

Reinforced Concrete -1

credit 3

14.2.22

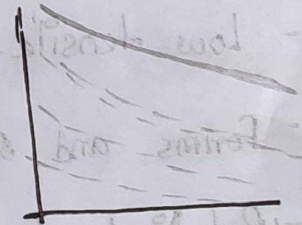
Book - Design of Concrete Structures [H. Nilson, David Dolon]
7th, 14th
Reinforced Concrete - Mechanics & Design [James. K. Wight]

Concrete :

- Concrete is a stonelike material obtained by mixing cement, sand, other aggregate and water.
- is being used for thousands of years, lime mortar 12000 B.C.
- Compressive strength high. Tensile strength small.
- It is not economical to use concrete in members subject to tension

Why is strength the property most valued in concrete by Engineers?

→ Strength of concrete is commonly considered its most valuable property, although in many practical cases, other properties like durability & impermeability may in fact be more



important. Nevertheless strength usually gives the over all picture of quality of concrete. Strength of concrete are following types

- Compressive,
- Tensile
- Flexural
- Shear

From above discussion, it can be said that if a desirable strength if concrete structure can be acquired then the other properties will be fullfilled.

- Factors affecting choice of Reinforced Concrete for structure
 - economy. Economical compare to concrete.
 - Easily give shape to our desire architectural and structural function
 - Fire resistance
 - Rigidity
 - Low maintainance
 - Availability of materials

• Factors that may cause one to select a material other than reinforced concrete.

- Low tensile strength
- Forms and shoring
- Relatively low strength per unit of weight or volume.
- Formwork
 - ↳ Removal of forms
 - ↳ Fresh concrete requires support weight until strength is adequate.
 - ↳ Labour/Materials cost not required for that other types of materials.
- Time dependent volume changes
 - ↳ Concrete & steel undergo similar expansion and contraction
 - ↳ Concrete undergoes drying shrinkage, which may cause deflections & cracking
 - ↳ Creep of concrete under sustained loads causes an increase in deflection with time.

Concrete Properties

- Concrete strain at max, compressive stress, ϵ_u

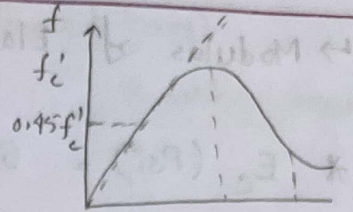
• ϵ_u varies between 0.0015 - 0.003

• For normal strength concrete, $\epsilon_u \sim 0.002$

- ϕ Maximum useable strain, ϵ_u

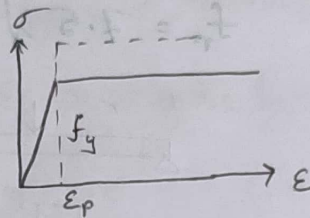
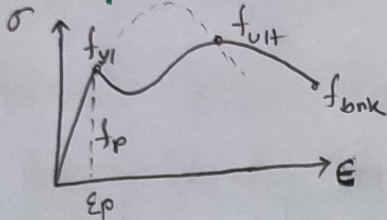
• ACI code: $\epsilon_u = 0.003$

• Used for flexural and axial compression



Concrete brittle material

Steel Properties



The elastic perfectly plastic (EPP) model for steel assumes the stress to vary linearly with strain up to yield point (f_y) and remain constant beyond that.

Concrete -

Age	7 days	14 days	28 days	3 month	6 month	1 yr	2 yr	5 yr
Strength ratio	0.67	0.86	1.0	1.17	1.23	1.27	1.31	1.3

Normally use 28 day strength for design strength

□ Poisson's Ratio, ν

↳ $\nu \sim 0.15$ to 0.20 , usually use, $\nu = 0.17$

↳ Modulus of Elasticity for normal weight concrete ($w_c \approx 150 \text{ pcf}$)

$$* E_c (\text{Psi}) = 57000 \sqrt{f'_c (\text{Psi})}$$

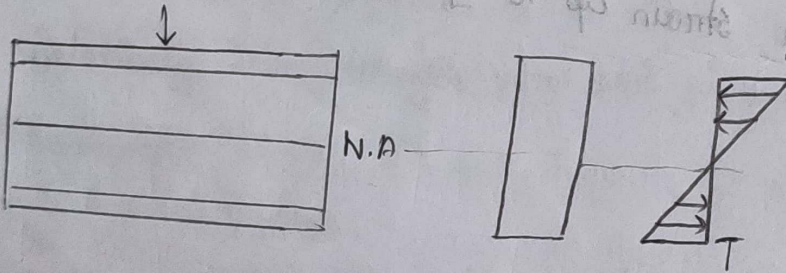
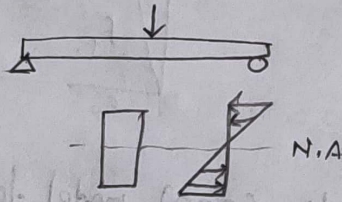
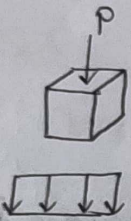
$$E_c (\text{Psi}) = 33 w^{1.5} \sqrt{f'_c (\text{Psi})}$$

w = unit weight

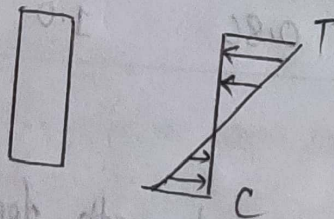
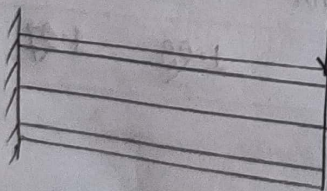
f'_c = compressive strength at 28 days.

□ Modulus of Rupture, f_r

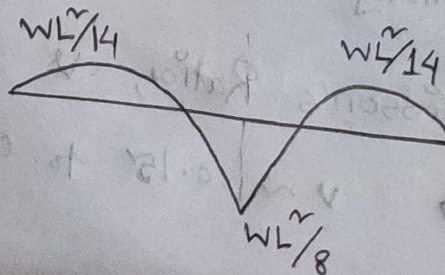
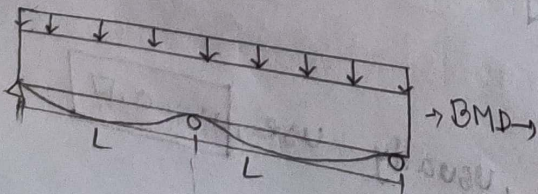
$$f_r = 7.5 \sqrt{f'_c (\text{Psi})}$$



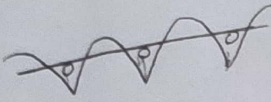
Cantilever beam



Continuous beam

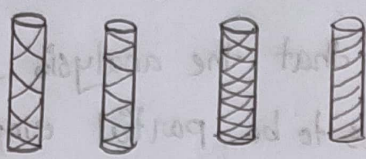
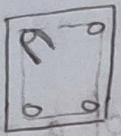


[Interior Support moment -ve]



18.5.21

Reinforcing Bars (Deformed bars)



Bonding ensure 3.3×10^{-6}

• Why is Mild steel Reinforcing Bar?

