

Compound Interest(Preli. & Written)

Instructor:

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1. How much interest will TK. 2,000 earn at an annual rate of 10% in one year if the interest is compounded every 6 months?

- A) 200
- B) 210
- C) 220
- D) None of these

$$\begin{array}{r}
 \text{1st} \\
 \text{2nd} \\
 \hline
 \end{array}
 \begin{array}{r}
 \frac{S}{100} \\
 \frac{101.5}{100} \\
 \hline
 \end{array}
 \begin{array}{r}
 \\
 \\
 \hline
 \end{array}
 \begin{array}{r}
 \\
 \\
 \hline
 \end{array}$$

$200 + 5 = 205$

5%

2100

$$\begin{array}{r}
 \frac{S}{100} \\
 \frac{100.5}{100} \\
 \hline
 \end{array}
 \begin{array}{r}
 \\
 \\
 \hline
 \end{array}
 \begin{array}{r}
 \\
 \\
 \hline
 \end{array}$$

$201 + 5 = 205$

$$2000 \left(1 + \frac{10}{100}\right)^4$$

100			
110	5		
100	5	10.5	
100	5	10.5	11.55
<hr/>			
400	+15	+21	+11.55 = 447.55

11.5.5.

2. There is a 60% increase in an amount in 6 years at simple interest. What will be the compound interest on Tk. 12,000 after 3 years at the same rate?

- A) 2160
- B) 3120
- ~~C) 3972~~
- D) 6240
- E) None of these

12,000

$100 + 10 = 110$ rate of interest = 10%
 $\rightarrow 110 + 11$ \downarrow
 $= 121$ $\rightarrow 10$ $10 + 1 = 11$
 $\rightarrow 10 \cdot 1$

$\rightarrow 10 \quad 1 \quad 1.1$
 $\hline 30 + 2 + 1.1 = 33.1\%$ $\rightarrow 10$
 $\rightarrow 10 \quad 1$

$30 + 3 + 0.1$
 $3600 + 360 + 12$
 $= 3972$

$\rightarrow 10 \quad 1 \quad 1.1$
 $\hline 30 + 2 + 1.1$
 $\hline = 33.1$

3. The difference between CI and SI for 3 years Rs. 992. If rate of interest is 10%. Find the Principal?

A. Rs. 22000

B. Rs. 30000

C. Rs. 28000

D. Rs. 32000

10		
10	1	
10	1	1.1

$2 + 1.1 = 3.1$

$$\frac{992 \times 100 \times 10}{31} = 32000$$

4. The least number of complete years in which a sum of money put out at 20% compound interest will be more than doubled is:

- A. 3
- ~~B. 4~~
- C. 5
- D. 6

Rule of 72:

$$\frac{72}{\text{Rate of interest}} = \frac{72}{20}$$

$$100 \left(1 + \frac{20}{100}\right)^n = 200$$

$$\left(1 + \frac{20}{100}\right)^n = 2$$

$$n = \left\lceil \log \left(1 + \frac{20}{100}\right)^2 \right\rceil \approx 4 \text{ years.}$$

5. What will be the compound interest on a sum of Tk. 25,000 after 3 years at the rate of 12% p.a.?

- A. Tk. 9000.30
- B. Tk. 9720
- C. Tk. 10123.20
- D. Tk. 10483.20
- E. None of these

