

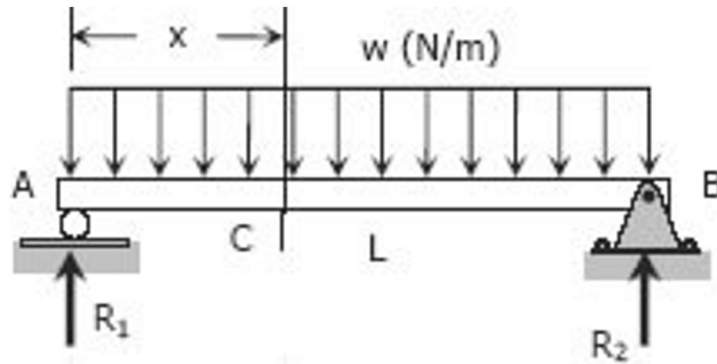
1. Inflection point – if BMD passes through zero bending moment then this point is called POI.
2. Dangerous point/Section – A point/section where the shear passes through zero is called dangerous section.
3. SFD – The algebraic sum of all vertical forces of one side at any section
4. BMD – The algebraic sum of all moments of the external forces to one side of any section
5. bending stresses, or flexure stresses - The stresses caused by the bending moment are known as
6. Yield strength = At stress-strain diagram at in which point strain increased but stress doesn't increase
7. Ultimate strength – It is the maximum stress that a material can withstand before it breaks or weakens.
8. Necking – At failure time, the narrowing of steel specimen
9. Hardness – the resistance of material to scratching or abrasion or penetration
10. Thermal strain - Thermal strains are strains that develop. when a material is heated or cooled
11. Modulus of rigidity - ratio of shear stress to shear strain
12. Poisson's ratio – it is the amount of transversal elongation divided by the amount of axial compression.
13. Ductility - the ability of a material to have its shape changed without losing strength or breaking
14. Lap joint - When two plates are folded under or above each other, this type of joint is called a lap joint.
15. Butt joint - both plates are combined by placing the plates on each other or on each other.
16. Efficiency of riveted joint - The ratio of the strength of the joint to the strength of the solid plate
17. Hoops stress - Hoop stress is the stress that occurs along the pipe's circumference when pressure is applied
18. Longitudinal stress - Longitudinal stress is defined as the stress produced when a pipe is subjected to internal pressure.
19. Hooks law - the strain of an elastic object or material is proportional to the stress in proportional limit.
20. Pitch – It is the distance from the center of one rivet to the center of the next rivet measured parallel to the seam.
21. shear center - Shear center is a point on the beam-section where the application of loads does not cause its twisting
22. Side fillet – when the weld is parallel to the direction of load then it is known as side fillet.
23. Stiffness - the property of material for which the element is able to resist deformation or deflection under the action of an applied force.
24. Transvers filet – when the weld is perpendicular to the direction of load
25. Butt fillet - Butt fillet is taken from the thicker end of the beef tenderloin. Butt fillets are very tender and taste fantastic roasted, grilled or fried.
26. REPEATING SECTIOIN – pitch
- 27.

Derivattion

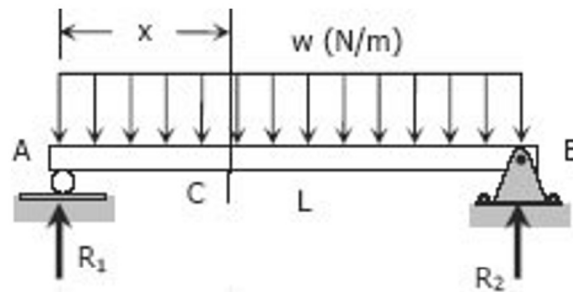
1. Sfd bmd
2. Thin wall
3. Maximum shearing stress of rectangular beam is 50 % more than average stress
4. Derive formula for horizontal shearing stress
5. Bending stress, shear stress

Relation among Load Shear and Moment

Consider a simple beam shown of length L that carries a uniform load of w (N/m) throughout its length and is held in equilibrium by reactions R_1 and R_2 .



$$R_1 = R_2 = wL/2$$



- $V_x = R_1 - wx = wL/2 - wx$
- $M_x = R_1 * x - w * x^2/2$
- $M_x = wLx/2 - w * x^2/2$
- Differentiate M with respect to x

$$\frac{dM}{dx} = \frac{wL}{2} \frac{dx}{dx} - \frac{w}{2} 2x \frac{dx}{dx} \quad \Rightarrow \quad \frac{dM}{dx} = \frac{wL}{2} - wx$$

$$\therefore \frac{dM}{dx} = V$$

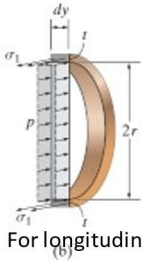
- Thus, the rate of change of the bending moment with respect to x is equal to the shearing force, or **the slope of the moment diagram at the given point is the shear at that point.**

- Differentiating V with respect to x

$$\frac{dV}{dx} = -w = \text{Load}$$

Thus, the rate of change of the shearing force with respect to x is equal to the load **the slope of the shear diagram at a given point equals the load at that point.**

