

লগারিদম

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বিগত বিসিএস এর প্রশ্ন বিশ্লেষণ

- $\log_{\sqrt{x}} 8 = 3\frac{1}{3}$ হলে x এর মান কত? [৪৬তম বিসিএস]
- যদি $\log\left(\frac{a}{b}\right) + \log\left(\frac{b}{a}\right) = \log(a + b)$ হয়, তবে- [৪৫তম বিসিএস]
- $2 \log_{10} 5 + \log_{10} 36 - \log_{10} 9 = ?$ [৪৪তম বিসিএস]
- ✓ • $2^{\log_2 3 + \log_2 5}$ [৪৩তম বিসিএস]
- $\log_x \frac{1}{9} = -2$ হলে, x এর মান কত? [৪২তম বিসিএস]
- $\log_2 \log_{\sqrt{e}} e^2 = ?$ [৪১তম বিসিএস]
- কোন শর্তে $\log \frac{1}{a} = 0$ [৪০তম বিসিএস]
- $\log_x \frac{1}{8} = -2$ হলে, x এর মান কত? [৩৮তম বিসিএস]
- $\log_x \frac{3}{2} = -\frac{1}{2}$ হলে, x এর মান কত? [৩৭তম বিসিএস]

বিগত বিসিএস এর প্রশ্ন বিশ্লেষণ

- $\log_{\sqrt{3}} 81 =$ কত? [৩৬তম বিসিএস]
- $\log_a x = 1, \log_a y = 2$ এবং $\log_a z = 3$ হলে, $\log_a \frac{x^3 y^2}{z}$ এর মান কত? [৩৫তম বিসিএস]

৭৩ → ১

$$2^{\textcircled{3}} = 8$$

$$2^{\square} = 8$$

Q.

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Ans: 3

$$\log_2 8 = \textcircled{3}$$

$$\log_3 81 = 4$$

Diagram illustrating the logarithm operation:

- The expression $\log_3 81$ is shown with a triangle pointing to the base 3, which is circled and labeled "Base".
- The number 81 is circled and labeled "Argument".
- The result 4 is circled and underlined.

$$3 \times 3 \times 3 \times 3 = 81$$

$$3^4 = 81$$

$$\log_a N^x = x$$

\Rightarrow \log_a \rightarrow \log

$$\rightarrow \boxed{a > 0, a \neq 1}$$

$$\log_{-2} x^{-1} = \frac{1}{2}$$

\Rightarrow \log_{-2} \rightarrow \log

$$\rightarrow (-2)^{\frac{1}{2}} = x$$

$$\Rightarrow \sqrt{-2} = x$$

$$\log_1 4$$

$$\log_0 5 =$$

Ans:

$$1^1 = 1$$

$$1^2 = 1$$

$$1^{\text{Ashik}} = 1$$

$$\log_a \textcircled{N} = \textcircled{x}$$

$$N > 0$$

$$\rightarrow a^{\textcircled{x}} = \textcircled{N}$$

$$= \textcircled{N}$$

a \downarrow স্বাভিক সংখ্যা

$$e = 2.71828 \dots$$

$$2^{-2} = \frac{1}{2^2} = \frac{1}{4}$$

$$2^2 = 4$$

$$2^0 = 1$$

$$\log_2 8$$

3

power 2, 4, 8, 16

$$a^{(3)} \times a^{(2)} = a^{(3+2)}$$

$$\log_a (M \times N) = \log_a M + \log_a N$$

$$\log_a \frac{M}{N} = \log_a M - \log_a N$$

$$\log_a m^{\textcircled{3}} = \boxed{3 \log_a m}$$

$$\log_a m^3 = \log_a m \times m \times m = \log_a m + \log_a m + \log_a m$$

$$= \textcircled{3} \log_a m$$

$$8^{\frac{1}{3}} = 2^{\frac{3}{3} \times \frac{1}{3}} = 2^1$$

$$\log_2 8 = 3$$

$$\log_8 2 = \frac{1}{3} = \frac{1}{\log_2 8}$$

$$\log_a b = \frac{1}{\log_b a}$$

$$\log_2 64 = 6$$

$$\begin{array}{r} \log_2 64 = \log_4 64 \times \log_2 4 \\ \hline 6 = 3 \times 2 \end{array}$$

