

LCM & HCF

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Multiple → গুণিতক

12) 9)

12 → 12, 24, 36, 48, 60, 72, 84, 96, 108, 120, ...

18 → 18, 36, 54, 72, 108, 126, ...

Common multiple → 36, 72, 108, ...

Least common multiple → 36
সর্বোচ্চ → LCM = 36

36 x 108 72 144

Factor \rightarrow 2, 3, 4, 6

12 \rightarrow 1, 2, 3, 4, 6, 12

18 \rightarrow 1, 2, 3, 6, 9, 18

common factors \rightarrow 1, 2, 3, 6

Highest
HCF \rightarrow 6 \Rightarrow 6

LCM of 12 & 18 is 36

HCF " " " " " 6

$$36 \times 6 = 216$$

$$12 \times 18 = 216$$

product of two numbers = product of their HCF and LCM

$$N_1 \times N_2 = \text{HCF} \times \underline{\text{LCM}}$$

$$\underline{\underline{N_1}} = \frac{\text{HCF} \times \text{LCM}}{\underline{N_2}}$$

HCF of 12, 18 \rightarrow

LCM of 12, 18 \rightarrow 36

Ratio of 12, 18 \rightarrow 12:18 = 2:3

$$\text{LCM} \rightarrow \frac{(2 \times 3) \times 6}{36} = \underline{36}$$

$$\text{HCF} \rightarrow \frac{36}{2 \times 3} = 6$$

$$2 \times 3 = \underline{6}$$

$$6 \times 2 = \underline{12}$$

$$6 \times 3 = \underline{18}$$

$$\frac{36}{2} = 18$$

$$\frac{36}{3} = \underline{12}$$

a) 4 b) 6 ~~c) 12~~ ~~d) 36~~ 5) 25.6

Q1: Find the highest common factor of 36 and 84. [Pubali Bank (SO) 23]

12

36 \rightarrow 1, 2, 3, 4, 6, 9, 12, 18, 36

84 \rightarrow 1, 2, 3, 4, 6, 7, 12, 14, 21, 28, 42, 84

$36 = 2 \times 2 \times 3 \times 3$
 $84 = 2 \times 2 \times 3 \times 7$

HCF $\rightarrow 2 \times 2 \times 3$

12

$$\begin{array}{r} 2 \overline{) 36} \\ \underline{2 \overline{) 18}} \\ 3 \overline{) 9} \\ \underline{3} \\ 3 \end{array}$$

$$\begin{array}{r} 2 \overline{) 84} \\ \underline{2 \overline{) 42}} \\ 3 \overline{) 21} \\ \underline{3} \\ 7 \end{array}$$

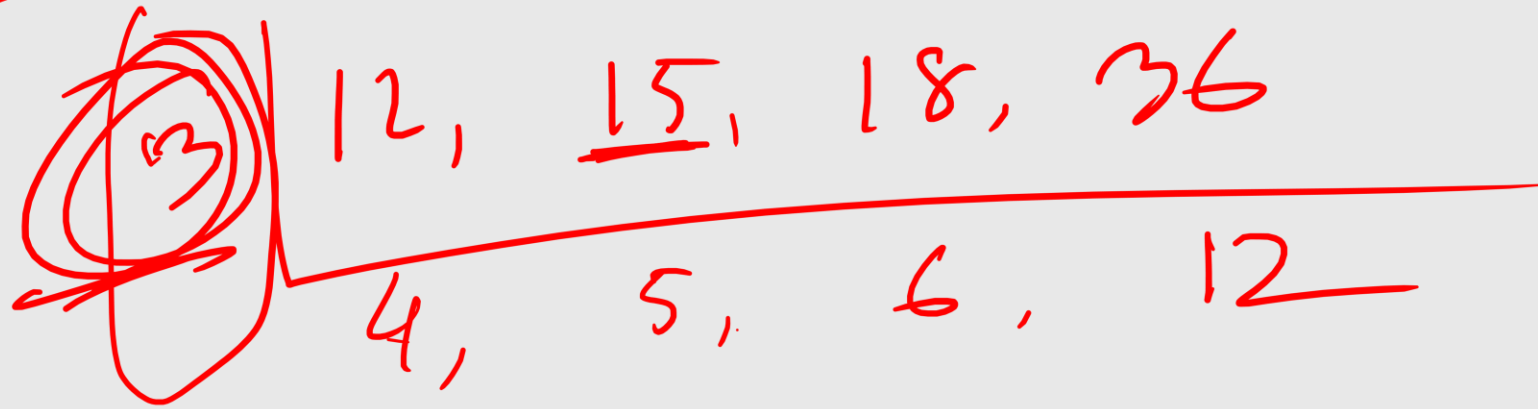
$$\begin{array}{r} \textcircled{36) 84} \left(2 \right. \\ \underline{72} \\ \textcircled{12) 36} \left(3 \right. \\ \underline{36} \\ 0 \end{array}$$