- The coefficient of concrete and steel (0.3×10^{-6} and 3.3×10^{-6}) are sufficiently close to resist undesirable differential thermal deformation.
- Corrosion resistance of bare steel is poor where as together use minimizes excellent corrosion resistant >> maintainan cost.
- Thermal conductivity of concrete is relatively low and provides insulation for steel rebars.

← Working stress Design Method

Strength Design Method

the service loads are increased sufficiently by factors to obtain the load at which failure is considered to be imminent. These factors are factored or factored service loads to occur.

Strength provided \geq strength required to carry factored loads

Advantage of USD over WSD

- 1) Consider mode of failure
- 2) Non linear behavior of concrete
- 3) More realistic F.S.

16.2.22

BMBC

ACI Building Codes

It is understandable that the analysis for strength of a reinforced concrete member has to be partial empirical although national.

These semi-national principles and methods are being constant as a result of theoretical and experimental research accumulate.

The American Concrete Institute (ACI), serves as clearing house for these changes, issues building code requirements.

Design Philosophy

WSD & USD, \rightarrow Ultimate strength Design
 \hookrightarrow Working Stress Design

Strength Design Method

the service loads are increased sufficiently by factors to obtain the load at which failure is considered to be 'imminent / close to occur'.
- factored load or factored service load.

$$\text{Strength provided} \geq \left[\begin{array}{l} \text{Strength required to} \\ \text{carry factored loads} \end{array} \right]$$

Advantage of USD over WSD

- ① Consider mode of failure
- ② Non linear behavior of concrete
- ③ More realistic F.S. (factor of safety)

④ Ultimate load prediction 5%

⑤ Saving

Safety Provisions

Structures and structural members must always be designed to carry some reserve load above what is expected under normal use.

There are 3 main reasons why some sort of safety factors ^{are necessary} in structural design -

- > Variability in resistance
- > Variability in loading
- > Consequences of failure

Consequences of failure

A number of subjective factors must be considered in determining an acceptable level of safety.

- Potential loss of life
- Cost of ~~clearing~~ the debris and replacement of the structure and its contents.
- Cost to society
- Type of failure warning of failure, existence of alternative & load paths.

Loading

1. Specifications

- BNBC (Bangladesh National Building Code.)

ACT, IS,

Environmental loads -

- Earthquake

- Tsunami

- Wind

- Soil
pressure

- Ponding of Rainwater

- Temperature Differential

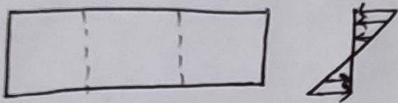
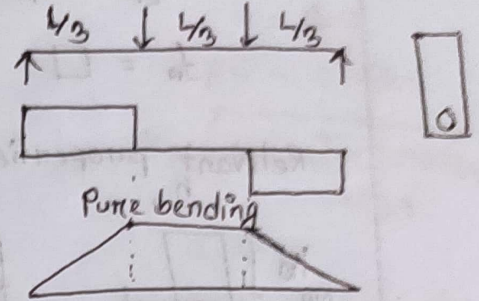
- Snow loads

$$f_s = n f_c$$

$$n = \frac{E_s}{E_c} = \frac{29 \times 10^6 \text{ (fixed)}}{57000 \sqrt{f'_c} \text{ (Psi)}}$$

13th edition ई

Article - 3.3 : Reinforced concrete beam behavior



load एवं परिभाषित बाड़ील crack बढ़ाव
moment समान रहनि, समान crack रूझाव
अनुभवना बिनि । Hair crack

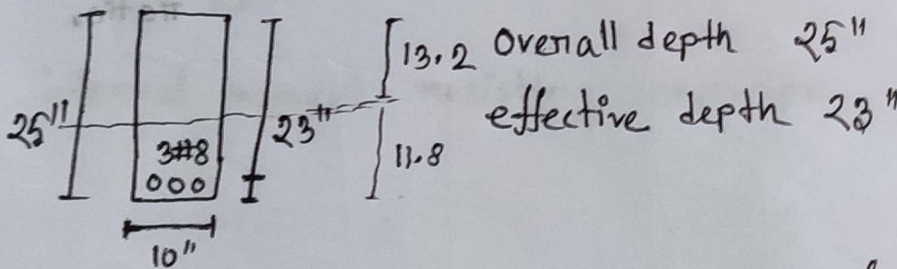
Concrete can not axially carry tensile load.

failure condition \hookrightarrow diagram non-linear -

Working Stress Design (WSD)

Ultimate strength Design (USD)

Stresses elastic section cracked - $3\#8 = 3 \text{ no. } 8 \text{ bar}$



Check weather the beam is cracked, if applied bending moment

$M = 90 \text{ kip-ft}$. Also calculation relevant properties,

$$I_t = 14740 \text{ in}^4$$

$$f_{ct} = \frac{M c}{I} = \frac{90 \times 12 \times 1000 \times 11.8}{14740} =$$

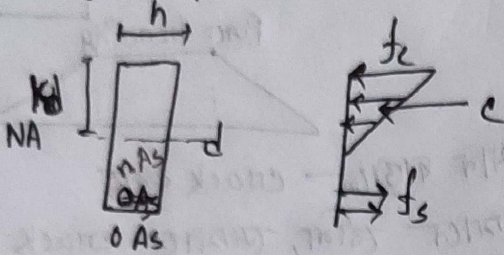
$$264.5 \text{ psi}$$

Tensile strength

$$f_{at} > f_n$$

$$f_n = \square$$

Relevant properties -

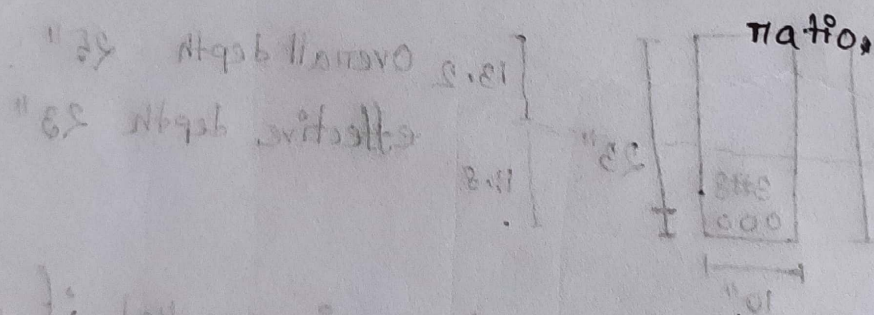


location of neutral axis can be found by equating the moment of tensile & compression triangles,

$$b \cdot kd \cdot \frac{kd}{2} = n A_s (d - kd) \quad (\text{moment})$$

$$kd = \square$$

$$k = \sqrt{(pn)^2 + 2pn} - pn \quad \text{where } p = \rho = \frac{A_s}{bd} = \text{reinforcement ratio}$$



