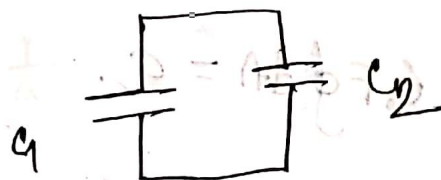


(Par-v)

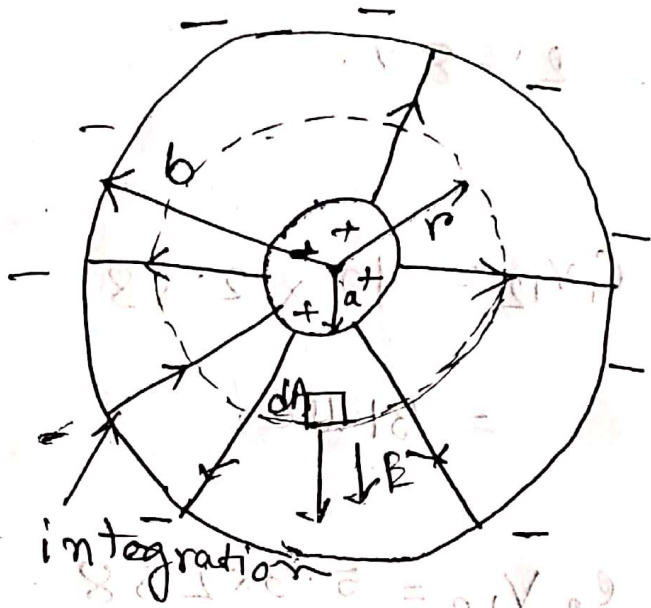


$$C_1 = 3.55 \mu\text{F.}$$

$$C_2 = 8.95 \mu\text{F.}$$



Spherical capacitor:



charge on each plate.

path of integration

$$\epsilon_0 \oint \vec{E} \cdot d\vec{A} = Q_{enc}$$

$$\Rightarrow \epsilon_0 \oint E dA = Q$$

$$\Rightarrow \epsilon_0 E \oint dA = Q$$

$$\Rightarrow \epsilon_0 E 4\pi r^2 = Q$$

$$E = \frac{Q}{4\pi\epsilon_0 r^2}$$

Potential difference between two plates, plates,

$$V_B - V_A = - \int_A^B \vec{E} \cdot d\vec{l}$$

$$= \int_A^B E \, dl$$

$$= - \int_A^B E \cdot dr$$

$$= - \int_b^a \frac{q}{4\pi\epsilon_0 r^2} dr$$

$$= - \frac{q}{4\pi\epsilon_0} \int_b^a \frac{dr}{r^2}$$

$$V_B - V_A = - \frac{q}{4\pi\epsilon_0} \left(-\frac{1}{a} + \frac{1}{b} \right)$$

$$= \frac{q}{4\pi\epsilon_0} \left(\frac{1}{a} - \frac{1}{b} \right)$$

$$V = \frac{q}{4\pi\epsilon_0} \cdot \frac{b-a}{ab}$$

$$\text{Capacitance, } C = \frac{q}{V} = \frac{q}{\frac{q}{4\pi\epsilon_0} \cdot \frac{b-a}{ab}}$$

$$= \frac{4\pi\epsilon_0 \cdot ab}{b-a}$$

Isolated sphere;