$$\checkmark \log_a b = \log_m b \times \log_a m \quad \boxed{\times}$$

$$\checkmark \log_{\log} \text{ଅର୍ଥକ} = \log_{\log} \text{ଅର୍ଥକ} \times \log_{\log} \text{ଅର୍ଥକ}$$

$$\log_a b = \log_m b \times \log_a m \quad \text{✓} \quad \textcircled{+}$$

$$= \log_m b \times \frac{1}{\log_m a}$$

↖

$$\log_a b = \frac{\log b}{\log a}$$

$$\log_a b = \frac{\log b}{\log a}$$

$$\boxed{10^2 = 100}$$

$$\begin{array}{c} \log \\ \swarrow \searrow \\ \textcircled{10} \quad \textcircled{100} \end{array} = 10^2 = 100$$

$$\log_{10} 100 = 2$$

$$\log_{10} 100 = 100$$

Samira

\log_{samira} shakib

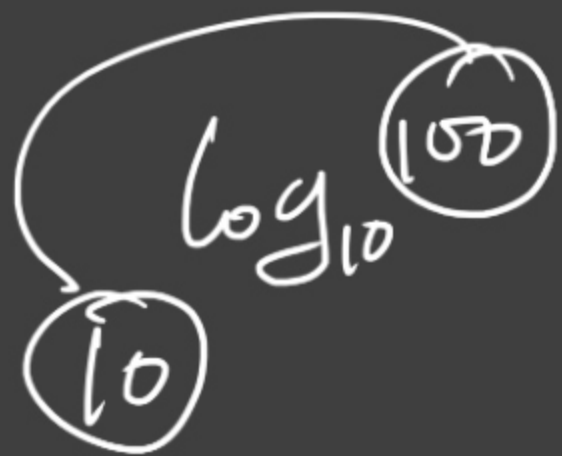
= shakib

$$\log_a b = b$$

$$\log_{10} 10 = 1$$

$$\log_{10} \log_{10} 100 = 100$$

$$\log_{10} \log_{10} 100 = 100$$

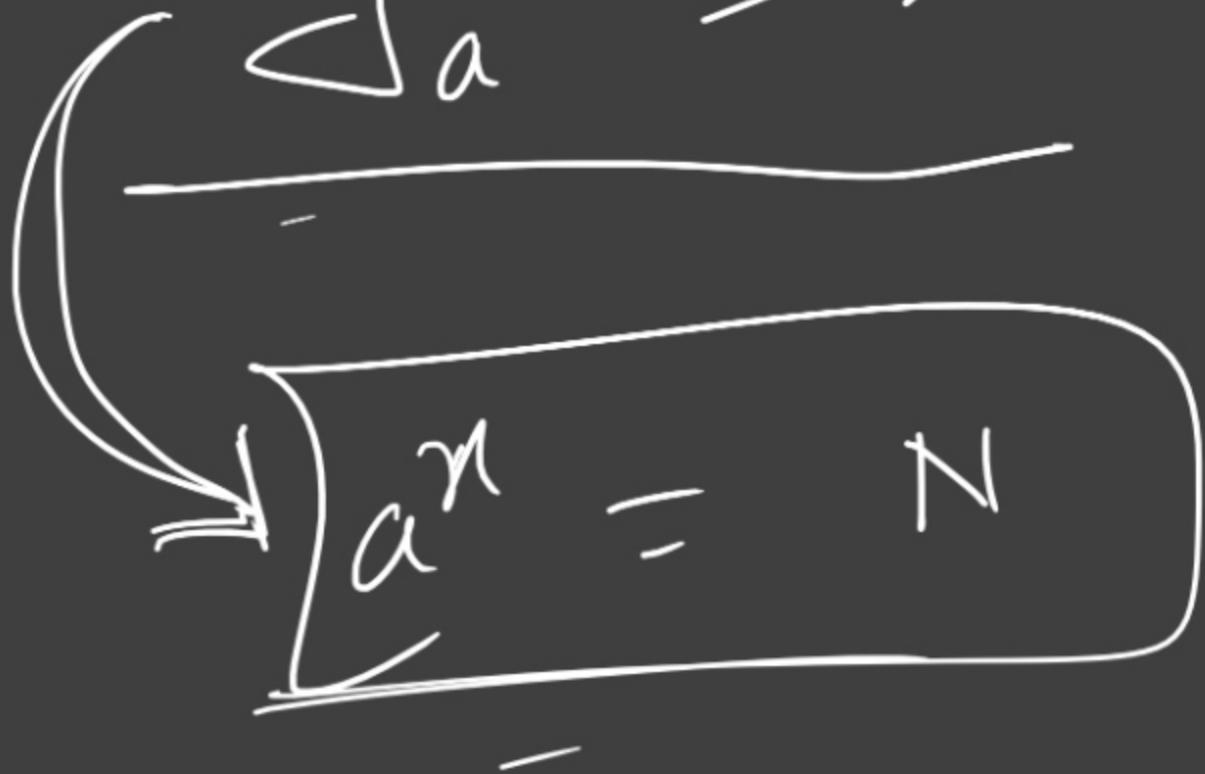


$$= 100 \log_{10} 10$$



$$= y \log_a x$$

$$\log_a N = x$$


$$a^x = N$$

লগারিদমের সূত্রাবলি

- যদি $a^x = N$ ($a > 0, a \neq 1$) হলে, $x = \log_a N$ [যেখানে $N > 0$]
- $\log_a (m \times n) = \log_a m + \log_a n$
- $\log_a \left(\frac{m}{n}\right) = \log_a m - \log_a n$
- $\log_a m^n = n \log_a m$
- $\log_a m = \log_b m \times \log_a b$
- $\log_a m = \frac{\log m}{\log a}$

লগারিদমের সূত্রাবলি

- $a^{\log_a b} = b$
- $\log_a a = 1$