Check whether the beam is cracked if applied bending moment is 30 kip-ft. Also calculate relevant properties.

$$I = \frac{1}{12} b d^3 = \frac{1}{12} \times 10 \times 20^3 = 6666.67 \text{ in}^4$$

$$I_{cr} = \frac{1}{12} b k^3 n^2 (n - kd) + n A_s (d - kd)^2$$

$$I_{cr} = \frac{1}{12} \times 10 \times 10^3 \times 0.02^2 (0.02 - 0.02 \times 15) + 0.02 \times 3 \times (15 - 0.02 \times 15)^2$$

$$I_{cr} = 0.0001 \times 10^4 \times 0.02^2 \times 0.02 \times 15 + 0.02 \times 3 \times 14.7^2$$

$$I_{cr} = 0.0001 \times 10^4 \times 0.02^2 \times 0.02 \times 15 + 0.02 \times 3 \times 216.09$$

$$I_{cr} = 0.0001 \times 10^4 \times 0.02^2 \times 0.02 \times 15 + 0.02 \times 648.27$$

$$I_{cr} = 0.0001 \times 10^4 \times 0.02^2 \times 0.02 \times 15 + 12.9654$$

$$I_{cr} = 0.0001 \times 10^4 \times 0.02^2 \times 0.02 \times 15 + 12.9654$$

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$$I_{cr} = 0.0001 \times 10^4 \times 0.02^2 \times 0.02 \times 15 + 12.9654$$

location of neutral axis =

২য় load বাড়বে, neutral axis ওত উল্টবে নাহবে।

$$p = \frac{3 \times 0.79}{10 \times 23}$$

$$= 0.0103$$

$$n = 8$$

$$pn = 0.0824$$

$$k = \sqrt{0.0824^2 + 2 \times 0.0824} - 0.0824$$

$$= 0.33$$

$$kd = 0.33 \times 23 = 7.63$$

$$\text{Total compression} = \frac{f_c}{bkd}$$

= comp. area \times average comp.

stress

$$= 10 \cdot kd \cdot \left(\frac{f_c + 0}{2} \right) = \frac{1}{2} f_c \cdot bkd$$

$$\text{Total tensile force} = A_s f_s$$

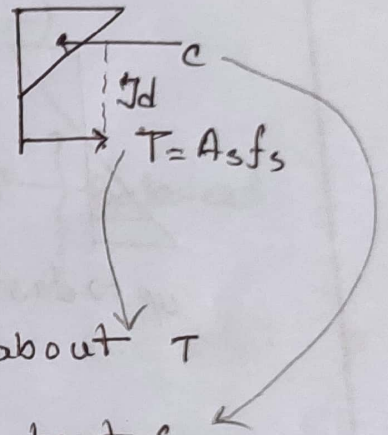
$$jd = d - \frac{kd}{3}$$

$$J = 1 - \frac{k}{3}$$

$$M = A_s f_s jd = Tjd \rightarrow \text{Taking moment about } T$$

$$M = \frac{1}{2} f_c j k b d^2 \rightarrow \text{Taking moment about } c$$

$$= cjd$$



internal moment resisting capacity - minimum μ_{min}

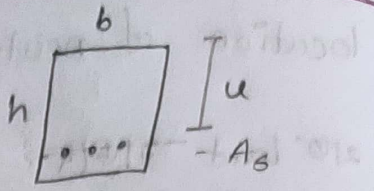
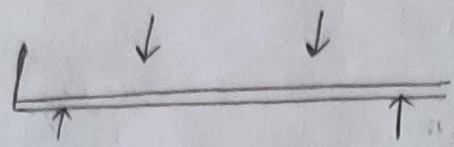
by secondary moment must be less than μ_{min}

- Concrete will not

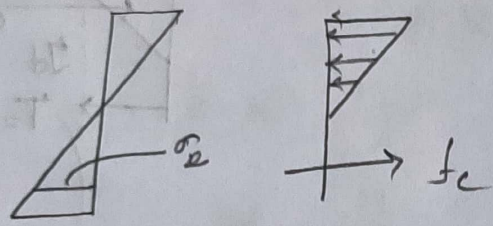
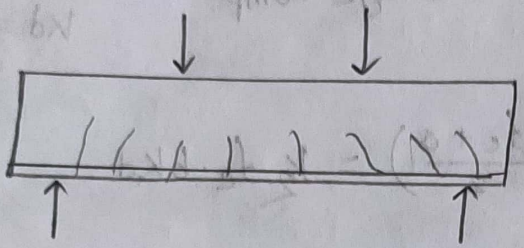
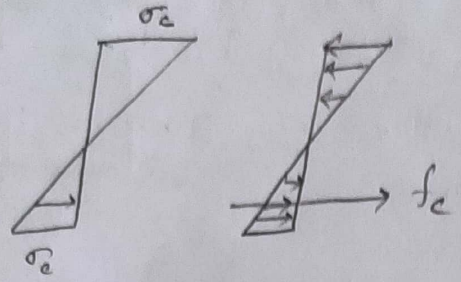
Compression failure - Concrete will yield first and steel will yield stress

the member is known as over-reinforced section.

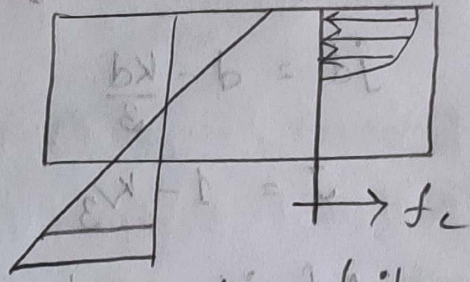
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fig 3.2



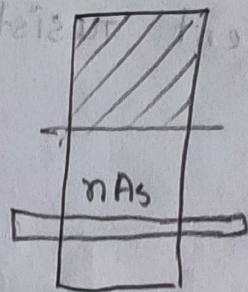
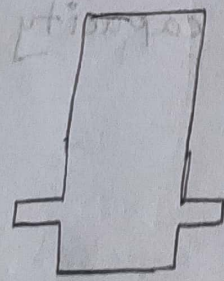
no cracking



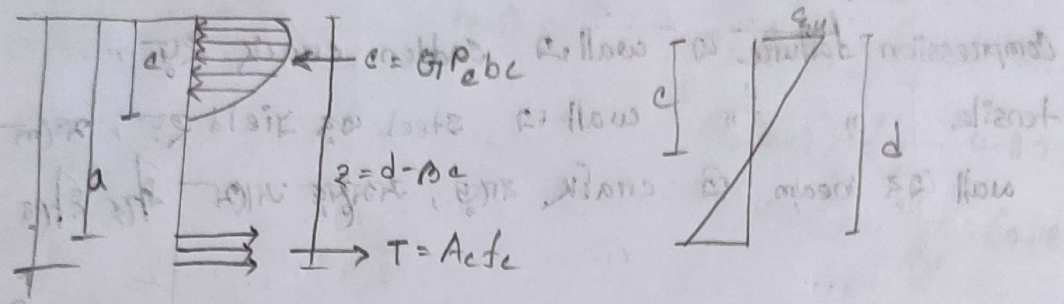
up to elastic limit



Just before failure
(USD method) = M



Flexural Strength - General Analysis

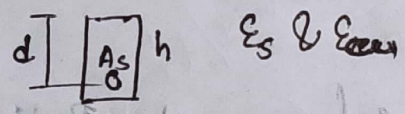


Three possibilities in inelastic Behavior -

- Compression Failure - (overreinforced beam)
- Tension Failure - (under reinforced beam)
- Balanced Failure - (Balanced reinforcement)

$f_y = 60000 \text{ psi}$ (Steel yield)

$\epsilon_y = \frac{f_y}{E_s}$



} Balanced

Balanced reinforcement ratio, $\rho = \frac{A_s}{bd}$

Tension Failure: Steel will yield first and concrete will fail

by secondary condition. ρ will be less than ρ_b .