From spherical capacitor,

$$C = 4\pi\epsilon_0 \frac{ab}{b-a}$$

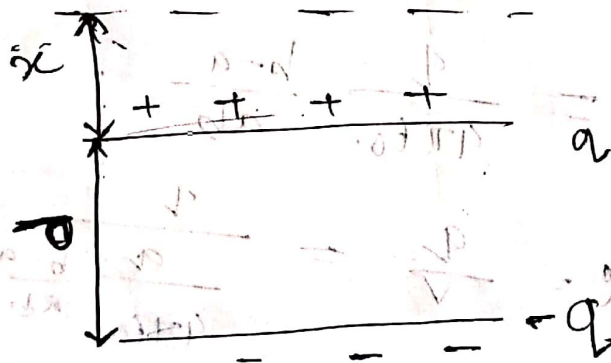
$$C = 4\pi\epsilon_0 \frac{a}{1 - \frac{a}{b}}$$

$$b \rightarrow \infty \\ a = R$$

$$\epsilon \epsilon_0 \cdot \epsilon_0$$

$$\therefore C = 4\pi\epsilon_0 \cdot R$$

Energy stored per unit volume;

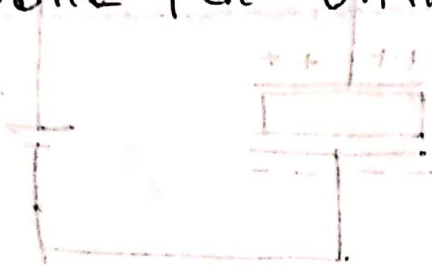


$$w = v dq \\ \int_0^q dw = \int_0^q \frac{d'}{c} dq$$

$$W = \frac{1}{c} \frac{q^2 v}{2}$$

$$= \frac{1}{2} cv^2 = \frac{1}{2} qv$$

Work per unit volume, = $\frac{\frac{1}{2} cv^2}{Ad}$



$$= \frac{\frac{1}{2} \frac{\epsilon_0 A}{d} v^2}{Ad}$$

$$= \frac{1}{2} \epsilon_0 \frac{v^2}{d}$$

$$= \frac{1}{2} \epsilon_0 E^2$$

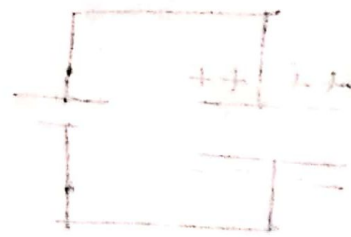
Again, we know,

$$Fx = W$$

$$F = q \cdot \frac{E}{2}$$