$$\text{HCF} \Rightarrow \underline{\underline{12}}$$

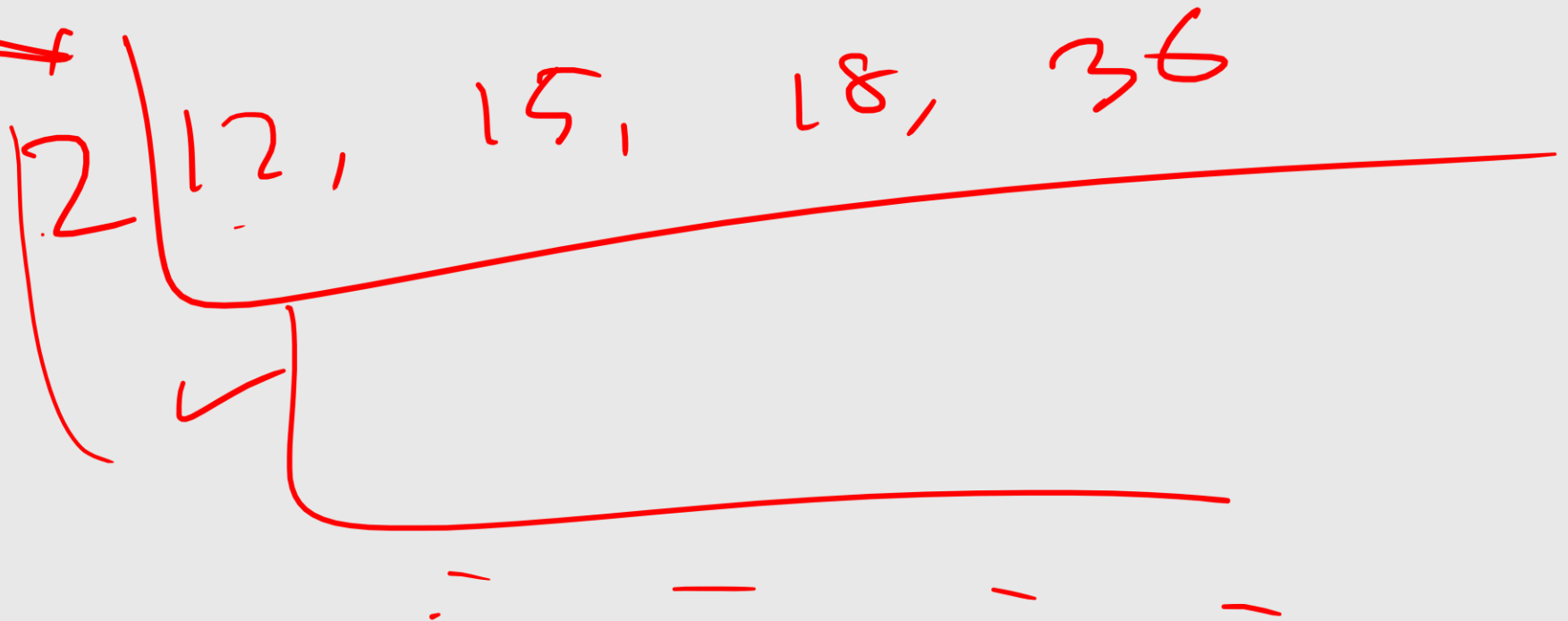
$$\begin{array}{r} \checkmark \checkmark \\ \checkmark \checkmark \quad 2 \mid 36, 84 \\ \quad \quad \quad 2 \mid 18, 42 \\ \quad \quad \quad \quad 3 \mid 9, 21 \\ \quad \quad \quad \quad \quad 3, 7 \end{array}$$