- Concrete fail first - secondary.

Compression Failure: Concrete will yield first and steel will not reach yield stress.

this section is known as over reinforce section,

Compression failure is ~~better~~ ^{not better} than tensile failure. ~~Safest~~

Compression failure is wall is sudden crack રૂપ.

tensile " " wall is steel এর yield રૂપ, અને

wall এর beam is crack થાય, સમગ્ર આખર ફીટ ફીટ વાળું,

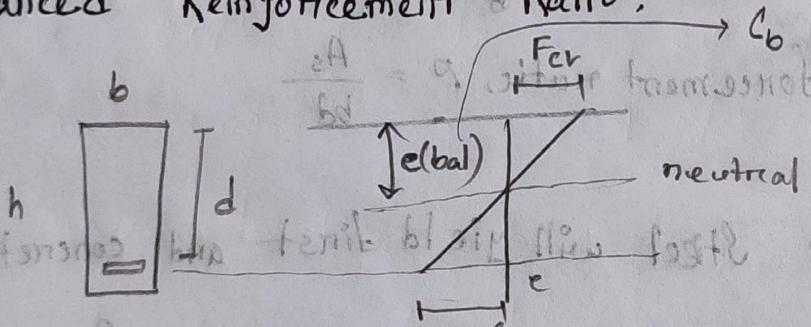
$f_c < f_y$
 $\rho > \rho_b$

over reinforce is - neutral axis
 under " " - " નીચે

(over reinforced beam) - tension failure
 (under reinforced beam) - compression failure
 (balanced reinforcement) - balanced failure

balanced {
 (steel ના yield) $f_y = 60000 \text{ psi}$
 $\frac{f_y}{E_s} = \rho_b$

Balanced Reinforcement Ratio.



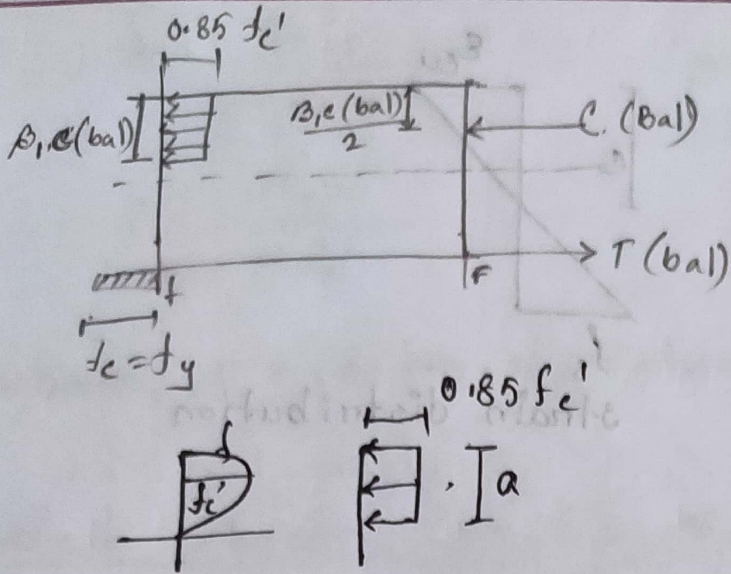
(a) Beam Section

(b) balanced strain distribution.

$$\frac{\rho_b}{\epsilon_{cu}} = \frac{d}{\epsilon_{cu} + \epsilon_y} \quad \rho_b = \left(\frac{\epsilon_{cu}}{\epsilon_{cu} + \epsilon_y} \right) d$$

$\epsilon_{cu} = 0.003 \sim 0.004$

ACI, $\epsilon_{cu} = 0.003$



$$T(\text{bal}) = C_c(\text{bal})$$

$$A_s(\text{bal}) \times f_y = 0.85 f_c' a_b b$$

$$A_s(\text{bal}) \times f_y = 0.85 f_c' (B_1 c_b) b$$

$$A_s(\text{bal}) = \frac{1}{f_y} \cdot (0.85 B_1 f_c' c_b b)$$

$$T(\text{bal}) = A_s f_y$$

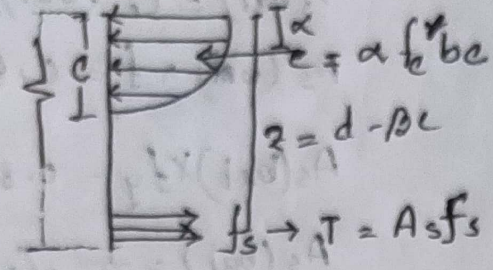
$C_c =$ Compression area \times Compression stress
 with \downarrow beam \times depth of
 beam comp. block $\rightarrow a \rightarrow B_1 c$

$$\rho_b = \frac{A_s(\text{bal})}{bd} = \frac{0.85 B_1 f_c'}{f_y} \times \frac{b}{bd} \times \left(\frac{\epsilon_{cu}}{\epsilon_{cu} + \epsilon_y} \right) d$$

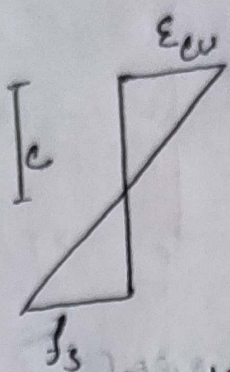
$$\rho_b = \frac{0.85 B_1 f_c'}{f_y} \left(\frac{\epsilon_{cu}}{\epsilon_{cu} + \epsilon_y} \right)$$

Substitute $\epsilon_{cu} = 0.003$ and multiplying both numerator and denominator by $E_s = 29,000,000$

$$\rho_b = 0.85 \times \frac{B_1 f_c'}{f_y} \cdot \left(\frac{87,000}{87,000 + f_y} \right)$$



Stress distribution



strain distribution

Under reinforced section :

The value of f_s here is equal to f_y .

1. $f_s = f_y$.
2. $c = \alpha f_c' b e$
 $a = \frac{f_y A_s}{f_c' b e}$ = area of compression block.
3. $\alpha = 0.72$ for f_c' less or equal to 4000 psi and decrease by 0.04 for every 1000 psi above 4000 psi.
4. $\beta = 0.425$ for f_c' \leq 4000 psi and decrease by 0.025 for every 1000 psi above 4000 psi.