For circumferential direction

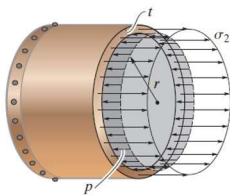


$$\Sigma F_x = 0;$$

$$2[\sigma_1(t dy)] - p(2r dy) = 0$$

$$\sigma_1 = \frac{pr}{t}$$

For longitudinal direction



$$\Sigma F_y = 0;$$

$$\sigma_2(2\sqrt{\pi}rt) - p(\pi r^2) = 0$$

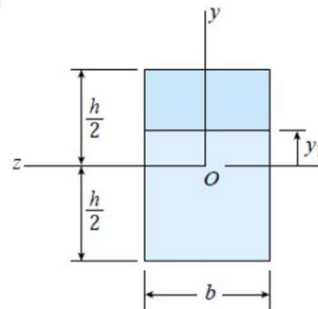
$$\sigma_2 = \frac{pr}{2t}$$

(c)



Cylindrical pressure vessels, such as this gas tank, have semi-spherical end caps rather than flat ones in order to reduce the stress in the tank.

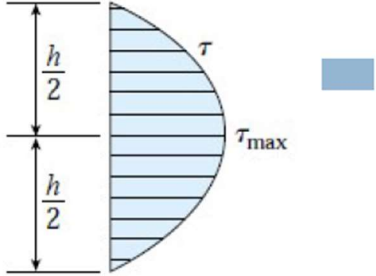
Distribution of Shear Stresses in a Rectangular Beam



- The first moment Q of the shaded part of the cross-sectional area is obtained by multiplying the area by the distance from its own centroid to the neutral axis

$$Q = b\left(\frac{h}{2} - y_1\right)\left(y_1 + \frac{h/2 - y_1}{2}\right) = \frac{b}{2}\left(\frac{h^2}{4} - y_1^2\right)$$

Same result can be obtained by integration

$$Q = \int y dA = \int_{y_1}^{h/2} yb dy = \frac{b}{2} \left(\frac{h^2}{4} - y_1^2 \right)$$
$$\tau = \frac{V}{2I} \left(\frac{h^2}{4} - y_1^2 \right)$$


This equation shows that the shear stresses in a rectangular beam vary quadratically with the distance y_1 from the neutral axis.

$$\tau_{\max} = \frac{Vh^2}{8I} = \frac{3V}{2A}$$

$A = bh$ is the cross-sectional area.

Thus, the maximum shear stress in a beam of rectangular cross section is 50% larger than the average shear stress V/A .

Pure bending can be for full beam or a particular section of beam, where shear force is 0 in every points.

Assumptions

- The material of the beam is homogeneous and isotropic.
- The value of the Young's modulus of elasticity is the same in tension and compression.
- The transverse section which were plane before bending remain plane after bending also.
- The beam is initially straight and all longitudinal filaments bend into circular arcs with a common center of curvature.
- The radius of curvature is so large compared with dimensions of the beam cross section.
- Each layer of the beam is free to expand or contract independently of the layer, above or below it.

FLEXURAL STRESSES IN BEAMS

- Derivation of Flexure Formula
- Consider two adjacent sections AB & CD of a part of unbent beam separated by a distance 'L', After bending has occurred because of load, sections AB and CD rotate relative to each other but remain straight and undistorted (Assumption 1)

Md Kamruzzaman's screen

FLEXURAL STRESSES IN BEAMS

(a) Part of Unbent Beam

(b) Part of Bent Beam

FLEXURAL STRESSES IN BEAMS

- Fiber 'AC' at the top is shortened by an amount CC' and is in compression.
- Fiber 'BD' at the bottom is extended by an amount DD' and is in tension.
- Fiber 'EF' between Fiber AC and BD whose length is unchanged and is called neutral surface.



From distant C, Stress is S
From distant y, Stress is (Sy)/C

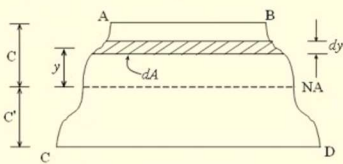


Fig. Cross Section of a Beam.

FLEXURAL STRESSES IN BEAMS

- Derivation of Formula:
 - Let 'ABCD' be any cross-section of a prismatic beam. The shaded strip dA is an elementary part of the cross-section, its distance from N.A is 'y'.
 - Let, 'S' be the stress in the top fiber and 'C' be the distance of these fibers from NA.
 - Hence, elementary stress on dA is, $= \frac{S \times y}{C}$
 - Hence, elementary force on dA is, $= S \times \frac{y}{C} \times dA$
 - Hence, elementary moment about NA is, $= \left(S \times \frac{y}{C} \times dA \right) \times y$
 $= \frac{S}{C} \times y^2 \times dA$



FLEXURAL STRESSES IN BEAMS

$$\text{Resisting Moment, } M_R = \int_{-c}^c \frac{S}{C} \times y^2 dA = \frac{S}{C} \int_{-c}^c y^2 dA = \frac{S}{C} I$$

$$[\ominus I = \int y^2 dA = \text{Moment of Inertia}]$$

Resisting Moment, M_R = Bending Moment, M

$$\Rightarrow M = \frac{S}{C} \times I \quad \Rightarrow S = \frac{M \times C}{I}$$

Here: S = Stress in top & bottom fiber of the beam in psi or ksi

M = Bending Moment in lb-in or k-in

C = Distance of NA from Top or Bottom fiber in

I = Moment of Inertia in in^4