$$\text{HCF} \Rightarrow \underline{2 \times 2 \times 3} = \textcircled{12}$$

HCF



LCM



Q2: What is the H.C.F of the numbers 36, 54 and 90? [Pubali Bank (SO)-13]

a) 6

b) 9

c) 12

d) 18

Q3: The greatest number that exactly divides 105, 1001 and 2436 is:

[AD-14]

a) 3

b) 7 ✓

c) 11 ✗

d) 21 ✗

Handwritten calculations showing the prime factorization of 105, 1001, and 2436 to find their greatest common divisor (GCD).

105) 1001 (9
945

56) 105 (1
56

49) 56 (1
49

7) 2436 (348
21

33
28

56
56
0

7) 49 (7
49
0

Diagram showing the prime factorization of 105, 1001, and 2436. The prime factors are 3, 5, 7, 11, 13, and 17. The common prime factor is 7.

Q4: The greatest number which can divided 1356, 1868 and 2764 leaving the same remainder 12 in each case is- [Pubali Bank (PO)-23]

$$1356 - 12 = 1344$$

$$1868 - 12 = 1856$$

$$2764 - 12 = 2752$$

~~2-2.5~~

~~701~~

~~701~~

64

124

156

260

25

~~10-15~~

~~60+~~

~~70+~~

~~100+~~

Q5: Find the greatest number that will divide 43, 91 and 183 so as to leave the same remainder in each case? [Pubali Bank (TAT)-17]

$$91 - 43 \rightarrow 48$$

$$183 - 43 \rightarrow 140$$

$$183 - 91 \rightarrow 92$$

HCF of 48, 140, 92 is 4

✓ ~~4~~

5) 7

9) 9

2) 13

X

$$\begin{array}{r} \text{5) } \textcircled{\underline{31}} \\ \underline{30} \end{array}$$

(6

31, 41, 71

$$\begin{array}{r} \text{5) } \textcircled{\underline{41}} \text{ (8)} \\ \underline{40} \\ \hline 1 \end{array}$$

$$\begin{array}{r} \text{5) } \textcircled{\underline{21}} \text{ (14)} \\ \underline{20} \\ \hline 1 \end{array}$$

①

31, 41, 71

$$\begin{array}{l} 41 - 31 = \textcircled{10} \\ 41 - 71 = \textcircled{30} \\ 71 - 31 = \textcircled{40} \end{array}$$

⑤

Q6: Find the largest number which divides 62, 132 and 237 to leave the same remainder in each case. [SPCBL (Off)-23] (H.W)