$T = \text{Area of steel} \times \text{stress in steel}$

$c = T$
 $\Rightarrow \alpha f_c' b e = A_s f_y$

$$c = \frac{A_s f_y}{\alpha f_c' b}$$

$$\rho = \frac{A_s}{bd}$$

$$c = \frac{\rho f_y d}{\alpha f_c'}$$

where, c = depth of neutral axis from compression face

Nominal Moment Capacity (M_n):

$$M_n = T_2 = A_s f_y (d - \beta c)$$

$$c = \frac{\rho f_y d}{\alpha f_c'}$$

$$M_n = A_s f_y \left(d - \frac{\beta \rho f_y d}{\alpha f_c'} \right)$$

$$\beta = 0.425$$

$$\alpha = 0.72$$

$$= A_s f_y \left(1 - 0.59 \frac{f_y}{f_c'} \rho \right)$$

Taking

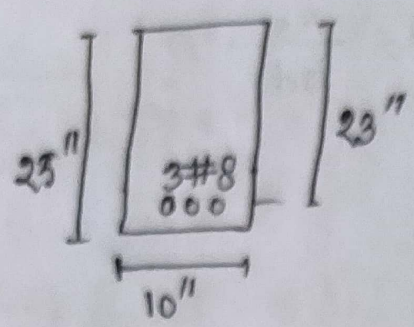
$$M_n = c_2 = \alpha f_c' b c (d - \beta c)$$

$$= \alpha f_c' b \frac{\rho f_y d}{\alpha f_c'} \left(d - \beta \frac{\rho f_y d}{\alpha f_c'} \right)$$

$$= \rho f_y b d \left(d - 0.59 \frac{f_y \rho}{f_c'} d \right)$$

$$= \rho f_y b d^2 \left(1 - 0.59 \frac{\rho f_y}{f_c'} \right) = R b d^2$$

Problem :



$$f_y = 60000 \text{ psi}$$
$$f_c = 4000 \text{ psi}$$

- determine
1. Working moment capacity
 2. Nominal moment at which the beam will fail.

Solⁿ : 1. Working moment capacity

$$M = \frac{1}{2} f_c J k b d^2$$

$$M = A_s f_s J d$$

(যাওঁতে কম মান পাব
সম্পূৰ্ণ নিৰ্ভৰ হিমাৰ
কৰিব)

Relevant properties :

$$n = 8, k = 0.33, J = 0.89$$

f_c = allowable stress of concrete

$$= 0.45 f_c' = 0.45 \times 4000 = 1800 \text{ psi}$$

f_s = allowable stress of steel

$$= 0.4 f_y = 0.4 \times 60000 = 24000 \text{ psi}$$

$$M = \frac{1}{2} \times 1800 \times 0.89 \times 60.33 \times 10 \times 23^2 = 1.39 \times 10^6$$

$$= 116.5 \text{ k-ft}$$

$$M = 2.37 \times 24000 \times 0.89 \times 23 = 1.16 \times 10^6 = 97.03 \text{ k-ft}$$

2. Nominal moment capacity : (depends on mode of failure)

$\rho < \rho_b$ \Rightarrow under reinforce.

$$\rho_b = 0.85 \beta_1 \frac{f_c'}{f_y} \frac{\epsilon_{cu}}{\epsilon_{cu} + \epsilon_y}$$

$\beta_1 = 0.85$ for

$f_c' \leq 4000 \text{ psi}$

and decrease by

0.05 for every

1000 psi above

4000 psi.

Here, $\beta_1 = 0.85$

$$\epsilon_y = \frac{f_y}{E_s} = \frac{60000}{29 \times 10^6} = 0.0021$$

$$\epsilon_{cu} = 0.003$$

$$\rho_b = 0.85 \times 0.85 \times \frac{4000}{60000} \times \frac{0.003}{0.003 + 0.0021}$$

$$= 0.028$$

$$\rho = \frac{A_s}{bd} = \frac{2.37}{10 \times 23} = 0.0103$$

$$\rho < \rho_b$$

Thus, the section is underreinforce section and tension failure will occur.

$$M_n = A_s f_y d (1 - 0.59 \frac{f_y}{f_c'} \rho)$$

$$= 2.97 \times 10^6 \text{ lb-in}$$

$$= 247.5 \text{ k-ft}$$

$$c = \frac{\rho f_y d}{\alpha f_c'} = \frac{0.0103 \times 60000 \times 23}{0.72 \times 4000} = 4.93''$$

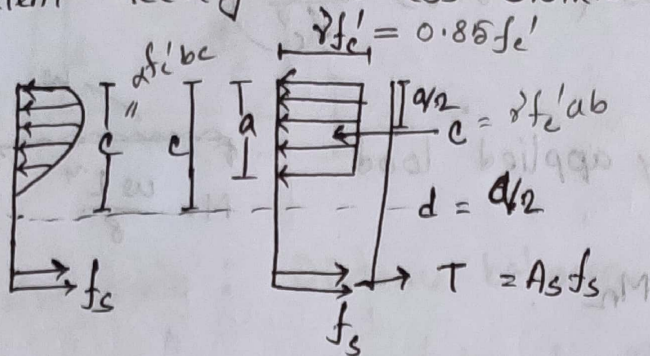
$$c_b = ?$$

12.04.2022

Equivalent Rectangular Stress Distribution

Condition:

$$f_c = \alpha f_c' \quad b e = \beta f_c' a b$$



$$a = \beta_1 c$$

$\beta_1 = \beta = 0.85$ for $f_c' \leq 4000$ psi and decrease by 0.05 for every 1000 psi above 4000 psi.

$$\beta = \alpha / \beta_1 = 0.85 \text{ for } f_c' \leq 6000 \text{ psi}$$

Under reinforced Section:

$$f_s = f_y$$

$$C = T$$

$$\Rightarrow 0.85 f_c' a b = A_s f_y$$

$$a = \frac{A_s f_y}{0.85 f_c' b} = \frac{\rho f_y d}{0.85 f_c'} \quad \left[\rho = \frac{A_s}{b d} \right]$$

Moment Nominal moment Capacity, $M_n = T \cdot z = A_s f_y (d - a/2)$

$$M_n = C \cdot z = 0.85 f_c' a b (d - a/2)$$

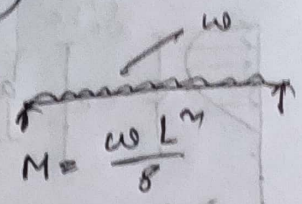
$$= 0.85 f_c' \beta_1 c b \left(d - \frac{\beta_1 c}{2} \right) \quad [a = \beta_1 c]$$

$$= 0.85 f_c' \beta_1 \beta f_c' a b \cdot b \left(d - \frac{\beta_1 \beta f_c' a b}{2} \right)$$