$$W = q \cdot \frac{E}{2} \cdot x$$

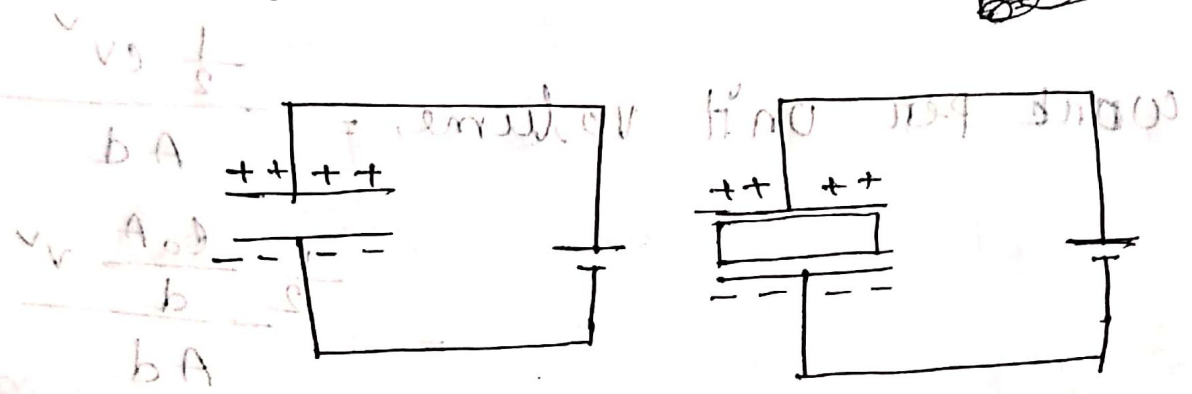
$$= \frac{1}{2} qv$$



Capacitor with dielectric material

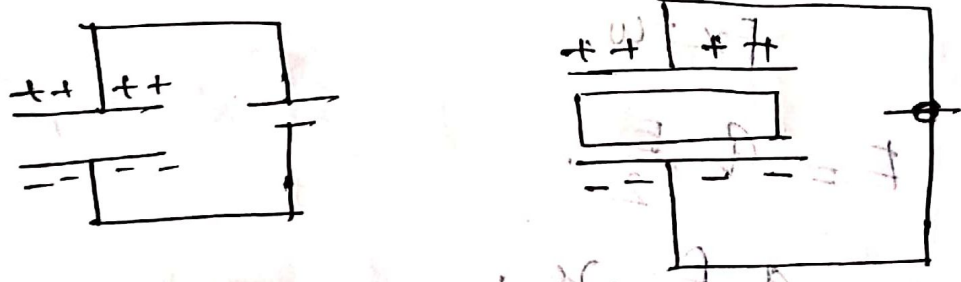
1) When battery is connected;

$q = \frac{C}{V}$
 ~~$q = \frac{C}{V}$~~ $V = Ed$



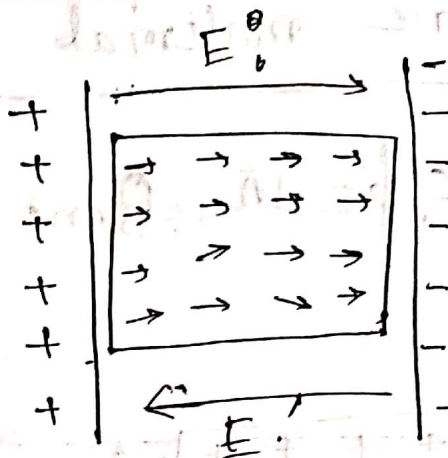
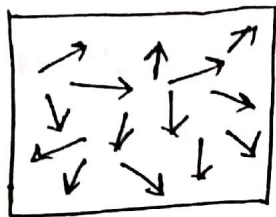
$Q \rightarrow$ increase $C \rightarrow$ increase
 $E \rightarrow$ unchanged
 $V \rightarrow$ unchanged.

2) When battery is removed;



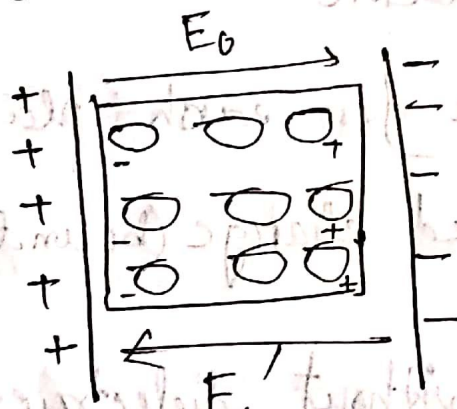
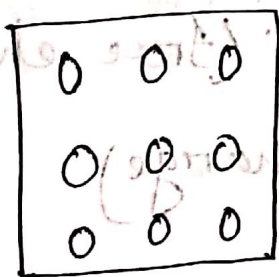
$Q \rightarrow$ unchanged $C \rightarrow$ increases,
 $E \rightarrow$ decreases,
 $V \rightarrow$ decreases

Polar dielectric



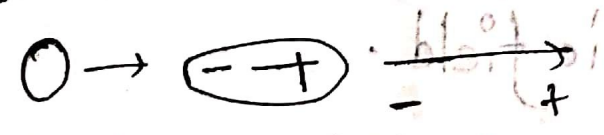
net Field, $E = E_0 - E'$

Non-polar-dielectric:



$\epsilon = \frac{q}{V}$

Phenomenon \rightarrow Polarization :-



induced dipole

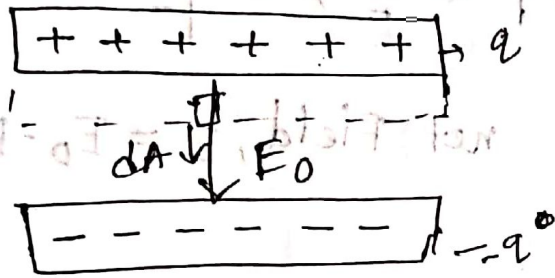
induced dipole moment. \vec{P}

dielectric constant, $k = \frac{E_0}{E}$ or $k = \frac{V_0}{V}$

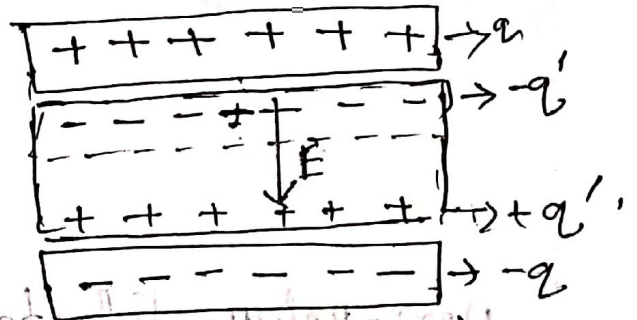
$k = \frac{C}{C_0}$

Dielectric material and Gauss' law:

$$\epsilon_0 \oint \vec{E} \cdot d\vec{A} = Q_{enc}$$



without dielectric



with dielectric.

$q \rightarrow$ charge for each plate (free charge).

$q' =$ induced charge (bound charge)

$E_0 \rightarrow$ field without dielectric.

$E' \rightarrow$ induced electric field.

$E \rightarrow$ net field when dielectric material is used.

$A \rightarrow$ plate area.

$$\frac{Q}{\epsilon_0} = \dots$$

$$\Rightarrow \frac{q}{k} = q - q'$$

$$\Rightarrow q' = q - \frac{q}{k} = q \left(1 - \frac{1}{k} \right)$$

When, $k=1$, $q'=0$.

Gauss law,

$$\epsilon_0 \oint \vec{E} \cdot d\vec{A} = q - q'$$

$$\Rightarrow \epsilon_0 \oint \vec{E} \cdot d\vec{A} = \frac{q}{k}$$

$$\Rightarrow \boxed{\epsilon_0 \oint k \vec{E} \cdot d\vec{A} = q}$$

↳ Gauss law when there is dielectric medium.

without dielectric,

$$\text{Gauss law, } \epsilon_0 \oint \vec{E} \cdot d\vec{A} = Q_{\text{enc}}$$

$$\Rightarrow \epsilon_0 \cdot E_0 \cdot A = q$$

$$\Rightarrow E_0 = \frac{q}{\epsilon_0 A} \quad \text{--- (i)}$$

with dielectric medium,

$$\text{Gauss' law; } \epsilon_0 \oint \vec{E} \cdot d\vec{A} = Q_{\text{enc}}$$

$$\Rightarrow \epsilon_0 \cdot E \cdot A = q - q'$$

$$\Rightarrow E = \frac{q - q'}{\epsilon_0 A}$$

$$= \frac{q}{\epsilon_0 A} - \frac{q'}{\epsilon_0 A} \quad \text{--- (ii)}$$

we know,

$$E = \frac{E_0}{K}$$

$$= \frac{q}{K \epsilon_0 A} \quad \text{--- (iii)}$$

$$\vec{E} = \vec{E}_0 - \vec{E}'$$

from (ii) and (iii), $\frac{q}{K \epsilon_0 A} = \frac{q}{\epsilon_0 A} - \frac{q'}{\epsilon_0 A}$