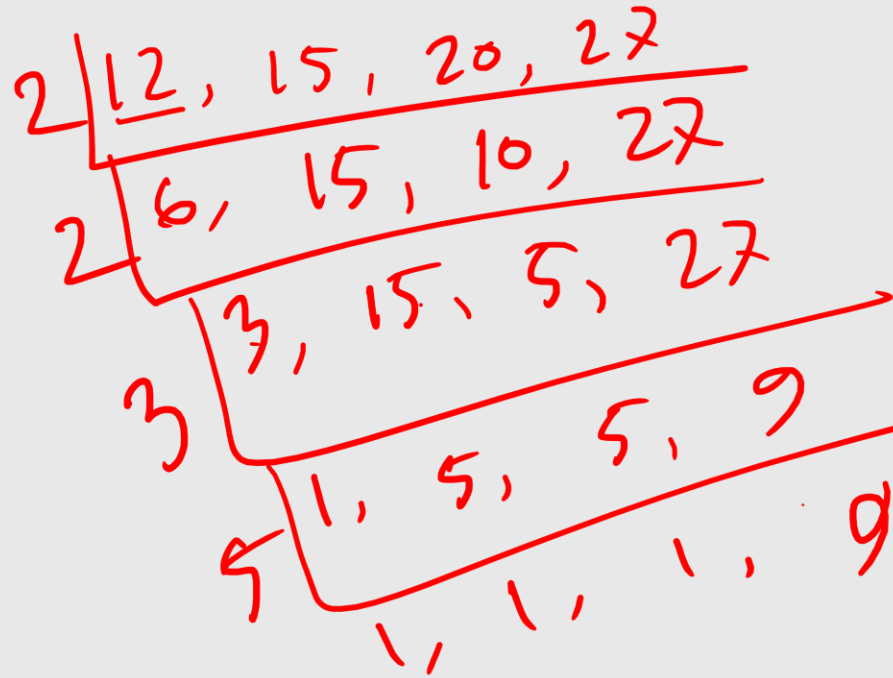
Q7: Find the least number exactly divisible by 12, 15, 20 and 27.

a) 540

b) 430

c) 320

d) ~~300~~



12 → 12, 24, 36

15 → 15, 30, 45

Q8: What is the smallest number of apples that can be distributed equally (without cutting any apple) among 6, 10, 14 and 18 boys? [BB (AD) 22]

6, 10, 14, 18

6

→

6, 12, 18

10

→

10, 20, 30, 40

14

→

14, 28, 42, 56

18

→

18, 36, 54

LCM

Q9: Six bells start ringing together and ring at intervals of 4, 8, 10, 12, 15 and 20 seconds respectively. How many times will they bring together in 60 minutes?

Handwritten work for the problem:

$\checkmark 2 \quad \checkmark 2 \quad \checkmark 2 \quad \checkmark 2$
 $2 \quad \checkmark 2 \quad \checkmark 2$
 $\frac{10}{2} + 1 = 6$
 $\frac{60}{2} = 30 + 1$
 $\frac{60}{2} = 31$

(4) 12 24 36 48 60
 (5) 15 30 45
 (6) 20 40
 (10) ~~10~~

$\sqrt{4, 8, 10, 12, 15, 20}$
 120s
 2 min
 $\frac{60}{2} = 30$ times

$\frac{60}{2} = 30 + 1$
 $\frac{60}{2} = 31$

(1) 2n
 (1) 2m
 (1) 2n

$\frac{60}{2} = 30$ times

Q10: Which is the larger between two numbers if they are in the ratio of **6:13**

and their least common multiple is **312**? [Comb Bank (SO)-23 (21 Based)]

$$\checkmark \frac{312}{6} = 52$$

$$\checkmark \frac{312}{13} = 24$$

Let, the number be $6n, 13n$

Lcm of $6n, 13n \rightarrow 78n$

$$\text{A.T.Q, } 78n = 312$$

$$n = \frac{312}{78} = 4$$

$$6 \times 4 = 24$$

$$13 \times 4 = 52 \checkmark$$

Q11: The ratio of two numbers is 3:4 and their HCF is 4. Their LCM is: (Pubali (JO)-23]

$$(3 \times 4) \times 4 = 48$$

Q12: The ratio between two numbers is ~~3:4~~ and their least common multiple is 180. What is the first number?

$$\frac{180}{3} = 60$$

$$45 : 60 = 3 : 4$$

$$60 : 45 = 4 : 3$$

$$\frac{180}{4} = 45$$

45

Q13: Find the largest number of five digits which, when divided by 16, 24,

30 or 36, leaves the same remainder 10 in each case.

BB (AD) - 2025

Lcm of 16, 24, 30, 36 \rightarrow 720

1440

2160

2880

720) 99999

138

2799

2160

6399

5760

639

639

5

400

$$99999 - 639 \Rightarrow \underline{\underline{99360}} + 10 \Rightarrow$$

~~99370~~

~~99360~~

~~99350~~

99340

99370

Am

Thank You