$$12\% = 10 + 2\%$$

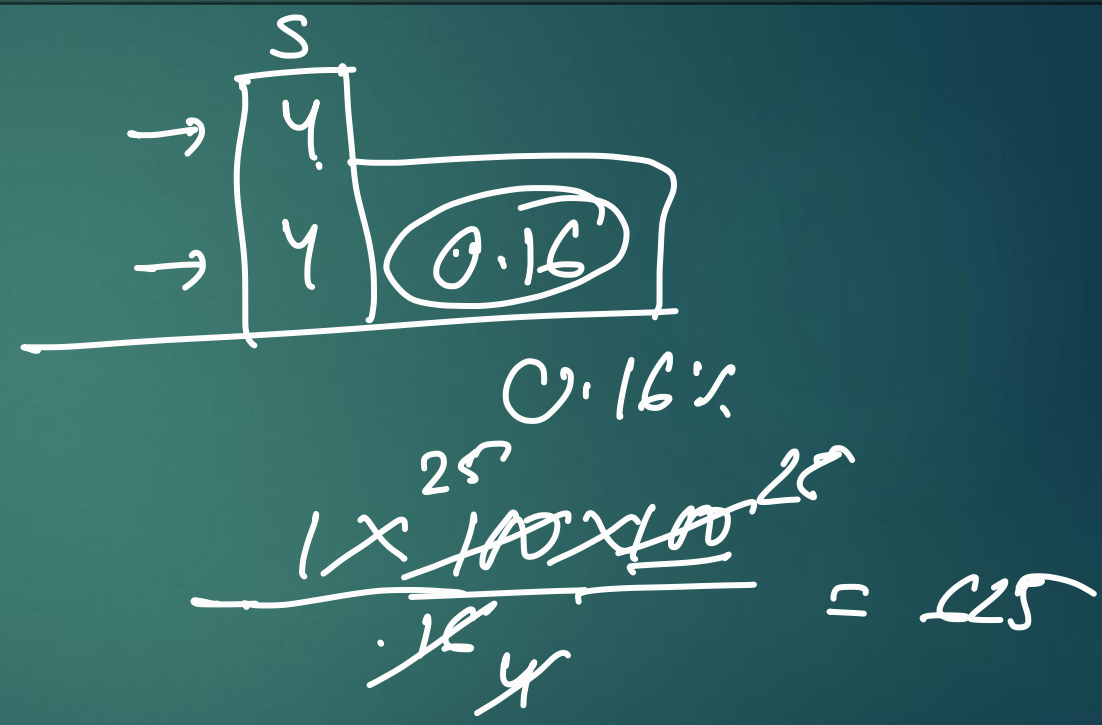
$$2500 + 500 = \underline{3000}$$

$$\begin{array}{r} \underline{3000} \\ \rightarrow \underline{3000} \quad 360 \\ \rightarrow \underline{3000} \quad 360 \quad 403.2 \\ \hline 9000 + 720 + 403.2 \\ = \underline{\underline{10123.2}} \end{array}$$
$$\begin{array}{r} \underline{3360} \quad 320 \\ \quad \underline{672} \\ \hline 4032 \end{array}$$

6. The difference between simple and compound interests compounded annually on a certain sum of money for 2 years at 4% per annum is Tk. 1.

The sum is:

- A. 625
- B. 630
- C. 640
- D. 650



7. If the compound interest on a sum for 2 years at 12.5% per annum is TK 510 the simple interest on the same at the same rate for the same period of time is :

- A. TK. 400
- B. TK. 450
- C. TK. 460
- D. TK. 480

$12.5 = 10 + 2 + 0.5$
 $1.25 + 0.250 + 0.0625$
 1.5625

12.5	✓
12.5	1.5625

$25 + 1.5625 = 26.5625\%$

1.25	.125
x 2	.250
	0.0625
	0.3125
	1.2500
	1.5625

$1\% = .125$
 $2\% = 0.250$
 0.0625

$30 \quad 480$
 $\rightarrow 510 \times 25 \times 10000$
~~265625~~
~~10625~~
~~425~~
~~12~~
 $= 480$

8. What will be the difference between simple and compound interest at 10% per annum on a sum of Tk.1000 after 4 years?

- A. Tk.31
- B. Tk. 32.10
- C. Tk. 40.40
- ~~D. Tk. 64.10~~

Handwritten calculations on a chalkboard:

$1000 \times 10\% = 100$

1000			
100	1		
100	1	1.1	
100	1	1.21	

$30 + 22 + 12.1 = 64.10$

5.31%

9. The compound interest on a certain sum for 2 years at 10% per annum is Rs. 525. The simple interest on the same sum for double the time at half the rate percent per annum is:

- A. 400
- B. 500
- C. 600
- D. 800

$$\frac{2 \times 525 \times 20}{2 \times 100} = 500$$

4 → 20%
5%

10. What is the difference between the compound interest on Tk. $\boxed{5000}$ for $\boxed{1.5}$ years $\boxed{4\%}$ per annum compounded yearly and half-yearly?

$$\frac{200}{5200}$$

- ~~A. 2.04~~
- B. 3.06
- C. 4.80
- D. 8.30

yearly

$$200 + 104$$

$$\boxed{= 304} \rightarrow$$

$$\begin{array}{r} 306.04 \\ 304.00 \\ \hline 2.04 \end{array}$$

Half yearly 1.02

$$\begin{array}{r} 100 \\ 100 \quad 2 \\ 100 \quad 2 \quad 2.04 \\ \hline 300 + 4 + 2.04 \\ \boxed{= 306.04} \end{array}$$