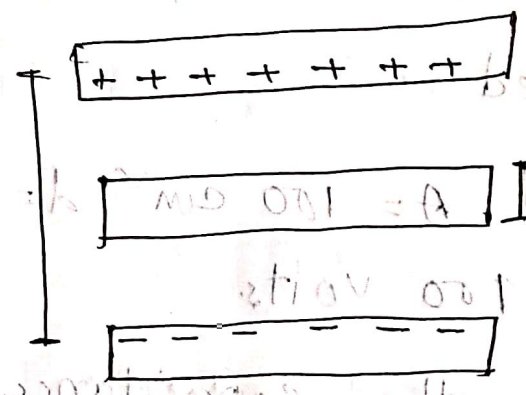
$\alpha-5^\circ$ Figure 30-12 shows a dielectric slab of dielectric constant k placed between the plates of a parallel plate capacitor of plate area A and separation d . A potential difference V_0 is applied with no dielectric present; the battery is then disconnected and the dielectric slab inserted.

Assume that $A = 100 \text{ cm}^2$, $d = 1.0 \text{ cm}$, $b = 0.50 \text{ cm}$
 $k = 7.0$, $V_0 = 100 \text{ volts}$.

- calculate the capacitance C_0 before the slab is inserted.
- calculate the free charge Q .
- calculate the electric field strength in the gap.
- calculate the electric field strength in the dielectric.

e) calculate the potential difference between the plates.

f) Calculate the capacitance with the slab in the place.



a)
$$C = \frac{\epsilon_0 A}{d} = \frac{8.854 \times 10^{-12} \times 100 \times 10^{-4}}{10^{-2}}$$

$$= 8.9 \mu\text{F}$$

b)
$$q = C V = 8.9 \times 10^{-6} \times 100 = 8.9 \times 10^{-4} \text{ C}$$

c)
$$E_0 = \frac{q_0}{\epsilon_0 A} = \frac{8.9 \times 10^{-10}}{8.854 \times 10^{-12} \times 100 \times 10^{-4}}$$

$$= 10^4 \text{ V m}^{-1}$$

d)
$$E = \frac{E_0}{k} = \frac{10^4}{7.0} = 1.4 \times 10^4 \text{ V m}$$

e)
$$V = - \int_a^b \vec{E} \cdot d\vec{l}$$

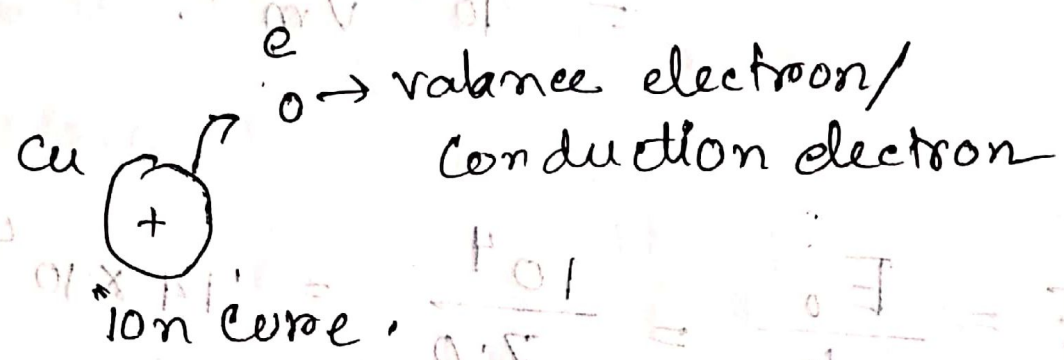
$$V = E_0 (d-b) + E b$$

$$= 57 \text{ V}$$

f)
$$C = \frac{q_0}{V} = \frac{8.9 \times 10^{-10}}{57}$$

$$= 16 \text{ pF}$$

current, current density, resistivity, conductivity; drift velocity -



Drift velocity of Cu:

$n \rightarrow$ no. of electron per $m^3 \approx 10^{29}$.

average velocity $\langle v \rangle \approx 10^6 \text{ ms}^{-1}$.

Time between two collision, $\tau = 3 \times 10^{-14} \text{ s}$.

$$\frac{8.1 \times 10^{-10}}{3 \times 10^{-14}} = \frac{v_d}{V}$$