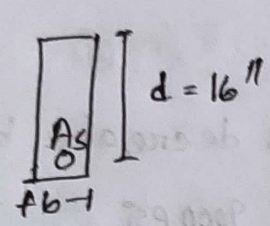
$$= 0.85 f_c' \beta_1 \beta a b \left(d - \frac{\beta_1 \beta f_c' a b}{2} \right)$$

$$= \rho f_y b d^2 \left(1 - 0.59 \rho \frac{f_y}{f_c'}\right)$$

moment produced by applied load



moment capacity M_n



Ultimate moment capacity / Design moment =

$$M_u = \phi M_n \quad \phi = \text{Capacity Reduction Factor}$$

Value of ϕ depends on -

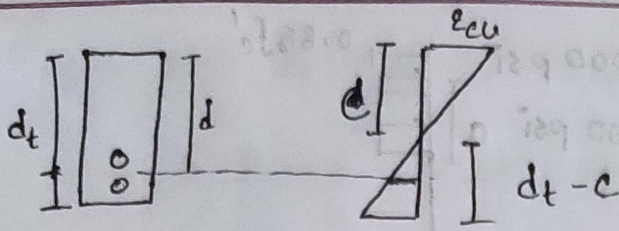
- ① Mode of failure
- ② Consequence of failure

(beam column এর failure এর মান কমাতে ϕ use করি) Tensile/compression এর ϕ কমা

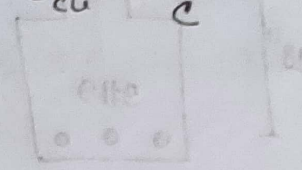
$\phi = 0.9$ if $\epsilon_t \geq 0.005$	— Tensile
$\phi = 0.65$ if $\epsilon_t \leq 0.002$	— Compression

$$\phi = 0.65 + (\epsilon_t - 0.002) \frac{250}{3}$$

ϵ_t = Net tensile strength



$$\epsilon_t = \epsilon_{cu} \frac{d_t - c}{c}$$



Effective depth : - Distance between compression phase and centroid of the tensile reinforcement.

$d_t =$ Distance between compression phase and furthest layer of reinforcement. (जगत्प्रेमिणि)

$d_t > d$ for multiple layer reinforcement

$d_t = d$ for single layer reinforcement.

मार्गदर्शक प्रश्न ultimate moment = ?

$$\frac{10 \times 18 \times 0.8 \times 0.8 \times 0.8}{20} = \frac{A_s \times 0.8 \times 0.8 \times 0.8}{20}$$

$$10 \times 18 = A_s$$

$$\frac{1 \times 18}{(0.8 \times 18) - (0.8 \times 0.8)} = \frac{A_s}{bd} = \rho$$

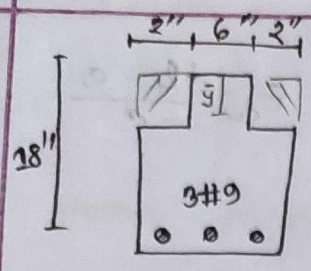
$$10 \times 18 = A_s$$

जब $\rho > \rho_{lim}$, the section is under reinforced section

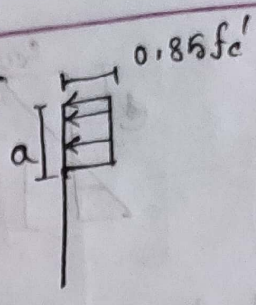
$$\rho_t = \rho$$

$$0.8 \times 18 \times 0.8 \times 0.8 \times 0.8 = 0.8 \times 18 \times 0.8 \times 0.8 \times 0.8$$

$$0.8 \times 18 \times 0.8 \times 0.8 \times 0.8 = A_s \times 0.8 \times 0.8 \times 0.8 \times 0.8$$



$f_c' = 5000 \text{ psi}$
 $f_y = 6000 \text{ psi}$
 $M_n = ?$
 $M_u = ?$



$c = 0.85 f_c' a b$

Soln:

Balance steel ratio, $\rho_b = 0.85 \beta_1 \frac{f_c'}{f_y} \frac{\epsilon_a}{\epsilon_u + \epsilon_y}$

$\beta_1 =$

$\beta_1 = 0.85 - 0.05 = 0.80$

$\epsilon_y = \frac{f_y}{E_s} = \frac{60000 \text{ psi}}{29 \times 10^6 \text{ psi}} = 0.002$

$\rho_b = 0.85 \times 0.80 \times \frac{5}{60} \times \frac{0.003}{0.003 + 0.002}$
 $= 0.034$

$\rho = \frac{A_s}{bd} = \frac{3 \times 1}{10 \times 18 - (2 \times 3 \times 2)}$
 $= 0.017$

$\rho < \rho_b$, so, the section is under reinforced section.

Steel will yield, $f_s = f_y$

$c = 0.85 f_c' a b$ (अवस्थागत बाहू शक्ति)
 $= 0.85 f_c' \times (2 \times 3) \times 2$
 $i = A_s f_y = 3 \times 60$

$$c = 0.85 f_c' \times ab - 0.85 f_c' \times (2 \times 3 \times 2)$$

$$\Rightarrow 3 \times 60 = 0.85 \times 5000 \times a \times 10 - 0.85 \times 5000 \times 2 \times 3 \times 2$$

$$\Rightarrow a = 5.44''$$

$$c = \frac{a}{\beta_1} \Rightarrow c = \frac{5.44}{0.80} = 6.8''$$

$$M_n = A_s f_y \times (d - a/2) \times$$

$$= A_s f_y (d - \bar{y})$$

$$= 3 \times 60000 (18 - 3.06)$$

$$= 2.68 \times 10^6$$

$$\epsilon_t = \epsilon_u \frac{d_t - c}{c}$$

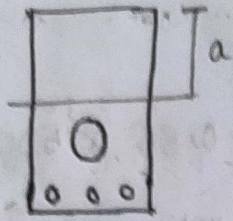
$$= 0.003 \times \frac{18 - 6.8}{6.8} = 0.0049 < 0.005$$

$$\phi < 0.9$$

$$M_u = \phi M_n$$

$$= 0.9 \times 2.68 \times 10^6$$

$$=$$



Over reinforced section:

under reinforced $\rightarrow f_s = f_y$
 $c = T = A_s f_y$

for over reinforced $\rightarrow f_s < f_y$

$$f_s = \epsilon_s E_s$$

$$= \epsilon_u \frac{d-c}{c} E_s$$

$$T = A_s f_s = A_s E_s \epsilon_u \frac{d-c}{c}$$

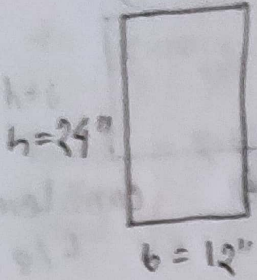
$$c = 0.85 f_c' a b = 0.85 f_c' \beta_1 c b \quad \frac{812 - 81}{8.2} \times 1000.0 =$$

$$c = T \Rightarrow 0.85 \beta_1 f_c' b c = A_s E_s \epsilon_u \frac{d-c}{c}$$

$$c = ?$$

$$M_u = \phi M_n = \phi A_s f_y (d - a) = \phi A_s f_y \left(d - \frac{A_s f_y}{0.85 f_c' b} \right)$$