11. The difference between the compound and simple interest on a sum of 5% rate of interest per annum for 3 years is Tk. 36.60, Then the sum is-

- A. 8000
- B. 8400
- C. 4400
- D. ~~4800~~

$$\begin{array}{r}
 5 \\
 5 \quad \left[\begin{array}{l} 0.25 \\ 0.25 \quad 0.2625 \end{array} \right. \\
 5 \\
 \hline
 0.50 + 0.2625 = 0.7625
 \end{array}
 \qquad
 \begin{array}{r}
 5.25 \\
 5 \\
 \hline
 0.2625
 \end{array}$$

$$\begin{array}{r}
 36.60 \times 100 \\
 \hline
 0.7625 \times 12 \times 2 \\
 \hline
 3660 \times 100 \times 100 \\
 \hline
 2025 \\
 \hline
 205 = 4800
 \end{array}$$

12. A sum of Tk. 50,000 is invested at 8% p.a. compounded annually. After how many years will the investment amount double?

- A) 8.5 years
- ~~B) 9 years~~
- C) 9.5 years
- D) 10 years

$$\frac{72}{8} = 9$$

13. A loan is to be returned in two equal yearly instalments. If the rate of interest is 10% p.a. compounded annually and each instalment is Rs. 5,808, then 60% of the total interest (nearest to a Rs.) charge in this scheme

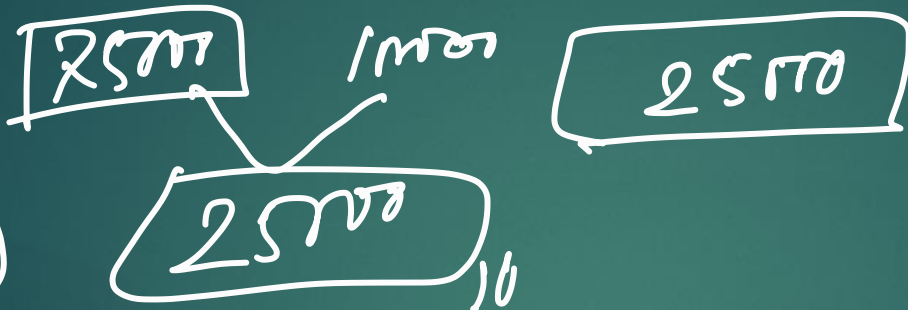
- A. 917
- ~~B. 922~~
- C. 913
- D. 911

$$\begin{aligned}
 PV &= CF \left\{ \frac{1 - (1+r)^{-n}}{r} \right\} \\
 &= 5808 \left\{ \frac{1 - \left(1 + \frac{10}{100}\right)^{-2}}{\frac{10}{100}} \right\} \\
 &= 5808 \left\{ \frac{1 - (1.10)^{-2}}{1/10} \right\} \\
 &= 5808 \left(\frac{1 - \frac{1}{1.21}}{1/10} \right)
 \end{aligned}$$

$PV =$ present value
 $CF =$ cash flow / instalment
 1.10^2
 $= 1.21$

14. An investment of Tk. 75,000 grows to Tk. 1,00,000 in 3 years under compound interest. What is the annual rate of interest (compounded annually)?

- A) 9%
- B) 9.5%
- ~~C) 10%~~
- D) 10.5%



$$10 \quad |$$

$$10 \quad | \quad 1$$

$$10 \quad | \quad 1 \quad 1$$

$$30 + 2 + 1.1 = 33.1\%$$

$$\frac{25000}{75000}$$

$$33.33\%$$

$$33.1\%$$

$$33.33\%$$

$$33.1\%$$

$$= 5808 \times \left(\frac{\frac{1.21 - 1}{1.21}}{\frac{1}{10}} \right)$$

$$= \underline{5808} \times \frac{0.21}{1.21} \times \frac{10}{1} = \overset{480}{\cancel{58080}} \times \frac{21}{121} = \underline{10080}$$

$$\begin{array}{r} 5808 \\ \times 2 \\ \hline 11616 \end{array}$$

$$= (11616 - 10080)$$

$$= 1536$$

$$\begin{array}{r} 153.6 \\ 6 \\ \hline 921.6 \end{array}$$





Thank You