- $\log_a 1 = 0$
- $\log_a b = x$ হলে, $a^x = b$
- $x^{\log_a y} = y^{\log_a x}$
- $\log_{a^n} b^m = \frac{m}{n} \log_a b$

Type-1

মান নির্ণয়

$\log_3 81 =$ কত?

4

$\log_{\sqrt{3}} 81 =$ কত?

8

$$3^4 = 81$$

$$\left(3^{\frac{1}{2}}\right)^8 = 81$$

$$\log_2 \frac{1}{32} = ?$$

$$\underline{\underline{-5}}$$

$$\frac{1}{32} = \frac{1}{2^5} = 2^{-5}$$

$$\log_2 32 = 5$$

$3\sqrt{3}$ এর 3 ভিত্তিক লগ কত?

$$\log_3 3\sqrt{3} = 3/2$$

$$\frac{x\sqrt{x}}$$

$$\frac{x^{3/2}}$$

$$\begin{aligned} 3\sqrt{3} &= 3^1 \times 3^{1/2} \\ &= 3^{1+1/2} \\ &= 3^{3/2} \end{aligned}$$

$$\log_8 2 = ?$$

H.W

$$\log_{2\sqrt{5}} 20 = ?$$

$$\underline{\underline{2}}$$

$$(2\sqrt{5})^1 = 2\sqrt{5}$$

$$\underline{\underline{(2\sqrt{5})^2}} = 4 \times 5 = \underline{\underline{20}}$$

$$\log_5 \sqrt{5} = ?$$

H.W

$$\log_{3\sqrt{2}} \frac{1}{324} = ? \quad \underline{\underline{-4}}$$

$$\log_{\cancel{3\sqrt{2}}} \frac{324}{\cancel{3\sqrt{2}}} = \underline{\underline{4}}$$

$$(3\sqrt{2})^1 = \underline{\underline{3\sqrt{2}}}$$

$$(3\sqrt{2})^2 = 9 \times 2 = \underline{\underline{18}}$$

$$(3\sqrt{2})^3 = \underline{\underline{\sqrt{\quad}}}$$

$$(3\sqrt{2})^4 = 81 \times 4 = 324$$

$\log_3 243 =$ কত?

H.W

$\log_7 343 =$ কত?