10 → Beam



$$f_c' = 5000 \text{ psi}$$

$$f_y = 60,000 \text{ psi}$$

$$d =$$

Moment eq $M = \frac{1}{2} f_c' J k b d^2$

যদি $b > d$ রোগা সুবিশিষ্টক, কারণ bending d এর জন্য বেশি বাড়বে।

So, maximum moment বাড়বে।

$$\hookrightarrow \text{deflection} \propto \frac{1}{i E_s} \quad i = \frac{b h^3}{12} \quad b \times h$$

So, deflection কম হবে

Calculate the amount of reinforcement to ensure:

1. Tension failure
2. Balanced failure
3. Compression failure

1. Tension failure

$$\rho_b = \frac{A_s}{b d} =$$

$$A_s b = \rho_b \times b d = 0.034 \times 12 \times 24 = 9.792$$

$$h = 24$$

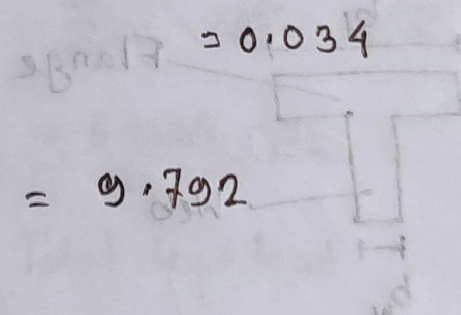
$$d = h - (\text{---}) = 21$$

$$A_s b = \rho_b \times b d = 0.034 \times 12 \times 21 = 8.57 \text{ in}^2$$

$$d = h - (\text{---}) A_s = 10 \text{ in}^2 \quad (\text{over reinforced section})$$

$$A_s = 6.00 \text{ in}^2 \quad (\text{Under reinforced section})$$

17.05.22



Design of Simply reinforced Beam (USD method)

Minimum thickness of beam, $t =$

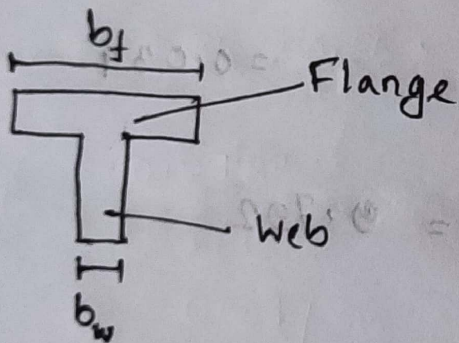
	Simply supported	one end cont.	Both end cont.	Cantilever
$t =$	$\frac{L}{6}$	$\frac{L}{18.5}$	$\frac{L}{24}$	$\frac{L}{8}$

Minimum reinforcement

$$A_s = \frac{3\sqrt{f_c'}}{f_y} b_w d \geq \frac{200 b_w d}{f_y}$$

Maximum reinforcement

$$\rho_{max} = 0.85 \beta_1 \frac{f_c'}{f_y} \frac{\epsilon_u}{\epsilon_u + 0.005}$$



$$\rho = \frac{A_s}{b d}$$

$$A_s = \rho \times b d = 0.02 \times 10 \times 25 = 5 \text{ in}^2$$

$$\rho = 0.02$$



$$A_s = \rho \times b d = 0.02 \times 10 \times 25 = 5 \text{ in}^2$$

(over reinforced section) $\rho > \rho_{max}$

(Under reinforced section) $\rho < \rho_{max}$

$A_s = \rho \times b d$

Problem - 1 : Design a simply supported beam over 20' span

to carry a superimposed dead load = 2 k/ft and a live load = 2.5 k/ft. Follow USD method and use $f_c' = 4000$ psi and $f_y = 60000$ psi.

(additional load)

[Superimposed বর্ধিত dead load আলাদা হিসাব করে]

Solⁿ: $t_{min} = \frac{20 \times 12}{16} = 15$ in.

Let, 12x18 in section will be used

Load calculation:

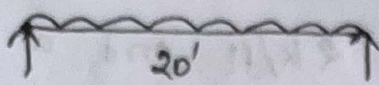
1. Dead load :

① Self weight of the beam : $\frac{12 \times 18}{12 \times 12} \times 150 = 225$ lb/ft
 $= 0.225$ k/ft

② Superimposed dead load = 2 k/ft
 Total dead load = $\frac{2 + 0.225}{2.225} = 2.225$ k/ft

2. Live load = 2.5 k/ft

3. Factored load $W_u = 1.2 DL + 1.6 LL = 1.2 \times 2.225 + 1.6 \times 2.5 = 5.87$ k/ft

$$w_a = 6.67 \text{ K/ft}$$


$$M_{\text{Max}} = \frac{w_a L^2}{8}$$

$$= \frac{6.67 \times (20)^2}{8}$$

$$= 333.5 \text{ K-ft}$$

Dead load, live load γ (স্বাভাবিক ও নিম্নতম), safety γ (সুরক্ষার গুণক)

Depth check :

$$M_u = \phi M_n$$

$$M_n = \rho f_y b d^2 \left(1 - 0.59 \frac{\rho f_y}{f_c'} \right)$$

$$= \rho f_y b d^2 \left(1 - 0.59 \frac{\rho f_y}{f_c'} \right)$$

$$\rho_{\text{max}} = 0.85 \times 0.85 \times \frac{4}{60} \times \frac{0.003}{0.003 + 0.005}$$

$$= 0.018$$

Let, $\rho = 0.017$ $\phi = 0.9$

$$M_u = \phi M_n$$

$$\Rightarrow 333.5 \times 12 = \phi \rho f_y b d^2 \left(1 - 0.59 \frac{\rho f_y}{f_c'} \right)$$

$$= 0.9 \times 0.017 \times 60 \times 12 \times d^2 \left(1 - 0.59 \frac{0.017 \times 60}{4} \right)$$

$$\Rightarrow d = 20.67'' \quad (\text{depth required})$$

$$t = 18''$$

$$\therefore d_{\text{act}} = 18 - 2.5 = 15.5 \quad (\text{Actual depth}) < d_{\text{required}}$$

Section should be revised.

Trial #2: 12" x 24"

$$\text{Self weight} = \frac{12 \times 24}{12 \times 12} \times 150 = 300 \text{ lb/ft} = 0.3 \text{ k/ft}$$

$$\text{Super imposed dead load} = 2 + 0.3 = 2.3$$

$$\text{Factored load } w_u = 1.2 \times DL + 1.6 LL = 1.2 \times 2.3 + 1.6 \times 2.5 = 6.76 \text{ k/ft}$$

$$M_u = \phi M_n$$

$$M_{\max} = \frac{w_u L^2}{8} = \frac{6.76 \times 12^2}{8} = 338$$

$$338 \times 12 = 0.9 \times 0.017 \times 60 \times 12 \times d^2 \left(1 - 0.59 \frac{0.017 \times 60}{4} \right) = 338$$

$$d =$$

$$t = 18$$

$$d_{\text{act}} = 24 - 2.5 = 21.5 > d_{\text{required}}$$

$$\frac{\rho b A}{d' b A} = \rho = 0.017$$

$$\frac{0.017 \times 60}{1.1 \times 12 \times 21.5} = 0.017$$

24.05.22

Reinforcement Calculation:

$$A_s = \rho b d$$

$$M_u = \phi M_n = \phi A_s f_y \left(d - \frac{a}{2}\right)$$

$$a = \frac{A_s f_y}{0.85 f_c' b}$$

$$\Rightarrow A_s = \frac{M_u}{\phi f_y \left(d - \frac{a}{2}\right)} = \frac{338}{0.9 \times 60 \left(21.5 - \frac{1.47 A_s}{2}\right)}$$

$$a = \frac{A_s \times 60}{0.85 \times 4 \times 12} = 1.47 A_s \text{ in}$$

$$\therefore A_s = 4.06 \text{ in}^2$$

Method 2:

$$A_s = \frac{M_u}{\phi f_y \left(d - \frac{a}{2}\right)}$$

$$\text{let, } a = 6'' \quad \left[\frac{t}{4} \text{ or } \frac{d}{4} \right]$$

assume $a = 6''$

$$= \frac{338 \times 12}{0.9 \times 60 \left(21.5 - \frac{6}{2}\right)} = 4.06 \text{ in}^2$$

$$\text{check } a = \frac{A_s f_y}{0.85 \times f_c' b}$$

$$= \frac{4.06 \times 60}{0.85 \times 4 \times 12} = 5.97 \text{ in}$$

a ^{মান} $\frac{t}{4}$ ^{সহায়ক} $\frac{d}{4}$ না আছে তাহলে check করতে হবে।

হবে।

A_s को eqⁿ solve करने पर $A_s < P_{max} b d$ 20 20 1
 ग्रहण acceptable.

$$A_{smin} = \frac{3\sqrt{f_c'}}{f_y} b w d = \frac{3\sqrt{4000}}{60000} \times 12 \times 21.5$$

$$= 0.82 \text{ in}^2$$

$$A_{smin} = \frac{200}{f_y} b w d = \frac{200}{60000} \times 12 \times 21.5 = 0.86 \text{ in}^2$$

minimum को अक्ष्य पर 20 को अधिकतम reinforcement प्राप्त

20 1

$$A_{smin} = \frac{3\sqrt{f_c'}}{f_y} \times b w d \geq \frac{200}{f_y} b w d \text{ should be.}$$

Bar size #5

A =

$$A_1 = 0.6 \text{ in}$$

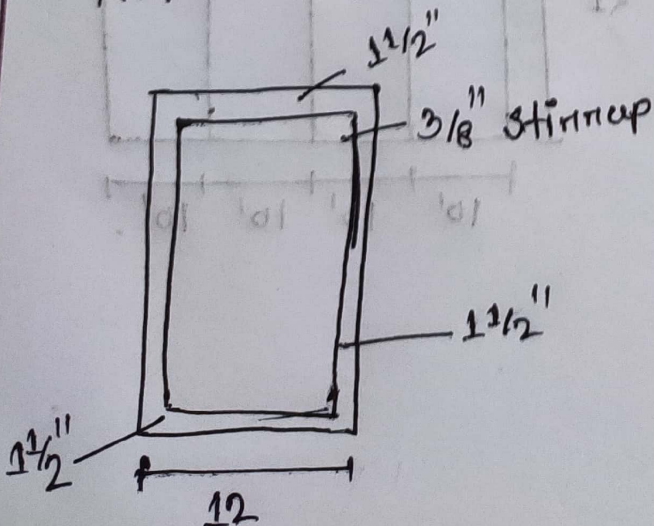
$$n = \frac{4.06}{0.6} = 6.77 \approx 7$$

$$A_1 = \frac{4.06}{0.6}$$

4#9 $A_s = 4.00 \text{ in}^2$

6#8 $A_s = 4.74 \text{ in}^2$

7#7 $A_s = 4.20 \text{ in}^2$



6#8 $\rightarrow A_s = 4.06 \text{ in}^2$

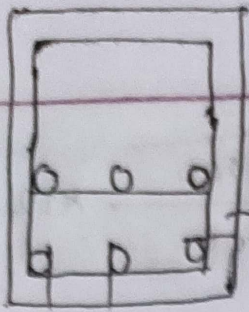
7#7 $\rightarrow A_s = 4.20 \text{ in}^2$

8#

$$b - 2 \times 1.5 - 2 \times \phi_s \rightarrow \text{stirrup}$$

$$= 12 - 3 - 0.75$$

$$= 8.25 \text{ in.}$$



min 1"
 1.33 x max^m agg. size

d = p
 min^m = 1"

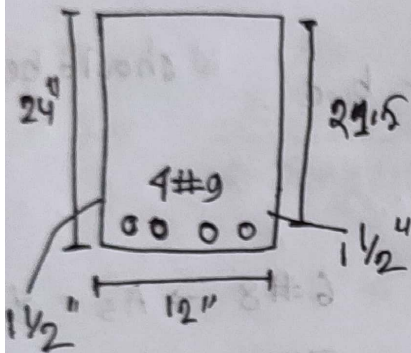
1.33 max^m aggregate size

dia = 1", 5 टा के layer पर

अवकाश 5x1 + 20mm

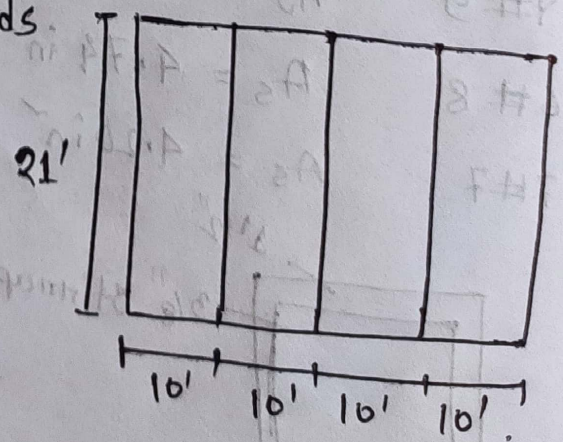
$$अवकाश (4\frac{1}{2}) \times 1 = 9 > 8-25$$

किस layer के अवकाश 4 टा bar पर था, 1



Design a beam using the following information.

1. slab thickness = 6"
2. live load on the floor = 50 psf
3. beams are fixed at both ends.
4. $f_c' = 3000$ psi
5. $f_y = 60,000$ psi
6. Design method WSD.



Qualitative beam moment diagram:



$$U_3 = \frac{V_{max}}{\sum f_i d}$$

$$\Sigma = \pi d$$

05.06.2022