H.W

$$\log_5 \sqrt[3]{5} = \text{কত?}$$

H-w

$$\log_{10} 0.001 = ? \quad \boxed{-3}$$

$$0.001 = \frac{1}{1000}$$

$$\rightarrow 10^3 = \underline{1000}$$

$$\log_5(\sqrt[3]{5} \cdot \sqrt{5}) = ?$$

$$5/6$$

$$\sqrt[3]{5} \cdot \sqrt{5}$$

$$5^{\frac{1}{3}} \cdot 5^{\frac{1}{2}}$$

$$5^{\frac{1}{3} + \frac{1}{2}}$$

$$= 5^{\frac{5}{6}}$$

$$\log_2 \log_{\sqrt{e}} e^2 = ? \quad \underline{2}$$

$$\log_2 (\log_{\sqrt{e}} e^2)$$

$$\log_2 4 = \textcircled{2}$$

$$\log_{\sqrt{e}} e^2 = 4$$

$$(\sqrt{e})^2 = e$$

$$(\sqrt{e})^4 = e^2$$

$2^{\log_2 3 + \log_2 5}$ এর মান কত?

$$\textcircled{2}^{\log_2 15} = 15$$

$$\log_2 3 + \log_2 5$$

$$= \log_2 3 \times 5 = \textcircled{\log_2 15}$$

Type-2

log এর সমাধান

Equation

$$\log_a b = x$$
$$\underline{a^x = b}$$

✓ $\log_{10} x = 3$ হলে, x এর মান কত?

$$10^3 = x$$

$$\boxed{1000 = x}$$

$\log_{12} x = 4$ হলে, x এর মান কত?

$$12^4 = x$$

log_x 4 = 2 হলে, x এর মান কত? 2

$$x^2 = 4$$

$$x = \pm \sqrt{4}$$

$$= \pm 2$$

$$(-2)^2 = 4$$

$$(2)^2 = 4$$

$\log_x 144 = 4$ হলে, x এর মান কত?

How

$\log_{2\sqrt{5}} 400 = \underline{x}$ হলে x এর মান কত?

4

$$(2\sqrt{5})^4 = 16 \times 25 = 400$$

\log_x $\left(\frac{1}{27}\right) = 3$ হলে, x এর মান কত?

$$x^3 = \frac{1}{27}$$

$$x^3 = \frac{1}{3^3}$$

$$x^3 = \left(\frac{1}{3}\right)^3 \Rightarrow x = \left(\frac{1}{3}\right)$$

$\log_x \frac{1}{81} = -4$ হলে, x এর মান কত?

Hw

$$x^{-4} = \frac{1}{81}$$

$$x^{-4} = \frac{1}{3^4}$$

$$x^{-4} = 3^{-4}$$

$$\Rightarrow x = 3$$

$\log_x \frac{1}{9} = -2$ হলে, x এর মান কতো?

H.W

$\log_x \frac{3}{2} = -\frac{1}{2}$ হলে x এর মান কতো?

১১২

$\log_{\sqrt{8}} x = 3\frac{1}{3}$ হলে x এর মান কত?

$$\log_{\sqrt{8}} x = \frac{10}{3}$$

$$\sqrt{8}^{\frac{10}{3}} = x$$

$$\therefore x = 32$$

$$8^{\frac{1}{2}} \times \frac{10}{3}$$

$$2^{\frac{10}{2}} \times \frac{10}{3}$$

$$2^5 = 32$$

$\log_a x = 1$, $\log_a y = 2$ এবং $\log_a z = 3$ হলে, $\log_a \frac{x^3 y^2}{z} = ?$

$$\textcircled{a^1} = x \quad \textcircled{a^2} = y \quad \textcircled{a^3} = z$$

$$\log_a \frac{x^3 y^2}{z}$$

$$= \log_a \frac{\cancel{a^3} (a^2)^2}{\cancel{a^3}}$$

$$= \log_a a^4 = \underline{4}$$

Type-3

Log এর সরলীকরণ

$$3 \log 2 + \log 5 = ?$$

$$\log 2^3 + \log 5$$

$$\log 8 + \log 5 = \log 8 \times 5 = \boxed{\log 40}$$

$$\log_2 64 + \log_2 8 = ?$$

$$\begin{array}{c} \swarrow \searrow \\ \underline{6} \end{array} + \begin{array}{c} \downarrow \\ \underline{3} \end{array} = \underline{\underline{9}}$$

$$\log_2 64 \times 8 = \log_2 512 = \underline{\underline{9}}$$

$$\log_{\sqrt{2}} 4 \times \log_{\sqrt{3}} 3 = ?$$

↓

4

x

2

=

8

$$2 \log_{10} 5 + \log_{10} 36 - \log_{10} 9 = ?$$

$$= \log_{10} 25 + \log_{10} 36 - \log_{10} 9$$

$$= \log_{10} \frac{25 \times 36}{9} = \log_{10} 100 = \underline{\underline{2}}$$

$$\log_2 \sqrt{6} + \log_2 \sqrt{\frac{2}{3}} = ?$$

$$\begin{aligned} \sqrt{6} &= \sqrt{2 \times 3} \\ &= \sqrt{2} \times \sqrt{3} \end{aligned}$$

$$\log_2 \sqrt{6} = \log_2 \sqrt{\frac{2}{3}}$$

$$\log_2 \sqrt{2} \times \sqrt{3} + \frac{\sqrt{2}}{\sqrt{3}}$$

$$= \log_2 2 = \underline{1}$$

$$\frac{\log 36}{\log 6} = \text{কত?}$$

$$\log \frac{a}{b} = \log a - \log b$$

$$\frac{\log 6^2}{\log 6} = \frac{2 \log 6}{\log 6} = 2$$

$$\log_2 1 = 0$$

$$= \log_2 \log_2 \log_2 16 = \text{কতো?}$$

$$\log_2 16 = 4$$

$$\log_2 4 = 2$$

$$\log_2 (\log_2 4)$$

$$= \log_2 2 = \underline{1}$$

$$\log \frac{a^3 b^3}{c^3} + \log \frac{b^3 c^3}{d^3} + \log \frac{c^3 d^3}{a^3} - 3 \log b^2 c = ?$$

$$\log \frac{\cancel{b^3} \cancel{b^3}}{\cancel{c^3}} \times \frac{\cancel{b^3} \cancel{c^3}}{\cancel{d^3}} \times \frac{\cancel{c^3} \cancel{d^3}}{\cancel{a^3}} - \log (b^2 c)^3$$

$$2 \log b b c^3 - \log b^2 c^3 = 0$$

Type-4

বিবিধ

$$\log_7(\sqrt[5]{7} \cdot \sqrt{7}) - \log_3 \sqrt[3]{3} + \log_4 2 = \text{কতো?}$$

$$7^{\frac{1}{5}} \cdot 7^{\frac{1}{2}}$$

$$7^{\frac{1}{5} + \frac{1}{2}} = 7^{\frac{7}{10}}$$

$$a^{\frac{1}{n}} = \sqrt[n]{a}$$

$$\begin{aligned} \frac{7}{10} - \frac{1}{3} + \frac{1}{2} &= \frac{21 - 10 + 15}{30} \\ &= \frac{26}{30} = \frac{13}{15} \end{aligned}$$

$$\log(a^a \cdot b^b \cdot c^c) = 0 \text{ হলে } \underline{a^a \cdot b^b \cdot c^c} = ?$$

$$\log_2 1 = 0$$

$$a^a \cdot b^b \cdot c^c = \underline{1}$$

$$\log_4 2 = \frac{1}{\log_2 4} = \underline{\underline{\frac{1}{2}}}$$

$\log_a b \times \log_b c \times \log_c d =$ কতো?

$$\frac{\log b}{\log a} \times \frac{\log c}{\log b} \times \frac{\log d}{\log c}$$

$$\frac{\log d}{\log a} = \log_a d$$

✓ $\log_{\sqrt{a}} b$ + $\log_{\sqrt{b}} c$ + $\log_{\sqrt{c}} a$ এর মান কতো? ✓

$$\frac{2 \log \sqrt{b}}{\log \sqrt{a}} \times \frac{2 \log \sqrt{c}}{\log \sqrt{b}} \times \frac{2 \log \sqrt{a}}{\log \sqrt{c}}$$

$$2 \times 2 \times 2 = 8$$

$$\log_a \log_a \log_a (a^{a^b}) = \text{কতো?}$$

$$\log_2 \log_2 \log_2 16$$

H.w

$$\log_a (\log_a a^b)$$

$$\log_a (a^b)$$

Ans: b

$$\log_a a^b = \underline{b}$$

$$\log_k \frac{a^n}{b^n} + \log_k \frac{b^n}{c^n} + \log_k \frac{c^n}{a^n} = \text{কতো?}$$

HW

$p = \log_a(bc)$ হলে, $p + 1 = ?$

$$p = \log_a bc$$

$$p + 1 = \log_a bc + 1$$
$$= \log_a bc + \log_a a = \log_a abc$$

Thank You